

# Forest Cover Type Classification using AdaBoost

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# 1 Introduction

Starting from the Forest Cover Type Dataset, the aim of this project is to train seven binary classifiers (one for each of the classes in CoverType) and use them to make multi-class predictions, with the one-vs-all encoding technique. To do so we will implement AdaBoost algorithm from scratch and we will run it using Decisions Stumps. We will then use external cross-validation to evaluate the multiclass classification performance (zero-one loss) for different values of the number  $T$  of AdaBoost rounds and the hyperparameters tuning to determine the optimal number of Adaboost rounds ( $T$ ) and the learning rate.

The dataset contains tree observations from four areas of the Roosevelt National Forest in Colorado, including information on tree type, shadow coverage, distance to nearby landmarks, soil type, and local topography. The aim is to correctly predict to which of the seven classes each tree belongs.

To solve this problem of classification and make predictions, we implemented AdaBoost from scratch and we run it using decision stumps. To implement the algorithm we used the software Python, whereas to clean the dataset and for the pre-processing of data we used the software R.

## 2 State of art

Today, machine learning is the premise of big innovations and promises to continue enabling companies to make the best decisions through accurate predictions. But what happens when the error susceptibility of these algorithms is high and unaccountable? In these case, the so called *Ensemble Learning* will help us improving our base classifier algorithm.

In the next lines we will see what are Ensemble Learning, how are they implemented and in particular we will focus on the method called *AdaBoost Classifier*, the one used for the current project of classification.

Before to underline the approach to Ensemble method, it is important to understand which type of base classifier we will use to make our first *base* predictions. An ensemble method works as boosting algorithm that helps with the improvement of a less efficient one. In this case our AdaBoost algorithm ensemble method will improve the base classifier

### 2.1 Decision Stump and Decision Tree

The decision tree is a method of supervised learning used both for regression and classification. Each tree is made up of nodes and leaves. The nodes are the places where data, based on some conditions, are splitted; whereas the leaves are the places where data ends after the splitting. In each tree, the nodes are tagged with tests and the leaves are tagged with labels. The aim is to obtain the features for which we obtain the best split, and to do so we can use Gini function (it refers to Gini impurity) or Scale Entropy (it refers to Information Gain).

A decision stump is a one-level decision tree, that means that it only has one node and two leaves. It is weak learner.

Decision stump is one of the most straightforward classification algorithms. It is a binary classification algorithm with the idea of Only focus on one feature each time and find a point that can separate data the most. Binary classification is for classifying two categories, such as 0 and 1.

We can write the equation as follows:

$$H = \{h_{a,c} : a \in \mathbb{R}, c \in \{+1, -1\}\}$$

$$h_{(a,c)}(x)\{c = -1 \text{ if } x \leq a, c = 1 \text{ if } x > a\}$$

We need to find one number ( $a$ ). If the input value is larger than  $a$ , we classify it as 1. If it is smaller or equal to  $a$ , we classify it as -1. Our goal is to find the best number to classify our training data the most.

In reality, we can barely find a point that can perfectly separate the data. Therefore, we need a way to measure the performance. The most elementary way is to calculate the total point that we classify wrong.

$$E_{in} = \frac{\sum_n^N [y_n \neq \hat{y}_n]}{N}$$

We can also evaluate the purity of the two subgroups using the **Gini Index**.

$$1 - \sum_{k=1}^K \left( \frac{\sum_n^N [y_n = k]}{N} \right)^2$$

If two subgroups are entirely pure, the Gini index will be 0.

Last, **Entropy** is another evaluation method of the threshold's performance. Entropy is an information theory metric that measures the impurity or uncertainty in a group of observations. It can be calculated as follows:

$$E = - \sum_{i=1}^N p_i \log_2 p_i$$

where  $p_i$  is the probability of randomly selecting an example in class  $i$ .

As far as Entropy refers to **Information Gain**, we need to introduce also this last metric. We can define information gain as a measure of how much information a feature provides about a class. Information gain helps to determine the order of attributes in the nodes of a decision tree.

The main node is referred to as the parent node, whereas sub-nodes are known as child nodes. We can use information gain to determine how good the splitting of nodes in a decision tree.

It can help us determine the quality of splitting, as we shall soon see. The calculation of information gain should help us understand this concept better.

$$Gain = E_{parent} - E_{children}$$

The term Gain represents information gain.  $E_{parent}$  is the entropy of the parent node and  $E_{children}$  is the average entropy of the child nodes.

## 2.2 Ensemble methods

Ensemble methods are techniques that create multiple models and then combine them to produce improved results. Ensemble methods usually produce more accurate solutions than a single model would.

In the state of art there exist several Ensemble Methods, the most popular are: voting, stacking, bagging and boosting. In the next lines, we will underline the last one, the Boosting Ensemble Method, because of the usage in the project of the AdaBoost, one of the main ensemble methods in the class of boosting technique.

The term 'boosting' is used to describe a family of algorithms which are able to convert a base classifier to strong models. The classifier is weak if it has a substantial error rate, but the performance is not random (resulting in an error rate of 0.5 for binary classification). Boosting incrementally builds an ensemble by training each model with the same dataset but where the weights of instances are adjusted according to the error of the last prediction. The main idea is forcing the base classifier to focus on the instances which are hard.

### 2.2.1 AdaBoost

AdaBoost (adaptive boosting) is one of the main boosting algorithm. This method combine a weak learners (in our case decision stumps) to make classification and each of the stumps is made made by taking the previous stump's mistakes into account.

Boosting is an ensemble method, so it combines results of multiple models in such a way that together they will perform much better than each individual. In particular, with boosting techniques, training gives more importance to the data that was miss-classified by the previous models and to decide the output, a weighted voting is needed.

AdaBoost has been designed for solving two-class classifications problems, where the goal is to classify each example in one of the two classes. To pass from two-class to multi-class classification problems with AdaBoosting, the most used techniques reduce the multi-class problems into multiple binary-class problems. Nevertheless it is possible to extend the AdaBoost algorithm to the multi-class case without reducing it to multiple two-class problems.

