

# SEARCHING FOR NEW PHYSICS IN $b \rightarrow s\ell^+\ell^-$ TRANSITIONS AT THE LHCb EXPERIMENT

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Doctor of Philosophy*



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April 9, 2016



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## ABSTRACT

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Flavour Changing Neutral Currents are transitions between different quarks with the same charge such as  $b \rightarrow s$  processes. These are forbidden at tree level in the Standard Model (SM) but can happen through loop diagrams, which causes the branching ratio of this type of decays to be small, typically  $\sim 10^{-6}$  or less. Particles beyond the SM can contribute in the loops enhancing the branching fractions of these decays, which are therefore very sensitive new physics. In this work two analysis of semileptonic  $b \rightarrow s\ell^+\ell^-$  decays are presented. First,  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decays are analysed to measure their branching fraction as a function of the square of the dimuon invariant mass,  $q^2$ . Furthermore, an angular analysis of these decays is performed for the first time. Secondly,  $B^0 \rightarrow K^{*0}\ell^+\ell^-$  decays are analysed measuring the  $R_{K^{*0}}$  ratio between the muon,  $B^0 \rightarrow K^{*0}\mu^+\mu^-$ , and electron,  $B^0 \rightarrow K^{*0}e^+e^-$ , channels, which is interesting as it is largely free from uncertainties due to the knowledge of the hadronic matrix elements. This thesis is organised in the following way. Chapter 1 introduces the Standard Model and the concept of flavour and explains how rare decays can help us in the quest for physics beyond the SM. Chapter 2 describes the LHCb detector, which was used to collect the data analysed in this thesis. This chapter also includes studies performed to validate the hadronic physics in LHCb simulation software. Chapter 3 deals with the measurement of the differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decay, while Chapter 4 describes its angular analysis. Finally, Chapter 5 reports the measurement of the  $R_{K^{*0}}$  ratio.

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## DECLARATION OF AUTHORS CONTRIBUTION

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I am one of the main authors of the two analysis reported in Chapters 3, 4 and 5. For the analysis of  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decays I collaborated with Michal Kreps, who took care of implementing the decay model to re-weight the simulation and provided simulated samples. Furthermore, I want to thank him for the advice given throughout. The work on this analysis was published and can be found at Ref. [1]. For the  $R_{K^{*0}}$  analysis, described in Ch. 5, I actively participated in most stages of the analysis collaborating with Simone Bifani. In particular I took care of the production of various simulated samples, participated in the definition of the selection, in the yields extraction and I provided a fit and data-reduction framework. Finally, as a service work for the LHCb experiment, I developed the tools used to perform the validation studies described in Sections 2.11–2.13.

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## ACKNOWLEDGEMENTS

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First of all I would like to thank Nigel, who always supported me in these years and granted me many good opportunities. I think I could not hope for a better supervisor. A big ‘thank you’ also to Simone, I think we’ve had a good collaboration for the  $R_{K^{*0}}$  analysis and he taught me a lot. Thanks also to the people of the Birmingham LHCb group: Cristina, Jimmy and the new students and a ‘thank you’ also to Michal, who adopted us, Birmingham students, for a while. A special ‘thank you’ goes to Pete, who shared with me this three years experience. I think it would have been a very different and less interesting experience without him. A ‘thank you’ also goes to the members of the LHCb collaboration and in particular of the Rare Decays Working Group.; in particular to the working group conveners Gaia, Tom and Marco and to Gloria, who patiently guided me through the depths of the LHCb software. A thank you also to the other  $R_{K^{*0}}$  analysts: Marie-Hélène, Martino, Francesco and Sam for the good collaboration. Finally, I’m grateful to Vincenzo and the LHCb Bologna group, who kindly hosted me for a few months and in particular to Umberto for all the wisdom he shared. I want also to thank the LTA folks, who were with me during the long period I spent at CERN and especially Lewis, Didier and Mark, adventure companions. And speaking about CERN people a great ‘thank you’ to Lorenzo and Federico, because when it’s 1pm I always feel that I should be in front of the trays. Going now to who is always waiting for me in Italy when I go back, a big ‘thank you’ to my family: my dad Orazio, my mum Paola and my sisters Giulia and Silvia, for all their support and all the italian food they brought me while I was living abroad. A big ‘thank you’ also to my friends Ivan, Enrico, Martina, Federico, Luca, Valentina, Letizia all the physicists and all the others. And finally, last but not least, a giant thank you to Lucia, who is the engine of my life and to whom this thesis is dedicated.



*A Lucia,  
perché quando tutto perde di senso  
tu sei il mio piccolo mondo felice.*

*Nec per se quemquam tempus sentire fatendumst  
semotum ab rerum motu placidaque quiete.  
(Lucretius, De rerum natura, vv. 462-463 )*



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# CHAPTER 1

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## Introduction

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The Standard Model of particle physics (SM) is a Quantum Field Theory (QFT) describing strong and electroweak (EW) interactions. It was formulated in its current form in the mid-70s and has been an extremely successful predictive theory since then. Almost all known phenomena from 1 eV up to several hundred GeV are described well by the SM and experiments at the Large Hadron Collider (LHC) are now probing the SM up to and above the TeV scale. As an example of the level of accuracy of the SM, Tab. 1.1 reports the predicted and measured values of the widths of the  $Z$  and  $W$  bosons [2]. Finally, in 2012 the Higgs boson, which is one of the fundamental building blocks of the theory, was observed [3, 4]. This is a critical ingredient of the SM as it introduces a mechanism that produces particles' masses [5]. Despite its success, experimentally well-established effects, like neutrino oscillations and the presence of dark matter, remain outside the reach of the SM. Furthermore, the model does not include the description of gravity, which can be neglected at the EW energy scale. This motivates the search for new physics.

Table 1.1: Predicted and measured values of the decay widths of the  $Z^0$  and  $W$  bosons [2].

| Quantity       | Predicted               | Measured                |
|----------------|-------------------------|-------------------------|
| $\Gamma_{Z^0}$ | $2.4960 \pm 0.0002$ GeV | $2.4952 \pm 0.0023$ GeV |
| $\Gamma_W$     | $2.0915 \pm 0.0005$ GeV | $2.085 \pm 0.042$ GeV   |

The SM is based on the symmetry groups of strong,  $SU(3)_C$ , and electroweak,  $SU(2)_W \times U(1)_Y$ , interactions. The subscripts C, W and Y stand for colour charge, weak isospin and hyper-charge respectively. The Lagrangian describing the SM results from the application of the principle of invariance of the wave function under the unitary group transformations given by the product  $SU(3)_C \otimes SU(2)_W \otimes U(1)_Y$ , and leads to conservation laws such as the conservation of electric and strong charge. The model has then 26 free parameters, which have to be experimentally measured.

Particles included in the SM can be grouped into a few categories depending on their properties and ability to interact with each other. The first distinction is between fermions, half-integer spin particles, and bosons, integer spin particles. Fermions constitute the basic building blocks of matter, while bosons are the mediators of the interactions. Since the concept of bosonic mediators of interactions arises because of local gauge symmetry [6], they are called “gauge bosons”. The list of the known interactions with their force carrier and properties is reported in Tab. 1.2. The matter of which we are made of is mainly composed of electrons and protons, which have spin 1/2; protons are in turn composed of  $u$  and  $d$  quarks, which again have spin 1/2. Among fermions one can then consider two smaller groups: quarks

Table 1.2: Fundamental forces of nature together with their gauge bosons, ranges and relative strengths, as they act on a pair of protons in an atomic nucleus [2]. Gravity is not included in the SM and the graviton is hypothetical at the current time.

| Interaction | Mediator          | Strength   | Range (m)  | Mediator mass                                                      |
|-------------|-------------------|------------|------------|--------------------------------------------------------------------|
| Strong      | $g$               | 1          | $\infty$   | 0                                                                  |
| EM          | $\gamma$          | $10^{-3}$  | $\infty$   | 0                                                                  |
| Weak        | $Z^0, W^\pm$      | $10^{-16}$ | $10^{-18}$ | $W^\pm = 80.399 \text{ GeV}/c^2$<br>$Z^0 = 91.188 \text{ GeV}/c^2$ |
| Gravity     | $g^0$ (graviton?) | $10^{-41}$ | $\infty$   | 0                                                                  |

and leptons. Quarks carry colour charge and therefore can interact through the so-called strong interaction, while leptons, which do not carry colour charge, are insensitive to it. For each particle a corresponding anti-particle exists with opposite quantum numbers. Finally, fermions are divided into three families having similar properties but different masses. This last classification embedded in the SM is also called “flavour structure” and it will be the main tool used in this thesis; a more detailed description of it is given in the following sections. A schematic view of the fundamental particles in the SM is shown in Fig. 1.1.

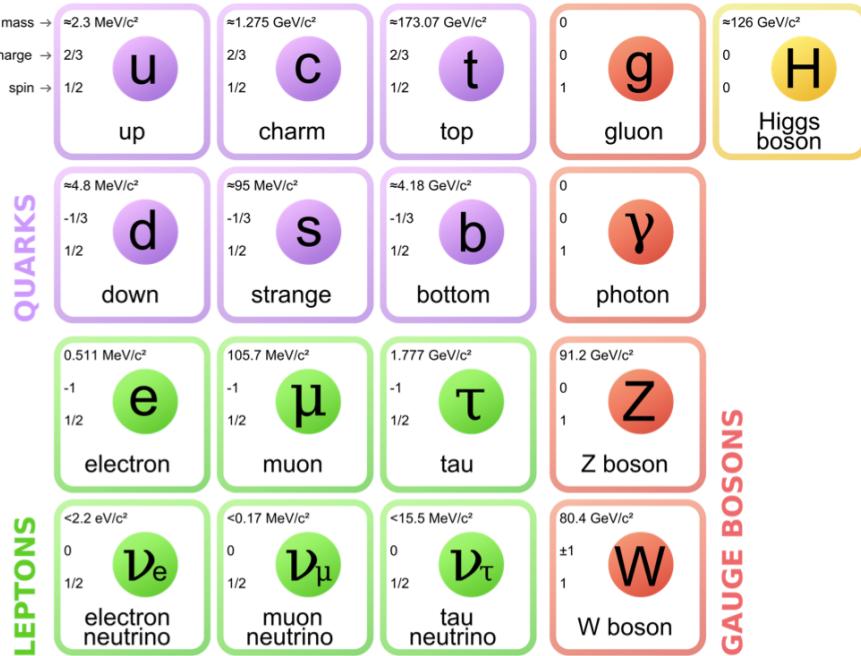


Figure 1.1: A scheme of the fundamental particles in the SM with their properties [7].

Due to the asymptotic freedom of the strong interaction quarks cannot be observed alone but are always combined with other quarks to form color singlets [8]. Non-fundamental particles composed of quarks are called hadrons and are classified into two groups: mesons, where the color singlet is achieved by the combination of a quark and an antiquark ( $q \bar{q}$ ), and baryons formed from three quarks ( $q q q$ ) of different colours. Recently, in 2014 and 2015 evidence for new states, formed by four and five quarks, was found [9, 10].

## 1.1 The electroweak interaction

The electromagnetic interaction is responsible for binding electrons and nuclei together to form atoms and its mediator is the photon. The weak interaction is responsible for the  $\beta$  decay of nuclei and is mediated by the exchange of  $W^\pm$  and  $Z^0$  bosons. Unlike the electromagnetic force, that affects only charged particles, all known fermions interact through the weak interaction. The weak interaction is also the only one that violates the parity symmetry, which states that interactions are invariant under an inversion of spatial coordinates. This symmetry breaking arises from the fact that only left-handed fermions interact through the weak interaction as discovered by Wu in 1957 [11]. Similarly, the weak interaction is the only one that also breaks the CP symmetry, which combines parity transformations and charge conjugation. This is particularly interesting because all interactions are believed to be invariant under the CPT transformation, which combines the CP transformation and time reversal. Hence, breaking CP the weak interaction implies that the process is also not invariant under time reversal transformations.

In 1968 Salam, Glashow and Weinberg unified the weak and electromagnetic forces into a single theory, where the coupling constants of the electromagnetic,  $e$ , and weak,  $g$ , interactions are related through the weak mixing angle,  $\theta_W$  by the relation  $g \sin \theta_W = e$  [2]. The electroweak symmetry is spontaneously broken by the Higgs mechanism [12] and this causes the  $W^\pm$  and  $Z$  bosons to become massive (see Tab. 1.2) and consequently the weak force has a very short range. In fact, using Heisenberg's Principle,  $\Delta E \Delta t > \hbar$ , together with Einstein's formula  $\Delta E = mc^2$ , which relates mass and energy, and knowing that the maximum space that a particle can cover in a time  $\Delta t$  is  $r \sim c\Delta t$ , qualitatively  $r \sim \hbar/mc$ . In this picture the carriers of the weak force can travel  $r \sim 2 \cdot 10^{-3}$  fm. In contrast, the photon must be massless in the theory, which accounts for the long range of the electromagnetic force. The EW interactions are divided into Charged Currents (CC) and Neutral Currents (NC). In the first group, quarks and leptons interact with the  $W^\pm$  bosons, producing decays such as  $\mu^+(\mu^-) \rightarrow e^+ \nu_e \bar{\nu}_\mu (e^- \bar{\nu}_e \nu_\mu)$  and  $n(\bar{n}) \rightarrow p e^- \bar{\nu}_e (\bar{p} e^+ \nu_e)$ . The

study of these processes confirmed that only the left-handed (right-handed) component of fermions (anti-fermions) takes part in weak processes. The CC interactions have a peculiarity: they are the only interactions in the SM that violate flavour conservation at tree level, while any other interaction not conserving flavour has to proceed through higher order processes. The second group of EW interactions, NC, corresponds to diagrams mediated by a photon or a  $Z$  boson interacting with a fermion and its anti-fermion.

## 1.2 Flavour and the CKM matrix

“Flavour” in particle physics refers to the quark-lepton composition of a particle. The introduction of flavour quantum numbers was motivated in order to explain why some decays, although kinematically allowed, had never been observed. All leptons are assigned a quantum number  $L_\ell = 1$  (where  $\ell = e, \mu, \tau$ ), which in the SM is conserved by all interactions. This conservation is experimentally well established; for example decays like  $\mu^- \rightarrow e^- \gamma$  have never been observed. In the hadronic sector particles carry flavour numbers described as:

- *Isospin*:  $I_3 = 1/2$  for the up quark and  $I_3 = -1/2$  for the down quark;
- *Strangeness*:  $S = -(n_s - \bar{n}_s)$ , where  $n_s$  and  $\bar{n}_s$  are the numbers of strange and anti-strange quarks respectively;
- *charmness, bottomness, topness*: in analogy to strangeness they are respectively defined as  $C = -(n_c - \bar{n}_c)$ ,  $B = -(n_b - \bar{n}_b)$ ,  $T = -(n_t - \bar{n}_t)$ .

As mentioned previously, in the SM the only interaction violating flavour conservation is the weak interaction when mediated by  $W^\pm$  bosons.

Measuring branching fractions of weak decays like  $\pi \rightarrow \mu\nu_\mu$  and  $K \rightarrow \mu\nu_\mu$ , corresponding respectively to  $ud \rightarrow \mu\nu_\mu$  and  $us \rightarrow \mu\nu_\mu$  processes, suggested the existence of more than one coupling constant for different quarks. Nicola Cabibbo, in order to

preserve the universality of weak interactions, suggested that the differences could arise from the fact that the doublets participating in the weak interactions are an admixture of the mass eigenstates [2, 13]. He therefore introduced the Cabibbo angle,  $\theta_c$ , proposing that eigenstates participating to the weak interaction are rotated with respect to the flavour eigenstates.

$$\begin{pmatrix} d_W \\ s_W \end{pmatrix} = \begin{pmatrix} \cos \theta_c & \sin \theta_c \\ -\sin \theta_c & \cos \theta_c \end{pmatrix} \begin{pmatrix} d \\ s \end{pmatrix} = \begin{pmatrix} \cos \theta_c \cdot d + \sin \theta_c \cdot s \\ \cos \theta_c \cdot s - \sin \theta_c \cdot d \end{pmatrix} \quad (1.1)$$

In a six quark system one angle is not sufficient to describe a rotation but the mixing can be generalised using a  $3 \times 3$  unitary matrix, called the CKM matrix, from the names of Cabibbo, Kobayashi and Maskawa [13, 14]. The unitarity of the matrix is required to preserve the universality of the weak interaction. Theoretically, a  $N \times N$  complex matrix depends on  $2 \cdot N^2$  real parameters. Requiring unitarity ( $AA^\dagger = A(A^*)^T = I$ ), the number of independent parameters left is

$$(N-1)^2 = \underbrace{\frac{1}{2}N(N-1)}_{\text{Number of mixing angles}} + \underbrace{\frac{1}{2}(N-1)(N-2)}_{\text{Number of complex phases}} . \quad (1.2)$$

Therefore a  $3 \times 3$  matrix depends then on 4 real parameters: three real constants and one imaginary phase. The imaginary phase generates the CP-violation which was observed in weak interactions. Figure 1.2 displays examples of CC processes together with the CKM elements associated with their vertices. Equation 1.3 reports the most

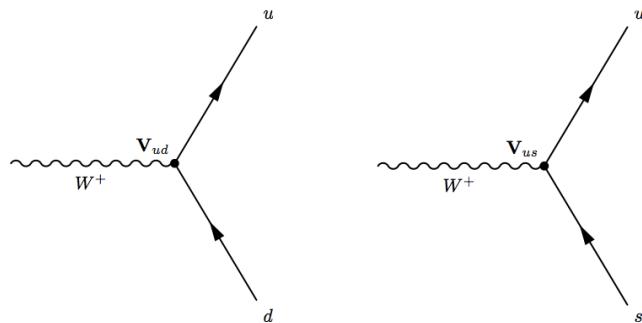


Figure 1.2: Feynman diagrams with CKM weights on weak interaction vertices as defined in Eq. 1.3.

recent measured values of its elements [2] together with the widely used Wolfenstein parametrisation which highlights the hierarchical structure of the matrix. In fact, elements on the diagonal, corresponding to transitions between quarks of the same generation, are approximately 1 and become smaller and smaller going farther from the diagonal. In the formula  $\rho$ ,  $A$ , and  $\lambda$  are the real constants and  $\eta$  the imaginary phase and Eq. 1.4 shows how they are related to the three mixing angles; terms further from the diagonal are proportional to higher powers of  $\lambda$ .

$$\begin{aligned} V &= \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 0.9743 \pm 0.0002 & 0.2253 \pm 0.0007 & 0.0035^{+0.0002}_{-0.001} \\ 0.2252 \pm 0.0007 & 0.9734 \pm 0.0002 & 0.00412^{+0.0011}_{-0.0005} \\ 0.0087 \pm 0.0003 & 0.0404^{+0.0011}_{-0.0005} & 0.99915^{+0.00002}_{-0.00004} \end{pmatrix} \\ &= \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & A\lambda^2 & 1 \end{pmatrix} + O(\lambda^4) \end{aligned} \quad (1.3)$$

$$\begin{aligned} \lambda &= \sin(\theta_{12}) = \sin(\theta_c) \\ A\lambda^2 &= \sin(\theta_{23}) \\ A\lambda^3(\rho - i\eta) &= \sin(\theta_{13})e^{i\delta} \end{aligned} \quad (1.4)$$

The unitarity of the CKM matrix imposes constraints to its elements of the form:

$$\sum_i |V_{ik}|^2 = 1 \text{ and } \sum_k V_{ik} V_{jk}^* = 0. \quad (1.5)$$

These correspond to constraints on three complex numbers, which can be viewed as the sides of triangles in the  $(\rho, \eta)$  plane; these are called “unitarity triangles”. The most commonly used unitarity triangle arises from  $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$ . Figure 1.3 shows a representation of such triangle together with a plot summarising the most up-to-date experimental constraints to its parameters [15]. Due to these unitarity constraints flavour-changing neutral currents are forbidden at tree level in the SM.

The precise measurement of the parameters of the CKM matrix is a powerful sta-

bility test of the SM and sets a solid basis for new physics searches in the flavour sector. One of the main goals of the LHCb experiment is to measure precisely the angle  $\gamma$ , which is currently the least constrained by measurements.

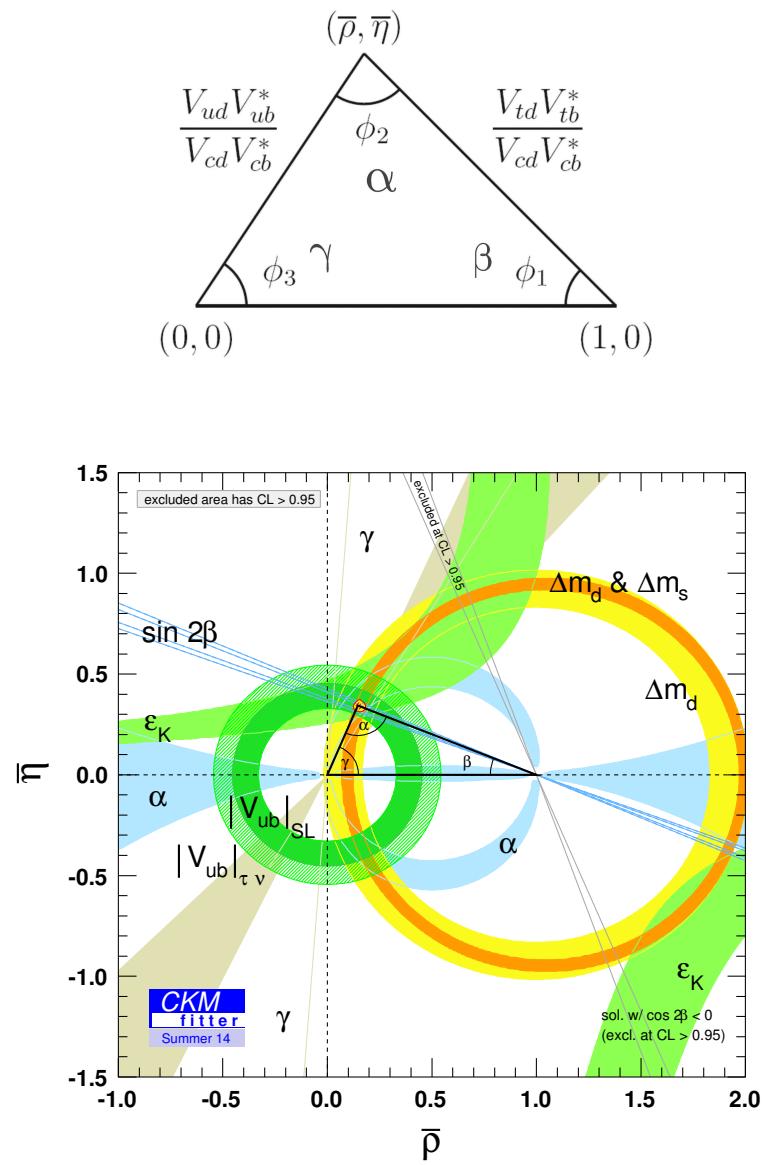


Figure 1.3: (top) A representation of the unitarity triangle and its parameters. (bottom) A summary of the most up-to-date measurements of the unitarity triangle parameters [15].

## 1.3 The puzzles of the SM

Despite the experimental confirmation of many predictions of the SM, the theory has several limitations and is unable to account for some well-established experimental facts:

- *Dark matter*: experimental evidence tells us that the content of visible matter in the universe is not sufficient to account for the observed rotation of galaxies [16]. The most natural way to solve the problem is the hypothesis of a form of matter that interacts with the gravitational field but not with the other SM interactions.
- *Matter-antimatter asymmetry*: a large asymmetry is observed between the quantity of matter and antimatter in the universe,  $O(10^{-9})$ . Assuming that both were equally created in the initial state of the universe, a condition such as the violation of the CP symmetry is necessary to account for the observed imbalance. However, the magnitude of CP violation predicted by the SM,  $O(10^{-20})$ , is not sufficient to account for the observed asymmetry [17].
- *Gravity*: even though the gravitational force was the first to be discovered this is not included in the SM. When introducing gravity in the framework of QFT the theory diverges. On the other hand gravity becomes irrelevant for the small masses of particles and can be neglected to a good approximation at the EW energy scale. Many attempts have been made but there is not yet a consistent theoretical framework through which gravity can be introduced in the SM [18].
- *Neutrino oscillation*: measurements of solar and atmospheric neutrinos, as well as neutrinos from nuclear reactors, have established that neutrinos can change flavour while propagating in space. This is not predicted in the SM, in fact in the SM neutrinos are massless, while an oscillation requires a non-zero mass [19, 20, 21, 22].

- *The hierarchy problem:* the mass of a scalar (spin 0) particle, such as the Higgs boson, suffers from quantum corrections due to the physics at high energy scales. As new physics can appear anywhere up to the Planck scale,  $\sim 10^{19}$  GeV, at which gravity cannot be neglected any more, these corrections can be very large and it would require a high level of fine-tuning for them to cancel out and give such a small value as the one measured for the Higgs Mass,  $\sim 126$  GeV/ $c^2$  [23, 3].

In conclusion, even though the SM has been very successful in describing the properties of the observed particles and their interactions so far, because of its many puzzles, it is believed only to be part of a more general theory or only to be valid up to a certain energy scale.

### 1.3.1 The flavour problem

Flavour Changing Charged Currents (FCCC) that are mediated by the  $W^\pm$  bosons are the only sources of flavour changing interaction in the SM and, in particular, of generation changing interactions, where a quark or a lepton of a family transforms into one of another family. Another class of processes is the Flavour Changing Neutral Currents (FCNCs), e.g. transitions from a  $b$  quark with a charge of -1/3 to a  $s$  or  $d$  quark with the same charge. Examples of FCNC transitions in the quark and lepton sector are shown in Fig. 1.4. FCNCs are experimentally observed to be highly suppressed which derives from the unitarity of the CKM matrix, however there is no fundamental reason why there cannot be FCNCs at tree level. In fact the CKM matrix could be part of a larger matrix involving for example quark-lepton terms. This would introduce new sources of FCNCs but could also allow for natural explanations of the equality of the proton and electron charges. Furthermore, the observation of neutrino oscillation proves that flavour is not always conserved suggesting flavour structures beyond the SM. Finally, the values of the terms of the CKM matrix and the PMNS matrix [24, 25], which is the mixing-matrix equivalent to the CKM in the lepton sector, are not explained in the SM but have to be measured

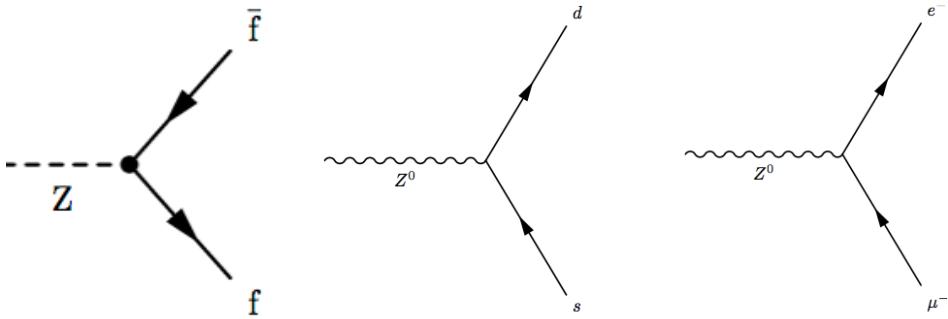


Figure 1.4: Feynman diagrams of a neutral current allowed in the SM (left), where  $f$  represents any fermion, and FCNCs processes forbidden in the SM (center-right).

experimentally. These open problems motivate searches for flavour symmetries and deeper motivations for flavour conservation.

