

Derivative

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The Derivative

Definition

The Derivative is the rate of change of function $f(x)$ with respect to an independent variable (x) .
It's the slope of the tangent line at a point x

$$\frac{df}{dx} = \lim_{\Delta x \rightarrow 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

Example :

$$f(x) = x^2$$

$$\frac{df}{dx} = \lim_{\Delta x \rightarrow 0} \frac{(x + \Delta x)^2 - x^2}{\Delta x}$$

$$\lim_{\Delta x \rightarrow 0} \frac{x^2 + 2x\Delta x + (\Delta x)^2 - x^2}{\Delta x}$$

$$\lim_{\Delta x \rightarrow 0} \frac{2x\Delta x}{\Delta x} + \frac{(\Delta x)^2}{\Delta x}$$

$$\lim_{\Delta x \rightarrow 0} 2x + \Delta x$$

$$\lim_{\Delta x \rightarrow 0} 2x$$

Power law: derivative of $f(x) = x^n = nx^{n-1}$

Chain law: Two function $f(x), g(x)$ $\frac{d}{dx} f(g(x)) = \frac{df}{dg}(g(x)) \cdot \frac{dg}{dx}(x) = f'(g(x)) \cdot g'(x)$

Example:

$$f(x) = \ln(x)$$

$$g(x) = x^3$$

$$f(g(x)) = \ln(x^3)$$

$$f'(g(x)) = 3 \ln(x^3) x^2$$

Links

- [Identities](#)