### 2.3 External Cross-Validation & Hyperparameters Tuning

The external cross-validation is used to evaluate the goodness of a learning algorithm. Assuming the hyperparameters fixed, the aim is to estimate

$$\mathbb{E}[l_D(A)]$$

To do so we can use a technique called K-fold (external) cross-validation.

We start partitioning our entire dataset,  $S$ , in  $K$  subsets (the so called 'folds')  $D_1, \dots, D_K$  of size  $m/K$  each (where  $m$  is the total number of observations). Let's define  $S^{(i)} \equiv S/D_i$ , we will have that  $D_i$  is our *testing part* of the  $i$ -th fold while  $S^{(i)}$  is the *training part*.

In order to get the information more clear in the conceptual part, we will make an example. If we partition  $S = \{(x_i, y_1), \dots, (x_{20}, y_{20})\}$  in  $K = 4$  subsets

$$\begin{aligned} D_1 &= \{(x_1, y_1), \dots, (x_5, y_5)\} & D_2 &= \{(x_6, y_6), \dots, (x_{10}, y_{10})\} \\ D_3 &= \{(x_{11}, y_{11}), \dots, (x_{15}, y_{15})\} & D_4 &= \{(x_{16}, y_{16}), \dots, (x_{20}, y_{20})\} \end{aligned}$$

then  $S^{(2)} = \{(x_1, y_1), \dots, (x_5, y_5), (x_{11}, y_{11}), \dots, (x_{20}, y_{20})\}$ .

The  $K$ -fold CV estimate of  $\mathbb{E}[l_D(A)]$  on  $S$ , denoted by  $l_S^{CV}(A)$ , is then computed as follows:

we run  $A$  on each training part  $S^{(i)}$  of the folds  $i = 1, \dots, K$  and obtain the predictors  $h_1 = A(S^{(1)}), \dots, h_K = A(S^{(K)})$ . We then compute the (rescaled) errors on the testing part of each fold,

$$l_{D_i}(h_i) = \frac{K}{m} \sum_{(x,y) \in D_i} l(y, h_i(x))$$

Finally, we compute the CV estimate by averaging these errors

$$l_S^{CV}(A) = \frac{1}{K} \sum_{i=1}^K l_{D_i}(h_i)$$

So, intuitively, cross-validation consist in using a limited sample (the training set) to estimate how well the learning algorithm will perform, in general, when used to make predictions based on data different from the ones contained in the training set.

As far as tuning hyperparameters concerned, we face the problem of finding the best parameters so to obtain a predictor with small risk. This is typically done by minimizing a risk estimate computed using the training data. As  $\Theta$  may be very large, possibly infinite, the minimization is generally not over  $\Theta$ , but over a suitably chosen subset  $\Theta_0 \subset \Theta$ . If  $S$  is our training set, then we want to find  $\theta^* \in \Theta_0$  such that:

$$l_D(A_{\theta^*}(S)) = \min_{\theta \in \Theta_0} l_D(A_{\theta}(S))$$

The estimate is computed by splitting the training data in to two subset  $S_{train}$  and  $S_{dev}$ . The development set  $S_{dev}$  is used as surrogate test set. The algorithm is run on  $S_{train}$  once for each value of the hyperparameter in  $\Theta_0$ . The resulting predictors are tested on the dev set. In order to obtain the final predictor, the learning algorithm is run once more on the original training set  $S$  using the value of the hyperparameter corresponding to the predictor with smallest error on the validation set.

### 3 Data

The dataset Forest Cover Type contains 581012 records (each one represents a tree) and 55 columns.

The label set  $Y$  is defined as  $Y = \{1,2,3,4,5,6,7\}$  and represent by the variable *CoverType*, which contains the seven classes of trees located in the Roosevelt National Forest.

There are 54 input (prediction) variables, that represent some characteristics of the trees, location and the soil in which are planted. More in detail, these features are: *Elevation*, *Aspect*, *Slope*, *Horizontal Distance to Hydrology*, *Vertical Distance to Hydrology*, *Horizontal Distance To Roadways*, *Hill shade (9 am)*, *Hill shade (Noon)*, *Hill shade (3 pm)*, *Horizontal Distance to Fire Points*, *4 areas of Wilderness* and *40 types of soil*.

The goal is to find a classification rule from the training data, so that when we give a new input we can assign it a class label from  $\{1,2,3,4,5,6,7\}$ .

#### 3.1 Descriptive analysis of variables

Using the *describe* (or *summary*) command in R, we obtained a quick descriptive analysis of the dataset. Already looking at the results of this analysis we pointed out that there are no NULL values (for each variable we have 581012 observations), there are no missing values and the variables are all numeric. The first ten variables are continuous variables, whereas the other ones are categorical features.

In the following table are summarized the descriptive statistics for the first 10 variables (continuous variables):

	vars	n	mean	sd	median	trimmed	mad	min	max	range	skew	kurtosis	se
Elevation	1	581012	2959.37	279.98	2996	2983.39	259.46	1859	3858	1999	-0.82	0.75	0.37
Aspect	2	581012	155.66	111.91	127	150.10	126.02	0	360	360	0.40	-1.22	0.15
Slope	3	581012	14.10	7.49	13	13.49	7.41	0	66	66	0.79	0.58	0.01
Horizontal_Distance_To_Hydrology	4	581012	269.43	212.55	218	243.88	197.19	0	1397	1397	1.14	1.37	0.28
Vertical_Distance_To_Hydrology	5	581012	46.42	58.30	30	37.56	40.03	-173	601	774	1.79	5.25	0.08
Horizontal_Distance_To_Roadways	6	581012	2350.15	1559.25	1997	2203.24	1541.90	0	7117	7117	0.71	-0.38	2.05
Hillshade_9am	7	581012	212.15	26.77	218	215.09	23.72	0	254	254	-1.18	1.88	0.04
Hillshade_Noon	8	581012	223.32	19.77	226	225.11	17.79	0	254	254	-1.06	2.07	0.03
Hillshade_3pm	9	581012	142.53	38.27	143	143.36	37.06	0	254	254	-0.28	0.40	0.05
Horizontal_Distance_To_Fire_Points	10	581012	1980.29	1324.20	1710	1797.61	1111.95	0	7173	7173	1.29	1.65	1.74

Figure 1: Descriptive statistics

An interesting thing to notice is that the variable *Vertical Distance To Hydrology* takes negative values (as the minimum value is -179). As this variable is defined as a distance (*vertical distance to nearest surface water features*), and distances take only positive values, it does not make so much sense. A possible explication to this fact is that the nearest hydrology point is below the tree, so it takes negative values because the nearest hydrology point is below the sea level.