## 1.4 Beyond the Standard Model

From the previous sections it is evident that, despite the great success of the SM, there is a need to explore theories Beyond the SM (BSM). Among the most promising approaches there are those involving Super-Symmetry (SUSY) [26] and extra-dimensions [27]. In SUSY new degrees of freedom are introduced to suppress the diverging terms of the Higgs mass. This theory assumes that for each fermion there is a corresponding boson and, since bosons and fermions contribute with opposite sign to the mass term, these would naturally cancel out. Supersymmetry also provides a candidate for dark matter. In fact the lightest Super-Symmetric particle, the neutralino, which in R-parity [28] conserving variants of the theory must be stable, is a weakly interacting potentially heavy particle. The idea to introduce extra-dimensions was triggered by the fact that gravity is not relevant in particle physics but it would be natural if all forces had similar strength. By adding extra dimensions to the normal three spatial dimensions, one can restore the strength of gravity, as this could be dispersed by the wider space available. In all these approaches constraints to masses and couplings must be imposed to maintain compatibility with the SM at the electroweak scale and the existing experimental observations.

### 1.4.1 Flavour and BSM theories

Most BSM theories predict processes violating flavour conservation. Therefore, the observation or non-observation of these processes can give important information about new physics. BSM theories can be classified according to the amount of flavour violation they introduce. The first class of models to consider is that with Minimal Flavour Violation (MFV). These are models in which the only sources of flavour changing transitions are governed by the CKM matrix and the CKM phase is the only source of CP violation. This definition is driven by the fact that usually a solution of the hierarchy problem is expected at the TeV scale, while the very small amount of flavour violation observed in measurements seems to indicate that the SM would remain valid up to much higher energy scales. It is therefore assumed that new physics must respect flavour symmetry principles, which also makes these types of models naturally compatible with the SM. Examples of such models include the MSSM with minimal flavour violation and the SM with one extra-dimension. Reviews of MFV models are presented in Refs. [29, 30]. A powerful test of MFV is provided by the study of ratios between  $b \rightarrow d$  and  $b \rightarrow s$  transitions, because their hamiltonians share the same structure. One particularly important example is the ratio between the decay rates of  $B^0$  and  $B_s^0$  into dimuons [31], as this is a purely leptonic decay free from hadronic uncertainties. In the SM such ratios are approximately equal to  $|V_{td}/V_{ts}| \sim 1/25$ , only modified by phase space and hadronic matrix elements, while they can take very different values in non-MFV models.

In the quest for new physics an important role is also played by simplified models as an intermediate model building step. Instead of constructing theories valid up to the GUT scale one can consider simplified models, where the SM is extended by the addition of new degrees of freedom with a limited number of parameters. Such models are easier to constrain but can nevertheless point in the right direction to build more complete theories. The choice of the new sector to add can be driven by the need to explain existing tensions between measurements and SM predictions or by theoretical prejudice. Two models especially relevant when studying rare

decays, which are the main topic of this thesis, are  $Z'$ -penguins and leptoquarks. A  $Z'$ -penguin is a FCNC process involving a neutral field arising from an extra  $U(1)$  gauge symmetry, for example  $U(1)_{B-L}$ , where B and L are the baryon and lepton numbers. As for the SM penguins, the  $Z'$  field contributes in loops causing modifications of the effective couplings with respect to the SM. A survey of  $Z'$  models can be found in Ref. [32]. Leptoquarks are bosonic particles that carry both quark and lepton flavour quantum numbers, which for simplicity are assumed to be scalar. A tree level exchange of a leptoquark induces processes such as  $b \rightarrow (s, d)\ell^+\ell^-$ , and therefore can result in an enhancement of their decay rates with respect to the SM [33]. Leptoquarks would also provide a natural explanation for non-universal couplings to leptons.

## 1.5 Rare decays: a tool to search for new physics

In the Standard Model FCNC processes are forbidden at tree level but can occur through loop diagrams such as penguin or  $W$  box diagrams (see Fig. 1.5). The branching fractions of decays going through these processes are small, typically  $\sim 10^{-6}$  or lower, and therefore they are called “rare decays”. Additional contributions to the virtual loops are not necessarily suppressed with respect to the SM component which makes these decays very sensitive to new physics. This approach to new physics searches is interesting as new particles could be at high mass scales that are not accessible via direct production at colliders but their effect could be observed in loops. Radiative and penguin decays are particularly interesting because they are theoretically well understood, which allows precise comparisons with measurements. Furthermore, they provide a large quantity of observables that can be affected by new physics, not only decay rates, but also CP asymmetries and angular observables such as forward-backward asymmetries. The joint analysis of different observables can help to build a consistent picture and rule out specific models.

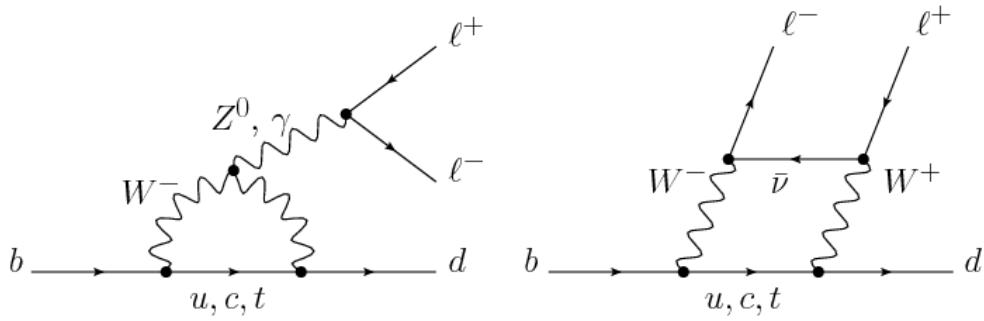


Figure 1.5: Loop Feynmann diagrams allowing  $b \rightarrow d$  FCNC processes: penguin diagram (left) and  $W$  box (right).

### 1.5.1 Theoretical framework: the effective Hamiltonian

Rare decays of  $b$  hadrons are governed by an interplay between weak and strong interactions. The large masses of the  $W^\pm$  and  $Z^0$  bosons and top quark compared to that of the  $b$  quark allow the construction of an effective theory that divides the problem of calculating weak decay amplitudes into two parts: “short-distance” and “long-distance” effects separated at an energy scale  $\mu$ . The first part, dealing with short distance physics, handles perturbative contributions due to energy scales above the  $b$  mass. The second part typically deals with non-perturbative contributions. A classic example of an effective theory is the Fermi theory of weak interactions which describes the  $\beta$  decay in terms of a four-fermion interaction, where the short distance physics is hidden into a point-like vertex as illustrated in Fig. 1.6.

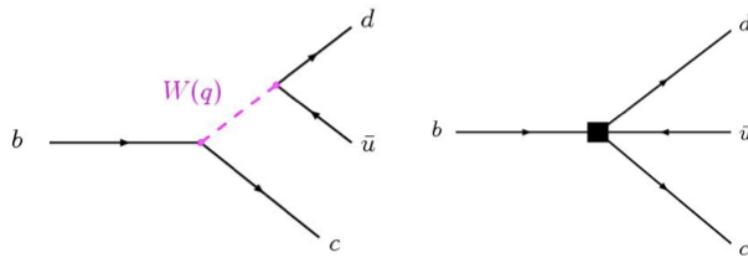


Figure 1.6: Example of a Fermi theory in which the full theory (left) is divided into (right) a short distance contribution, hidden in the vertex, and a long distance contribution.

The effective hamiltonian [34] relevant to  $b \rightarrow s/d\gamma$  and  $b \rightarrow s/d\ell^+\ell^-$  transitions can be written as:

$$\mathcal{H}_{eff} = \frac{-4G_F}{\sqrt{2}} \left[ \lambda_q^t \sum C_i(\mu, M) \mathcal{O}_i(\mu) + \lambda_q^u \sum C_i(\mu, M) (\mathcal{O}_i(\mu) - \mathcal{O}_i^u(\mu)) \right], \quad (1.6)$$

where  $G_F$  denotes the Fermi coupling constant and the  $\lambda$  constants are the CKM factors,  $\lambda_q^t = V_{tb}V_{tq}^*$  and  $\lambda_q^u = V_{ub}V_{uq}^*$ . In  $b \rightarrow s$  quark transitions, which are the main topic of this thesis, the doubly Cabibbo-suppressed contributions can be neglected as  $\lambda_s^u \ll \lambda_s^t$ . To obtain this formula the Operator Product Expansion (OPE) [35] method is used, which implements a summation over all contributing operators weighted by corresponding constants called Wilson coefficients. In this Hamiltonian the long-distance contributions are described by the operators,  $\mathcal{O}_i$ , while the short-distance physics is encoded in the Wilson Coefficients,  $C_i$ . Operators and coefficients are evaluated at the renormalisation scale  $\mu$ . Any particle that contributes to the decay and has a mass greater than the scale  $\mu$  will affect the value of at least one of the Wilson coefficients, including SM particles as the top quark.

In order to describe SM processes the effective theory must be matched with the SM by requiring the equality between each term in effective theory and the full theoretical calculation at a matching scale, typically the EW scale ( $\mu_W$ ). Then, using the scale independence of the effective Hamiltonian, one can derive a renormalisation group equation for the Wilson Coefficients [36]. Taking into account only SM contributions and using  $\mu_W = m_b$ , the Wilson Coefficients have values:

$$C_7^{SM} = -0.3, \quad C_9^{SM} = 4.2, \quad C_{10}^{SM} = -4.2 \quad (1.7)$$

and new physics contributions appear in the Wilson Coefficients in the form of additive factors:

$$C_i = C_i^{NP} + C_i^{SM}. \quad (1.8)$$

The amplitudes of exclusive hadronic decays can be calculated as the expectation values of the effective Hamiltonian. Given an initial state  $I$  and a final state  $F$

(e.g.  $I = B^0$  and  $F = K^{*0}\mu^+\mu^-$ ) the decay amplitude can be calculated as

$$\begin{aligned} A(I \rightarrow F) &= \langle I | \mathcal{H}_{eff} | F \rangle = \\ &= \frac{G_F}{\sqrt{2}} \sum V_{CKM}^i \underbrace{C_i(\mu)}_{\substack{\text{Perturbative} \\ \text{Includes new physics}}} \cdot \underbrace{\langle I | \mathcal{O}_i(\mu) | F \rangle}_{\substack{\text{Non-perturbative} \\ \text{Known physics}}} , \end{aligned} \quad (1.9)$$

where  $\langle I | \mathcal{O}_i(\mu) | F \rangle$  are the hadronic matrix elements also called “form factors”. These can be evaluated using non perturbative methods such as lattice calculations. However, due to the limitations of these methods, they represent the dominant source of uncertainty in theoretical calculations.

### 1.5.2 Operators

Separating the left- and right-handed components the effective Hamiltonian is

$$\mathcal{H}_{eff} = \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{\alpha_e}{4\pi} \sum_{i=1}^{10} [C_i \mathcal{O}_i + C'_i \mathcal{O}'_i] . \quad (1.10)$$

A complete basis is given by a set of 10 operators, where  $\mathcal{O}_{1,2}$  are the tree level W operators;  $\mathcal{O}_{3-6,8}$  are penguin diagrams mediated by gluons; and  $\mathcal{O}_{7,9,10}$ , which are the operators that are relevant for radiative and leptonic penguin processes are defined as [31]:

$$\begin{aligned} \mathcal{O}_7 &= \frac{m_b}{e} (\bar{s} \sigma^{\mu\nu} P_R b) F_{\mu\nu}, & \mathcal{O}'_7 &= \frac{m_b}{e} (\bar{s} \sigma^{\mu\nu} P_L b) F_{\mu\nu}, \\ \mathcal{O}_9 &= (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \ell), & \mathcal{O}'_9 &= (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \ell), \\ \mathcal{O}_{10} &= (\bar{s} \gamma_\mu P_L b) (\bar{\ell} \gamma^\mu \gamma_5 \ell), & \mathcal{O}'_{10} &= (\bar{s} \gamma_\mu P_R b) (\bar{\ell} \gamma^\mu \gamma_5 \ell), \end{aligned} \quad (1.11)$$

where  $P_{L/R} = (1 \mp \gamma_5)/2$  denote the left- and right-handed chiral projections and  $F_{\mu\nu}$  is the electromagnetic field tensor. The  $\mathcal{O}'$  operators correspond to right-handed coupling obtained by swapping  $P_R$  and  $P_L$  in the equations. In the SM, as well as in MFV models where the flavour violation is entirely ruled by the CKM matrix, the  $C'$  Wilson Coefficients are suppressed by the strange coupling,  $C'_i \sim (m_s/m_b) C_i$ .

The operator  $\mathcal{O}_7$  relates to penguin diagrams that are mediated via a photon. It represents the dominant contribution to the radiative  $b \rightarrow s\gamma$  transition and contributes to  $b \rightarrow s\ell^+\ell^-$  processes when the virtual photon decays into a dilepton pair. The semileptonic  $\mathcal{O}_9$  and  $\mathcal{O}_{10}$  correspond to penguin diagrams mediated by a  $Z^0$  boson and  $W$  mediated box diagrams. These are the dominant contributions in semileptonic  $b \rightarrow s\ell^+\ell^-$  decays. The vertices corresponding to the radiative and semileptonic operators are illustrated in Fig. 1.7

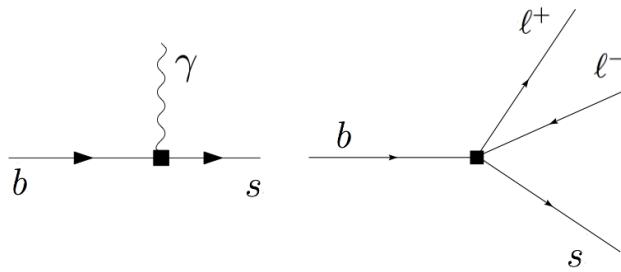


Figure 1.7: Interaction vertices corresponding to the radiative (left) and semileptonic (right) operators.

It is also common to express the semileptonic operators in a basis with left and right projected leptons

$$\begin{aligned} \mathcal{O}_{LL} &= (\mathcal{O}_9 - \mathcal{O}_{10})/2 & \mathcal{O}_{LR} &= (\mathcal{O}_9 + \mathcal{O}_{10})/2 \\ \mathcal{O}_{RR} &= (\mathcal{O}'_9 - \mathcal{O}'_{10})/2 & \mathcal{O}'_{RL} &= (\mathcal{O}'_9 + \mathcal{O}'_{10})/2 \end{aligned} \quad (1.12)$$

where the Wilson Coefficients are redefined as

$$\begin{aligned} C_{LL} &= C_9 - C_{10}, & C_{LR} &= C_9 + C_{10}, \\ C_{RR} &= C'_9 - C'_{10}, & C'_{RL} &= C'_9 + C_{10}. \end{aligned} \quad (1.13)$$

This basis is particularly useful in frameworks where BSM physics at a high mass scale respects the  $SU(2)_W$  part of the SM gauge symmetry group. Finally, in the picture presented in this section all operators were considered as universal with respect of the flavour of the involved leptons. However, BSM models often contain sources of lepton universality violation leading to a split of the same operators depending on the lepton considered:  $C_i \rightarrow C_i^e, C_i^\mu, C_i^\tau$  and  $\mathcal{O}_i \rightarrow \mathcal{O}_i^e, \mathcal{O}_i^\mu, \mathcal{O}_i^\tau$ .

### 1.5.3 Phenomenology of $b \rightarrow s\ell^+\ell^-$ decays

Semileptonic  $b$  hadron decays are characterised by two kinematic regimes which are treated theoretically in different ways; Table 1.3 shows a scheme of the  $q^2$  spectrum. The ‘high  $q^2$ ’ is the region of low hadron recoil,  $q^2 > 15 \text{ GeV}^2/c^4$ , and is characterised by the energy of the hadron being less than the energy scale of QCD interactions within the meson,  $\Lambda_{QCD} \sim 1 \text{ GeV}$ . In this region theoretical calculations of  $B$  meson decays can be simplified by working in the heavy quark limit,  $m_b \rightarrow \infty$ . In this limit a Heavy Quark Effective Theory (HQET) [37] can be constructed in which the heavy quark interacts only via ‘soft’ hadronic processes and an OPE in  $1/m_b$  is valid. The ‘low  $q^2$ ’ region is where the light spectator quark is energetic and cannot be neglected. Furthermore, the light quark interacts not only via ‘soft’ hadronic processes, as in HQET, but also via the so-called ‘collinear’ hadronic processes. The boundary of this region can be set at  $\sim 7 \text{ GeV}^2/c^4$  which corresponds to the threshold for  $c\bar{c}$  production,  $(2m_c)^2$ . In this region the hadronic interactions are handled by expanding in terms of the energy of the emitted energetic hadron,  $1/E_h$ , forming the so-called Soft-Collinear Effective Theory (SCET) [38]. In both regions decay rates can be predicted using the different methods and the biggest uncertainties come from the limited knowledge of hadronic transition matrix elements. The intermediate region is characterised by the presence of charmonium resonances, produced though tree level  $b \rightarrow \bar{c}cs$  transitions and no precise theoretical calculation is available [39].

As can be seen in Fig. 1.8 the very low  $q^2$  region is characterised by a peak due to the virtual photon contribution, associated with  $C_7$ . In the region  $1 - 6 \text{ GeV}^2/c^4$  the

Table 1.3: A scheme of the  $q^2$  spectrum.

| $q^2$                             | $E_{K^{*0}}$                    | Regime                | Valid theory |
|-----------------------------------|---------------------------------|-----------------------|--------------|
| $\sim 0 \text{ GeV}^2/c^4$        | $\sim m_B$                      | Max. recoil           | SCET         |
| $< 6 \text{ GeV}^2/c^4$           | $>> \Lambda_{QCD}$              | Large recoil          |              |
| $q^2 \sim m_{J/\psi, \psi(2S)}^2$ | $\sim 3 \text{ GeV}$            | $c\bar{c}$ resonances | –            |
| $q^2 > 15 \text{ GeV}^2/c^4$      | $E_{K^{*0}} \sim \Lambda_{QCD}$ | Low recoil            | HQET         |
| $q^2 = (m_B - m_K^{*0})^2$        | $E_{K^{*0}} \sim 0$             | Zero recoil           |              |

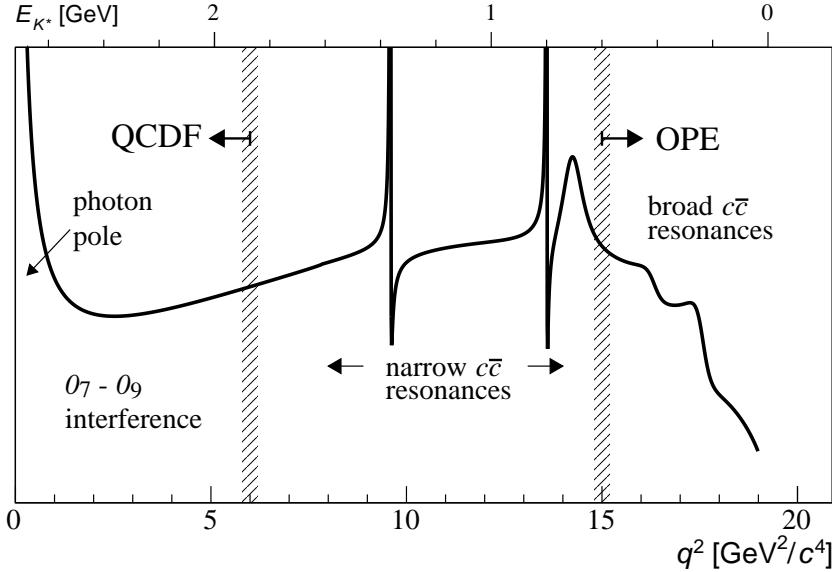


Figure 1.8: A typical  $q^2$  spectrum of  $b \rightarrow s\ell^+\ell^-$  processes characterised by the photon pole at low  $q^2$ , charmonium resonances at central  $q^2$  and broad resonances at high  $q^2$  [31].

interference between  $C_7$  and  $C_9$  becomes large, yielding sensitivity to new physics in  $C_9$ . The  $7 - 15$   $\text{GeV}^2/\text{c}^4$  interval is dominated by the charmonium resonances,  $J/\psi$  and  $\psi(2S)$ . Although these decays can be experimentally vetoed in principle charmonia affect the entire  $q^2$  space. Finally, at high  $q^2$  broad charmonium resonances can contribute, like those observed by LHCb in  $B^+ \rightarrow K^+ \mu^+ \mu^-$  decays [40].

### 1.5.4 Observables in $b \rightarrow s\ell^+\ell^-$ decays

Rare decays and especially semileptonic  $b \rightarrow s\ell^+\ell^-$  processes offer a number of observables which can be used to study BSM models. The most direct effects appear in decay rates that can be enhanced by new physics but the precision on these measurements is often limited by uncertainties on the non-perturbative part of the calculations. Therefore, it is important to also look for different observables. One important class of observables are angular quantities that can often carry complementary information with respect to branching ratio measurements. The most basic of these observable are forward-backward asymmetries that characterise the angular

distribution of final particles. For the  $B^0 \rightarrow K^* \mu^+ \mu^-$  decay combinations of observables have been proposed that are independent of form factor uncertainties at leading order [31].

Another way to build safe observables is to construct ratios between similar decays, in which uncertainties due to the hadronisation process cancel out. These observables include the  $R_H$  ratios, between  $B^0$  decays into electrons and muons, that are described in detail in Ch. 5. It is also interesting to compare decays which proceed via the same fundamental process but where the spectator quark has a different flavour. This is the case of  $B^+ \rightarrow K^+ \mu^+ \mu^-$  and  $B^0 \rightarrow K_s^0 \mu^+ \mu^-$  decays, which are both  $b \rightarrow s$  transitions where the spectator quark is an  $u$  quark in the first case and a  $d$  quark in the second. The normalised difference of the branching fractions of these decays is called isospin asymmetry.

## 1.6 Experimental status

To set the background for the analyses described in this thesis, this section reports a brief review of recent results of new physics searches involving rare decays or lepton flavour violation. Among these, results recently obtained by the LHCb experiment show a series of anomalies with respect to the SM that have the potential to yield to BSM scenarios.

### 1.6.1 Dimuon decays of $b$ hadrons

Decays of  $B$  mesons into a pair of muons are two-body decays where the two muons are back to back in the hadron rest frame. The simple signatures of these decays makes them easy to study and the fact that they are unaffected by hadronic physics in the final state makes predictions very clean and precise. Therefore these are essential tests of the SM. The  $B^0 \rightarrow \mu^+ \mu^-$  and  $B_s^0 \rightarrow \mu^+ \mu^-$  decays are FCNCs that can only happen via loops and furthermore they are CKM-suppressed, which makes

them particularly rare. In addition to that the decay of a pseudo-scalar  $B$  meson into two muons has a significant helicity suppression. The latest SM predictions for these decay rates are [41]:

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (3.65 \pm 0.23) \times 10^{-9} \text{ and} \quad (1.14)$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (1.06 \pm 0.09) \times 10^{-10}. \quad (1.15)$$

The uncertainties on these values are dominated by the knowledge of the decay constants and CKM-elements. BSM models can produce significant enhancement to these decay rates and the measurement of their ratio is a stringent test of the MFV hypothesis. A combination of the LHCb and CMS results measured the values [42]:

$$\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-) = (2.8^{+0.7}_{-0.6}) \times 10^{-9} \text{ and} \quad (1.16)$$

$$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-) = (3.9^{+1.6}_{-1.4}) \times 10^{-10}. \quad (1.17)$$

Neither decay had been previously observed, while now the  $B_s^0$  decay is observed with a significance of  $6\sigma$  and evidence for the  $B^0$  decay is found at  $3\sigma$  significance level. The measured branching fractions are compatible with SM predictions within  $2\sigma$  and put strong constraints on the available parameter-space for BSM theories. Figure 1.9 shows the fit the dimuon invariant mass of  $B$  meson candidates where the peaks of the two decays are visible.

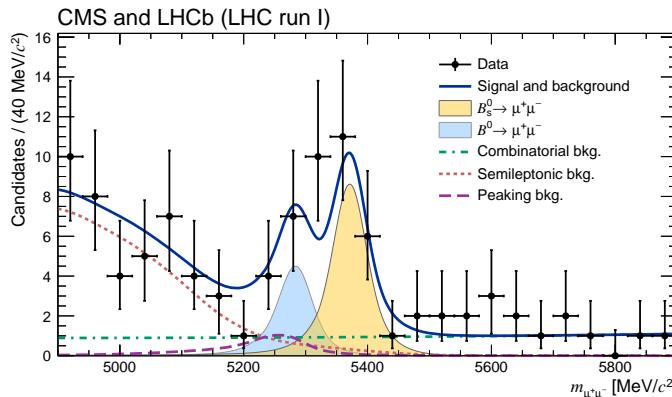


Figure 1.9: Dimuon invariant mass of  $B$  candidates showing peaks corresponding  $B_s^0 \rightarrow \mu^+ \mu^-$  and  $B^0 \rightarrow \mu^+ \mu^-$  decays [42].

### 1.6.2 Semileptonic $b \rightarrow s\ell^+\ell^-$ decays of $b$ hadrons

At the LHC it is possible to collect large data samples of semileptonic decays, especially those with muons in the final state. Many branching fractions of semileptonic  $B$  meson decays were recently measured at the LHCb experiment, including  $B \rightarrow K\mu^+\mu^-$ ,  $B \rightarrow K^{*0}\mu^+\mu^-$  and  $B_s^0 \rightarrow \phi\mu^+\mu^-$  [43, 44, 45]. Baryon decays were also studied at LHCb: including the rare  $\Lambda_b \rightarrow \Lambda\mu^+\mu^-$  decay [1], whose analysis is described in this thesis. In contrast to purely leptonic decays, SM predictions for semileptonic decays are affected by the knowledge of hadronic form factors, which results in relatively large uncertainties,  $\mathcal{O}(30\%)$ . As a result measurements are now typically more precise than predictions.

