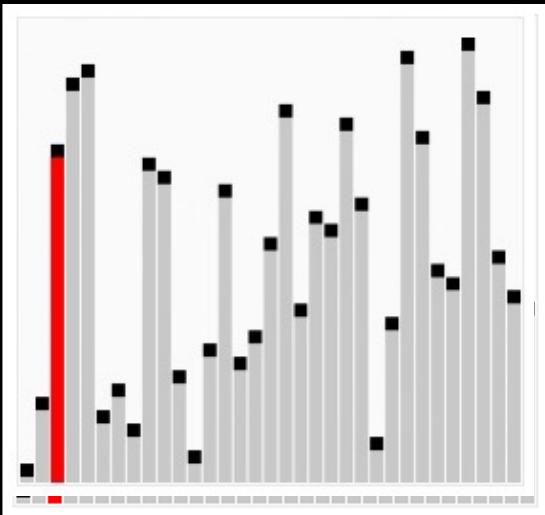


Which sorting algorithm is this?



START AT 3:06

In a file on your IDE, create a "person" struct with attributes name and age. Then, in int main(void), create an array of 2 persons. Iterate through the array and print each name and age.

```
typedef struct
{
    string name;
    int age;
} person
```

```
int main (void)
{
    person people[2];
    people[0].name = "Luca";
    people[0].age = 19;
```

```
3
3
int scores[5];
for (int i=0; i<2; i++)
{
    printf("%s is %i years old",
    people[i].name, people[i].age);
}
```

CS50 Section 3

- Searching and Running Times
- Structs
- Sorting
- Recursion

## Runtime

- Best Case?     $\mathcal{O}(1)$  ~ constant

$\mathcal{O}(n)$  - linear

$\mathcal{O}(\log n)$  - logarithmic

- Worst Case?

$\mathcal{O}(1)$

$\mathcal{O}(n)$

$\mathcal{O}(2^n)$

# Searching

- Linear Search



## Searching and Run Times

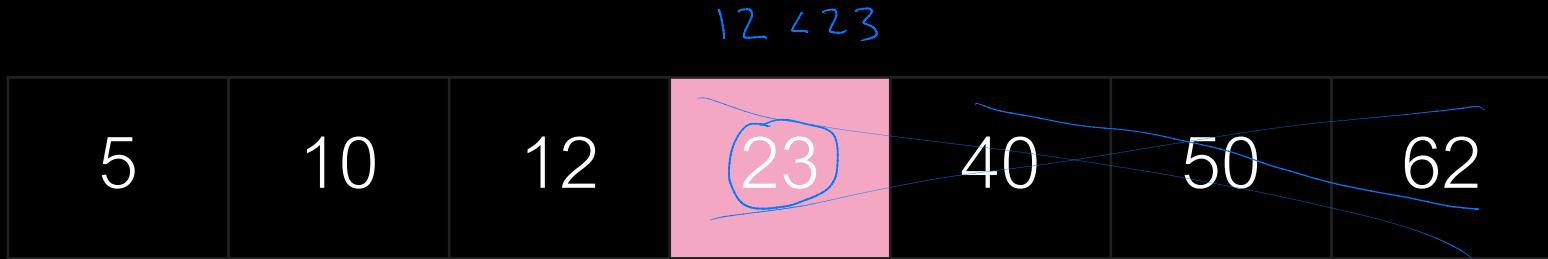
- Linear Search

1            2            3            4            5            6            7            8

- Best Case?       $\Theta(1)$
- Worst Case?       $\Theta(n)$

## Searching and Run Times

- Binary Search – Let's look for the number 12.



## Searching and Run Times

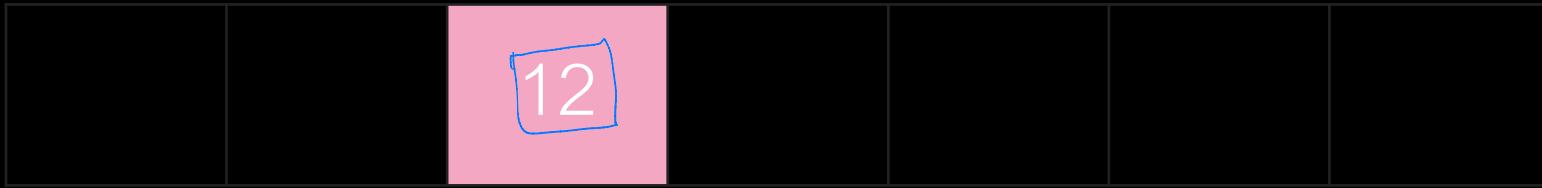
- Binary Search – Let's look for the number 12.



