On the Learning Parity with Noise Problem

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Cryptography schemes

- address the security of communication across an insecure medium
- are usually based only on complexity assumptions (standard model)

- Problem: What if someone constructs large quantum computers
- Cryptography world may fall apart:

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Schemes that are believed to resist classical & quantum computers

- Code-based cryptography
- Lattice-based cryptography

Our contribution

We investigate about the Learning Parity with Noise (LPN) problem
 We propose a Threshold Public Key Encryption scheme based on LPN

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- Dimension ℓ (security parameter), $q \gg \ell$, $\tau \in \left(0, \frac{1}{2}\right)$
- Search: find $s \in \mathbb{Z}_2^{\ell}$ given "noisy random inner products"

Errors
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, i.e. $\Pr(e_i = 1) = \tau$

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Hardness of LPN

The best known attacks against search LPN problem takes

- $2^{\Theta(\ell/\log \ell)}$ having the same number of samples q
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where ℓ is the security parameter

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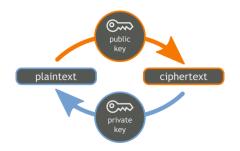
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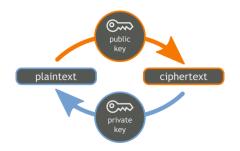
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Solution: Threshold PKE

- The secret key is split into shares and each share is given to a group of users.
- users can decrypt or sign only if enough, a threshold, cooperate

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A Threshold Public-Key Encryption scheme which is:

based on LPN

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- based on LPN
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Key Generation

The receiver R chooses

- a secret key $s \xleftarrow{R} \mathbb{Z}_2^{\ell}$
- $A \stackrel{R}{\leftarrow} \mathbb{Z}_2^{q \times \ell}$ and the error $e \leftarrow \operatorname{Ber}_{\tau}^q$, where $\tau \in \Theta(\frac{1}{\sqrt{\ell}})$ and computes the pk as $(A, b = As \oplus e)$

Encryption of a message bit $m \in \mathbb{Z}_2$

Sender S

Receiver R

choose a vector
$$f \leftarrow \operatorname{Ber}_{\tau}^q$$
 compute $u = f \cdot A$
$$c = \langle f, b \rangle \oplus m \qquad \underbrace{(u, c)}_{}$$

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Decryption

The receiver R computes $d = c \oplus \langle s, u \rangle$

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Decryption

The receiver R computes $d = c \oplus \langle s, u \rangle = \cdots = \langle f, e \rangle \oplus m$

- Key Generation
- Key Assembly
- Encryption
- Partial Decryption
- Finish Decryption



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Key Generation

- All the receivers share a matrix $A \stackrel{R}{\leftarrow} \mathbb{Z}_2^{q \times \ell}$
- Each receiver R_i indipendently choose a secret key $s_i \xleftarrow{R} \mathbb{Z}_2^{\ell}$ and an error $e_i \leftarrow \operatorname{Ber}_{\tau}^q$
- the public key for $\mathtt{R_i}$ is the pair $(A,b_i=As_i\oplus e_i)$

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Key Assembly

The combined public key is the pair (A, b), where

$$oldsymbol{b} = igoplus_{i \in I} oldsymbol{b}_i$$

and I is the users subset

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Receivers R_i, R_j

$$(\textit{\textbf{C}}_{1},\textit{\textbf{c}}_{2}) \leftarrow \texttt{ThLPN}.\texttt{Enc}(\textit{m},\textit{\textbf{b}})$$

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Encryption function (Alekhnovich scheme)

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Receiver $\underline{\mathtt{R_i}}$

$$d_i \leftarrow \texttt{ThLPN.Pdec}(\mathit{C}_1, \mathit{c}_2, \mathit{s}_i)$$



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A semi-honest party:

- 1 Follows the protocol properly
- 2 Keeps a record of all its intermediate computations

Security

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Decryption: from the LPN hardness assumption, as each R_i is generating LP samples

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- Problem: if the same message is encrypted multiple times then it is possible to recover information about the secret key from the ciphertexts

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- relation between standard LPN and some variants
- Does LPN with noise rate τ imply anything about LPN with $\tau' < \tau$? Is there a threshold?
- how to get some basic primitives from standard LPN?

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