Among the measurements of angular observables that can be affected by new physics, particular interest was raised by the measurement of a set of observables in  $B^0 \rightarrow K^{*0}\mu^+\mu^-$  decays, free from form factors uncertainties at leading order [46]. Most of the measurements are found to be in agreement with SM predictions with the exception of the  $P'_5$  observable, shown in Fig. 1.10, which presents a local  $3.7\sigma$  deviation confirmed by a recent analysis with higher statistics [47]. Attempts to build a consistent picture point to a new physics contribution to the Wilson Coefficient  $C_9$  [48]. An angular analysis of  $B^+ \rightarrow K^+\mu^+\mu^-$  decays was also performed, where observables are found to be compatible with SM predictions [49]. Other observables

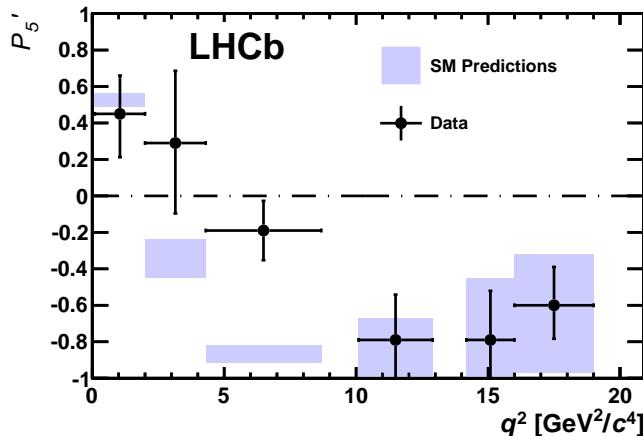


Figure 1.10: Measurement of the  $P'_5$  observable as a function of  $q^2$ , showing a tension with SM predictions in the 2–6  $\text{GeV}^2/\text{c}^4$  region [46].

|                    | $B^0 \rightarrow K^+ \mu^+ \mu^-$ |                           | $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ |                                 |
|--------------------|-----------------------------------|---------------------------|--------------------------------------|---------------------------------|
|                    | 1.1–6 [GeV $^2/c^4$ ]             | 15.0–22.0 [GeV $^2/c^4$ ] | 1.1–6 [GeV $^2/c^4$ ]                | 15.0–19.0 [GeV $^2/c^4$ ]       |
| $\mathcal{A}_{CP}$ | 0.004 $\pm$ 0.028                 | -0.005 $\pm$ 0.030        | 0.094 $\pm$ 0.047                    | -0.074 $\pm$ 0.044              |
| $\mathcal{A}_I$    | $-0.10^{+0.08}_{-0.09} \pm 0.02$  | $-0.09 \pm 0.08 \pm 0.02$ | $0.00^{+0.12}_{-0.10} \pm 0.02$      | $0.06^{+0.10}_{-0.09} \pm 0.02$ |

Table 1.4: Measurement of CP and isospin asymmetry in  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  decays from the LHCb experiment [31].

for which the sensitivity to form factors effects is reduced are the CP asymmetry between  $B$  and  $\bar{B}$  decays,  $\mathcal{A}_{CP}$ , and the isospin asymmetry between  $B^0$  and  $B^+$  decays,  $\mathcal{A}_I$ . Due to the small size of the corresponding CKM elements, CP asymmetries of  $B^0 \rightarrow K^{(*)} \mu^+ \mu^-$  decays are tiny in the SM,  $O(10^{-3})$ . In BSM models new sources of CP violation can arise and therefore  $\mathcal{A}_{CP}$  measurements are a powerful test of the SM. The isospin asymmetry is not zero in the SM due to isospin breaking effects in the form factors. This is expected to be  $\sim 1\%$  at low  $q^2$  and increase to  $\sim 10\%$  as  $q^2$  tends to zero. The LHCb experiment, using the full dataset collected in Run I, corresponding to an integrated luminosity of 3 fb $^{-1}$  and  $\sim 10^9$   $B$  decays, measured both of these asymmetries to be consistent with zero [43, 50], as reported in Tab. 1.4. Recently, progress was made measuring also electron channels. The branching fraction of the  $B^0 \rightarrow K^{*0} e^+ e^-$  decay was measured to be  $(3.1 \pm 1.3) \times 10^{-7}$  in the dilepton mass interval 30–1000 MeV/ $c^2$  [51]. Furthermore, for the first time angular observables were measured for this decay and found to be consistent with SM predictions [52].

Given the wide set of available measurements, theorists have implemented global fits including results from rare decays analyses, as well as inputs from  $B_s^0$  mixing and Higgs measurements, in order to understand if the existing anomalies could be caused by a common factor. The results of such global fits agree that there is a tension with respect to the SM at the level of 3–4 standard deviations, depending on the set of assumptions made. In particular they favour a shift  $C^{NP} \sim -1$  to the  $C_9$  Wilson Coefficient, related with the penguin diagram mediated by a  $Z^0$  boson [53, 48, 54].

### 1.6.3 Lepton Flavour Violation searches

Several Lepton Flavour Violation (LFV) searches are linked to rare decays as they involve small branching ratios in the SM that can be enhanced by BSM physics. Lepton flavour conservation is experimentally well-established measuring the branching ratios of decays of muons into electrons and no neutrinos, but has no strong theoretical explanation in the context of the SM. In fact it is already observed that flavour is not conserved in neutrino oscillations. The best-studied decays violating lepton flavour are rare muon decays including  $\mu^+ \rightarrow e^+\gamma$  and  $\mu^+ \rightarrow e^+e^-e^+$ . Since muons can be abundantly produced and the final states are simple, these decays provide the best constraints to LFV. The present best upper limits are  $1.2 \times 10^{-11}$  for the radiative decay and  $1.0 \times 10^{-12}$  for  $\mu^+ \rightarrow e^+e^-e^+$  obtained respectively by the MEGA [55] and SINDRUM [56] experiments. Several LFV searches in the  $B$  sector have recently been performed at the LHCb experiment including decays such as  $B^0 \rightarrow e\mu$  [57] and  $\tau$  decays such as  $\tau \rightarrow \mu^+\mu^-\mu$  [58]. None of these searches has found evidence of new physics so far and therefore they set limits, constraining the parameter space available for BSM models. Figure 1.11 shows a summary of the best limits set at different times on LFV searches [59].

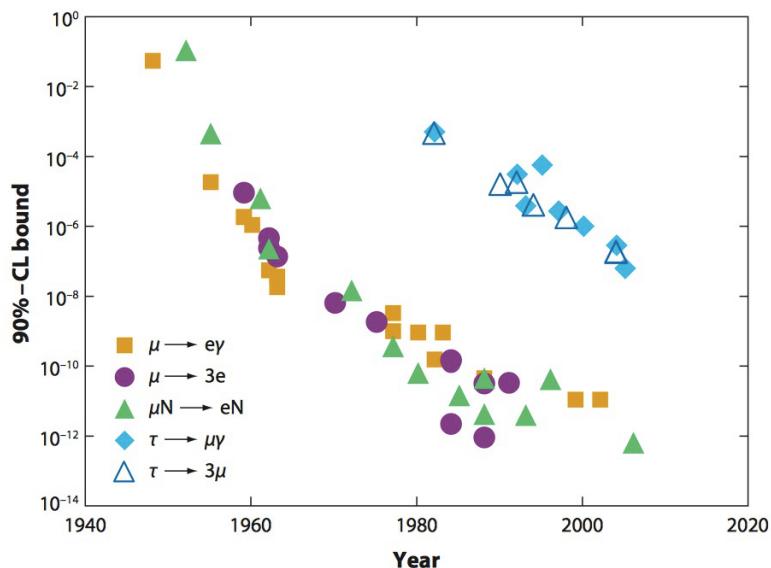


Figure 1.11: Summary of limits set in LFV searches as a function of time [59].

# CHAPTER 2

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## The LHCb detector at the Large Hadron Collider

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### 2.1 The Large Hadron Collider

The Large Hadron Collider (LHC) [60] is a synchrotron particle accelerator with a circumference of 27 km located about 100 m underground at CERN in the surroundings of Geneva, Switzerland. Two proton beams circulate in opposite directions around the ring and cross each other in four points, in which particle detectors are placed. These include two general-purpose detectors, ATLAS and CMS, sitting on opposite sides of the ring and two smaller detectors, ALICE and LHCb that are designed to study specific topics (see Fig. 2.1).

Each beam consists of a series of proton bunches, up to a maximum of 2835. Each bunch consists of about  $10^{11}$  protons and the bunch spacing is such that the nominal bunch crossing rate is 40 MHz. The beams are injected into pre-accelerators and then pass into the LHC through the CERN acceleration system shown in Fig. 2.1.

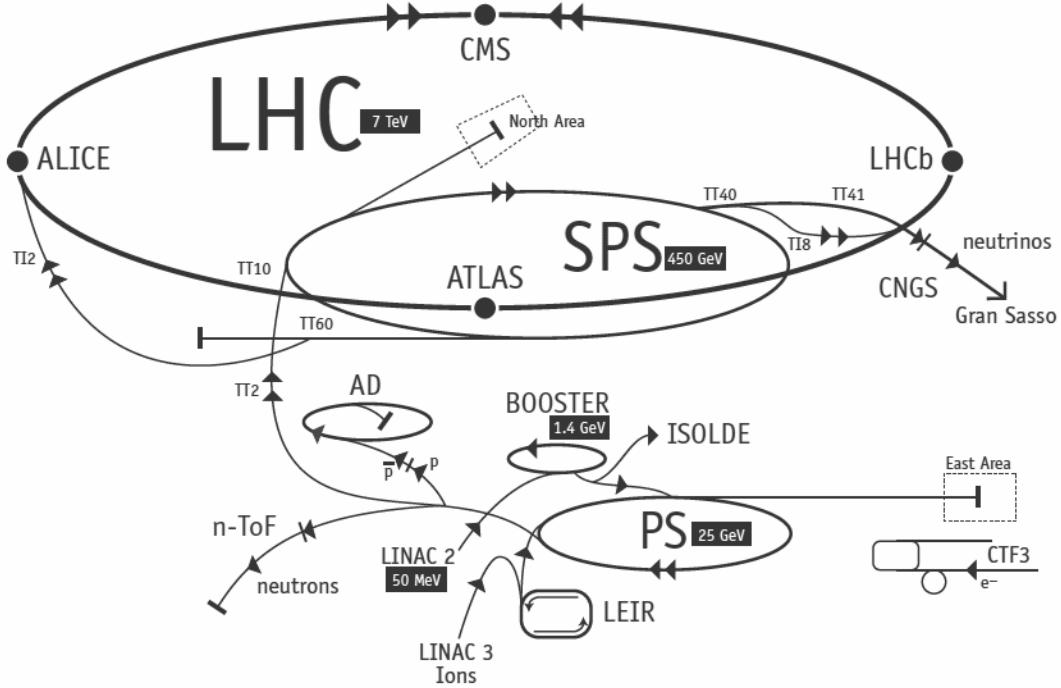


Figure 2.1: Schematic of CERN accelerators [61].

Protons are produced from hydrogen gas and are initially accelerated to an energy of 50 MeV in a linear accelerator (LINAC). Then they are injected into the Proton Synchrotron Booster (PSB), where they are boosted to an energy of 1.4 GeV, into the Proton Synchrotron (PS) to 25 GeV and into the Super Proton Synchrotron (SPS) to 450 GeV. Finally, protons enter into the LHC storage ring, where they are accelerated from injection energy to the final one by radio frequency (RF) cavities. The beams are steered around the ring by 8 T magnetic fields produced by 15 m long superconducting niobium-titanium dipole magnets and focused by quadrupole magnets. The LHC magnets use a design in which both proton beam pipes are contained in the same housing, allowing a common liquid helium cooling system to be used. The LHC began colliding proton beams in “physics mode” in 2009 at a centre of mass energy of  $\sqrt{s} = 900$  GeV and from April 2010 to November 2011 accelerated beams at  $\sqrt{s} = 7$  TeV (3.5 TeV per proton beam) with a maximum instantaneous luminosity of  $3 \cdot 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ , while in 2012 the energy was increased to 8 TeV. The LHC maximum design energy is 14 TeV, and its design luminosity is  $10^{34} \text{ cm}^{-2}\text{s}^{-1}$ . After a long shut down to upgrade and maintain the machine, a new

run started in June 2015, in which protons are collided at a centre of mass energy of  $\sqrt{s} = 13$  TeV. At this energy the total proton-proton cross-section is expected to be roughly 100 mb.

## 2.2 The LHCb detector

The LHCb detector [62] was designed to study decays of  $B$  and  $D$  mesons, mainly looking for CP-violating processes. In 2011, running at a centre of mass energy of 7 TeV, the cross-section for  $b\bar{b}$  production was measured to be  $284 \pm 53$   $\mu\text{b}$  [63], while it will be  $\sim 500$   $\mu\text{b}$  at the current LHC energy, 13 TeV. At these high energies, proton-proton interactions produce highly boosted virtual gluons which produce  $b\bar{b}$  pairs at small angles, close to the beam pipe. For this reason the LHCb detector is designed to have a very forward angular coverage. The detector is fully instrumented from 10 mrad to 300 mrad, corresponding to an interval  $2 < \eta < 5$ , where  $\eta$  is the “pseudorapidity”, a quantity defined as:

$$\eta = -\ln(\tan(\theta/2)), \quad (2.1)$$

where  $\theta$  is the angle between a particle’s momentum and the beam direction<sup>1</sup>.

At LHCb’s collision point the luminosity can be adjusted by displacing the beams from head on collisions while keeping the same crossing angle. This allows the experiment to keep an approximately constant instantaneous luminosity, compensating for the reduction in beam intensity due to extended operation periods. This also means that the average number of interactions per bunch crossing can be regulated, which is important because the detector efficiency, especially in detecting secondary vertices, decreases for events with an high number of primary vertices (PV). Reducing the particle occupancy through the detector also keeps radiation damage to a

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<sup>1</sup>LHCb’s reference system has the  $z$  axis in the direction of the beam, the  $x$  axis directed to the centre of the accelerator and  $y$  is directed upward. Then we define  $\theta$  as the angle with the beam direction and  $\phi$  as the position around the beam in the  $xy$  plane, taking  $\phi = 0$  on the  $x$  axis. The origin,  $(x, y, z) = (0, 0, 0)$ , corresponds to the centre of the interaction area.

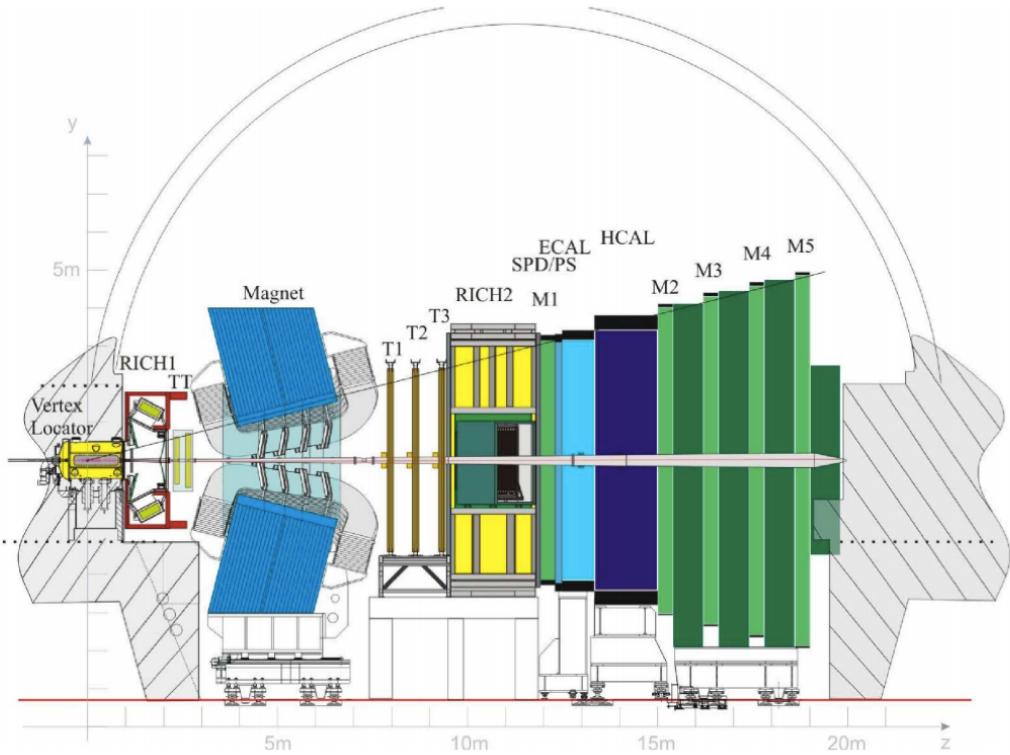


Figure 2.2: A side view of the LHCb detector [62].

minimum. Until the end of 2011 the instantaneous luminosity was  $3 \cdot 10^{32} \text{ cm}^{-2}\text{s}^{-1}$ , corresponding to an average number of 1.5 PVs per bunch crossing and at the end of 2011 LHCb had collected an integrated luminosity of  $1 \text{ fb}^{-1}$ . In 2012 the luminosity was increased and a further  $2 \text{ fb}^{-1}$  of data were collected.

Experiments like BaBar at the Stanford Linear Accelerator (SLAC), Belle at KEK at J-PARC (Japan) and the Tevatron experiments at Fermilab have made measurements in heavy flavour physics which have so far been found to be consistent with the SM predictions. However, some of the deviations from the SM are expected to be very small. Therefore LHCb was designed to make the most precise measurements in heavy flavour physics to test the consistency of the SM and look for new physics.

The LHCb detector comprises a high-precision tracking system consisting of a silicon-strip vertex detector surrounding the  $pp$  collision point, and larger silicon-strip and drift tubes detectors located on both sides of a dipole magnet with a bending power of about 4 Tm. Charged hadrons are identified using information from two Ring-

Imaging Cherenkov detectors (RICH) [64]. Photon, electron and hadron candidates are identified by a calorimeter system and muons by a system composed of alternating layers of iron and multi-wire proportional chambers [65]. A schematic view of the detector is shown in Fig. 2.2 and more details on each sub-detector are given in the following sections.

## 2.3 The magnet

Charged particle trajectories are deflected horizontally in the magnetic field so that their momentum can be measured from the radius of curvature. The LHCb dipole magnet is composed of two coils supported by an iron yoke and is shaped to fit the LHCb angular acceptance. Unlike the other LHC experiments, LHCb uses a warm magnet which can be easily ramped allowing the field polarity to be inverted periodically. When the polarity is flipped, particles of a given sign are bent in the opposite direction. This method is used to limit systematic uncertainties that arise due to performance variations in different areas of the detector, which average out using data taken in both polarities. A current of 5.85 kA flows in the magnet generating an integrated magnetic field of 4 Tm for 10 m long tracks. In order to achieve the required momentum precision the magnetic field must be mapped with a  $10^{-4}$  precision. For this reason a grid of 60 sensors is positioned inside the magnet and provides real time magnetic field maps.

## 2.4 Tracking system

$B$  mesons have lifetimes of approximately 1.5 ps. At the LHC energies, this means that they travel about 1 cm before decaying to form a displaced vertex. To study specific decays, it is therefore important to be able to separate the particles produced at the primary  $pp$  vertex and at the  $B$  decay secondary vertex (SV). The tracking system consists of the Vertex Locator (VeLo), and four tracking stations:

the Tracker Turicensis (TT), which are located before the magnet and the T1, T2 and T3 stations, located after the magnet. The latter three stations are in turn formed by two subsystems: the Inner Tracker (IT) close to the beam-line, where the particle density is greatest, and the Outer Tracker (OT) covering the rest of the acceptance.

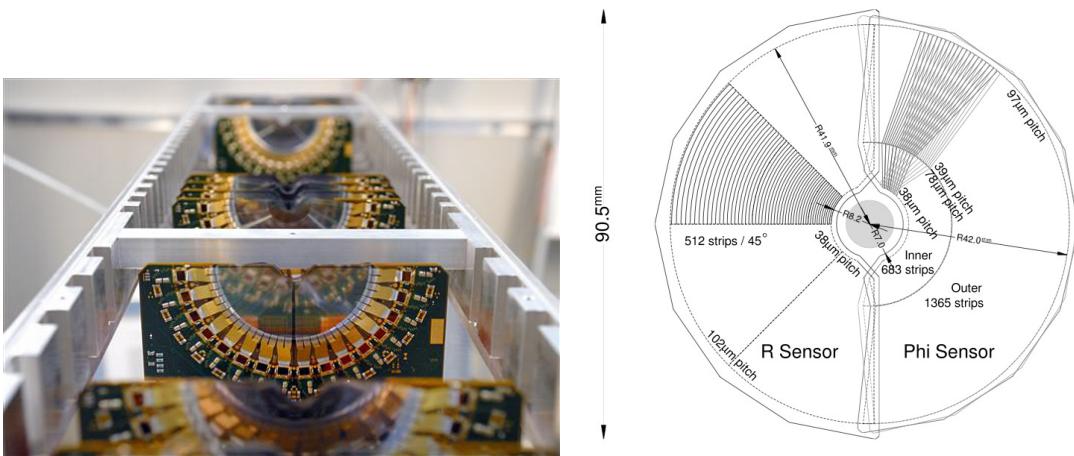


Figure 2.3: On the left VeLo sensors mounted in line and on the right a schematic view of one sensor [62].

The VeLo accurately measures positions of tracks close to the interaction point which is essential to reconstruct production and decay vertices of bottom and charm hadrons. The VeLo is composed by 21 silicon modules that surround the beam axis and are positioned from  $z = -18$  cm to  $+80$  cm. The sensitive region of the VeLo starts at an inner diameter of only 8 mm from the beam axis and it is able to detect particles within a pseudorapidity range  $1.6 < \eta < 4.9$ . The VeLo is housed in its own vacuum vessel of thin aluminium foil, which protects the vacuum of the beam pipe from any outgassing. The silicon layers composing the VeLo consist of two modules each including two types of sensors: the  $\phi$ -sensor, which measures the azimuthal position around the beam, and the R-sensor, which measures the radial distance from the beam axis. A sketch of the VeLo sensors is shown in Fig. 2.3. The sensors are  $300 \mu\text{m}$  thick and to ensure that they cover the full azimuthal angle the right-side module is placed 1.5 cm behind the left-side module on the  $z$ -axis and

they overlap. There are two modules which cover the backward direction and are used as a veto for multiple interactions; this is called the pileup system.

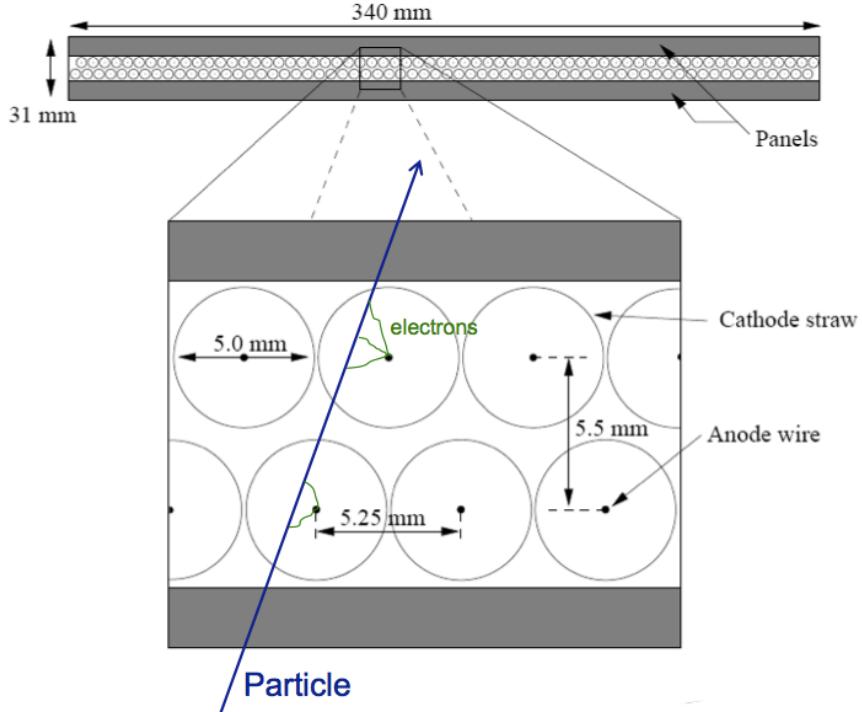


Figure 2.4: A sketch of the straw tubes which constitute the OT layers [62].

The IT and TT both use silicon strips and together constitute the Silicon Tracker (ST). Straw tubes are instead used in the OT, of which a sketch is shown in Fig. 2.4. The IT requires a higher inner granularity because of the greater flux of particles close to the beam pipe. In fact, it covers only 1.3% of the total area of IT plus OT but it contains about 20% of the tracks. Each ST station has four detection layers: the first and last are vertical, measuring the track position in  $x$ , while the second and third layers are rotated by an angle of +5 and -5 degrees, which allows the measurement of the  $y$  coordinate. The TT is placed upstream of the magnet to allow the reconstruction of tracks from low-momentum particles, which are bent out of the downstream acceptance. Overall the tracking system provides a measurement of momentum,  $p$ , with a relative uncertainty that varies from 0.4% at 5  $\text{GeV}/c$  to 1.0% at 200  $\text{GeV}/c$ . The impact parameter (IP), namely the minimum distance of a

track to a primary vertex, is measured with a resolution of  $(15 + 29/p_T) \mu\text{m}$ , where  $p_T$  is the component of the momentum transverse to the beam, in  $\text{GeV}/c$ . The  $z$ -axis position of a PV reconstructed with 35–40 tracks can be measured with a precision of roughly 50–60  $\mu\text{m}$ . The decay products of  $B$  mesons tend to have high IP values because the  $B$  decay imparts transverse momentum to them. Therefore, accurate IP and vertex displacement measurements allow LHCb to distinguish effectively between  $B$  meson decays and background processes.

## 2.5 Calorimeters

In general the main purpose of a calorimeter system is to determine the energy of particles but in LHCb it is mostly used to help the identification electrons and hadrons. Sampling calorimeters, as those used in LHCb, are composed of layers of absorber and active material. Particles interact with the absorber layers and produce a cascade of secondaries, that multiply quickly and are detected by the active part, which is usually composed of scintillating layers. The light produced is detected by photo-multipliers (PMTs) and it is approximately proportional to the energy of the deposited particles. Calibration is then used to translate the signal into an energy measurement. The LHCb’s calorimeter system consists of the Scintillator Pad Detector (SPD), the Pre-Shower Detector (PS) as well as the Electromagnetic Calorimeter (ECAL) and the Hadronic Calorimeter (HCAL). A sketch of the LHCb calorimeters is shown in Fig. 2.5. The SPD/PS cells are read out with PMTs located outside the LHCb acceptance, while the ECAL and HCAL have individual PMTs located on the modules. All four detectors are segmented, which allows the energy deposits to be associated to the tracks detected by the tracking system. The segmentation of the cells varies according to the distance from the beam pipe due to the different track density.

The most difficult identification in LHCb is that of electrons. The rejection of a high background of charged pions is achieved using a longitudinal segmentation of the

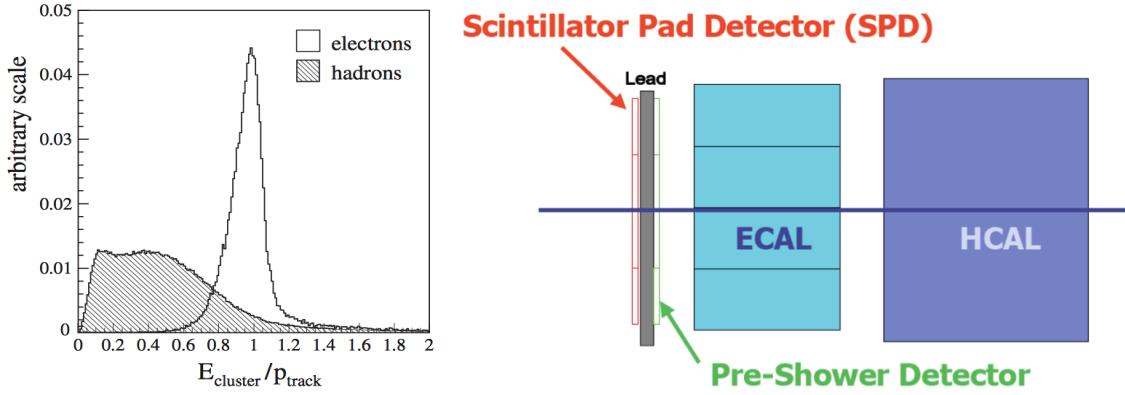


Figure 2.5: (left) The ratio of the energy deposited in the ECAL and the particle momentum, which allows the separation between electrons and hadrons [62]. (right) A schematic of the LHCb’s calorimeter system.

electromagnetic calorimeter which is provided by the PS detector added in front of the main electromagnetic calorimeter, ECAL. Electrons also have to be distinguished from high energy  $\pi^0$ s and photons. For this purpose the SPD calorimeter, detecting charged particles, is located in front of the PS and ECAL detectors. Figure 2.5 illustrates how the ratio between the energy detected in the ECAL and a particle’s momentum allows the separation of electrons and hadrons.