The categorical features refer to the belonging of the tree to a Wilderness Area (there are 4 wilderness areas) and the Type of Soil (there are 40 soil types). These categorical features are encoded with the *One Hot Encoding* technique, so they take value 1 if the tree belongs to the wilderness area/type of soil, or 0 if it does not.

Speaking about the response variable, Cover Type, there are different number of observations for each of the seven classes. Most of the observations are in the second (48.76%) and in the first (36.46%) class. The other classes have lower number of observation,

in particular the third class contains 6.15% of the total observations, followed by the seventh class (3.53%), the sixth class (2.99%), the fifth class (1.63%) and the fourth class (0.47%). The dataset in this case result to be unbalance and this could lead to lower effectiveness of the algorithm, especially when predicting minority classes. Having unbalanced classes could be misleading when it comes to evaluate the accuracy of an algorithm, because we could obtain high accuracy without actually making useful predictions. In this case confusion matrices perform better since they better summarize the performance of a classification algorithm.

Given the fact that we have an unbalanced dataset (the classes are not represented equally), measuring the performance of our model with accuracy could lead to misleading results. With imbalanced classes, it's easy to get a high accuracy without actually making useful predictions. So, we could follow two path:

1. Re-sample the dataset using under-sampling or over-sampling techniques. The former technique removes samples from over-represented classes whereas the latter add more samples from under-represented classes.
2. Use metrics obtained from confusion-matrix (e.g. F1 weighted, precision weighted, recall weighted, Matthews Correlation Coefficient), in this way we can summarize the performance of a classification algorithm, even if the dataset is unbalanced.

We decided to follow the second path, leaving the dataset unbalanced.

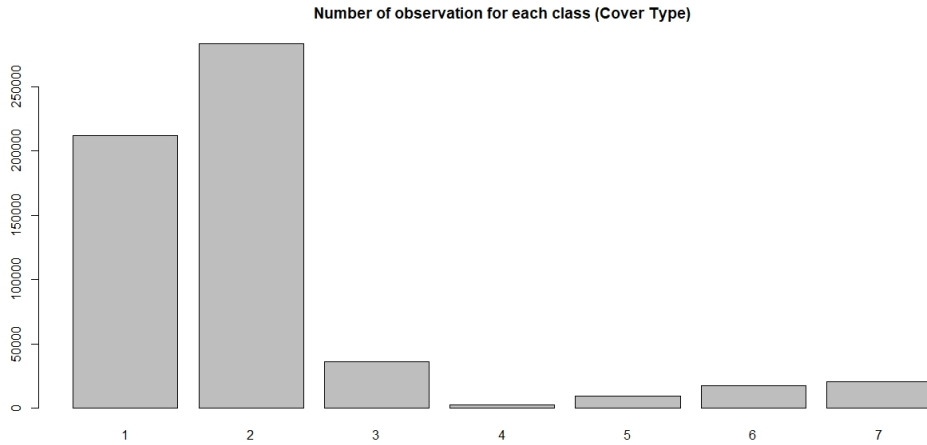


Figure 2: Number of observation for each class (Cover Type)

### 3.2 Outliers

To detect the presence of outliers we used the interquartile rule and the related visual tool (the box plot). Following this rule we define as extreme outliers the values that are below the lower limit and the values that are above the upper limit. We considered extreme outliers the observations which are more than 3 times the interquartile range below the first quartile or above the third quartile.

$$\text{lower limit} = Q1 - (3 \times IQR)$$

$$\text{upper limit} = Q3 + (3 \times IQR)$$

Where  $Q1$  represent the first quartile,  $Q3$  represent the third quartile and  $IQR$  represent the interquartile range ( $Q3 - Q1$ ).

Each of the 7 classes contain different types of trees, so when it comes to detect the presence of outliers in the 10 continuous variables we should group the observations by the CoverType.

We pointed out that there are 8963 extreme outliers in total. The following table summarizes the distribution of the outliers in the continuous variables grouped by CoverType.

Variable Name	1	2	3	4	5	6	7
Elevation	0	0	0	0	0	0	360
Aspect	0	0	0	0	0	0	0
Slope	96	63	0	0	0	0	33
Horizontal Distance To Hydrology	0	377	0	0	41	0	0
Vertical Distance To Hydrology	2293	3511	0	0	0	7	4
Horizontal Distance To Roadways	0	0	0	0	0	0	0
Hillshade 9am	411	610	0	0	0	3	12
Hillshade Noon	430	296	0	0	12	1	89
Hillshade 3pm	0	0	0	0	0	0	0
Horizontal Distance To Fire Points	0	19	0	0	295	0	0

Most of the outliers are in the class type 1 and 2, but it is mainly due to the fact that most of the observations are concentrated in these two classes. If we look at the proportion of outliers for each class it is possible to notice that the class with the higher number of outliers (in proportion) is the fifth (with 3.67% of outliers on the total), followed by the second (with 1.72% of outliers on the total) and the first (with 1.52% of outliers on the total) classes. The classes 3 and 4 do not present any outlier. These results are graphically represented with the barplot in Figure 3. As is it possible to notice from the