## Searching and Run Times

- Binary Search – Let's look for the number 12.

$12 = 12$



3 operations

$O(\log n)$

$\log_2 n$

$$\boxed{\log_2 7 \approx 3}$$

32  
16  
8  
4  
2  
1

## Searching and Run Times

- Binary Search – Let's look for the number 12.

5	10	12	23	40	50	62
---	----	----	----	----	----	----

- Best Case?  $\mathcal{O}(1)$
- Worst Case?  $\mathcal{O}(\log n)$



# Structs

```
typedef struct
```

```
{
```

```
    string name;
```

```
    int age;
```

```
}
```

```
person; ← name of the struct
```

Variables that  
your struct contains

```
struct person {
```

```
    string name;
```

```
    int age;
```

```
3
```

```
struct person
```

# Structs

```
typedef struct
```

```
{
```

```
    string name;
```

```
    int age;
```

```
}
```

```
person;
```

```
    vw inside  
    ↓  
    struct  
    p.name  
    → p.name = "Phyllis";  
  
    p.age = 19;
```

Why a struct?



group variables into  
a common entity

3: 30

## Exercise 1: Struct Practice

```
typedef struct          typedef struct
{                      {
    string name;      string name;
                        int month;
    int age;          int day;
}
person;                3
                        birth day;
```

Construct a struct called “birthday” that contains a variable *name* as a *string*, the variable *month* as an *int*, and the variable *day* as an *int*.

Create an array storing birthdays, initialize your contents, and print the contents of your array.

- Searching and Running Times
- Structs
- Sorting
- Recursion

## Bubble Sort

3	6	1	4	7	8	2	5
---	---	---	---	---	---	---	---

3 6 1 4 7 8 2 5

3 6 1 4 7 8 2 5

3 1 6 4 7 8 2 5

3 1 4 6 7 8 2 5

3 1 4 6 7 8 2 5

3 1 4 6 7 8 2 5

3 1 4 6 7 2 8 5

3 1 4 6 7 2 8 5

## Bubble Sort

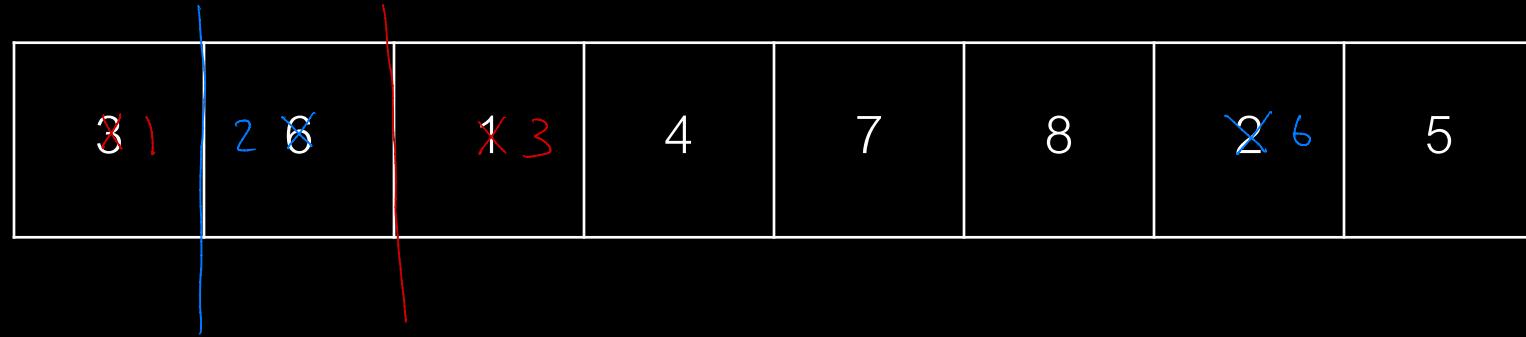
1	2	3	4	5	6	7	8
---	---	---	---	---	---	---	---

## Bubble Sort

3	6	15	4	7	8	21	2 <del>5</del> 1
---	---	----	---	---	---	----	------------------

- Best Case?  $\mathcal{O}(n) = \mathcal{O}(n-1) = \mathcal{O}(\log^{30} n)$
- Worst Case?  $\mathcal{O}(n^2)$    
  $n$  passes,  $n$  comparisons per pass  $\Rightarrow n^2$  operations  
  