The ECAL is formed by 66 lead layers (2 mm thick) separated by 4 mm thick plastic scintillator layers. In order to obtain the highest energy resolution the showers from high energy photons must be fully absorbed. For this reason the ECAL has a thickness of 25 radiation lengths and its resolution is measured to be  $\sigma_{\text{ECAL}}(E)/E = 10\%/\sqrt{E(\text{ GeV})} + 1\%$  [62], which results in a mass resolution of  $\sim 70 \text{ MeV}/c^2$  for  $B$  mesons and  $\sim 8 \text{ MeV}/c^2$  for  $\pi^0$ . The HCAL is mainly used for triggering and it is similar to the ECAL but with 4 mm thick scintillator layers and 16 mm thick absorber layers. The trigger requirements on the HCAL resolution do not depend on the containment of the hadron showers as much as for the ECAL, therefore, due to space limits, its thickness is only 5.6 interaction lengths and its resolution is given by  $\sigma_{\text{HCAL}}(E)/E = 69\%/\sqrt{E(\text{ GeV})} + 9\%$ .

### 2.5.1 Bremsstrahlung recovery for electrons

Bremsstrahlung is an electromagnetic radiation produced by charged particles that undergo an acceleration. Typically electrons produce Bremsstrahlung when deflected by atomic nuclei. The probability of emitting bremsstrahlung radiation is proportional to the inverse of the squared mass of the particle ( $1/m^2$ ) and therefore it is most relevant for electrons. At LHC energies, if electrons radiate after the mag-

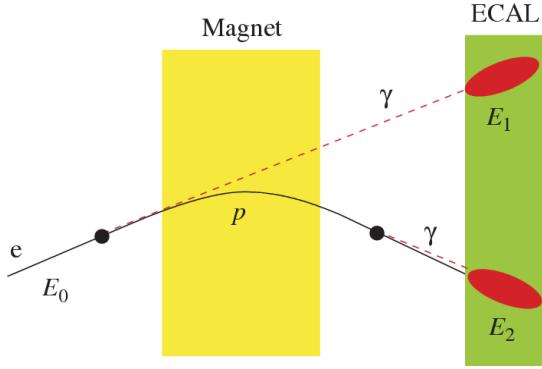


Figure 2.6: Schematic view of the bremsstrahlung recovery [62].

net, the photon will hit the same calorimeter cell as the electron and the energy will be automatically recovered, as illustrated in Fig. 2.6. However, if the photon is emitted before the magnet, the electron will be deflected by the magnetic field whereas the photon will continue on its initial trajectory, with its energy being deposited in a different part of the calorimeter. Missing this energy results in a poorer reconstructed invariant mass resolution, so it is desirable to recover these bremsstrahlung photons. A tool for bremsstrahlung recovery is available in the LHCb analysis software. This tool looks for other clusters in the calorimeter and, reconstructing the trajectory of the electron, checks if they may be associated with emitted photons. The photon energy is then added to the electron and its momentum is recalculated. For more information see Ref. [66].

## 2.6 RICH

The two RICH detectors are a special feature of LHCb, as it is the only experiment at LHC using them. These detectors take advantage of the Cherenkov radiation produced by particles passing through a medium with speed higher than the speed of light in the medium. The Cherenkov light, as shown in Fig. 2.7, is produced in cones with a specific opening angle depending on the velocity of the particle. The relation between the angle and the particle velocity can be written as

$$\cos \theta = \frac{1}{\beta n}, \quad (2.2)$$

where  $\beta = v/c$  and  $n$  is the refraction index of the medium.

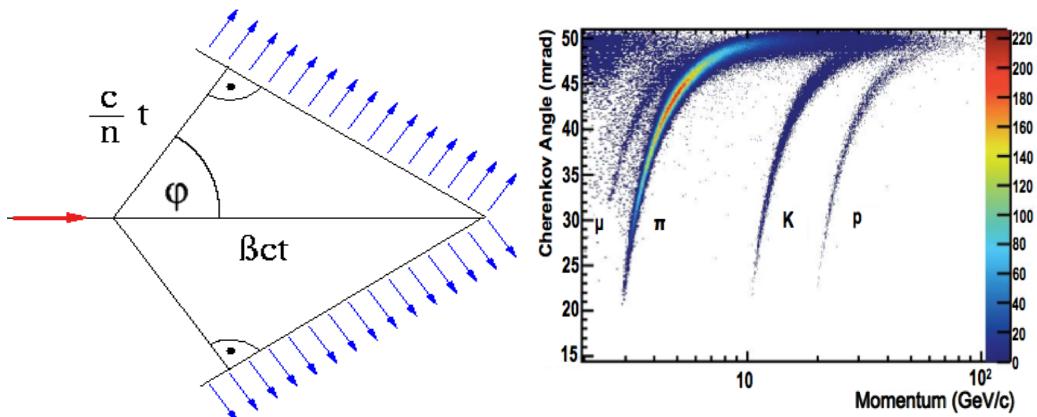


Figure 2.7: (left) A sketch of Cherenkov light emission [67]. (right) Measured Cherenkov angle as a function of particle momentum [62], where one can see that the study of the Cherenkov angle allows to distinguish particles' identities.

RICH 1 is located before the magnet in order to cover a larger angular acceptance. Its purpose is to ensure particle identification over the momentum range  $1 < p < 70 \text{ GeV}/c$ . It uses two radiators:  $C_4F_{10}$  that covers the momentum range  $5 - 70 \text{ GeV}/c$  and silica aerogel which covers  $1 - 10 \text{ GeV}/c$ . RICH 2 is positioned after the magnet and tracking stations and it identifies higher momentum particles from approximately  $20 \text{ GeV}/c$  up to beyond  $100 \text{ GeV}/c$  using  $CF_4$  as a radiator. The Cherenkov light produced when charged particles travel through the radiators, is reflected and focussed using mirrors, which are tilted so that a ring image is re-

flected onto arrays of PMTs. The radius of the ring can be used to measure the opening angle of the Cherenkov cone because of the known geometry. The photo-detectors are located outside of the LHCb acceptance in order to reduce the amount of material that the particles have to traverse. Pattern recognition algorithms are then used to reconstruct the Cherenkov rings.

## 2.7 The muon system

It is essential for many of the key physics analyses in LHCb to be able to identify muons in decay final states. Muons are the most penetrating particles that can be detected at LHC experiments, so the muon chambers are the farthest sub-detectors from the interaction point. The muon system consists of five stations (M1 - M5), the first one being located before the calorimeters in order to improve  $p_T$  measurements. The remaining four stations are behind the HCAL and are separated from each other by 80 cm thick iron blocks, which absorb hadrons, electrons and photons to ensure that only muons reach the final muon station. A schematic of the muon system is shown in Fig. 2.8. Only muons with a minimum momentum of 10 GeV/c traverse all of the five stations and, for positive identification of a muon, the trigger requires a signal in each of them. Each station has a detection efficiency of at least 95% and the detectors also provide position measurements. Since there is a larger particle flux close to the beam pipe, the stations are divided into four concentric rectangular regions (R1-R4) with increasing cell size, which results in a similar occupancy over the four regions. All of the muon stations use Multi Wire Proportional Chambers (MWPC) except for the inner region of M1, where the particle flux is too high. In this region triple-GEM (Gas Electron Multiplier) detectors are used because of their better ageing properties as they have to withstand a rate up to 500 kHz cm<sup>-2</sup> of charged particles. These detectors consist of three gas electron multiplier foils sandwiched between an anode and a cathode.

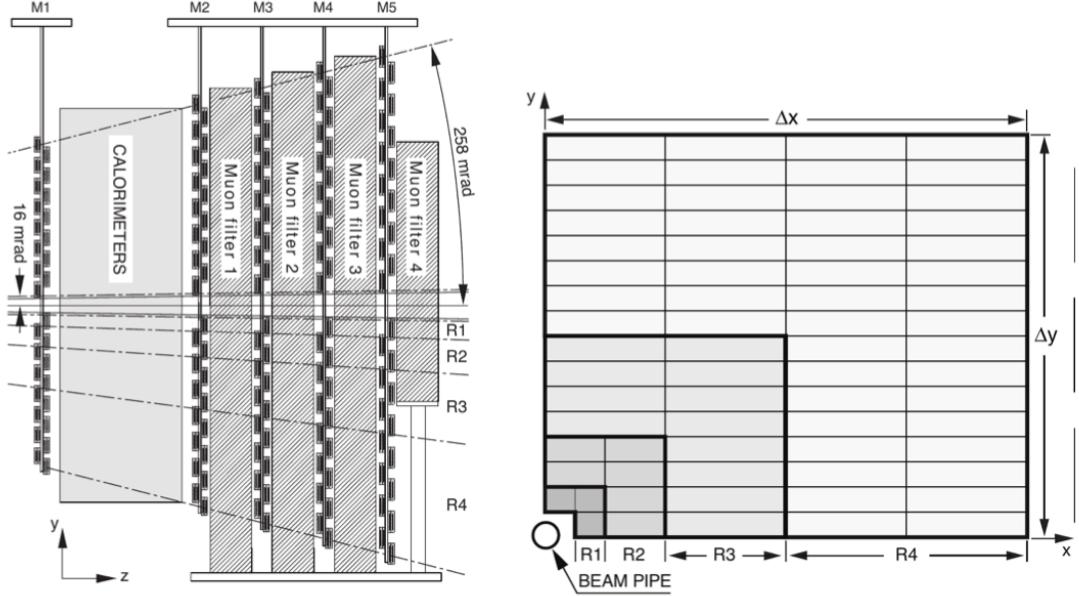


Figure 2.8: The LHCb muon system [62].

## 2.8 Particle identification

Particle identification (PID) is an important feature in LHCb and it is performed in various ways. The electromagnetic calorimeters can distinguish between pions and electron, the muon chambers identify muons and the RICH detectors can be used to identify heavier charged particles such as protons and kaons.

The RICH assigns an ID to a track calculating the global likelihood for the observed distribution of hits being consistent with the expected distribution from various ID hypotheses. The algorithm iterates through each track and recalculates the likelihood when the track PID hypothesis is changed to that of an electron, muon, kaon or proton. For electrons and muons additional information from the calorimeter and muon systems is also used. The hypothesis which maximises the likelihood is assigned to the track.

To quantify the quality of the ID the pion hypothesis is used as a reference point and the probability of a specific ID is given in terms of Log-Likelihood difference between the given ID hypothesis and the pion one. This variable is called Delta

Log-Likelihood (DLL) and denoted with ‘‘PID’’. For example,

$$\text{PID}_K = \text{DLL}_{K-\pi} = \log(\mathcal{L}_K) - \log(\mathcal{L}_\pi) \quad (2.3)$$

quantifies the probability of a particle being a kaon rather than a pion. Figure 2.9 shows the efficiency for correctly identifying and mis-identifying kaons and protons as a function of the measured momentum of the particle. For kaons the efficiency drops at momenta below 10 GeV, where they fall below threshold for the gas radiators. The DLL cuts enable LHCb physics analyses to distinguish between kinematically similar decays with different final states. For example, Fig 2.10 illustrates the power of particle identification, showing how the application of DLL cuts can be used to isolate  $B^0 \rightarrow \pi^+\pi^-$  decays from other two-body  $B$  decays. The identification of

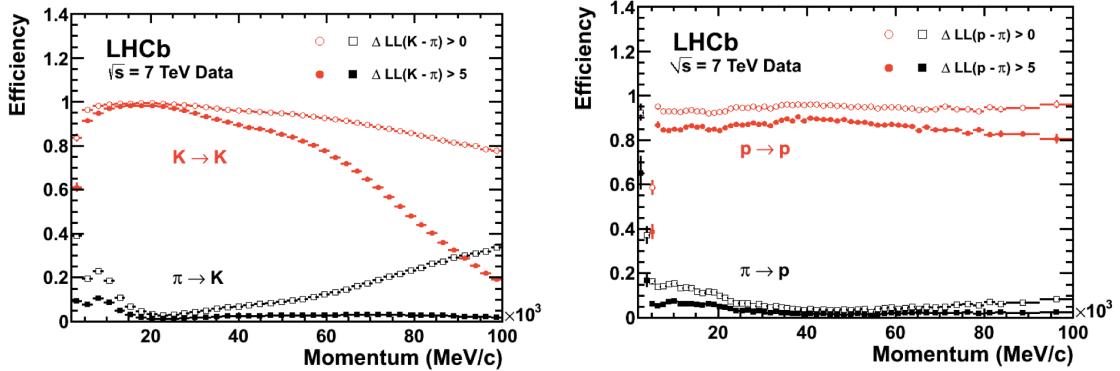


Figure 2.9: Particle identification performances for kaons (left) and protons (right) as a function of the measured momentum of the particles [62].

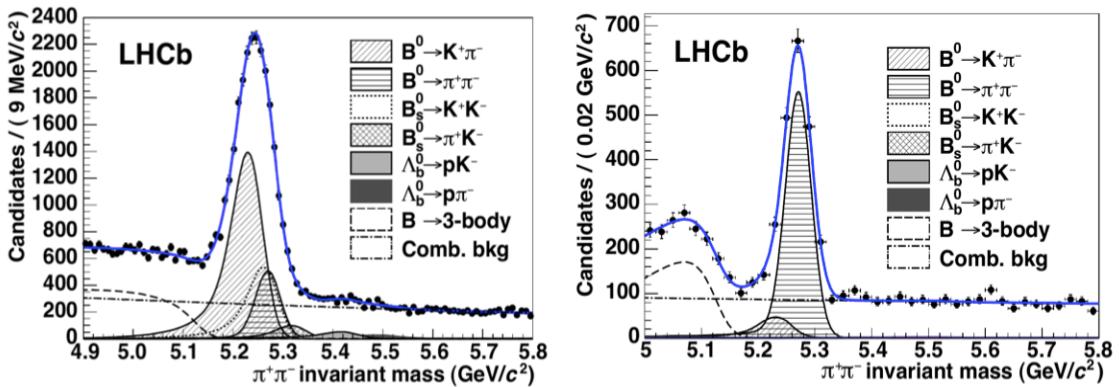


Figure 2.10: Invariant mass peak of the  $B^0 \rightarrow \pi^+\pi^-$  decay before (left) and after (right) the application of PID requirements [68].

muons is particularly important in LHCb and it is quantified using two variables: the  $\text{DLL}\mu$  and the `isMuon` variable. The latter is a boolean variable determined by defining a ‘field of interest’ around a track trajectory extrapolated through the muon chambers. The variable is set to true if hits in multiple muon stations are found in the field of interest.

### 2.8.1 PID calibration

In order to be able to calculate detection efficiencies, a “data-driven” method was developed. The calibration software is referred to as `PIDCalib` package [68]. This tool uses decays where final particles can be identified thanks to their kinematic properties. For example the  $K_s^0 \rightarrow \pi^+\pi^-$  decay has a clear signature with a displaced vertex and can be easily singled out from other decays and used to test pion ID efficiency. The narrow peaks of the  $J/\psi \rightarrow \mu^+\mu^-$  and  $J/\psi \rightarrow e^+e^-$  decays allow muon and electron efficiencies to be calibrated. A “tag-and-probe” method is used in this case, where only one of the two leptonic tracks is reconstructed requiring the correct identity and the other one is used to probe the PID efficiency. Finally,  $\phi \rightarrow KK$  samples and  $D^{*+} \rightarrow D(\rightarrow K^-\pi^+)\pi^+$  decays, where the  $D^{*+}$  is used to tag the decay, are used to test the kaon efficiency. In all cases the residual background is subtracted using the `sPlot` technique [69].

## 2.9 Trigger and software

The LHCb trigger system [70] consists of a hardware stage, L0, based on information from the calorimeters and muon system, followed by a software stage, the High-Level Trigger (HLT), which applies a full reconstruction of the events. To increase performance, the HLT is further split into two stages, HLT1 and HLT2. The HLT1 phase happens in real time and saves data to local disks while the HLT2 phase uses the resources available during periods with no beam. The event selected by the

HLT2 stage are then saved for offline analysis. Figure 2.11 shows a schematic of the trigger system. The bunch crossing frequency is 40 MHz, which corresponds to an instantaneous luminosity of  $2 \cdot 10^{32} \text{ cm}^{-2}\text{s}^{-1}$  for LHCb. About 15% of the total number of  $b\bar{b}$  pairs produced will contain at least one  $B$  meson with all of its decay products within the detector acceptance. This rate needs to be reduced to about 2 kHz at which the events can be written to disk.

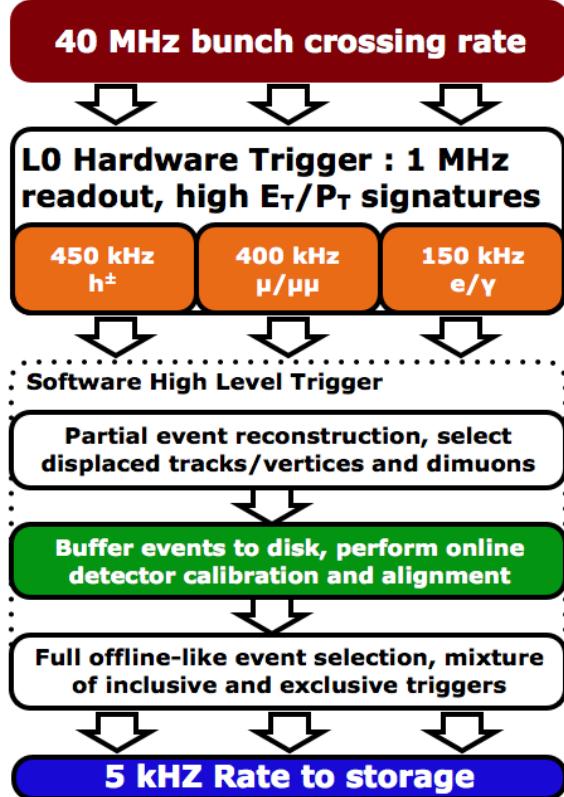


Figure 2.11: A schematic of the LHCb trigger system [62].

The L0 trigger reduces the rate of visible interactions from 10 MHz to 1 MHz. Due to the heavy mass of  $B$  mesons, they often produce particles with high energy and momentum. Therefore the trigger selects events with large deposits in the calorimeter or high  $p_T$  muons. The event is classified as L0Muon if it was triggered due to information from the muon detector, while the information from the calorimeters is used to divide the events into five categories: L0Photon, L0Electron, L0LocalPion, L0GlobalPion, L0Hadron. The PS detector information is converted to a photon flag (`PS && !SPD`) or an electron flag (`PS && SPD`). The “local” label of the L0Pion

trigger refers to  $\pi^0$  reconstructed through their  $\gamma\gamma$  decay, where the two photons fall in the same ECAL element, they are labelled “global” otherwise. The first four calorimeter triggers require energy clusters in the ECAL, while L0Hadron requires clusters also in the HCAL. The HLT1 uses information from the VELO and trackers performing a partial reconstruction of the event and reduces the rate to 2 kHz by adding requirements on the IP and  $\chi^2$  of tracks. Finally, the HLT2 involves a full reconstruction of the event and includes many “lines” designed to select specific decay structures.

LHCb also developed an extended simulation software in order to reconstruct efficiencies and signal shapes. In the simulation,  $pp$  collisions are generated using PYTHIA8 [71, 72] with a specific LHCb configuration [73]. Decays of hadronic particles are described by EvtGen [74], and final state radiation is generated using PHOTOS [75]. Finally, the interaction of the generated particles with the detector and its response are implemented using the GEANT4 toolkit [76] as described in Ref. [77]. For this analysis in this thesis, the ROOT framework [78] is used to analyse data and the RooFit package to perform maximum likelihood fits. A multivariate analysis is also performed based on the NeuroBayes package [79, 80], which provides a framework for neural network training.

## 2.10 Constrained kinematic fits

The resolution of key variables, such as the measured invariant mass of decaying particles, can be improved by imposing constraints on the measured quantities to remove redundant degrees of freedom. The four-momentum conservation can be ensured at each vertex and the origin and decay vertices of a particle are related via the momentum of the particle. Furthermore, additional constraints can be imposed due to a particular decay hypothesis such as the known invariant masses of final and intermediate particles. In order to do this the `DecayTreeFitter` tool was developed by the BaBar experiment and later used by LHCb [81]. The algorithm takes a com-

plete decay chain and parametrises it in terms of vertex positions, decay lengths and momentum parameters. These parameters are then fit simultaneously, taking into account the relevant constraints, including the information from photons. Figure 2.12 illustrates the effect of the application of the kinematical fit on the 4-body invariant mass of the final daughters of the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  decay. The resolution in this case improves by over a factor of 2. Furthermore, the  $\chi^2$  from the kinematic fit can be used to quantify the compatibility with a specific decay structure, which helps to separate candidates where random particles from the event have been added to the decay tree, or where one or more particles is not reconstructed or mis-identified.

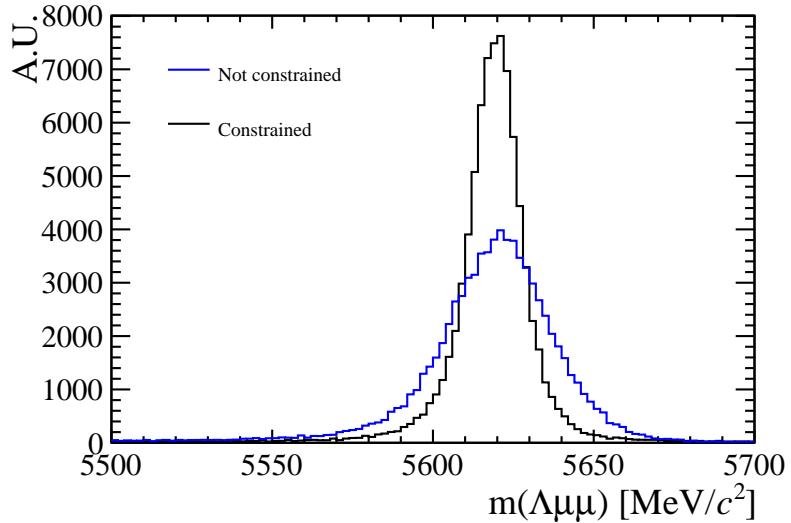


Figure 2.12: Invariant mass of the final daughters of simulated  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  decays calculated with and without constraints using the `DecayTreeFitter` tool.

## 2.11 Validation of hadronic processes in the simulation

Particle-antiparticle asymmetries are of major interest for LHCb and detection efficiencies are usually obtained from simulation. It is therefore important, in order to limit systematic uncertainties, to have a model that parametrises correctly the cross-sections of particles and antiparticles or at least their ratio.

The LHCb simulation software propagates particles through the detector using the

GEANT4 toolkit [62]. This offers a variety of models for physics processes over a wide range of energies for both electromagnetic and strong interactions. Given a combination of projectile, target and energy there can be several models applicable with different reliability and computational costs. GEANT4 provides a number of pre-packaged physics lists each representing complete and consistent sets of models chosen to be appropriate for a given use case. In LHCb mainly two hadronic physics lists are considered:

- **LHEP** (Low and High Energy Parametrisation): based on a parametrised modelling of all hadronic interactions for all particles. This list combines the High Energy Parametrised model (HEP) and the low energy one (LEP). There is a sharp switch from the low to the high energy model at 25 GeV. The modelling of elastic scattering off a nucleus and of nuclear capture also proceeds via parametrised models.
- **FTFP\_BERT**: includes the following models:
  - Bertini cascade model (BERT) [82], which simulates the intra-nuclear cascade, followed by pre-equilibrium and evaporation phases of the residual nucleus, for protons, neutrons, pions and kaons interaction with nuclei at kinetic energies below 9.9 GeV. The Bertini model produces more secondary neutrons and protons than the LEP model, yielding a better agreement with experiment data.
  - FTFP model, which implements high energy inelastic scattering of hadrons by nuclei using the FRITIOF model [83].

The change between the two models happens with a linear shift from BERT to FTFP that starts at 4 GeV and ends at 5 GeV.

Figure 2.13 summarises the composition of the different models.

When two models overlap in an energy interval the choice of the model for each interaction is made using a random number: the probability to select each model varies linearly from 0 to 100% over the overlap range. Because of the differences of the two models in the overlap region, unphysical discontinuities can be produced as a function of energy.

### 2.11.1 Geometry and interaction probability

The results presented in the following sections are produced using the version v45r0 of the full LHCb framework for simulation, **GAUSS** [77], which is interfaced to **GEANT4** v95r2p1. A simple geometry setup is used in order to be able to calculate in a clean way the interaction cross-sections in a specific material. This is constituted by a series of rectangular boxes filled with the most relevant materials for LHCb: Aluminium, Silicon and Beryllium. For each material three boxes are defined with different thicknesses (1mm, 10mm, 50mm). These values are chosen to be indicative of the amount of material present in the LHCb detector.

The simplest quantity available to extract the cross-section is the interaction probability,  $P_{int}$ , defined as:

$$P_{int} = \frac{N_{int}}{N_{tot}}, \quad (2.4)$$

where  $N_{int}$  is the number of particles which interacted in the material and  $N_{tot}$  is the number of generated particles. As **GEANT4** provides an ID for the end process

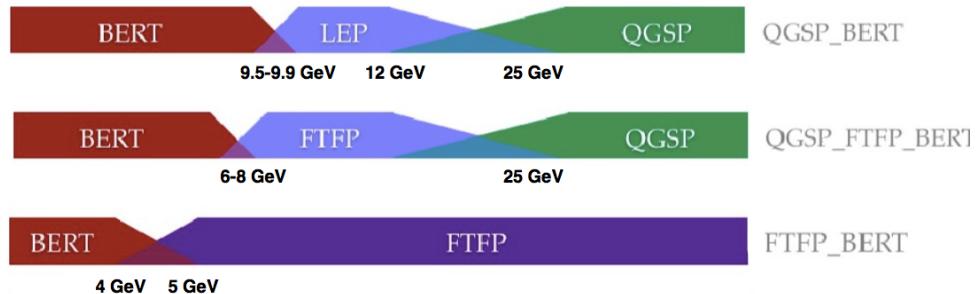


Figure 2.13: Diagram of LHEP, FTFP\_BERT and QGSP\_BERT models' composition as a function of energy.

of a particle (e.g. 121 for inelastic interaction, 111 for elastic, 201 for decay) it is possible to distinguish the inelastic and elastic probabilities of interaction and therefore cross-sections.

To compare simulation and data the cross-section and  $P_{int}$  are related through the following formula valid for thin layers:

$$\sigma_{int} = \frac{A}{\rho N_A \Delta x} \cdot P_{int}, \quad (2.5)$$

where  $\rho$  is the density of the material and  $A$  is its mass number,  $\Delta x$  is the thickness of the considered layer and  $N_A$  is the Avogadro number.

### 2.11.2 PDG prediction

In the Review of Particle Physics (PDG) [2] cross-sections of protons and neutrons are parametrised as:

$$\sigma_{tot}^{ab} = Z^{ab} + B^{ab} \log^2(s/s_M) + Y_1^{ab}(s_M/s)^{\eta_1} - Y_2^{ab}(s_M/s)^{\eta_2}, \quad (2.6)$$

$$\sigma_{tot}^{\bar{a}\bar{b}} = Z^{ab} + B^{ab} \log^2(s/s_M) + Y_1^{ab}(s_M/s)^{\eta_1} + Y_2^{ab}(s_M/s)^{\eta_2}, \quad (2.7)$$

where  $s_M = (m_a + m_b + M)^2$  and  $B^{ab} = \lambda \pi (\frac{\hbar c}{M})^2$ . Some of the constants in these equations are universal and valid for any kind of collision:  $M = 2.15$ ,  $\eta_1 = 0.462$ ,  $\eta_2 = 0.551$ ,  $\lambda = 1$  (for p, n and  $\gamma$ ) and 1.63 (for d). The other ones are characteristic of each type of collision and are listed in Tab. 2.11.2. In these formulae the particle-antiparticle asymmetry arises from the last term which has opposite sign in the two equations. This term becomes less and less important with increasing energies. Therefore a net asymmetry is found at low energies, while the cross-sections tend to a common point at high energy and continue increasing logarithmically.