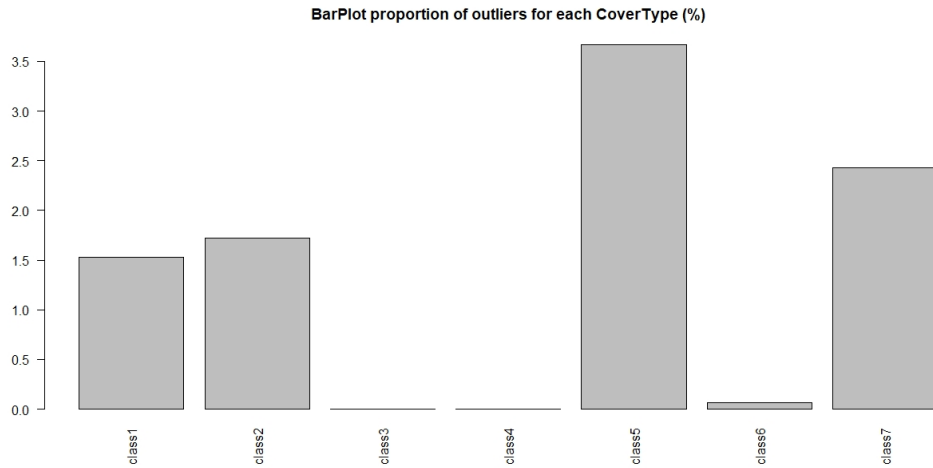


Figure 3: BarPlot: Proportion of outliers for each class (%)

table above, the variables with the higher number of outliers are *Vertical Distance To Hydrology* and *Hillshade 9am*. So, we take a look at the boxplots of these two variables to see how the outliers are distribute and how severe they are.



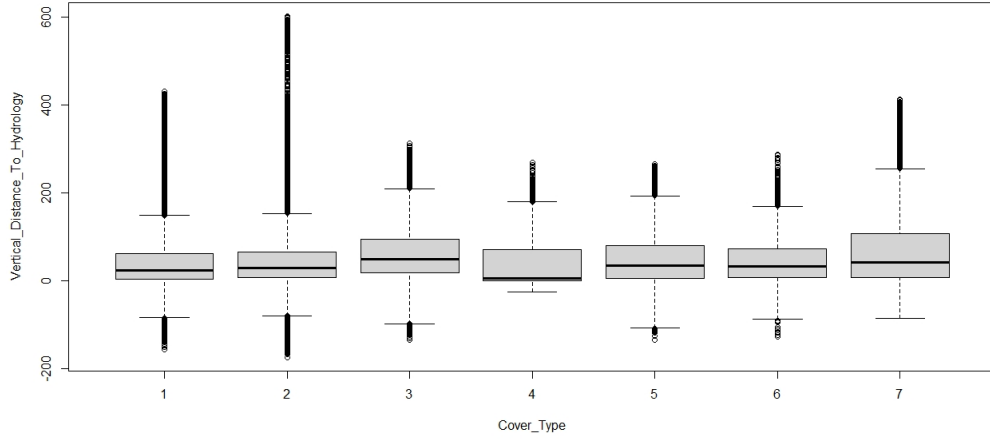


Figure 4: BoxPlot Vertical Distance To Hydrology

As we can notice from Figure 4, most of the outliers are in the first and second class type. Moreover, for these two classes the outliers seems largely out from the whiskers.

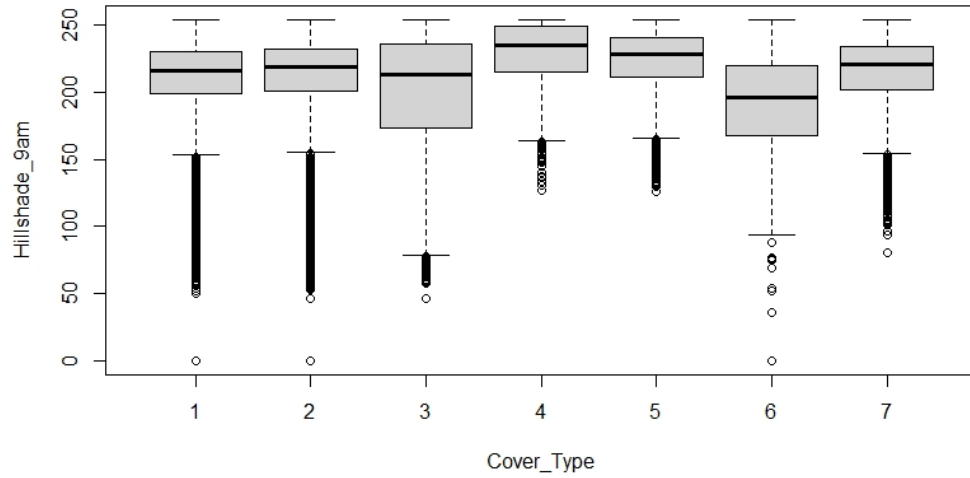


Figure 5: Boxplot Hillshade 9am

In Figure 5 we can notice how, also in this case most of the outliers are for the first and second class type. This is mainly due to the fact that most of the observations are in these two classes.

We decided to proceed dropping all the records containing extreme outliers, obtaining a new dataset with 572627 observations. With this operation we lose 8385 observations (1.44 % of observations), which is not a relevant quantity given the large number of observation that we have in this dataset.

### 3.3 Distributions and standardization

Taking a look to the distributions of the continuous variables (Figure 6) it is possible to notice that the variables are not normally distributed and in particular we are dealing with out-of-scale quantities. Scaling is particularly useful when dealing with distance-based algorithms, because they are using distances between data points to determine their similarity. On the other hand, it has not a big effect on tree-based algorithms as the decision tree splits a node on a feature that increases the homogeneity of the node. As we will deal with tree-based algorithms (Decision Stumps), we decided to do not rescale the variables, as this worsen the accuracy of our predictions.