 WHEN SMALLEST ELEMENT IS LAST IN ORIGINAL ARRAY

## Selection Sort



min

3, 1

## Selection Sort



7 + 6 + 5 + 4 + 3 + 2 + 1

$$(n-1) + (n-2) + \dots + 1$$

$$\frac{n(n-1)}{2} = \frac{n^2 - n}{2} = O(n^2)$$

## Selection Sort

3	6	1	4	7	8	2	5
---	---	---	---	---	---	---	---

- Best Case?  $\Omega(n^2)$
  - Worst Case?  $O(n^2)$
- $\uparrow$   
 $\Theta(n^2)$
- BEST = WORST

## Selection Sort

[1, 5, 2, 6, 3, 7]

```
int arr [6] = [3, 5, 2, 6, 1, 7];
```

```
for (int i=0; i<6; i++)  
{  
    min = arr[i];  
    idx = i;
```

```
    for (int j=i+1; j<6; j++)  
    {  
        if (min > arr[j])  
        {  
            min = arr[j];  
            idx = j;  
        }  
    }  
}
```

3

```
temp = arr[i];  
arr[i] = min;  
arr[idx] = temp;  
arr[4] = 3
```

3

i=0  
j=5  
min = arr[i] = 3  
idx = i;

j= 0  
min = 3;  
idx = 0;

j=1  
min = 3;  
idx = 0;

j=2  
min = 2;  
idx = 2;

j=3  
min = 2;  
idx = 2;

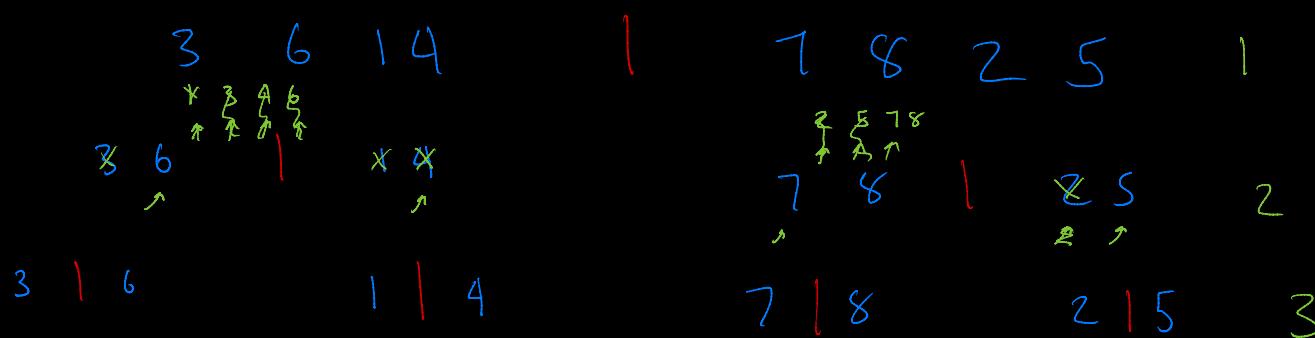
j=4  
min = 1;  
idx = 4;

RESTART AT 4

## Merge Sort

1 3 5 7  
↑  
n      2 4 6 8  
↑  
*n comparisons  
when merging*

3	6	1	4	7	8	2	5
1 2 3 4 5 6 7 8							



## Merge Sort

1	2	3	4	5	6	7	8
---	---	---	---	---	---	---	---

## Merge Sort

3	6	1	4	7	8	2	5
---	---	---	---	---	---	---	---

$n$  comparisons when merging  
 $\log n$  merges ]  $\Rightarrow n \log n$  runtime

- Best Case?  $\mathcal{O}(n \log n)$  ]  $\Rightarrow \Theta(n \log n)$
- Worst Case?  $\mathcal{O}(n \log n)$

Fun Sorts :D

3	6	1	4	7	8	2	5
---	---	---	---	---	---	---	---

Stalin Sort (fake sort vibes)

3	6	1	4	7	8	2	5
---	---	---	---	---	---	---	---

## Stalin Sort (fake sort vibes)



3 6 7 8

- Best Case?  $\mathcal{O}(n)$   
 $\Rightarrow \Theta(n)$
- Worst Case?  $\mathcal{O}(n)$

## Bogosort Sort

8

3	6	1	4	7	8	2	5
---	---	---	---	---	---	---	---

$8!$  possible permutations

Worst Case:  $n \cdot n! = O(n!)^2$

Best Case:  $\Omega(n)$

## Summary

Selection Sort

BEST :  $\Omega(n^2)$

WORST :  $O(n^2)$

Bubble Sort

BEST :  $\Omega(n)$   $\rightarrow$  Already sorted

WORST :  $O(n^2)$

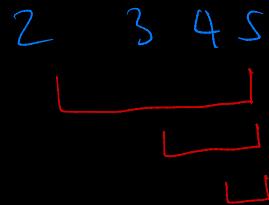
Merge Sort

BEST :  $\Omega(n \log n)$

WORST :  $O(n \log n)$

## Exercise: Reading and Understanding Code!

```
int values[n];  
for (int i = 0; i < n - 1; i++)  
{  
    int min_index = i;  
    for (int j = i + 1; j < n; j++)  
    {  
        if (values[j] < values[min_index])  
        {  
            min_index = j;  
        }  
    }  
    int temp = values[i];  
    values[i] = values[min_index];  
    values[min_index] = temp;  
}
```