### 2.11.3 Validation results

This section reports particle and antiparticle cross-sections and their ratios compared, where available, with predictions and with data from the COMPASS experiment [84]. Figure 2.14 shows the probability of interaction for protons and anti-protons in 10 mm of Aluminium using the FTFP\_BERT and LHEP models compared with COMPASS data and Fig. 2.15 shows the ratios of  $\sigma_{\bar{p}}^{tot}/\sigma_p^{tot}$  together with the PDG prediction. A difference of 40% is found between the two considered models for 1 GeV incoming anti-protons. This difference becomes negligible at higher energies. The discrepancies between the two physics lists for kaons and pions are of a few percents (2–3%) and usually constant with the energy. From the comparison with data and PDG predictions it can be qualitatively concluded that the FTFP\_BERT model gives a better description of hadronic interactions at low energies, while both models give good results at high energy, above  $\sim 10$  GeV.

The tool developed for these studies is not limited to cross-sections but can also give information on other simulated quantities. As an example, Fig. 2.11.3 shows a comparison between the types of particles generated in inelastic collisions of protons and anti-protons onto Aluminium using different models. Physics lists can give very different results, for example the LHEP model does not produce photons in inelastic collisions. However, it is difficult to use these quantities for validation as there is no data available for a comparison.

| Proj / Targ      | $Z^{ab}$ | $Y_1^{ab}$ | $Y_2^{ab}$ |
|------------------|----------|------------|------------|
| $\bar{p}, p / p$ | 34.71    | 12.72      | 7.35       |
| $\pi^\pm / p$    | 19.02    | 9.22       | 1.75       |
| $K^\pm / p$      | 16.56    | 4.02       | 3.39       |
| $K^\pm / n$      | 16.49    | 3.44       | 1.82       |
| $\bar{p}, p / n$ | 35.00    | 12.19      | 6.62       |

Table 2.1: Values for the constants  $Z^{ab}$ ,  $Y_1^{ab}$  and  $Y_2^{ab}$  [2], which parametrise hadronic cross-sections.

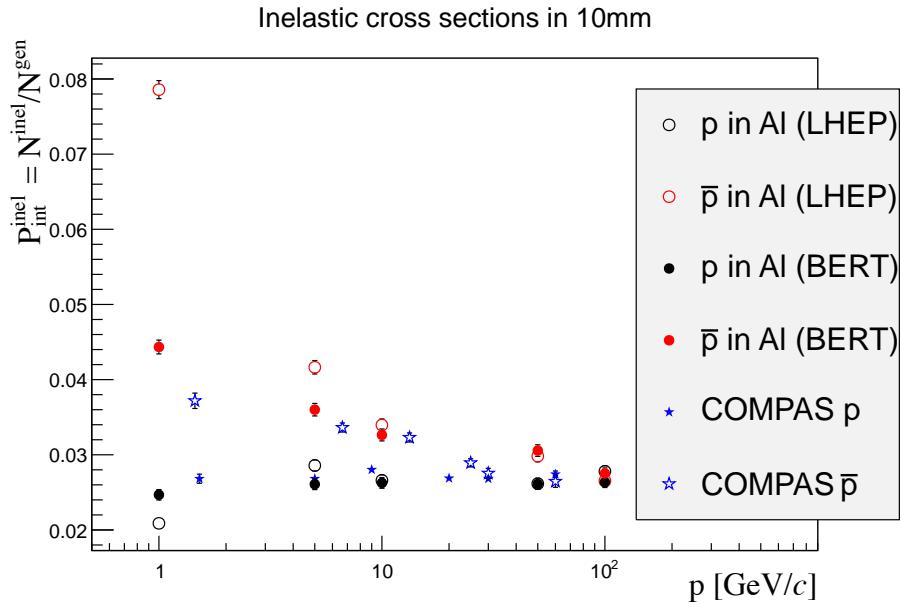


Figure 2.14: Probability of interaction for protons and anti-protons in Aluminium as a function of the projectile momentum. Two physics lists are used to generate events that can be compared with data from the COMPASS experiment.

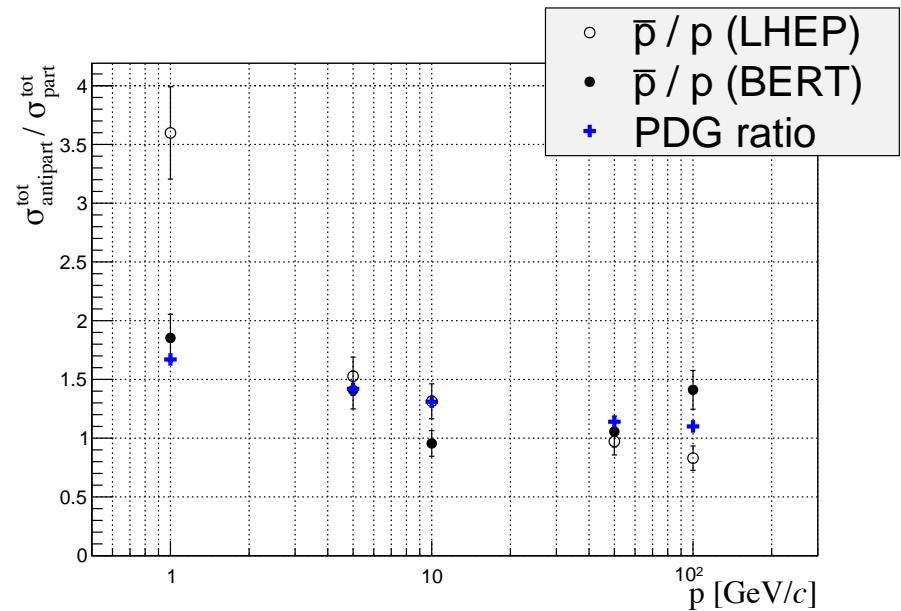


Figure 2.15: Ratio of antiproton over proton total interaction cross-section as a function of energy compared with PDG predictions.

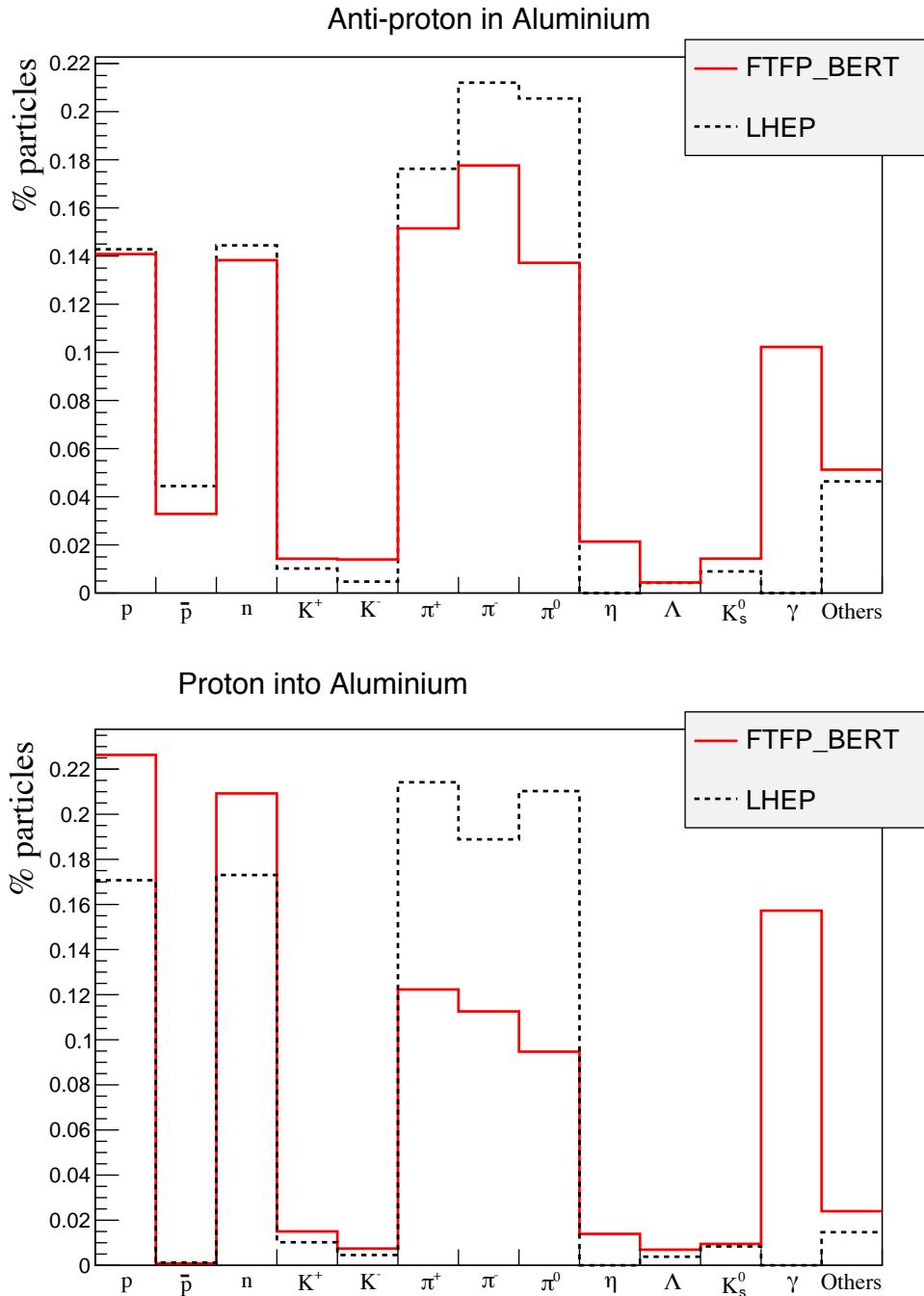


Figure 2.16: Composition of secondary particles produced in 100 GeV protons (top) and anti-protons (bottom) collisions in 1 mm Aluminium.

## 2.12 Material budget studies

It is important for many analysis to quantify the amount of material present in the detector, for example to estimate the amount of multiple scattering. In GEANT4 particles are propagated in steps through the detector and for each step the framework analyses the geometry to understand in what material the particle is and modifies its trajectory accordingly. A tool was developed where neutrinos are used as probes to scan the detector summing the radiation length seen at each step up to a certain point. Neutrinos are used as they do not bend in magnetic field and do not interact with the detector to any appreciable extent. Thin air planes are inserted after each sub-detector. When these are traversed by the neutrinos, the information about the accumulated radiation and interaction length is saved. In this way it is possible to obtain maps of the detector, such as the one shown in Fig. 2.17. Using the tool developed for this study it is also possible to obtain the cumulative interaction length. As an example Fig. 2.18 shows the average radiation length as a function of the distance from the interaction point. Furthermore, it is possible to displace the primary vertex from its position, normally set at the origin, in order to study how this translates into the amount of material traversed.

## 2.13 Validation and material budget studies conclusions

The studies outlined in the previous two sections are based on tools which are now officially part of the LHCb simulation framework. These tools were used to validate the framework when passing from GEANT4 version 9.5 to version 9.6. In particular a patch was provided by the GEANT4 team including improved kaon cross sections and it was verified these go into the right direction. The tool will continue to be used in the future, in particular to validate the upgrade to GEANT4 10, in 2016. Furthermore, the tools can be used by analyses sensitive to the quality of the simulation of particle and antiparticles cross-sections in order to study systematic effects and uncertainties.

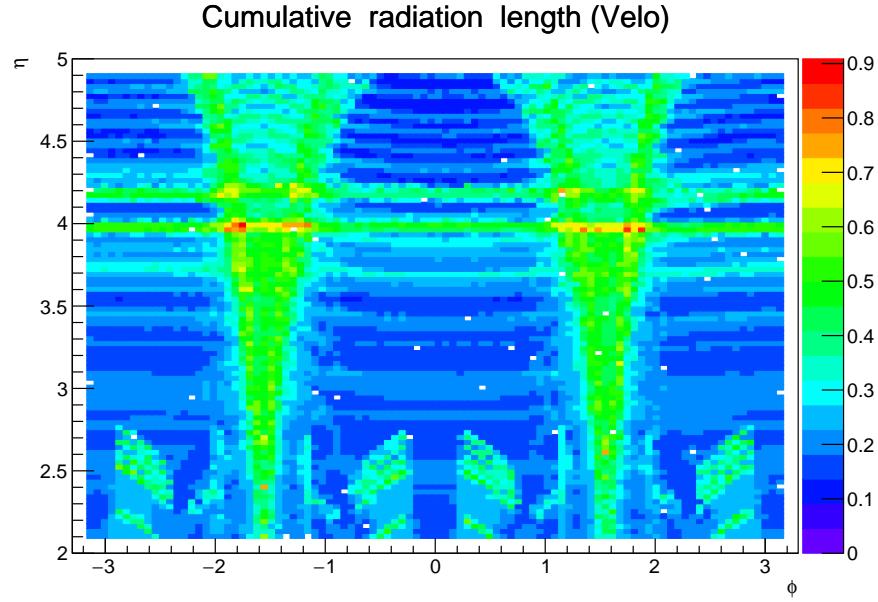


Figure 2.17: Map of cumulative radiation length seen by a particle starting from the interaction point up to the end of the VeLo.

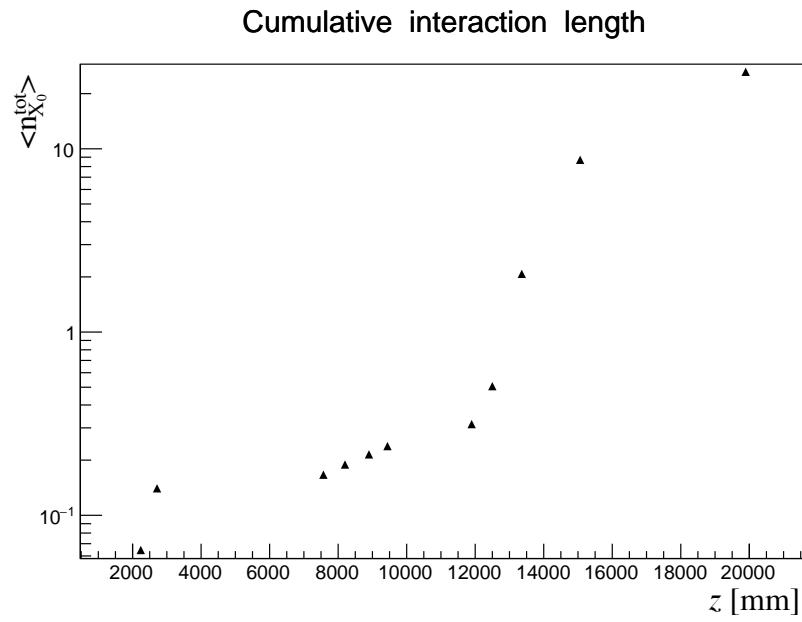


Figure 2.18: Average cumulative radiation length as a function of the horizontal distance from the interaction point. Each considered point corresponds to the end of a sub-detector: VeLo, RICH1, RICH2, tracking stations, ECAL and HCAL and muon detector.

## CHAPTER 3

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### Differential branching fraction of $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$

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The  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decay is a FCNC process governed by the  $b \rightarrow s\mu^+\mu^-$  quark level transition which, in the SM, proceeds only through loop diagrams (electroweak penguin or  $W$  box) as discussed in Sec. 1.5, and therefore it is highly sensitive to new particles entering the loops. Interest in  $\Lambda_b^0$  baryon decays arises, first of all, from the fact that the  $\Lambda_b^0$  has non-zero initial spin, which allows to extract information about the helicity structure of the underlying Hamiltonian that cannot be obtained from meson decays [85, 86]. Secondly, the  $\Lambda_b^0$  baryon can be considered to a first approximation as composed of a heavy quark and a light di-quark, therefore the hadronic physics differs significantly from  $B$  meson decays. This provides the possibility to better understand and test the hadronic physics in the theory, which could yield an improved understanding relevant also for the meson case.

With respect to  $B^0$  decays going through the same transitions, such as  $B^0 \rightarrow K^{*0}\mu^+\mu^-$ ,  $\Lambda_b^0$  decays can provide independent confirmations of the results as they involve the same operators but different hadronic matrix elements. Furthermore,  $\Lambda$  baryons

decay weakly, which results in complementary constraints with respect to  $B^0$  decays. Finally, the narrow width approximation, used in theoretical calculations, is fully applicable in the  $\Lambda_b^0$  case, which has  $\Gamma_{\Lambda_b^0} \sim 2.5 \cdot 10^{-6}$  eV. This is not the case for  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  decays because the contribution from the non-resonant channel  $B^0 \rightarrow K \pi \mu^+ \mu^-$  is unconstrained.

The theory of  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decays was widely investigated both in the context of the SM and in various BSM scenarios [87, 88, 89, 90, 91, 92, 93, 94, 95, 96, 97]. All authors start from the effective Hamiltonian outlined in Sec. 1.5.1. However, form factors, describing hadronic physics are not as well-developed as for the meson case because there are fewer experimental constraints, which leads to a relatively large spread in predicted branching fractions. For these reasons an interesting quantity to study is the differential branching fraction as a function of  $q^2$ . This still suffers from the limited knowledge of form factors but, as different approaches to form factors calculations are applicable in different  $q^2$  regions, it allows a more meaningful comparison with theory.

Experimentally, the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay was observed for the first time in 2011 by the CDF collaboration [98] and later updated in preliminary form using their full statistics [99]. The latter measurement yields  $\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-) = [1.95 \pm 0.34(\text{stat}) \pm 0.61(\text{syst})] \times 10^{-6}$  and the signal was observed only in the  $q^2$  region above the square of the  $\psi(2S)$  mass. Recently, the decay was also observed at LHCb [100] with a yield of  $78 \pm 12$  signal events using  $1 \text{ fb}^{-1}$  of integrated luminosity collected in 2011. The signal was also found only in the high  $q^2$  region, above  $m_{\psi(2S)}^2$ . The LHCb result for the branching fraction relative to the  $J/\psi \Lambda$  decay, which is used as a normalisation channel, is

$$\frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi \Lambda)} = [1.54 \pm 0.30 \text{ (stat)} \pm 0.20 \text{ (syst)} \pm 0.02 \text{ (norm)}] \times 10^{-3}$$

and for the absolute branching fraction,

$$\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-) = [0.96 \pm 0.16 \text{ (stat)} \pm 0.13 \text{ (syst)} \pm 0.21 \text{ (norm)}] \times 10^{-6}.$$

This chapter describes the measurement of the differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decay using  $3 \text{ fb}^{-1}$  of  $pp$  collisions collected by the LHCb experiment in 2011 and 2012.

### 3.1 Analysis strategy and $q^2$ regions

A typical  $q^2$  spectrum of  $b \rightarrow s\ell^+\ell^-$  decays was shown in Fig. 1.8. This is characterised by the presence of the photon pole at low  $q^2$  and the narrow peaks of the  $J/\psi$  and  $\psi(2S)$  resonances at intermediate values of  $q^2$ . In the analysis,  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  decays, in which the  $J/\psi$  decays into two muons and therefore has the same final state as the signal, are used as the normalisation channel. The rare and normalisation channels are naturally distinguished by the  $q^2$  intervals in which they are reconstructed. The  $\Lambda$  decay mode into a pion and a proton,  $\Lambda \rightarrow p\pi$ , is always used to reconstruct the decays. The intervals in which the rare channel is studied are:

- $0.1 < q^2 < 8 \text{ GeV}^2/c^4$ , where the signal is unobserved and the selection is optimised to observe it. The upper bound of this interval is chosen to be sufficiently far from the  $J/\psi$  radiative tail at low masses and reduce its contamination into the rare sample;
- $11 < q^2 < 12.5 \text{ GeV}^2/c^4$ , between two charmonium resonances, and
- $q^2 > 15 \text{ GeV}^2/c^4$ , above  $\psi(2S)$ .

The first interval, below the  $J/\psi$  resonance, is referred to as “low- $q^2$ ” region, while the two intervals above the  $J/\psi$  resonance ( $q^2 > 11 \text{ GeV}^2/c^4$ ) are referred to as “high- $q^2$ ” regions. These regions are then sub-divided into smaller intervals, as the available statistics allows, which results in  $\sim 2 \text{ GeV}^2/c^4$  wide bins. The binning used is the following:

$$[0.1, 2.0, 4.0, 6.0, 8.0], J/\psi, [11.0, 12.5], \psi(2S), [15.0, 16.0, 18.0, 20.0]. \quad (3.1)$$

In addition the result is also provided in two integrated regions:

- 1.1–6.0  $\text{GeV}^2/c^4$ : this interval is theoretically favoured to observe new physics effects since it is far from the photon pole, which dominates at low  $q^2$  values, reducing the sensitivity to new physics contributions. The lower bound of this interval is chosen to exclude the possible contribution from the  $\phi$  resonance, which appears at  $\sim 1 \text{ GeV}^2/c^4$ . The upper bound of the interval is chosen to exclude completely a small contribution from the  $J/\psi$  resonance that leaks below  $8 \text{ GeV}^2/c^4$ .
- 15.0–20.0  $\text{GeV}^2/c^4$ : this interval is the one that is expected to contain most of the rare decays and it is used as a natural cross check that the analysis is stable when performed in smaller bins.

## 3.2 Candidate types

This analysis deals with  $\Lambda$  baryons, which have a lifetime of  $(2.632 \pm 0.020) \times 10^{-10} \text{ s}$  [2]. These are considered long-lived particles in particle physics terms and can travel several metres into the detector generating well distinguished secondary vertices. In LHCb,  $\Lambda$  baryons can be reconstructed from tracks either with or without hits in the VeLo (see Sec. 2.4) and therefore two candidates types are defined as follows:

- **Downstream candidates**: built from tracks without hits in the VeLo, “downstream tracks”, also denoted as “DD”.
- **Long candidates**: built from tracks which also have hits in the VeLo, “long tracks”. These candidates, also denoted as “LL”, are characterised by a better momentum resolution than the downstream ones thanks to the longer lever arm available to their tracks.

Figure 3.1 shows the two types of candidates used in the analysis, together with other possible track types in LHCb, which are not used in this analysis. As the long

and downstream candidate categories are characterised by different resolutions and kinematic properties, the analysis is performed separately on the two samples and the results are then combined.

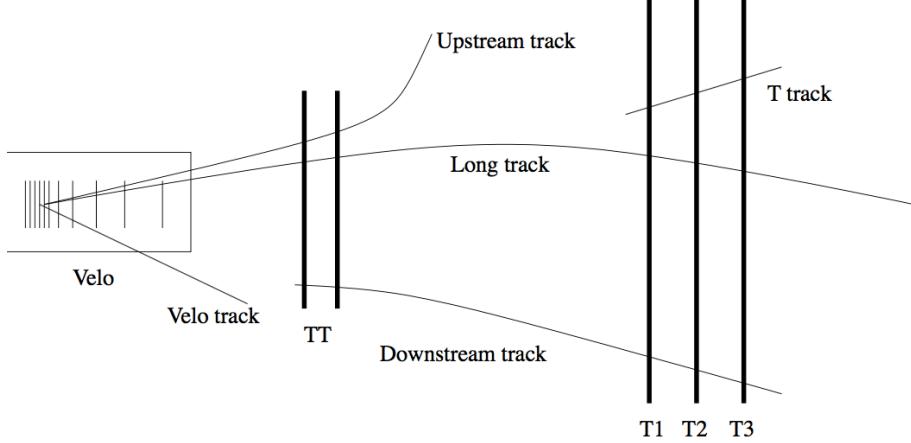


Figure 3.1: Representation of possible track types in LHCb. Candidates built from “long” and “downstream” tracks are used in this analysis [62].

### 3.3 Simulation

Samples of simulated events are needed in order to train a multivariate classifier, calculate the selection efficiency and study possible backgrounds; in particular for this analysis samples of  $\sim 2 \cdot 10^6 \Lambda_b^0 \rightarrow J/\psi \Lambda$  and  $\sim 5 \cdot 10^6 \Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  simulated decays are used. Samples of simulated  $B^0 \rightarrow J/\psi K_s^0$ ,  $B^0 \rightarrow K_s^0\mu^+\mu^-$  and  $B^+ \rightarrow \mu^+\mu^-K^{*+}$  decays are also used to study their contribution to the background. The events are generated using PYTHIA8; hadronic particles are decayed using EVTGEN and GEANT4 is used to simulate the interaction of final state particles with the detector. Simulated events are then reconstructed by the same reconstruction software that is used for real data. The L0 hardware trigger is emulated in the simulation, while for the software stage, HLT, the same code can be used as for data. Events are simulated using both 2011 and 2012 beam and detector conditions, in the same proportion as in recorded data. While the simulation gives a generally good description of data, some discrepancies remain. It is important that the simulation gives an accurate description of the data, in particular for the extraction of efficiencies. The next

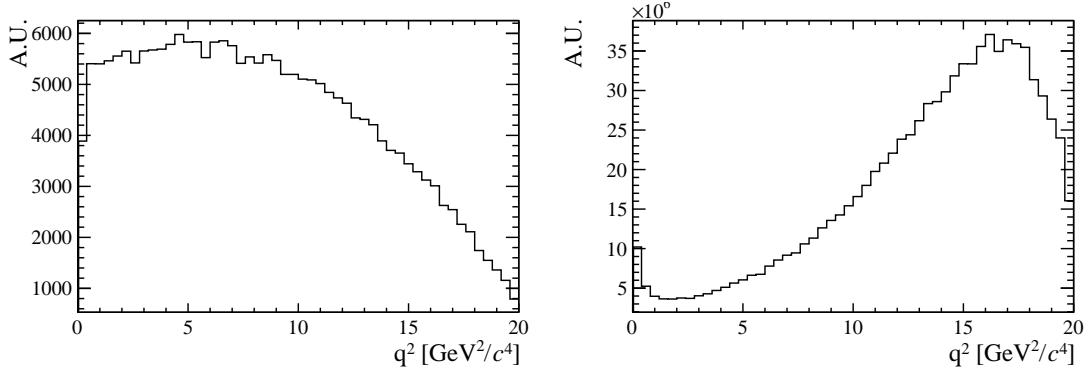


Figure 3.2: The  $q^2$  spectrum of  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  simulated events according to the phase space of the decay (left) and re-weighted using the decay amplitudes (right).

sections therefore describe corrections applied to the simulation in order to provide a better description of data. In Appendix B data distributions are compared with simulated ones for variables relevant to this analysis.

### 3.3.1 Decay Model

Little is known about the decay structure of  $\Lambda_b^0$  decays and therefore the simulation software generates events according to the phase space given by the available kinematics. To obtain a more realistic  $q^2$  dependence, the simulation is weighted using decay amplitudes based on the predictions in Ref. [101]. Equations in this paper are for the case of unpolarised  $\Lambda_b^0$  production and for this analysis they are extended to include polarisation. Details about the models used are given in Appendix A.1. The value of the  $\Lambda_b^0$  production polarisation,  $P_b$ , used in the calculations is  $P_b = 0.06$  as measured by LHCb [102]. Figure 3.2 shows the phase space  $q^2$  distribution and the one obtained by re-weighting the events. The latter can be qualitatively compared to the  $q^2$  spectrum of a generic  $b \rightarrow s\ell^+\ell^-$  decay shown in Fig. 1.8. For the normalisation mode, the decay model used is described in Appendix A.3, with amplitude magnitudes and production polarisation taken from the measurements in Ref. [102]. Phases are not yet measured and are therefore set to zero.