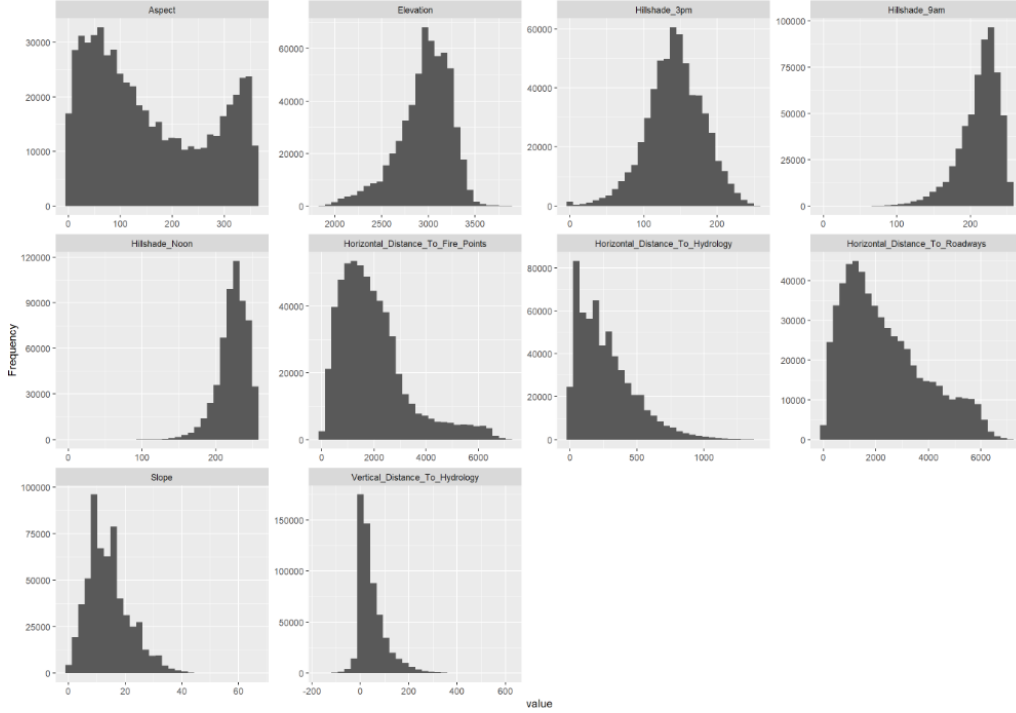


Figure 6: Distributions

### 3.4 Correlation

We now proceed analyzing the relationship between the ten continuous variables. We calculated the correlation between the continuous variables and we plot them with the following heatmap (Figure 7).

From Figure 7 it is possible to notice that there is a strong negative correlation (-0.79) between *Hillshade 9am* and *Hillshade 3pm*. This makes sense because the sun at 9am is on the opposite side with respect to the position of the sun at 3pm, so the shade of the hill at 9am will be the opposite than the one at 3pm. There is no correlation between *Hillshade 9am* and *Hillshade Noon*, whereas there is a strong positive correlation (0.6) between *Hillshade 3pm* and *Hillshade Noon*.

It is also interesting to notice that the correlation between CoverType and the continuous variables is very weak. There is almost no correlation between CoverType and Aspect, Hillshade 9am and Hillshade 3pm. The variable most correlated with CoverType is Elevation, with which it has a negative correlation (-0.27): the last classes (eg. class types 6 and 7) have lower values for the variable Elevation (we expect that the trees in the last classes are lower than the ones in the first classes).

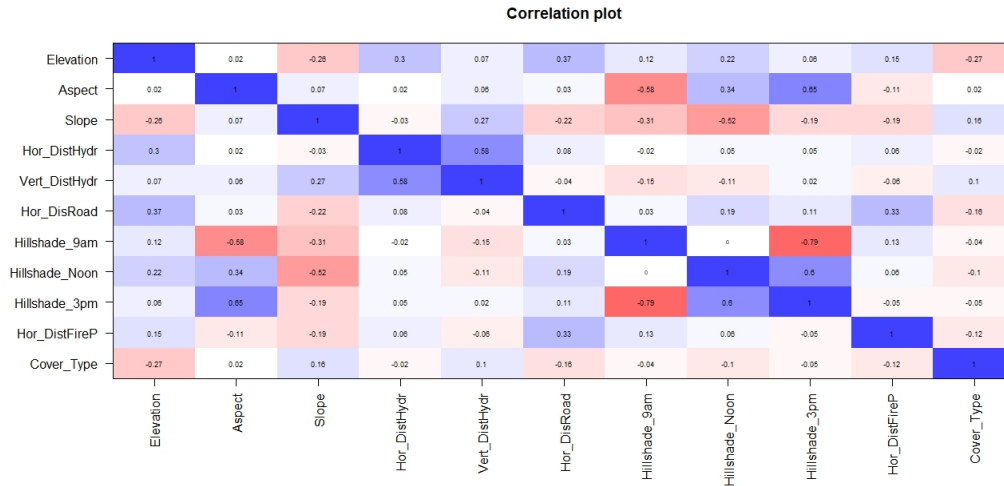


Figure 7: Correlation Plot (continuous variables)

## 4 Implementation and methodology

In order to create a classification algorithm from scratch we will introduce different classes of object and different function with different functionalities.

As we know, the main algorithm in this project is the AdaBoost classifier, but, as other ensemble method, it needs a base classifier from where to start: in this case the base classifier is a decision stump, a.k.a. Decision Tree with depth equal to 1.

In the following subsection we will explain how we create the 2 algorithms:

- Decision Stump
- AdaBoost

### 4.1 Decision Stump function

As we have previously introduced, Decision Stump algorithm is the base classifier that lets the AdaBoost work, in fact, in our case, we create a class object *Decision Stump* with one simple function, the *predict* function.

At every round of the Adaboost, the predict function will create from the root, two leaf according to the threshold that the ensemble method extracts. If the column value is lower than the threshold, the row will be predicted as  $-1$ , otherwise it will be predicted as  $1$ . This type of algorithm is very very simple and sometimes could not work so well because of the depth of the decision tree. Despite of that, the issue is partly solved by the AdaBoost that will improve the classification task.

With this type of algorithm we can only predict a binary response variable and in order to do that, for each of the 7 classes, we will make a one vs all prediction. What does that mean? Basically, for each class, we predict the tested class as  $1$  and all the other as  $-1$ . In our example we will have this differentiation among the 7 cover type's classes (e.g.  $1 = 1, -1 = [2, 3, 4, 5, 6, 7]$ ).