- Searching and Running Times
- Structs
- Sorting
- Recursion

# Recursion

- Base Case

- Recursive Call

↑  
calling yourself / the same  
function

Write a function that prints integers starting from ~~n~~ line by line,  
~~adding~~  
~~subtracting~~ one for each line until ~~n~~ is reached using  
recursion.

1  
2  
3  
4  
5  
6  
:  
n

## Recursion

```
void count(n)    ↗ Function  
{  
    if (n == 0)    ↙  
    {  
        return;  
    }  
    count_up_to(n - 1);  
    printf("%i\n", n);  
}
```

count(5) [ 1  
 2  
 3  
 4 ] count(4)  
 5 ] print 5

count(4) [ 1  
 2  
 3 ] count(3)  
 4 ] print 4

print 1  
print 2  
print 3  
print 4  
print 5

1  
2  
3  
4  
5

$$3! = 6$$

## Recursion

$$0! = 1$$
$$1! = 1$$

- **Base Case**

- Recursive Call

factorial (3)

return 3. factorial (2)

$$3 \cdot 2 = 6$$

factorial (2)

return 2. factorial (1)

↗

Write a function that determines the factorial of an integer n using recursion. Prompt the user for an integer and print out its factorial.

$$\begin{aligned}n! &= n(n-1) \cdots 1 \\&\equiv n(n-1)!\end{aligned}$$

int n = get\_int ("give int"), 3

result = factorial (n)

printf ("%d", result);

```
int factorial (int x)
{
    if (x ≤ 1) {
        return 1;
    }
    return x * factorial (x-1);
```

$$\text{factorial}(x) = x \cdot \text{factorial}(x-1)$$

factorial (1) = 1

## Exercise: Reading and Understanding Code!

```
int mystery(int n);
```

```
int main(void)
```

```
{  
    printf("%i\n", mystery(3));      3  
    printf("%i\n", mystery(5));      5  
}
```

→ factorial

```
int mystery(int n)  
{  
    if (n == 0)  
        return 1;  
  
    return n * mystery(n - 1);  
}
```

3

return  $3 * \text{mystery}(2)$

mystery(2)

return  $2 * \text{mystery}(1) = 2$

6

mystery(1)

return  $1 * \text{mystery}(0)$

mystery(0)

return 1

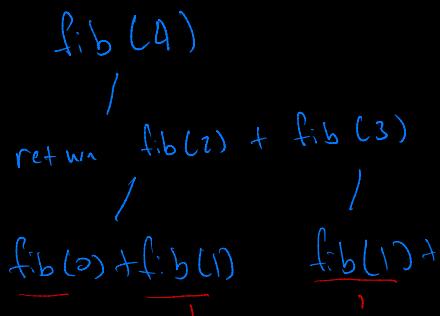
## Exercise 2: Fibonacci Numbers

0 1 1 2 3 5 8 13  
0 1 2 3 4 5

Write a recursive function *fib* that computes the nth Fibonacci number. The 0th Fibonacci number is 0, the 1st Fibonacci number is 1, and every subsequent Fibonacci number is the sum of the two preceding Fibonacci numbers.

*fib*(7) returns 13

$$\text{fib}(n) = \text{fib}(n-1) + \text{fib}(n-2)$$



```
int fib(int n)
{
    if (n == 0) {
        return 0;
    } else if (n == 1) {
        return 1;
    } else {
        use other calls to compute
        current call
        return fib(n-1) + fib(n-2);
    }
}
```

# Lab

SORT 1

reversed 10000.txt → reversed list of ints

SORT 2

random 10000.txt → random list of ints

SORT 3

Sorted - .txt → sorted list of ints

time ./sort1 <sort#> reversed10000.txt

BUBBLE

SELECTION

MERGE

Run 3 sorts on sorted list

Bubble should do the best

Sorted	Reversed	Random
Bubble	Merge	Merge
Merge	Bubble	Bubble
Selection	Selection	Selection

SORT 1: BUBBLE

2: MERGE

3: SELECTION

CS50 Section 3