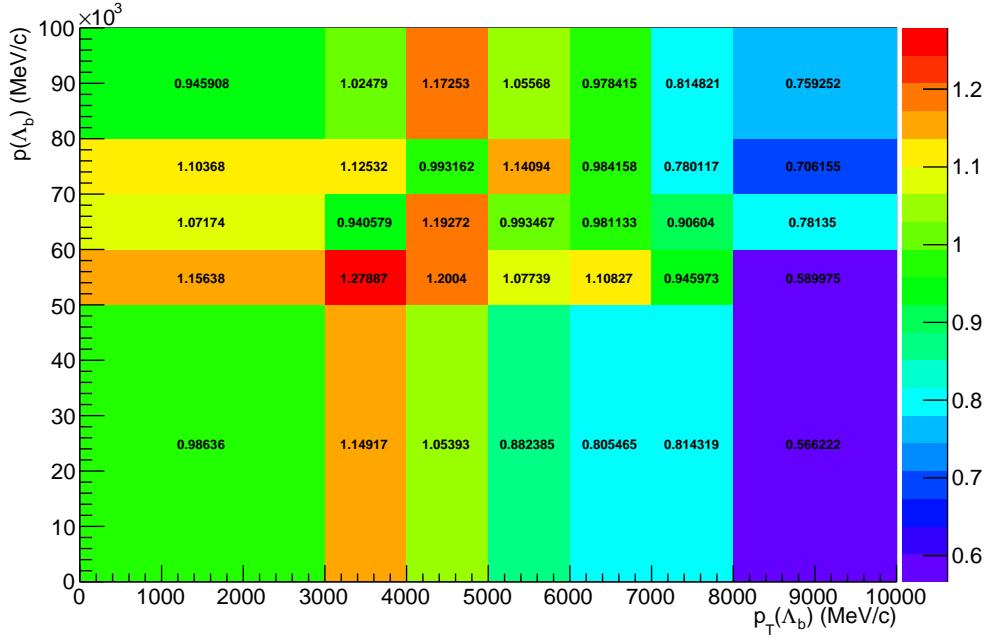
### 3.3.2 Kinematic re-weighting

Small data-simulation differences are found in the kinematic properties of the mother particle,  $\Lambda_b^0$ , which also affect the final state particles. The simulation is re-weighted by comparing the momentum and transverse momentum of  $\Lambda_b^0$  baryons in real and simulated  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates that satisfy the pre-selection requirements (see Sec. 3.4). To do this a high purity data sample is obtained by selecting a narrow invariant mass interval around the  $J/\psi$  and  $\Lambda_b^0$  peaks; this contains about  $4 \cdot 10^5$  candidates. The  $\Lambda_b^0$  invariant mass distribution is then fitted to estimate the number of background decays under the peak. Finally, the background fraction,  $f_b = B/(S + B)$ , is used to statistically subtract the background from the kinematical distributions as described by the equation:

$$S(p, p_T) = T(p, p_T) - f_b \cdot B(p, p_T), \quad (3.2)$$

where  $S(p, p_T)$  is the distribution of pure signal candidates, which we want to obtain,  $T(p, p_T)$  is the total distribution of signal plus background, namely the distribution of all events in the signal interval,  $5605 < m(p\pi\mu^+\mu^-) < 5635$  MeV/ $c^2$ , and  $B(p, p_T)$  is the pure background distribution obtained using candidates from the upper sideband,  $m(p\pi\mu^+\mu^-) > 5800$  MeV/ $c^2$ .

After the signal distributions have been obtained from data, they are compared with  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  simulated events and a weight,  $w(p_{\Lambda_b^0}, p_{T,\Lambda_b^0})$  is defined by taking the ratio of the two dimensional  $(p, p_T)$  distributions. The result is shown in Fig. 3.3, while Appendix B reports distributions of sideband subtracted data in the signal and sideband regions together with weighted and unweighted simulated events. In these plots the momentum and  $p_T$  distributions of  $\Lambda_b^0$  baryons match by construction but the re-weighting also improves the agreement between the kinematical distributions of all final particles. Small differences remain due to the finite binning used for the weights calculation. Quality variables, such as the  $\chi^2$  of tracks and vertices, show little dependence on the kinematics and are relatively unaffected by the weighting procedure.



## 3.4 Selection

This section describes the requirements applied to reconstruct  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  and  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  candidates. The selection procedure is divided into two steps: a pre-selection, where cuts are applied in order to be able to work with manageable datasets and a multivariate analysis (MVA) which combines information from several variables. As a first step good quality tracks are selected by imposing requirements on their basic kinematic properties, such as the  $p_T$  of the final particles, and quality requirements, such as the track  $\chi^2$ . The selection then forms a dimuon candidate from two oppositely charged muons. In events containing a dimuon candidate, two oppositely charged tracks are combined and retained as a  $\Lambda$  candidate if they form a good quality vertex which is well separated from all primary vertices. Finally, the dimuon and  $\Lambda$  candidates are combined to form  $\Lambda_b^0$  baryons with requirements placed on the properties of this combination.

### 3.4.1 Pre-selection

The full list of pre-selection cuts is reported in Tab. 3.1. In the table  $\chi_{IP}^2$  is defined as the projected distance from a vertex divided by its uncertainty, for example the  $\chi_{IP}^2(primary) > n$  requirement on  $\Lambda_b^0$  means that the  $\Lambda_b^0$  vertex must be at least  $\sqrt{n}$  standard deviations away from the primary vertex. Another quantity, found to be particularly powerful at removing combinatorial background, is a pointing variable called DIRA defined as the cosine of the angle between the direction of a particle's momentum and the flight direction from its mother vertex. Requiring a DIRA close to unity corresponds to the selection of particles with well-defined origin vertices. Figure 3.4 shows graphical representations of the  $\chi_{IP}^2$  and DIRA variables. The variable  $\chi_{FD}^2$  represents the flight distance of a particle from its origin vertex divided by the corresponding uncertainty. The  $\chi_{trk}^2/ndf$  and  $\chi_{vtx}^2/ndf$  quantities are the  $\chi^2$  from the fit to tracks and vertices, which are used to quantify their quality. The `GhostProb` quantity describes the probability of a track being fake. By

construction, cutting at a value of  $k$ , removes  $(1 - k) \cdot 100\%$  of fake tracks. The `hasRich`, `hasCalo` and `isMuon` variables are binary indicators that the information from the RICH, calorimeter and muon detectors is available for the track. Loose PID requirements on the proton are also applied in the pre-selection. Details about PID quality estimators are given in Sec. 2.8. A large mass window around the  $\Lambda_b^0$  peak is used to allow a fit to the sideband to be performed and to use sideband candidates to train a multivariate classifier. Rare candidates are selected by the  $q^2$  region requirements described in Sec. 3.1, while resonant candidates are further constrained to have dimuon invariant masses in a  $100 \text{ MeV}/c^2$  interval around the known  $J/\psi$  mass [2].

### 3.4.2 Neural Networks

The final selection is performed using a neural network classifier based on the NeuroBayes package. The input to the neural network consists of 14 variables carrying information about the kinematics of the decay, the quality of tracks and vertices and the PID of the muons. The list of the 10 most significant inputs is reported in Tab. 3.2, together with information about the importance of each input. Variables related to  $\Lambda$  and its daughters are considered as different inputs depending on the candidate type (long or downstream). This effectively corresponds to making a separate training for the two categories.

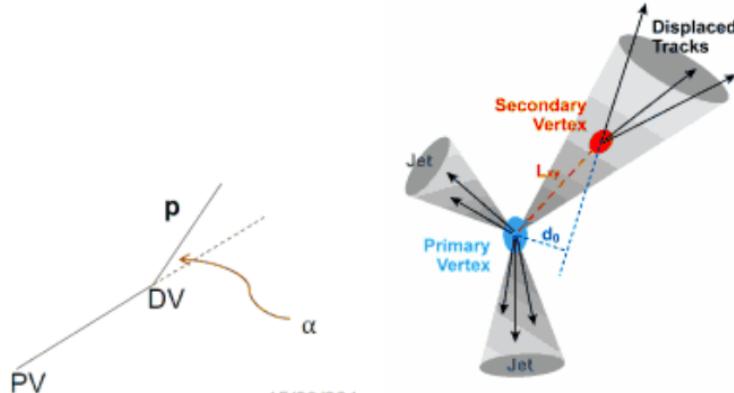


Figure 3.4: Graphical representation of the DIRA (left) and  $\chi_{\text{IP}}^2$  (right) variables.

| Particle              | Requirement                                                                                                                                                             |
|-----------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $\Lambda_b^0$         | $4.6 < m(p\pi\mu\mu) < 7.0 \text{ GeV}/c^2$<br>$\text{DIRA} > 0.9999$<br>$\chi_{\text{IP}}^2 < 16.0$<br>$\chi_{\text{FD}}^2 > 121.0$<br>$\chi_{\text{vtx}}^2/ndf < 8.0$ |
| $\Lambda$             | $\chi_{\text{vtx}}^2/ndf < 30.0(25.0)$<br>$\text{Decay time} > 2 \text{ ps}$<br>$ m(p\pi) - m_A^{\text{PDG}}  < 35(64) \text{ GeV}/c$                                   |
| $p/\pi$               | $p > 2 \text{ GeV}/c$<br>$p_{\text{T}} > 250 \text{ MeV}/c$<br>$\chi_{\text{IP}}^2 > 9(4)$                                                                              |
| $p$ (only long cand.) | $\text{hasRICH}$<br>$\text{PID}p > -5$                                                                                                                                  |
| $\mu$                 | $\text{isMuon}$<br>$\chi_{\text{trk}}^2/ndf < 5$<br>$\text{GhostProb} < 0.4$<br>$\text{PID}\mu > -3$<br>$\chi_{\text{IP}}^2 > 9.0$                                      |
| Dimuon                | $\chi_{\text{vtx}}^2/ndf < 12.0$<br>$ m(\mu\mu) - m_{J/\psi}^{\text{PDG}}  < 100 \text{ MeV}/c^2 \quad (J/\psi \Lambda \text{ only})$                                   |

Table 3.1: Summary of the pre-selection requirements. Where two values are given, the main one applies to long candidates and the one in parenthesis to downstream candidates.

The neural network is trained using representative samples of signal and background. A sample of simulated  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  candidates is used as a proxy for the signal, while for the background a representative sample is given by candidates in the upper  $m(p\pi\mu\mu)$  invariant mass sideband. Only the upper sideband,  $m(p\pi\mu\mu) > 6 \text{ GeV}/c^2$ , is used since it contains only combinatorial background, while the lower sideband may contain partially reconstructed and misreconstructed candidates. In the  $q^2$  spectrum of background samples the  $J/\psi$  and  $\psi(2S)$  peaks are still present indicating that charmonium resonances are often combined with other random tracks. These candidates do not give a good description of purely combinatorial background and, in order to avoid biases, they are removed from the training sample by rejecting candidates in a  $100 \text{ MeV}/c^2$  interval around the nominal  $J/\psi$  and  $\psi(2S)$  masses [2]. A total of  $3 \cdot 10^4$  events is used for the training from each sample. This corresponds to approximately  $\simeq 50\%$  of the available sideband data and  $\simeq 20\%$  of the simulated

Table 3.2: Summary of the 10 most significant inputs to the neural network in order of importance. Column “adds” gives the significance added by a given input when it is added to the list of those ranked above. Column “only this” provides the power of a given input alone and “loss” shows how much information is lost when removing only a given input.

| Input                                        | adds   | only this | loss  |
|----------------------------------------------|--------|-----------|-------|
| $\Lambda_{\text{DD}} p_T$                    | 143.11 | 143.11    | 29.20 |
| $\chi^2_{\text{DTF}}$                        | 77.81  | 134.00    | 51.10 |
| $\min(\chi^2_{\text{IP}}, \mu)$              | 61.31  | 113.62    | 29.76 |
| $\chi^2_{\text{IP}} \Lambda_b^0$             | 52.94  | 113.23    | 40.98 |
| $\chi^2_{\text{IP}} \pi_{\text{LL}}$         | 20.29  | 60.72     | 12.82 |
| $\min(\text{PID}, \mu)$                      | 17.91  | 59.11     | 13.44 |
| $\tau_{\Lambda_b^0}$                         | 16.24  | 35.36     | 11.24 |
| $\Lambda_b^0 \text{DIRA}$                    | 12.28  | 73.96     | 9.98  |
| $\Lambda_{\text{DD}} \text{flight distance}$ | 9.47   | 86.75     | 11.24 |
| $\chi^2_{\text{IP}} \Lambda_{\text{DD}}$     | 10.58  | 59.84     | 8.88  |

sample. The full simulated sample is not used in the training as the same sample will also be used to study efficiencies. For reproducibility the events are sampled uniformly.

The single most important variable used for downstream candidates is the transverse momentum of  $\Lambda$ , which allows random combinations of tracks to be rejected as these have preferentially low  $p_T$ . In contrast, for long candidates the most powerful variable is the  $\chi^2$  from a kinematic fit that constrains the decay products of the  $\Lambda_b^0$ , the  $\Lambda$  and the dimuon, to originate from their respective vertices. Other variables that contribute significantly are the  $\chi^2_{\text{IP}}$  of  $\Lambda_b^0$ ,  $\Lambda$  and muons, the separation between the  $\Lambda_b^0$  and  $\Lambda$  vertices and, finally, the muon PID.

Figure 3.5 shows distributions of neural network output for the signal and background samples and purity,  $P = N_{\text{sig}}/N_{\text{bkg}}$ , as a function of the neural network output. To check for potential overtraining, the distributions from test samples are also overlaid. These are found to follow the same shape but with different fluctuations giving no significant evidence of overtraining. In general it can be concluded that the neural network is able to separate signal from background and the training converged properly. It can happen that too much information is given

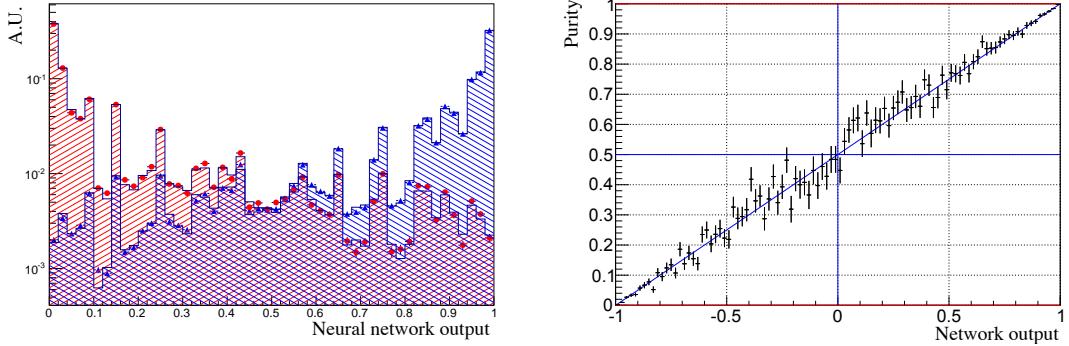


Figure 3.5: (left) Neural network output distribution for training (points) and test (stripes) samples, for signal (blue) and background (red) candidates. (right) Purity as a function of neural network output.

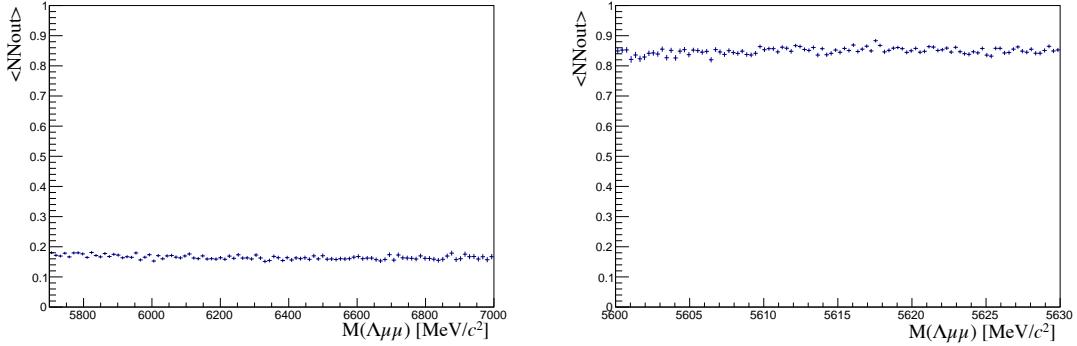


Figure 3.6: Average value of neural network output as a function of the 4-body invariant mass for data sideband (left) and simulated signal (right) candidates.

to the classifier, allowing the invariant mass of the candidates to be inferred from the input variables. This can generate fake peaks and it is therefore important to check for correlations between the 4-body invariant mass and the neural network output. Figure 3.6 reports the average neural network output as a function of the 4-body  $m(p\pi\mu\mu)$  invariant mass for data and simulation. The distributions are flat indicating that no significant correlation is present.

### 3.4.3 MVA optimisation

In the high- $q^2$  region, where the signal is already observed, the requirement on the neural network output is chosen to maximise the significance,  $N_S/\sqrt{N_S + N_B}$ , where  $N_S$  and  $N_B$  are the numbers of expected signal and background candidates

respectively.  $N_S$  is derived from simulation but, as an arbitrary number of events can be generated, it needs to be normalised. To do this, the invariant mass distribution of real  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates is fit after pre-selection (including all requirements except the MVA selection). This is possible as the peak of the resonant channel is already clearly visible before the MVA requirement. The resonant yield is then scaled by the ratio of the  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  and  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  branching fractions as measured by LHCb on 2011 data,

$$\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-)/\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi \Lambda) = 1.54 \times 10^{-3}, \quad (3.3)$$

and by the  $J/\psi \rightarrow \mu^+\mu^-$  branching fraction, *i.e.*

$$N_S = N_{J/\psi} \cdot \frac{\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-)}{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi \Lambda) \cdot \mathcal{B}(J/\psi \rightarrow \mu^+\mu^-)}. \quad (3.4)$$

The number of expected background candidates is derived by fitting the data side-band with an exponential and extrapolating into the signal region.

In the low- $q^2$  region, where the signal is unobserved, the so called ‘‘Punzi figure-of-merit’’,  $N_S/(n_\sigma/2 + \sqrt{N_B})$ , is maximised [103]. This figure-of-merit is considered to be optimal for discovery and the parameter  $n_\sigma$  corresponds to the number of expected standard deviations of significance, in this analysis  $n_\sigma = 3$  is used. Moreover, the Punzi shape does not depend on the relative normalisation between signal and background, which is important since the signal is still unobserved at low- $q^2$  and the existing predictions vary significantly for this region. The dependence of the figure-of-merit for both  $q^2$  regions is shown in Fig. 3.7, and curves of signal efficiency versus background rejection are shown in Fig. 3.8.

For the final selection the neural network output is required to be larger than 0.76 for candidates in the high- $q^2$  region and 0.97 for the low- $q^2$  ones. Using these requirements the neural network retains approximately 97% (82%) of long candidates and 96% (66%) of downstream candidates for the high- (low-)  $q^2$  selection, with respect to the pre-selected samples. After the full selection has been applied  $\sim 0.5\%$

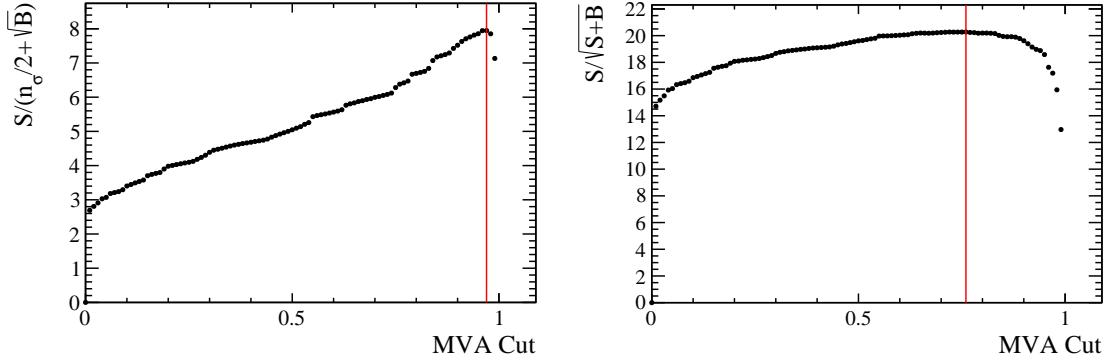


Figure 3.7: Dependence of the figure-of-merits on the neural network output requirement for the low- $q^2$  (left) and high- $q^2$  (right) regions. The vertical lines correspond to the chosen cuts.

of the events contain multiple candidates. In these cases candidates are rejected randomly such that only one is retained per event. To normalise the branching ratio measurement,  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates are selected using both, low- and high- $q^2$ , MVA requirements to normalise respectively low and high- $q^2$  intervals.

### 3.4.4 Trigger

Specific trigger lines are selected, corresponding to events triggered by the muons from which the reconstructed candidate is formed. This is denoted as Trigger On Signal (TOS). The trigger lines used in the analysis are listed in Tab. 3.3. The logical *or* of the lines on the same trigger level is required and the logical *and* of those on different levels. The `L0Muon` trigger requires hits in the muon detector and triggers if a muon with  $p_T > 1.5$  GeV/ $c$  is identified. The `L0Dimuon` trigger imposes the same requirement on the sum of the transverse momenta of two tracks. The `Hlt1TrackAllL0` trigger performs a partial reconstruction of the events and applies basic requirements on the values of the IP,  $\chi^2$  and  $p_T$  of tracks; it triggers if the L0 decision is confirmed. The `Hlt1TrackMuon` trigger applies looser requirements but in addition requires the `isMuon` variable (see Sec. 2.8) to be true to limit the yield. Finally, at the Hlt2 level, a complete reconstruction is done and a multivariate analysis is used to identify decay structures. One of the main variables used at this

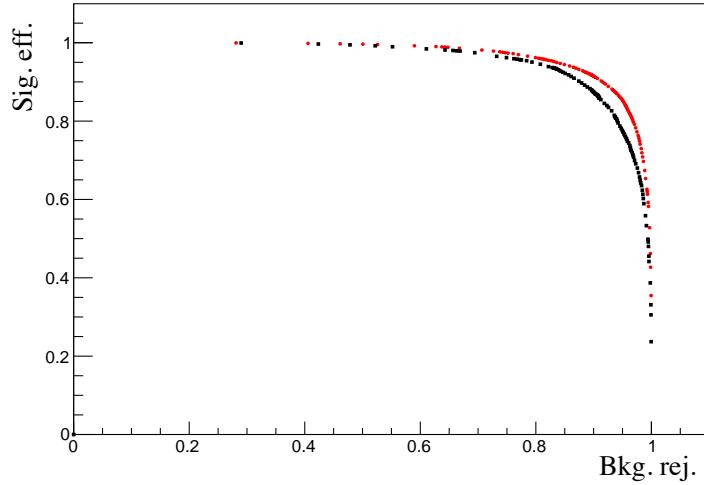


Figure 3.8: Receiver operating characteristic (ROC) curves for low- $q^2$  (black) and high- $q^2$  (red). They show the signal efficiency versus the background rejection. The optimal points on these curves are the closest ones to (1,1).

stage is the distance of closest approach, which is required to be less than 0.2 mm to form a 2-body object.

Table 3.3: Summary of the trigger lines used to select events at various levels. Trigger is always required to be due to the tracks of the candidate itself.

| Trigger Level | Lines                                                                                    |
|---------------|------------------------------------------------------------------------------------------|
| L0            | L0Muon<br>L0DiMuon                                                                       |
| Hlt1          | Hlt1TrackAllL0<br>Hlt1TrackMuon                                                          |
| Hlt2          | Hlt2Topo[2-4]BodyBBDT<br>Hlt2TopoMu[2-4]BodyBBDT<br>Hlt2SingleMuon<br>Hlt2DiMuonDetached |

### 3.4.5 Background from specific decays

Candidates from other decays can be incorrectly reconstructed as the decays of interest if some of their particles escape detection or are mis-identified. A survey of possible backgrounds concluded that the only physics background that needs to be taken into account explicitly comes from misreconstructed decays of  $B^0$  to  $K_s^0$

with two muons in the final state, where the  $K_s^0$  is incorrectly reconstructed as a  $\Lambda$  due to a  $p \rightarrow \pi$  identity swap. The lack of background from other decays is mainly due to the distinctive topology of the  $\Lambda$  decay, which is long-lived and decays at a displaced vertex. Simulated samples are used to study the effect of misreconstructed  $B^0 \rightarrow J/\psi K_s^0$  and  $B^0 \rightarrow K_s^0\mu^+\mu^-$  decays. In data, the  $B^0 \rightarrow J/\psi K_s^0$  contribution is clearly visible in the mass distribution of the resonant channel. This background is not suppressed by the application of specific cuts in this analysis because its mass shape is sufficiently distinct from the  $\Lambda_b^0$  signal and its contribution can be reliably modelled in the mass fits (see Sec. 3.5.1). An approximate estimate of the  $K_s^0$  background level for the rare mode is obtained using the yield in the resonant channel rescaled by the ratio of the known rare and resonant branching fractions. Details are given in Sec. 3.5.1 and predicted numbers of candidates are reported in Tab. 3.4. This contribution, although essentially negligible, is considered in the fit. The possible contamination due to  $B^+ \rightarrow \mu^+\mu^-K^{*+}$  decays, where the  $K^{*+} \rightarrow K_s^0\pi^+$ , is also investigated using a dedicated simulated sample and found to be negligible. Finally,  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  events in which a photon is radiated from one of the muons in the  $J/\psi$  decay, may be reconstructed with the wrong  $q^2$  value, avoid the  $J/\psi$  veto and hence be reconstructed in the rare channel sample. By analysing simulated events it was found that such radiative candidates only contribute in the  $q^2$  interval  $6 < q^2 < 8 \text{ GeV}^2/c^4$ . Of the  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  candidates 1.3% are reconstructed in this  $q^2$  interval but only 0.06% fall into the 4-body invariant mass window used for the fits. This corresponds to  $\sim 6$  candidates, 4 of which are in the downstream category. Given the low yield and that these candidates do not peak under the signal but show a decaying distribution at the edge of the fit mass window, this background is considered as part of the combinatorial background. Figure 3.9 shows the 4-body invariant mass distribution of simulated  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  events falling into the rare  $q^2$  region and the distribution of simulated  $B^+ \rightarrow \mu^+\mu^-K^{*+}$  events mis-reconstructed as  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  decays.

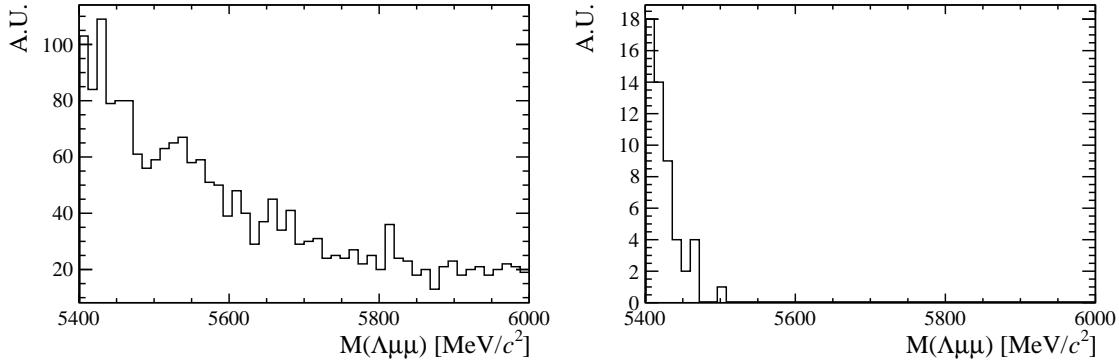


Figure 3.9: Invariant mass distributions of simulated  $B^+ \rightarrow \mu^+ \mu^- K^{*+}$  (left) and  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  (right) candidates passing the full  $\Lambda \mu \mu$  selection. Only  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates reconstructed in  $q^2 < 8 \text{ GeV}^2/c^4$  are selected. Distributions are shown in the invariant mass range relevant for the analysis (see Sec. 3.5.1).