### 4.2 AdaBoost function

The core part of the coding part is the *AdaBoost* class. We have already explained how it works and consequently I will not deep dive the theoretical concepts in this section. As for the *Decision Stump*, also in this case it has been created an *AdaBoost* class; the

difference with the base classifier class is the presence of one more function, the *fit* function, and the presence of one parameter that *Adaboost* takes as input.

Let's follow the order of the script, **fit** function. The objective of this function is to fit the model, already split into train and test set, with a Decision Stump as base classifier. First of all we initialized the weights to  $w_i = \frac{1}{N}$ ; after that, we start the iteration through classifiers. At the beginning we mentioned the number of AdaBoost rounds, the number of classifier to use, and in this function we repeat the process until the  $T$  round is reached. The process is the following: we make a greedy search to find the best threshold and feature, how we do that? We go in each column and for every unique value of the column selected, we make some basic prediction of 1 and -1 whether the record is lower or greater than the threshold (unique value). Once we do that, we define an error as  $error = \sum w_i[\hat{y}_i \neq y_i]$  and, if the error is greater than 0.5 we invert the prediction and the error becomes  $1 - error$ . Why? As far as this is a greedy research of the best configuration and as far as we have only a binary classification, if the error is greater than 0.5 means that we misclassified more than 50% of the records; inverting the polarity (from 1 to -1) we also have more correctly classified record and a lower error rate than before.

At the end of each round, we store a new threshold and a new feature only if the error of the round before was higher. When the error is defined as the best one for that Decision Stump, we upgrade the weights ( $w_i$ ), we normalize them to one and we go to the next base classifier (next round). At the end of round  $T$  we finish our fitting method and we can proceed with the next function, the *prediction* function, that will need the final weight  $w_i$  and the final alpha  $\alpha_i$  (all metrics explained before).

The **prediction** function is the last function of our algorithm, it has the objective of making the final prediction of our binary classification.

The function takes as input only the test set, and uses the previously stored greedy prediction,  $\alpha_i$  and  $w_i$  in order to make the final prediction  $\hat{y}_i$ .

As far as this classifier works with a *sign* function, we will have 7 final continuous  $\hat{h}$ , one for each 'one vs all' classifier. Of course we can evaluate our model for every binary prediction, but, the aim of the project is a multiclass classification, and in order to satisfy this problem, we will predict our final  $\hat{y}$  as the sign of the greatest final continuous prediction ( $\hat{h}$ ).

With this final result, we have completed the AdaBoost classifier from scratch using a Decision Stump as base classifier.

### 4.3 Hyperparameters tuning and External Cross Validation

Before to present the results of the project, we need to define hyperparameters (in this case we will see only the  $T$  rounds of AdaBoost as hyperparameters) and to apply external cross validation to get more accurate findings.

#### 4.3.1 Hyperparameters tuning

The  **$T$  rounds of Adaboost** are the number of base classifier that we want to tune before to make prediction on the test set. The idea is that, as we increase  $T$ , the evaluation metrics improve. Unfortunately we don't have machine with such a computing power to fulfill our desire, but, as far as from the next plot we can see, after the 100th round of Adaboost the evaluation metrics decline. We tuned this hyperparameter fixing temporarily the learning rate = 0.5. We will use  $T = 100$  round of Adaboost to train our model, as it is the value that return the better results in terms of evaluation matrix. In Figure 8 we displayed how the evaluation metrics behave given different values for  $T$ .

The second hyperparameter tuned is the **Learning Rate**, that controls the loss function

used for calculating the weight of the base models. We pointed out that the learning rate that improve our metrics is  $= 0.6$ , as it is possible to notice from Figure 9, where we displayed how the evaluation metrics change given different learning rates.

There is a trade-off between the learning rate and the number of rounds, as increasing the learning rate the estimators have an higher weight so owe need less of them. We finally decide to set the test size  $= 0.2$  (train size  $= 0.8$ ). This latter parameter is defined as constant during the all project.

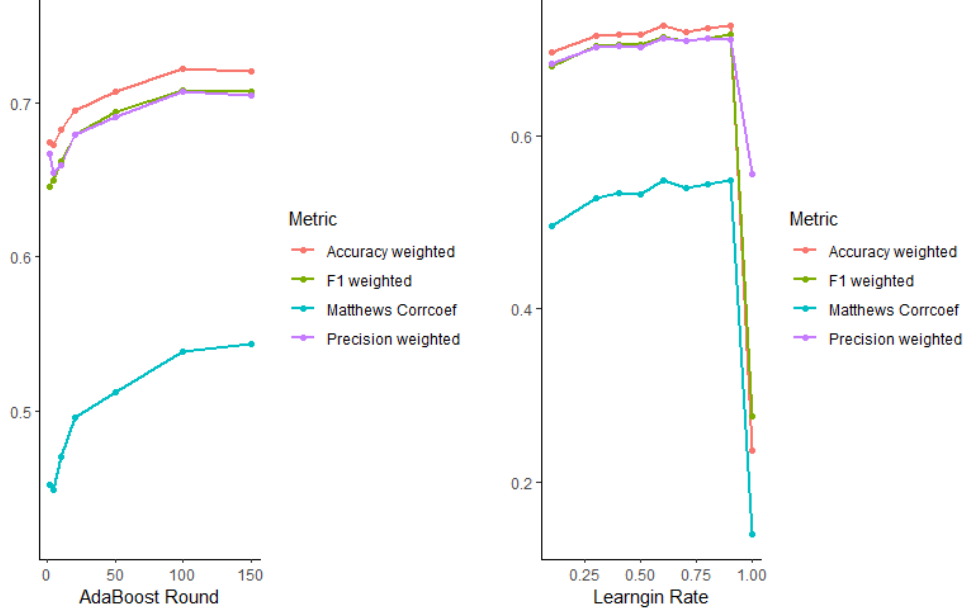


Figure 8: Hyperparameters tuning

#### 4.3.2 External Cross Validation

During the implementation of external cross validation we assume as fixed the hyperparameters ( $T$  rounds) and the goal is now to test the model on different training and validation set in order to see whether the model fits good despite the random sampling of the initial training set.

At each  $k$  folder of the cross validation, we will have an efficiency metric as output (in our case will be the accuracy) and at the end we will find the average accuracy as quality metric of the trained model. Theoretically, once we predict the response feature of the test set, we will find a similar accuracy to the average one, found with the external cross validation.

It is fundamental to choose in the right way the number of splits  $K$ , because choosing a wrong  $K$  could result in a mis-representative idea of the skill of the model. To balance the bias-variance trade-off associated with the choice of  $K$  in  $K$ -fold cross-validation, it has been shown empirically that using  $K = 5$  (or  $K = 10$ ), yield test error rate estimates that suffer neither from excessively high bias nor from very high variance.

## 5 Results

In conclusion of this project we show below the results obtained with the algorithm developed.

As far as the classification problem concerned we summarized our outcomes starting from a confusion matrix. In our case the classification matrix sums up on the diagonal the correctly classified observations, while on the other cells the miss-classified ones; in particular, each row represent the actual classes while the columns represent the predicted labels.

In order to read and describe in a more comprehensive way the matrix, we calculate some evaluation metrics that help with the understanding of the results. In particular we define the accuracy (weighted) as

$$accuracy(weighted) = \frac{\sum_{k=1}^K \frac{TP}{Total_{row_k} \times w_k}}{K \times W}$$

the Macro F1 score as

$$MacroF1Score = 2 \times \left( \frac{MacroAveragePrecision \times MacroAverageRecall}{MacroAveragePrecision^{-1} + MacroAverageRecall^{-1}} \right)$$

the Macro Average Precision as

$$MacroAveragePrecision = \frac{\sum_{k=1}^K Precision_k}{K}$$

where

$$Precision_k = \frac{TP_k}{TP_k + FP_k}$$

the Macro Average Recall as

$$MacroAverageRecall = \frac{\sum_{k=1}^K Recall_k}{K}$$

where

$$Recall_k = \frac{TP_k}{TP_k + FN_k}$$

and finally the Matthews Correlation Coefficient as

$$MCC = \frac{c \times s - \sum_k^K p_k \times t_k}{\sqrt{(s^2 - \sum_k^K p_k^2)(s^2 - \sum_k^K t_k^2)}}$$

To simplify the definition, it is necessary to consider the following intermediate variables:

- $c = \sum_k^K C_{kk}$  the total number of elements correctly predicted
- $s = \sum_i^K \sum_j^K C_{ij}$  the total number of elements
- $p_k = \sum_i^K C_{ki}$  the number of times that class  $k$  was predicted (column total)
- $t_k = \sum_i^K C_{ik}$  the number of times that class  $k$  truly occurred (row total)

While the firsts metrics vary from 0 (worst) to 1 (best), the latter describe how random our prediction has been. In particular, as every correlation metrics, a value of -1 defines an opposite prediction, a value of 0 defines a random guessing prediction and finally a value of 1 defines a perfect prediction.

Our results for these metrics are written in the table below

Metrics	Values
Accuracy weighted	0.727
F1 weighted	0.714
Precision wighted	0.712
Matthwes Correlation coefficient	0.548

Finally, we present a plot that describes perfectly the prediction that we made, how many correct prediction (HIT), and which wrong predictions were made in which classes. The plot displays the performance on the test set of the algorithm developed. Each class is represented with a different colour and the portion of bar with the wording "Hit" corresponds to the observations correctly classified. As it is possible to see from the graph the first three classes and the seventh class are mostly correctly classified, whereas the fifth class is the worst classified. The fourth and sixth classes are the also fairly well classified.