### 3.5 Yield extraction

Extended unbinned maximum likelihood fits are used to extract the yields of the rare and resonant channels. The likelihood has the form:

$$\mathcal{L} = e^{-(N_S + N_C + N_B)} \times \prod_{i=1}^N [N_S P_S(m_i) + N_C P_C(m_i) + N_B P_B(m_i)] \quad (3.5)$$

where  $N_S$ ,  $N_C$  and  $N_B$  are respectively the numbers of signal, combinatorial and  $K_s^0$  background candidates and the  $P_i(m_i)$  are the corresponding probability density functions (PDF). The fit variable is the 4-body  $m(p\pi\mu\mu)$  invariant mass obtained from a kinematical fit of the full decay chain in which each particle is constrained to point to its assigned origin vertex and the invariant mass of the  $p\pi$  system is constrained to be equal to the world average of the  $\Lambda$  baryon mass [2]. In the resonant case a further constraint is imposed, namely that the dimuon mass is equal to the known  $J/\psi$  mass. This method allows the mass resolution to be improved giving better defined peaks and therefore a more stable fit. For brevity, in the following these variables are simply referred to as ‘‘invariant mass’’.

### 3.5.1 Fit description

The fit is performed via the following steps:

- simulated distributions are fitted to extract initial parameters values;
- the resonant data sample is fitted;
- the rare sample is fitted with the values of some parameters fixed to those obtained in the previous cases.

In the first step, simulated  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  distributions are fitted using the signal PDF alone. This is done separately for downstream and long candidates. Figure 3.10 shows distributions of candidates selected in the resonant sample with the fit function overlaid. The signal is described as the sum of two Crystal Ball functions (CB) with common mean ( $m_0$ ) and tail slope ( $n$ ). This is also known as a Double Crystal Ball (DCB) function. A single Crystal Ball [104] is a probability density function commonly used to model processes involving energy loss. In particular it is used to describe resonances that have radiative tails. This function combines a Gaussian core with a power-law tail of slope  $n$  that takes effect beyond some threshold  $\alpha$  away from the peak value. This asymmetric function has the form

$$C(x; \alpha, n, \bar{x}, \sigma) = N \cdot \begin{cases} \exp\left(-\frac{(x-\bar{x})^2}{2\sigma^2}\right) & \text{if } \frac{(x-\bar{x})}{\sigma} > \alpha, \\ A \left(B - \frac{(x-\bar{x})}{\sigma}\right)^{-n} & \text{if } \frac{(x-\bar{x})}{\sigma} < \alpha, \end{cases} \quad (3.6)$$

where for normalisation and continuity

$$\begin{aligned} A &= \left(\frac{c}{|\alpha|}\right)^n \cdot \exp\left(-\frac{\alpha^2}{2}\right), \\ B &= \frac{n}{|\alpha|} - |\alpha|. \end{aligned} \quad (3.7)$$

The full PDF for the resonant signal channel,  $P_S(m)$ , is therefore:

$$P_S(m; m_0, \alpha_1, \alpha_2, f, n) = f \cdot \text{CB}(m; m_0, \sigma_1, \alpha_1, n) + (1 - f) \cdot \text{CB}(m; m_0, \sigma_2, \alpha_2, n), \quad (3.8)$$

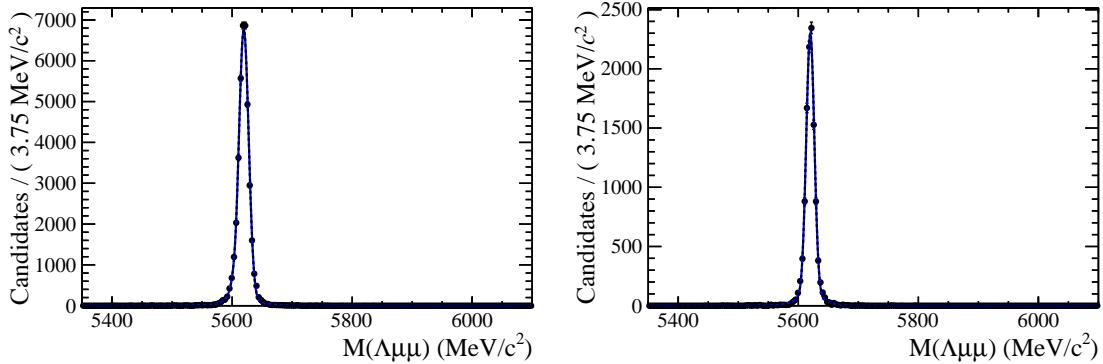


Figure 3.10: Invariant mass distribution of  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  downstream (left) and long (right) candidates. The points show simulated data and the blue line is the signal fit function.

where  $f$  is the relative fraction of candidates falling into the first CB function.

In a second step, the fit to the resonant channel data sample is performed. For this fit the tail slope parameter,  $n$ , which is highly correlated with  $\alpha_1$  and  $\alpha_2$ , is fixed to the value found in the fit to simulated candidates. In this fit two background components are modelled: the combinatorial background, parameterised with an exponential and the background from  $B^0 \rightarrow J/\psi K_s^0$  decays. The shape used to describe the  $K_s^0$  background is obtained from a  $B^0 \rightarrow J/\psi K_s^0$  simulated sample that has satisfied the full selection. The invariant distribution of these candidates is fitted with a DCB function, which is then used to model the  $K_s^0$  background in the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  fit. The fit to the simulated  $B^0 \rightarrow J/\psi K_s^0$  events is reported in Fig. 3.11. When the  $K_s^0$  shape is introduced in the fit to the data, all of its parameters are fixed. This is particularly important when fitting long candidates, because the contribution from the  $K_s^0$  peak smaller and therefore the values of the parameters would not be adequately constrained by data. On the other hand, in order to take into account possible differences between simulation and data in the definition of the absolute mass scale, an offset is introduced by adding a shift to the central value of the DCB,  $m_0 \rightarrow m_0 + m'$ , where  $m'$  is left free to vary in the fit. In summary, the free parameters in the fit to the resonant  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  sample are the yields of the signal and the combinatorial and  $K_s^0$  backgrounds, the slope of the exponential and the horizontal shift of the  $K_s^0$  shape. Note that all the parameters

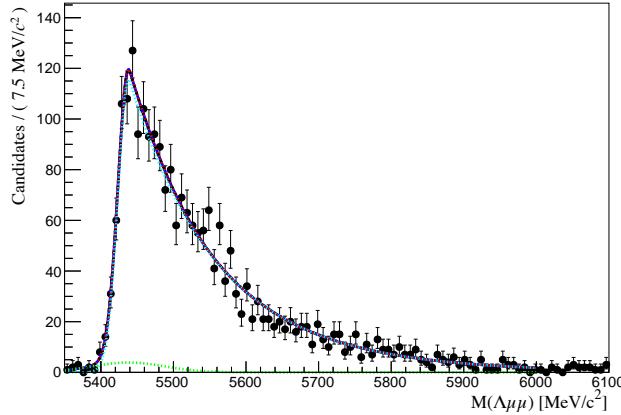


Figure 3.11: Invariant mass distribution of simulated  $B^0 \rightarrow J/\psi K_s^0$  events passing the full  $\Lambda\mu\mu$  selection with the fit function, a Double Crystal Ball, overlaid.

of the PDFs used to fit the long and downstream samples are independent.

Finally, the fit to the rare  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  data sample is carried out. In this case the fits to the long and downstream samples are performed simultaneously to obtain a more stable convergence. For this fit the signal is modelled with the same shape used in the resonant case as there is no physical reason why they should be different. This method is also useful to reduce systematic uncertainties as the result will be given as a ratio between rare and resonant quantities. However, the small candidate yields expected in the rare samples do not allow many parameters to be reliably extracted from the fits. Therefore, all parameters of the signal shape are fixed to the ones derived from the fit to the  $J/\psi\Lambda$  channel. However, to account for possible differences, arising from a different resolution in the various  $q^2$  regions, a scale factor is applied to the widths of the two Gaussian cores of the signal DCB:  $\sigma_1 \rightarrow c(q^2) \cdot \sigma_1$  and  $\sigma_2 \rightarrow c(q^2) \cdot \sigma_2$ , where the same scale factor,  $c$ , is applied to both widths but it is allowed to vary for each  $q^2$  region. These factors are fixed to values obtained by fitting rare  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  simulated events in each  $q^2$  bin and comparing the widths with those obtained from the fit to the resonant simulated sample, namely

$$c = \sigma_{\mu^+\mu^-}^{MC} / \sigma_{J/\psi}^{MC}. \quad (3.9)$$

These values are found to be  $\sim 1.9$  for downstream candidates and  $\sim 2.3$  for long

candidates, corresponding to the fact that in the resonant case a further constraint on the dimuon mass is used, which improves the resolution by a factor of  $\sim 2$ . The dependence of the scaling factor on  $q^2$  is found to be small. For the fits to the long and downstream samples the parameters are always separately fixed to the corresponding  $J/\psi \Lambda$  fits; in this analysis shape parameters are never shared between the two candidate categories.

The modelled background components are, also in the rare case, the combinatorial background, described with an exponential function and the  $K_s^0$  background. The slope of the background is visibly different depending on the  $q^2$  interval. This is partly due to the fact that at high  $q^2$  the combinatorial background changes slope because of a kinematical limit at low 4-body masses imposed by the  $q^2$  requirements. The exponential slopes are therefore left as independent parameters in each  $q^2$  interval. The background component from  $B^0 \rightarrow K_s^0 \mu^+ \mu^-$  decays is modelled using the same shapes used for the resonant channel. However, in this case the mass offset,  $m'$ , is fixed to that found for the resonant channel. The expected level of misreconstructed  $B^0 \rightarrow K_s^0 \mu^+ \mu^-$  candidates is small and does not allow its yield to be determined reliably. Therefore, this is fixed to the yield of  $B^0 \rightarrow J/\psi K_s^0$  decays rescaled by the expected ratio of branching fractions between the resonant and rare channels. The  $q^2$  distribution of  $B^0 \rightarrow K_s^0 \mu^+ \mu^-$  simulated events is used to predict the yield as a function of  $q^2$ . Table 3.4 reports the number of predicted  $B^0 \rightarrow K_s^0 \mu^+ \mu^-$  candidates in each  $q^2$  interval obtained with the following formula:

$$N_{K_s^0 \mu^+ \mu^-}(q^2) = N_{J/\psi K_s^0} \frac{B(B^0 \rightarrow K_s^0 \mu^+ \mu^-)}{B(B^0 \rightarrow K_s^0 J/\psi)} \cdot \frac{1}{\varepsilon_{rel}} \cdot B(J/\psi \rightarrow \mu^+ \mu^-) \frac{N(q^2)_{MC}}{N_{MC}^{tot}} \quad (3.10)$$

where  $N(q^2)_{MC}$  is the number of simulated rare candidates falling in a  $q^2$  interval after full selection and  $N_{MC}^{tot}$  is the total number of simulated events and  $\varepsilon_{rel} = \varepsilon_{\mu\mu}/\varepsilon_{J/\psi}$  is the relative selection efficiency between the two channels.

As the fit to the rare sample is performed simultaneously on long and downstream candidates, their two yields are not free to vary separately but are parameterised as

Table 3.4: Predicted numbers of  $B^0 \rightarrow K_s^0\mu^+\mu^-$  events in each considered  $q^2$  interval.

| $q^2$ [GeV $^2/c^4$ ] | Downstream | Long |
|-----------------------|------------|------|
| 0.1 – 2.0             | 0.9        | 0.1  |
| 2.0 – 4.0             | 0.9        | 0.1  |
| 4.0 – 6.0             | 0.8        | 0.1  |
| 6.0 – 8.0             | 1.1        | 0.1  |
| 11.0 – 12.5           | 1.9        | 0.2  |
| 15.0 – 16.0           | 1.1        | 0.1  |
| 16.0 – 18.0           | 2.0        | 0.2  |
| 18.0 – 20.0           | 1.1        | 0.1  |
| 1.1 – 6.0             | 2.1        | 0.1  |
| 15.0 – 20.0           | 4.2        | 0.5  |

a function of the common branching fraction using the following formula:

$$N(\Lambda\mu^+\mu^-)_k = \left[ \frac{d\mathcal{B}(\Lambda\mu^+\mu^-)/dq^2}{\mathcal{B}(J/\psi\Lambda)} \right] \cdot N(J/\psi\Lambda)_k \cdot \varepsilon_k^{rel} \cdot \frac{\Delta q^2}{\mathcal{B}(J/\psi \rightarrow \mu^+\mu^-)}, \quad (3.11)$$

where  $k = (\text{LL}, \text{DD})$ ,  $\Delta q^2$  is the width of the  $q^2$  interval and the only free parameter is the relative branching fraction ratio of the rare over  $J/\psi$  channels. For the branching fraction of the  $J/\psi \rightarrow \mu^+\mu^-$  decay the value reported in the PDG book,  $(5.93 \pm 0.06) \cdot 10^{-2}$  [2] is used and  $\varepsilon^{rel}$  corresponds to the relative efficiency between the rare and resonant channels obtained in Sec. 3.6. In this formula the efficiencies and the normalisation yield appear as constants, namely  $N(\Lambda\mu^+\mu^-)_k = C_k \cdot \mathcal{B}^{rel}$ .

### 3.5.2 Fit results

Figures 3.12 and 3.13 show fitted invariant mass distributions for the normalisation channel, selected with the high- $q^2$  and low- $q^2$  requirements respectively. Table 3.5 reports the measured yields of  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  candidates found using the low- and high- $q^2$  selections. Values for the signal shape parameters are shown on Fig. 3.12. Fits to the rare  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  samples are shown in Fig. 3.14 for the integrated  $15 < q^2 < 20$  and  $1.1 < q^2 < 6.0$  GeV $^2/c^4$   $q^2$  intervals, while fitted invariant mass distribution in all other considered  $q^2$  intervals are in Figs. 3.15 and 3.16 for downstream and long candidates respectively. The yields of rare candidates obtained

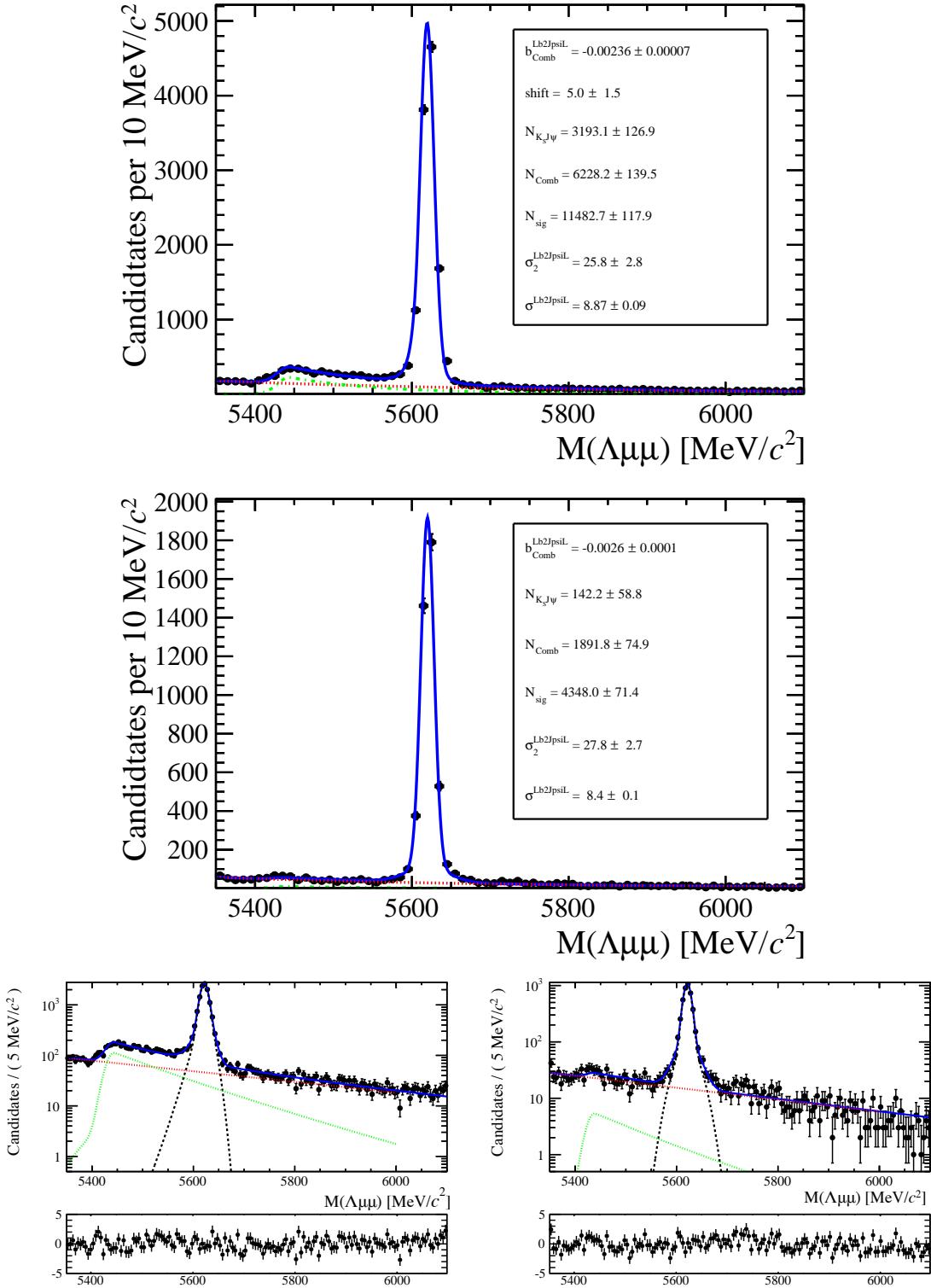


Figure 3.12: Invariant mass distributions of  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  downstream (top) and long (middle) candidates selected with high  $q^2$  requirements. Bottom plots are the same as the upper ones but shown in logarithmic scale. Black points show data. The blue solid line represents the total fit function, the black dashed line the signal, the red dashed line the combinatorial background and the green dashed line the  $B^0 \rightarrow K_s^0 \mu^+ \mu^-$  background.

Table 3.5: Number of  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates in the downstream and long categories found using the for low- and high- $q^2$  requirements; uncertainties are statistical only.

| Selection   | Long          | Downstream        |
|-------------|---------------|-------------------|
| high- $q^2$ | $4313 \pm 70$ | $11\,497 \pm 123$ |
| low- $q^2$  | $3363 \pm 59$ | $7225 \pm 89$     |

Table 3.6: Signal yields,  $N_S$ , obtained from the invariant mass fit to  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  candidates in each  $q^2$  interval together with their statistical significance. The  $8 - 11$  and  $12.5 - 15$   $\text{GeV}^2/c^4$   $q^2$  intervals are excluded from the study as they are dominated by resonant decays via charmonium resonances.

| $q^2$ [ $\text{GeV}^2/c^4$ ] | DD             | LL               | Tot. yield     | Significance |
|------------------------------|----------------|------------------|----------------|--------------|
| 0.1 – 2.0                    | $6.9 \pm 2.2$  | $9.1 \pm 3.0$    | $16.0 \pm 5.3$ | 4.4          |
| 2.0 – 4.0                    | $1.8 \pm 1.7$  | $3.0 \pm 2.8$    | $4.8 \pm 4.7$  | 1.2          |
| 4.0 – 6.0                    | $0.4 \pm 0.9$  | $0.6 \pm 1.4$    | $0.9 \pm 2.3$  | 0.5          |
| 6.0 – 8.0                    | $4.3 \pm 2.0$  | $7.2 \pm 3.3$    | $11.4 \pm 5.3$ | 2.7          |
| 11.0 – 12.5                  | $14.6 \pm 2.9$ | $42.8 \pm 8.5$   | $60 \pm 12$    | 6.5          |
| 15.0 – 16.0                  | $13.5 \pm 2.2$ | $43.5 \pm 7.2$   | $57 \pm 9$     | 8.7          |
| 16.0 – 18.0                  | $28.6 \pm 3.3$ | $88.8 \pm 10.1$  | $118 \pm 13$   | 13           |
| 18.0 – 20.0                  | $22.4 \pm 2.6$ | $78.0 \pm 8.9$   | $100 \pm 11$   | 14           |
| 1.1 – 6.0                    | $3.6 \pm 2.4$  | $5.7 \pm 3.8$    | $9.4 \pm 6.3$  | 1.7          |
| 15.0 – 20.0                  | $64.6 \pm 4.7$ | $209.6 \pm 15.3$ | $276 \pm 20$   | 21           |

from the fit are listed in Tab. 3.6 together with their significances. Most candidates are found in the downstream sample, which comprises  $\sim 80\%$  of the total yield. Note that, since the fit is simultaneous to the two candidate categories, their yields are not parameters free to vary independently but are correlated via the branching ratio. The statistical significance of the observed signal yields is evaluated as the change in the logarithm of the likelihood function,  $\sqrt{2\Delta \ln \mathcal{L}}$ , when the signal component is excluded from the fit, relative to the nominal fit in which it is present.

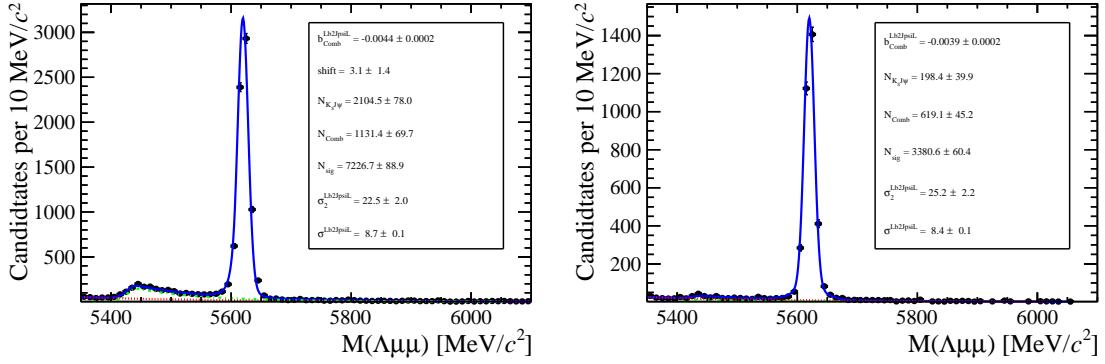


Figure 3.13: Invariant mass distribution of  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  for downstream (left) and long (right) candidates selected with low  $q^2$  requirements.

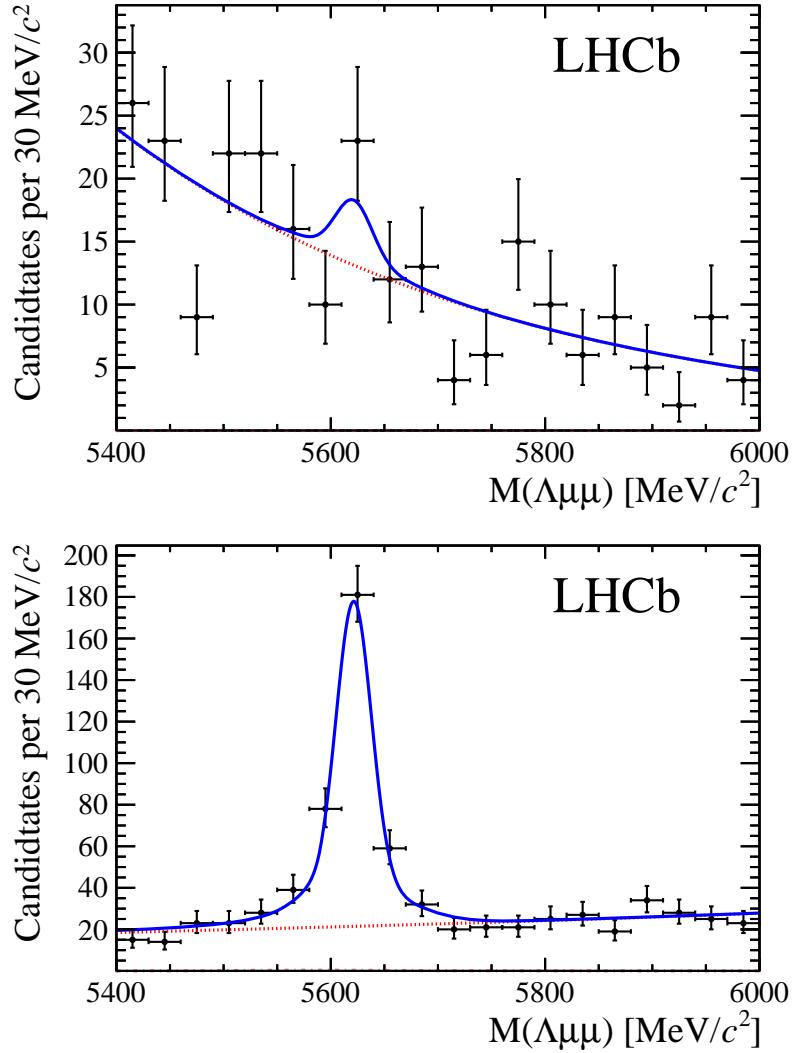


Figure 3.14: Invariant mass distributions of  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  candidates in the integrated  $0.1 - 6.0$  (top) and  $15 - 20 \text{ GeV}^2/c^4$  (bottom)  $q^2$  intervals. Points show data combining long and downstream candidates together. The blue solid line represents the total fit function and the dashed red line the combinatorial background.

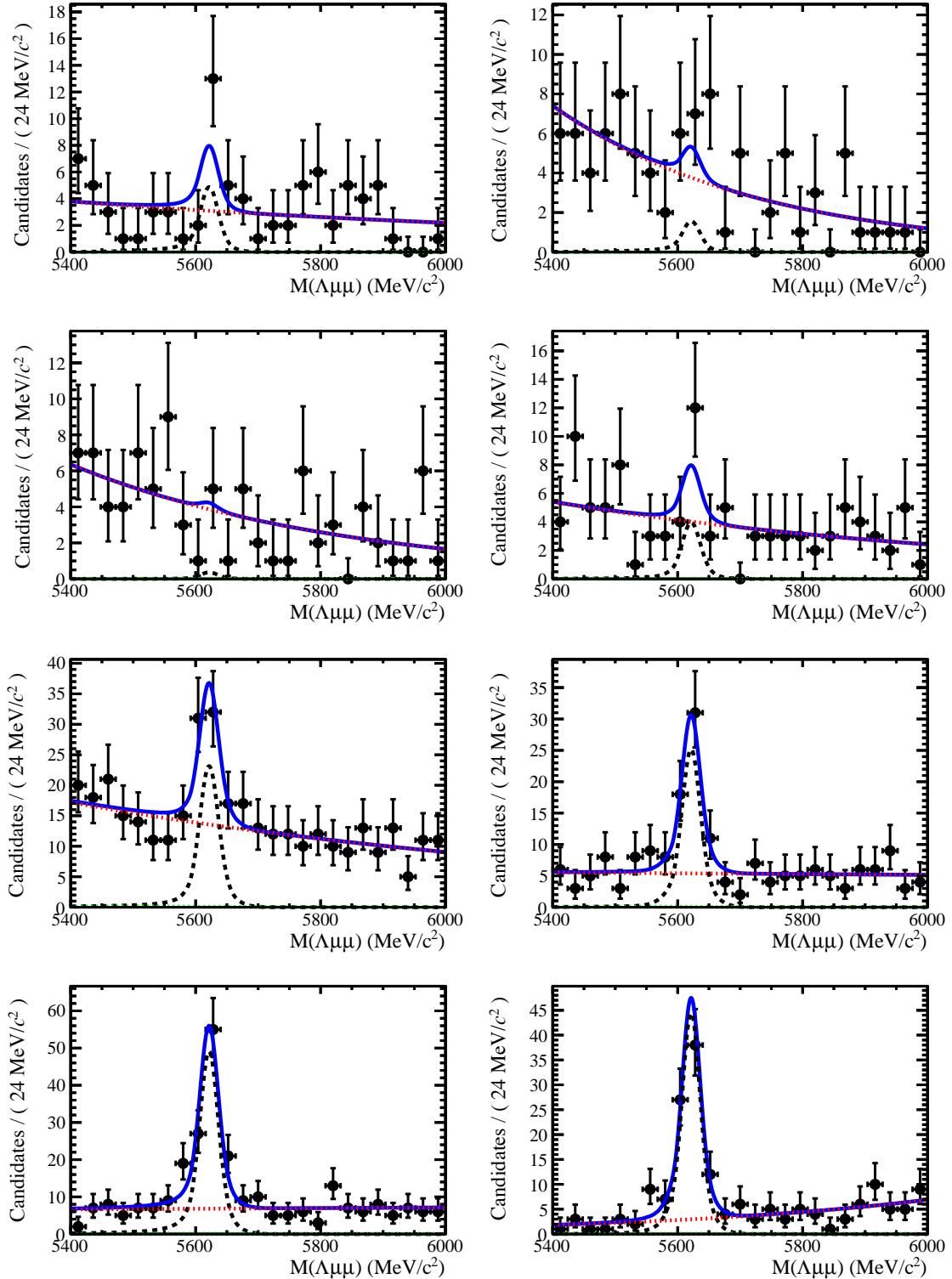


Figure 3.15: Invariant mass distributions of rare  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  downstream candidates in the considered  $q^2$  intervals.