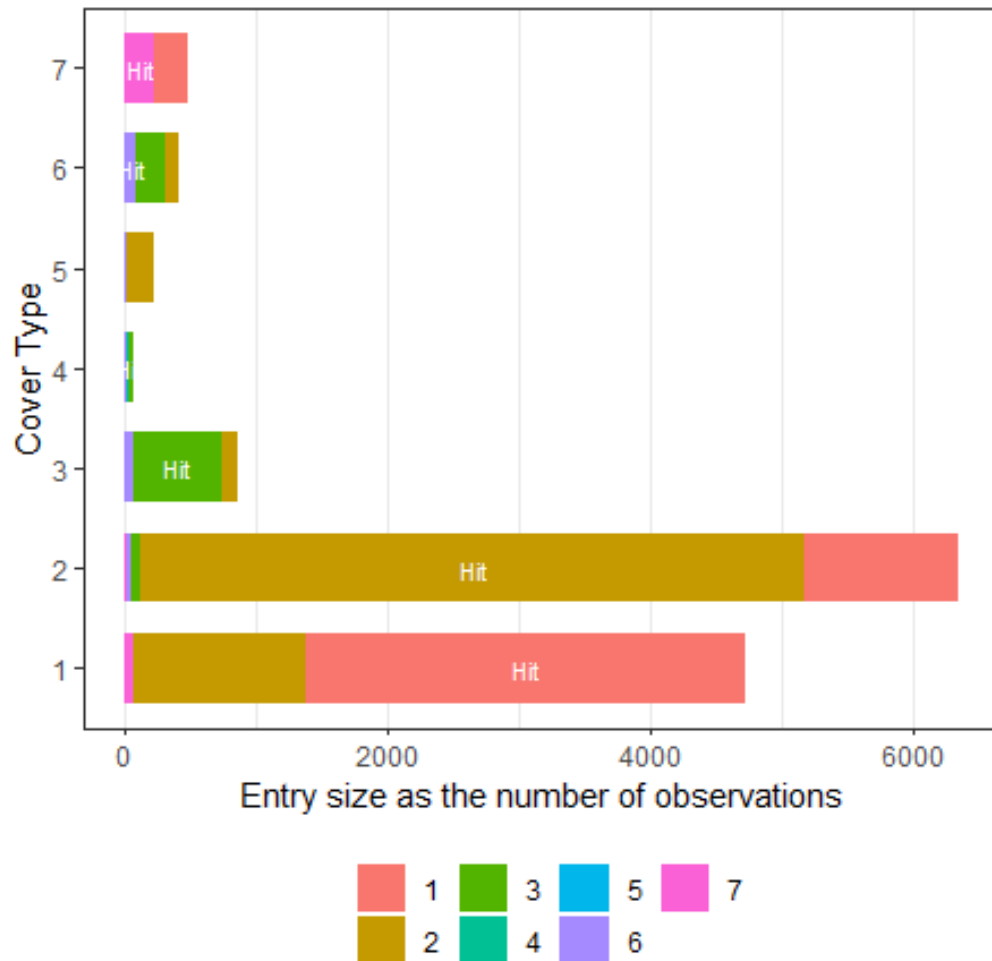


Figure 9: Barplot Confusion matrix

## 6 Conclusions

To sum up, we are satisfied of the results obtained running the AdaBoost algorithm developed from scratch, as most of the observations are correctly classified in the seven classes. The cause of the misclassification of some observation in the less frequent classes can be traced back to the unbalancing of classes, nevertheless the weighted evaluation metrics show good performances.

Moreover, we do not met any problems of over or under-fitting since the evaluations metrics obtained for the training and the test set resulted very close to each other. That last result is obtained also thanks to the fact that in each subset of the dataset, training or validation set, the classes are equally distributed as their original distribution was in the complete dataset. That is a proof of the well dataset's splitting method we used in order to define training validation and test sets. In particular, we can see how the majority classes (1 and 2) are always more present in the different subsets, while the other classes still do not appear as the first two.

In our opinion, one of the main limit of this algorithm is the fact that we are using as 'weak learner' of Adaboost, a decision stump. The decision stump is a tree with depth equal to 1 and as a consequence, could rarely create good split from the roots; in addition, the decision stump can only classified binary label while we are facing a multiclass classification problem. In fact, the tough part of the project has been to move from a binary classification problem to a multiclass classification problem, despite the fact that we successfully solved that issue, we are still using a binary classifier as 'Decision Stump' to make mutliclass predictions.

Comparing our algorithm built from scratch result with the scikit learn's one, we obtained similar values (or also better results from our algorithm). We show the results obtained (on the test set) from the two algorithms in the following table:

Metrics	Our algorithm	ScikitLearn's algorithm
Accuracy weighted	0.727	0.630
F1 weighted	0.714	0.627
Precision weighted	0.712	0.632
Matthews Correlation coefficient	0.548	0.407

The barplot in Figure 10 provide a visual representation of the confusion matrix obtained running the ScikitLearn's algorithm. As in the case of our algorithm, it does particularly well for the majority classes, whereas for the minority classes the classification is not that good. This algorithm perform particularly bad for the fourth class, where all the observations are misclassified, for this class our algorithm perform definitely better. Also for the seventh class our algorithm perform better than the one obtained from ScikitLearn's ones. So, in general, we could say that our algorithm built from scratch works fairly well and in most of the cases produce reliable predictions.



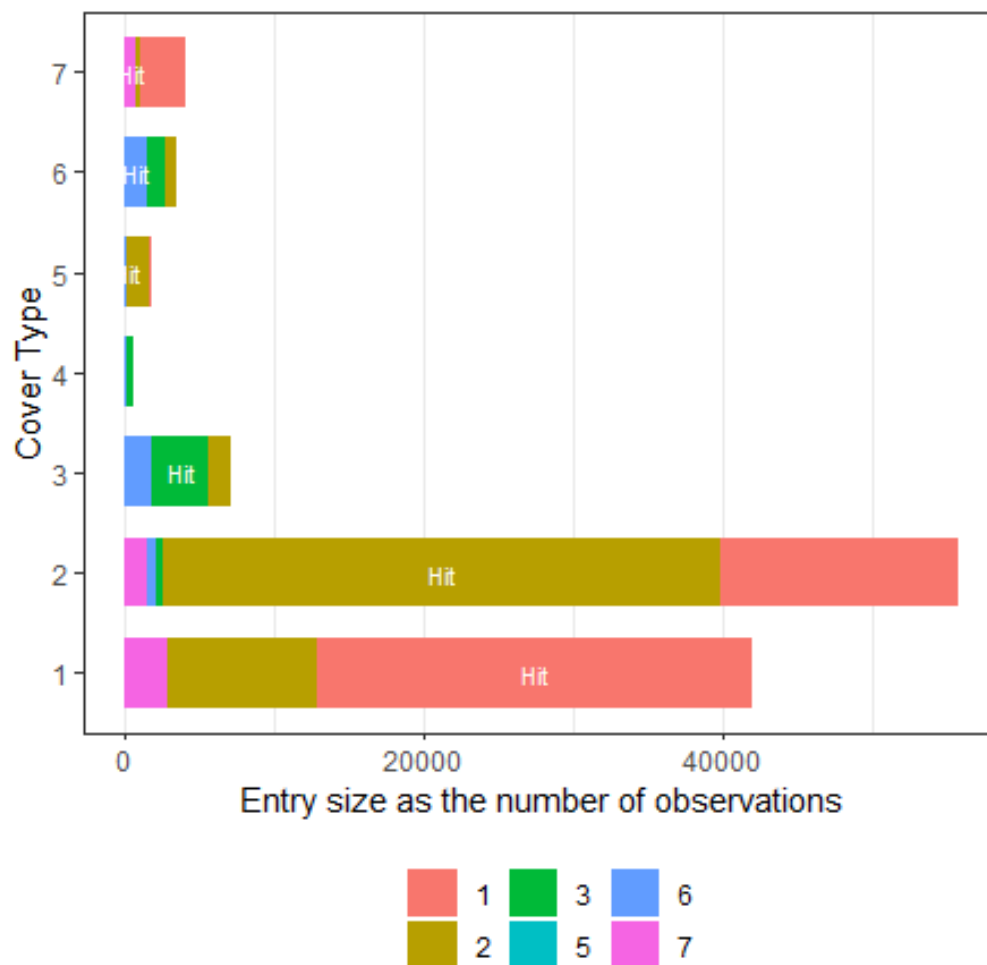


Figure 10: Barplot Confusion matrix ScikitLearn

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