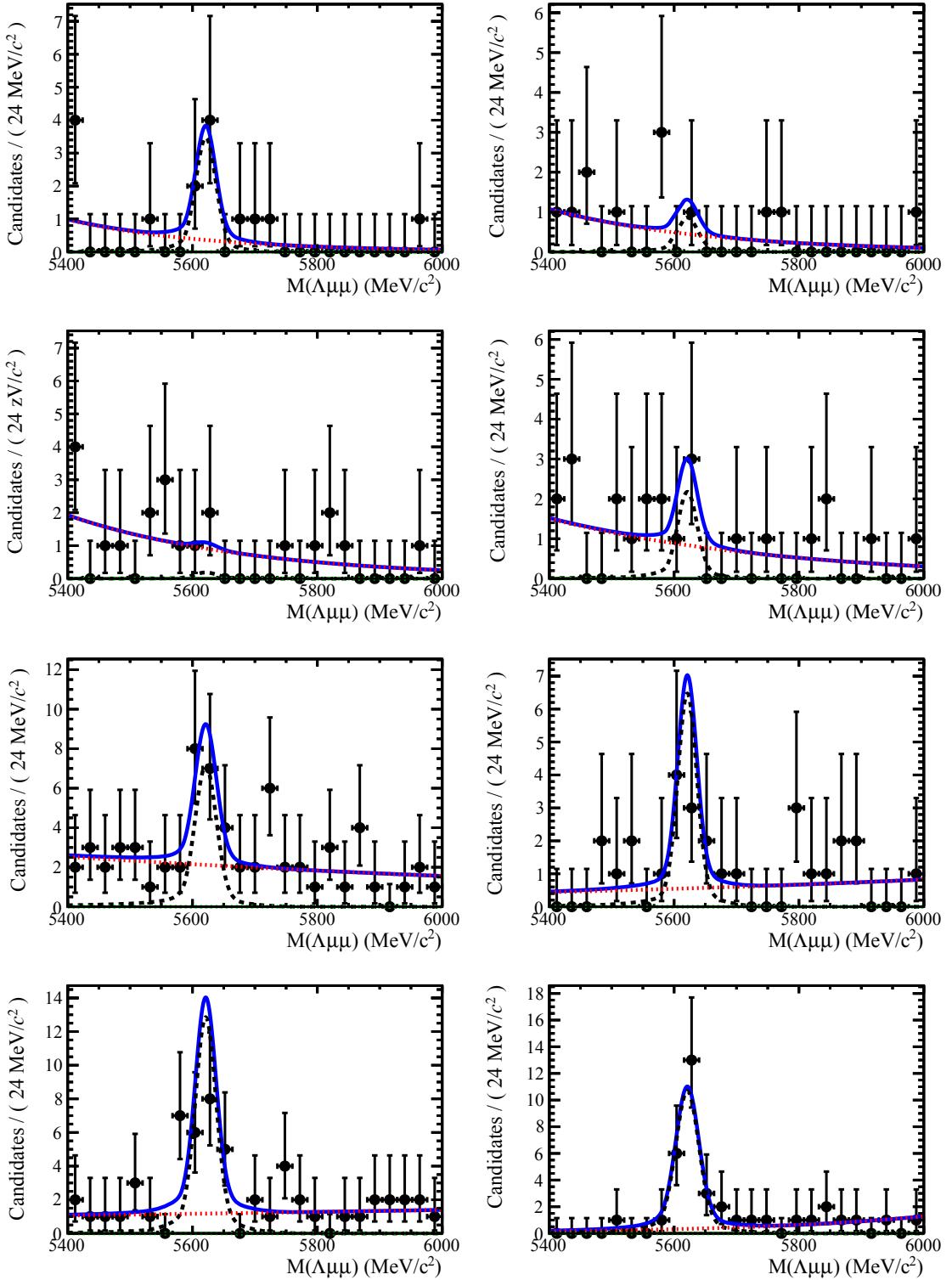


Figure 3.16: Invariant mass distributions of rare  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  long candidates in the considered  $q^2$  intervals.

## 3.6 Efficiency

The selection efficiency is calculated for each decay according to the formula

$$\varepsilon^{tot} = \varepsilon(Geom)\varepsilon(Det|Geom)\varepsilon(Reco|Det)\varepsilon(MVA|Reco)\varepsilon(Trig|MVA). \quad (3.12)$$

In this expression the first term gives the efficiency to have final state particles in the LHCb acceptance. The second term handles the possibility of  $\Lambda$  escaping the detector or interacting with it and therefore never decaying into  $p\pi$ ; this term is referred to as “detection” efficiency. The third term carries information about the reconstruction and pre-selection efficiencies, which are kept together given that boundaries between them are completely artificial. The fourth part deals with the efficiency of the neural network candidates that passed the pre-selection. Finally, the last term handles the trigger efficiency for candidates which are accepted by the full selection. Most of the efficiency components are evaluated using the simulated samples described in Sec. 3.3. Only the efficiency of the PID requirement for the proton (see Tab. 3.1) is separately derived with a data–driven method because the simulation does not provide a good description of PID variables. Representative absolute efficiencies’ values are given in the next sections. However, for the analysis itself only the relative efficiency,  $\varepsilon(\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-)/\varepsilon(\Lambda_b^0 \rightarrow J/\psi\Lambda)$ , is used.

### 3.6.1 Geometric acceptance

In order to save disk space and time the simulation only includes events in which the final muons are in the detector acceptance and therefore can be reconstructed. This corresponds to a requirement for each of the muons to be in an interval  $10 < \theta < 400$  mrad, where  $\theta$  is the angle between the muon momentum and the beam line. The efficiency of this requirement is obtained by using a separate simulated sample, where events are generated in the full space. The geometric efficiency varies between 18% at high- $q^2$  and 20% at low- $q^2$ ; Fig. 3.17 shows the dependence of this efficiency as a function of  $q^2$ .

### 3.6.2 Reconstruction and neural network efficiencies

The efficiency to reconstruct the decays together with the pre-selection requirements is evaluated from simulated data. The reconstruction efficiency is subdivided in “Detection” and “Reconstruction and pre-selection” efficiencies. In fact, since  $\Lambda$  is a long lived particle, there is a non-negligible probability that it interacts in the detector or escapes from it and therefore never decays in proton and pion. The reconstruction efficiency includes the probability for the tracks to produce observable signatures and to pass the pre-selection requirements. This component does not include the efficiency of the PID cut that appears in Tab. 3.1, which is kept separate because PID variables are not well described by the simulation. The detection efficiency varies between 88% at low- $q^2$  and 92% at high- $q^2$  while the reconstruction efficiency is almost flat in  $q^2$  at 6.6% for downstream candidates and 2.0% for long candidates. The MVA selection efficiency is again evaluated from simulated samples and it is observed to vary from 55% to 88% for downstream candidates and from 74% to 96% for long candidates. Fig. 3.17 shows the dependence of these efficiencies as a function of  $q^2$ . The sudden jump in MVA efficiency at  $\sim 9$  GeV/ $c^2$  is due to the fact that a different figure-of-merit is used to optimise the MVA requirement in the low- and high- $q^2$  regions, which results in different efficiencies.

### 3.6.3 Trigger efficiency

The trigger efficiency is again evaluated using a simulated sample. It increases with  $q^2$  and varies from  $\sim 57\%$  to  $\sim 86\%$  for both downstream and long candidates. Fig. 3.17 shows the dependence of this efficiency as a function of  $q^2$ . Using the high statistics resonant channel it is possible to crosscheck using data the trigger efficiency obtained using the simulation. In LHCb triggered events can fall into two categories: events triggered by a track which is part of a signal candidate, Trigger On Signal (TOS), or by other tracks in the event, Trigger Independent of Signal (TIS). As the TIS and TOS categories are not exclusive the TIS sample provides a

control sample which can be used to obtain the efficiency for TOS trigger. This can be calculated with the formula:

$$\varepsilon_{\text{TOS}} = \frac{\text{TIS and TOS}}{\text{TIS}}. \quad (3.13)$$

As data contains background the numbers of signal candidates in the “TIS” and “TIS and TOS” categories are not just determined by counting but from fits to the 4-body invariant mass,  $m(p\pi\mu\mu)$ , distributions after applying these requirements. This procedure takes the name of TISTOS method. Using the data-driven method an efficiency of  $(70 \pm 5)\%$  is obtained, while this is calculated to be  $(73.33 \pm 0.02)\%$  using the simulation. Results are therefore compatible within  $1\sigma$ .

### 3.6.4 PID efficiency

For long tracks a PID requirement on protons ( $\text{PID}_p > -5$ ) is applied. The simulation is known not to describe PID variables well and therefore a data-driven method is used to obtain this efficiency component. This is done using the `PIDCalib` package (see Sec. 2.8.1), which uses as calibration samples decays where particles can be identified due to their kinematic properties. In the case of protons a sample of  $\Lambda$  particles is used, where the proton can be identified because it always has the highest momentum. The package allows to divide the phase space in bins of variables relevant for PID performances; in this analysis momentum and pseudorapidity are used. Using the calibration sample the efficiency is derived in each two-dimensional bin. Finally, to take into account that the decay channel under study could have different kinematical distributions than the calibration sample these efficiency tables are used to re-weight the simulation. The PID efficiency varies from 97.3% at low- $q^2$  to 98.2% at high- $q^2$ .

Table 3.7: Absolute efficiency values for  $\Lambda_b^0 \rightarrow J/\psi \Lambda$ ; uncertainties are statistical only.

| Efficiency                 | Downstream            | Long                  |
|----------------------------|-----------------------|-----------------------|
| $\varepsilon(\text{Geom})$ | $0.1818 \pm 0.0003$   |                       |
| $\varepsilon(\text{Det})$  | $0.9017 \pm 0.0003$   |                       |
| $\varepsilon(\text{Reco})$ | $0.0724 \pm 0.0004$   | $0.0203 \pm 0.0002$   |
| $\varepsilon(\text{PID})$  | –                     | $97.89 \pm 0.005$     |
| $\varepsilon(\text{MVA})$  | $0.882 \pm 0.002$     | $0.942 \pm 0.002$     |
| $\varepsilon(\text{Trig})$ | $0.697 \pm 0.003$     | $0.734 \pm 0.005$     |
| Full Selection             | $0.0445 \pm 0.0003$   | $0.0140 \pm 0.0002$   |
| Total                      | $0.00729 \pm 0.00005$ | $0.00230 \pm 0.00003$ |

### 3.6.5 Relative efficiencies

In the previous sections absolute efficiencies values were given for the rare channel, which are summarised in Fig. 3.17. This section reports the corresponding relative efficiencies with respect to the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  channel, which will be used to correct the yields and obtain the differential branching fraction. Table 3.7 reports the absolute efficiency values for the  $J/\psi$  channel used to derive the relative efficiencies. Relative geometric, detection and PID efficiencies are listed in Tab. 3.8, while Tabs. 3.9 and 3.10 report relative reconstruction, trigger and MVA efficiencies separately for downstream and long candidates. Since the latter three components are obtained from the same simulated sample their statistical uncertainties are correlated. Therefore, the total of the three is also reported as a single efficiency and labeled ‘‘Full Selection’’. Finally, Tab. 3.13 reports the total of all relative efficiencies, which will be then used to correct the raw yields and calculate the differential branching fraction. Uncertainties reflect the statistics of both rare and resonant samples, while systematic uncertainties are discussed in following sections.

Table 3.8: Relative geometric, detection and PID relative efficiencies between  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  and  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  decays; uncertainties reflect the statistics of both samples.

| $q^2$ [GeV $^2/c^4$ ] | Geometric       | Detection       | PID               |
|-----------------------|-----------------|-----------------|-------------------|
| 0.1 – 2.0             | 1.2976 ± 0.0050 | 0.9751 ± 0.0006 | 0.99418 ± 0.00013 |
| 2.0 – 4.0             | 1.1541 ± 0.0043 | 0.9814 ± 0.0005 | 0.99523 ± 0.00013 |
| 4.0 – 6.0             | 1.1043 ± 0.0044 | 0.9872 ± 0.0006 | 0.99699 ± 0.00012 |
| 6.0 – 8.0             | 1.0778 ± 0.0045 | 0.9939 ± 0.0006 | 0.99805 ± 0.00011 |
| 11.0 – 12.5           | 1.0431 ± 0.0058 | 1.0074 ± 0.0007 | 1.00151 ± 0.00010 |
| 15.0 – 16.0           | 1.0426 ± 0.0084 | 1.0188 ± 0.0010 | 1.00431 ± 0.00008 |
| 16.0 – 18.0           | 1.0296 ± 0.0068 | 1.0255 ± 0.0008 | 1.00215 ± 0.00008 |
| 18.0 – 20.0           | 1.0288 ± 0.0087 | 1.0333 ± 0.0010 | 1.00226 ± 0.00005 |
| 1.1 – 6.0             | 1.1396 ± 0.0031 | 0.9835 ± 0.0004 | 0.99589 ± 0.00009 |
| 15.0 – 20.0           | 1.0320 ± 0.0048 | 1.0269 ± 0.0006 | 1.00281 ± 0.00006 |

Table 3.9: Relative efficiencies between  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  and  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  decays for downstream candidates; uncertainties reflect the statistics of both samples.

| $q^2$ [GeV $^2/c^4$ ] | Reconstruction | MVA           | Trigger       | Full Selection |
|-----------------------|----------------|---------------|---------------|----------------|
| 0.1 – 2.0             | 0.721 ± 0.009  | 0.706 ± 0.010 | 0.805 ± 0.011 | 0.410 ± 0.009  |
| 2.0 – 4.0             | 0.920 ± 0.010  | 0.661 ± 0.008 | 0.870 ± 0.010 | 0.529 ± 0.010  |
| 4.0 – 6.0             | 0.997 ± 0.010  | 0.662 ± 0.008 | 0.895 ± 0.010 | 0.590 ± 0.011  |
| 6.0 – 8.0             | 1.050 ± 0.011  | 0.665 ± 0.008 | 0.960 ± 0.010 | 0.671 ± 0.012  |
| 11.0 – 12.5           | 1.112 ± 0.014  | 1.007 ± 0.006 | 1.069 ± 0.009 | 1.197 ± 0.019  |
| 15.0 – 16.0           | 1.019 ± 0.018  | 1.000 ± 0.009 | 1.175 ± 0.012 | 1.197 ± 0.026  |
| 16.0 – 18.0           | 0.968 ± 0.014  | 0.961 ± 0.008 | 1.200 ± 0.010 | 1.115 ± 0.020  |
| 18.0 – 20.0           | 0.832 ± 0.016  | 0.943 ± 0.010 | 1.231 ± 0.012 | 0.966 ± 0.023  |
| 1.1 – 6.0             | 0.950 ± 0.007  | 0.663 ± 0.005 | 0.876 ± 0.007 | 0.551 ± 0.007  |
| 15.0 – 20.0           | 0.929 ± 0.010  | 0.963 ± 0.005 | 1.204 ± 0.007 | 1.077 ± 0.014  |

Table 3.10: Relative efficiencies between  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  and  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  decays for long candidates; uncertainties reflect the statistics of both samples.

| $q^2$ [GeV $^2/c^4$ ] | Recostruction | MVA           | Trigger     | Full Selection |
|-----------------------|---------------|---------------|-------------|----------------|
| 0.1 – 2.0             | 0.96 ± 0.02   | 0.863 ± 0.012 | 0.79 ± 0.02 | 0.65 ± 0.02    |
| 2.0 – 4.0             | 0.97 ± 0.02   | 0.803 ± 0.012 | 0.89 ± 0.02 | 0.69 ± 0.02    |
| 4.0 – 6.0             | 1.04 ± 0.02   | 0.824 ± 0.012 | 0.92 ± 0.02 | 0.79 ± 0.02    |
| 6.0 – 8.0             | 1.05 ± 0.02   | 0.825 ± 0.012 | 0.96 ± 0.02 | 0.84 ± 0.02    |
| 11.0 – 12.5           | 1.10 ± 0.03   | 1.002 ± 0.008 | 1.01 ± 0.02 | 1.10 ± 0.03    |
| 15.0 – 16.0           | 0.89 ± 0.03   | 0.987 ± 0.013 | 1.13 ± 0.02 | 0.98 ± 0.04    |
| 16.0 – 18.0           | 0.84 ± 0.03   | 0.985 ± 0.010 | 1.17 ± 0.02 | 0.97 ± 0.03    |
| 18.0 – 20.0           | 0.67 ± 0.03   | 0.944 ± 0.017 | 1.18 ± 0.02 | 0.75 ± 0.04    |
| 1.1 – 6.0             | 1.00 ± 0.02   | 0.820 ± 0.008 | 0.89 ± 0.01 | 0.73 ± 0.02    |
| 15.0 – 20.0           | 0.78 ± 0.02   | 0.973 ± 0.008 | 1.16 ± 0.01 | 0.89 ± 0.02    |

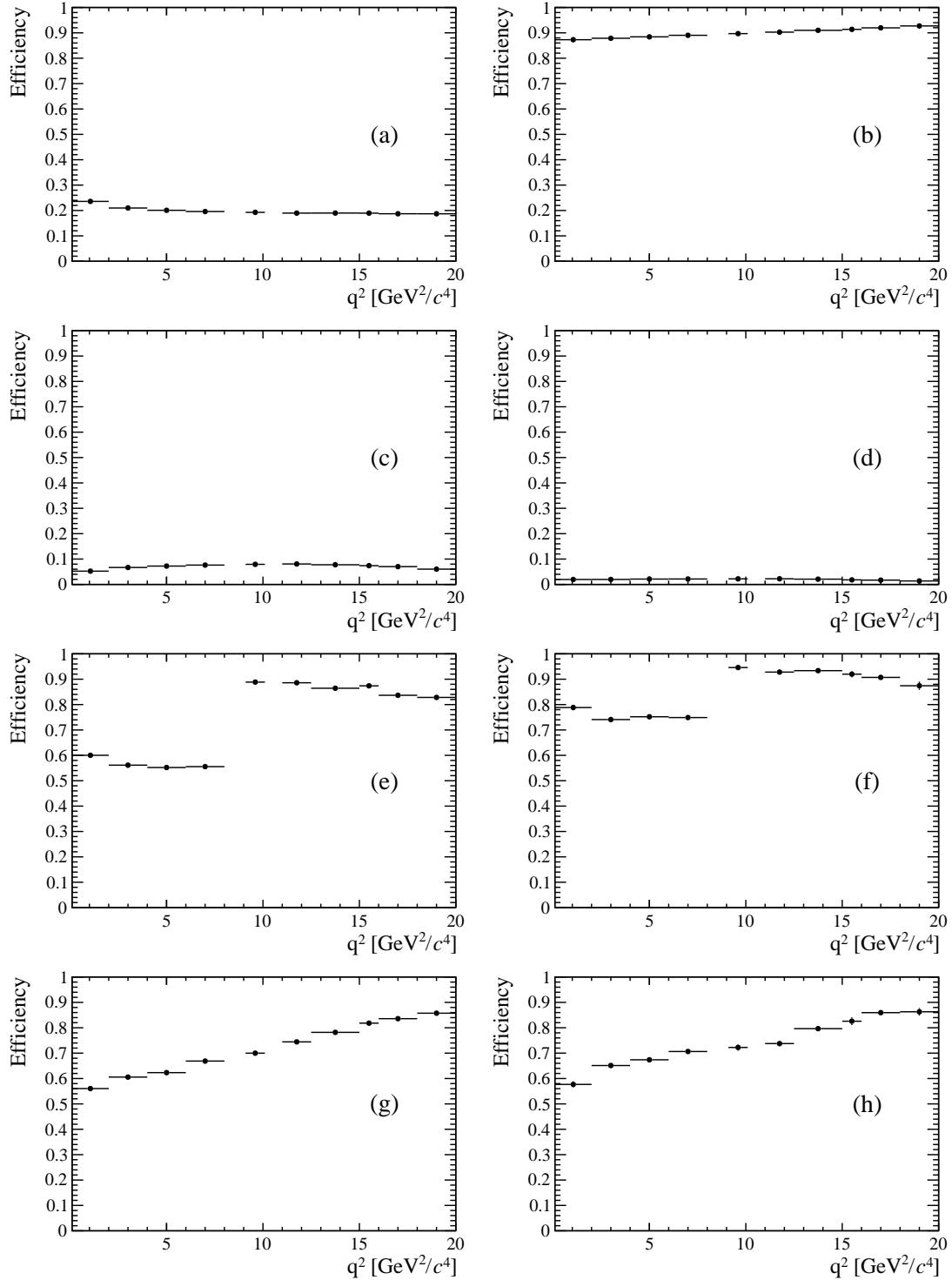


Figure 3.17: Absolute efficiencies as a function of  $q^2$ : geometric efficiency (a), detection efficiency (b), reconstruction efficiency for DD (c) and LL (d) candidates, MVA efficiency for DD (e) and LL (f) and trigger efficiency for DD (g) and LL (h).

## 3.7 Systematic uncertainties

This section describes the main considered sources of systematic uncertainty.

### 3.7.1 Systematic uncertainty on the yields

The choice of specific PDFs to model the invariant mass distributions could result in a bias. To asses the effect of the signal PDF choice as a first step a number of models are tried on the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  data sample to understand which ones are plausible. Table 3.11 reports the  $\chi^2$  and corresponding p-values obtained using different models including: the default model (a DCB function), a simple Gaussian function, a single Crystal Ball function and the sum of two Gaussians (Double Gauss, DG). The only two models that give a reasonable p-value are the default DCB and the sum of two Gaussian functions. In a second step simulated experiments are generated and fit with the two chosen models. Events are generated according to a density function given by the default model with parameters taken from the fit to data, separately for each  $q^2$  interval. In this way, for each  $q^2$  interval, a specific shape is reproduced including data-like background level and slope. Furthermore, a number of events comparable to the one found in data is generated. For each experiment a normalised bias is calculated as

$$b = \left( \frac{N_{\ell\ell}^{DCB}}{N_{J/\psi}^{DCB}} - \frac{N_{\ell\ell}^{DG}}{N_{J/\psi}^{DG}} \right) / \frac{N_{\ell\ell}^{DCB}}{N_{J/\psi}^{DCB}} \quad (3.14)$$

where  $N_{\ell\ell}^{model}$  and  $N_{J/\psi}^{model}$  are the numbers of rare and resonant candidates observed using a specific model. The average bias over 1000 pseudo-experiments is taken as systematic uncertainty. Note that in each case the rare and normalisation channels are fit with the same signal model and, while for the default case the rare parameters are fixed to what found for the resonant channel, they are left free to vary in the second model in order to asses at the same time the systematic due to the parameters constraints.

Table 3.11:  $\chi^2$ , NDF, p-values and number of signal events obtained fitting  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  data using different models.

| Model         | $\chi^2/ndf$ | NDF | p-value  | $N_{evts}$ |
|---------------|--------------|-----|----------|------------|
| DCB (default) | 1.0          | 187 | 0.51     | 9965.4     |
| Gauss         | 1.8          | 193 | $\sim 0$ | 9615.7     |
| Double Gauss  | 1.1          | 191 | 0.45     | 9882.4     |
| CB            | 1.5          | 191 | $\sim 0$ | 9802.4     |

For the background PDF systematic the rare channel is re-fit leaving the yield of the  $K_s^0$  component free to vary, which is instead fixed to the predicted value in the default fit. The same procedure as for the signal PDF is applied.

Results are reported in Tab. 3.12. The most affected  $q^2$  interval is the one in the middle of the charmonium resonances, where a combination of lower statistics and higher background leaves more freedom to the signal shape. Finally, a background component for  $B^+ \rightarrow K^{*+}(K_s^0\pi^+)\mu^+\mu^-$  decays is added to the fit, modelled using the distribution of simulated events after full selection. No significant bias is found for this component.

| $q^2$ [GeV $^2/c^4$ ] | Sig. PDF bias (%) | Bkg. PDF bias (%) | Tot. sys. (%) |
|-----------------------|-------------------|-------------------|---------------|
| 0.1 – 2.0             | 3.2               | 1.1               | 3.4           |
| 2.0 – 4.0             | 2.9               | 2.4               | 3.8           |
| 4.0 – 6.0             | 4.6               | 4.8               | 6.6           |
| 6.0 – 8.0             | 1.2               | 1.7               | 2.0           |
| 11.0 – 12.5           | 2.6               | 1.8               | 3.2           |
| 15.0 – 16.0           | 1.3               | 2.5               | 2.8           |
| 16.0 – 18.0           | 0.6               | 1.3               | 1.4           |
| 18.0 – 20.0           | 1.7               | 1.8               | 2.5           |
| 1.1 – 6.0             | 0.1               | 4.2               | 4.2           |
| 15.0 – 20.0           | 1.0               | 0.2               | 1.1           |

Table 3.12: Values of systematic uncertainties due to the choice of signal and background shapes in bins of  $q^2$ .

### 3.7.2 Systematic uncertainties on the efficiency determination

Systematic uncertainties on the efficiency determination are due to the limited knowledge of the decay properties such as the  $\Lambda_b^0$  lifetime and production polarisation. The systematic uncertainties are directly evaluated on the relative efficiencies as these are the ones that are actually used in the analysis. It should be noted that not all sources contribute to each part of the efficiency. For brevity, this section only reports estimates of the systematic uncertainties obtained, while the full information is contained in Appendix C.

#### 3.7.2.1 Effect of new physics on the decay model

New physics could affect the decay model used to simulate events by adding contributions to the  $C_7$  and  $C_9$  Wilson Coefficients. This would result in a modification of the simulated  $q^2$  spectra and therefore of the efficiency obtained from simulation. To asses this systematic the Wilson Coefficients are modified by adding a new physics component ( $C_i \rightarrow C_i + C_i^{\text{NP}}$ ). Figure 3.18 shows  $q^2$  spectra obtained weighting the simulation for a model embedding the default and 3 modified sets of Wilson Coefficients. The used values, reported on the plot legend, are inspired to maintain compatibility with the recent LHCb result about the  $P'_5$  observable [48]. The biggest effect is observed in the very low  $q^2$ , below  $2 \text{ GeV}^2/c^4$ , where the efficiency can change up to 7%, while it changes 3–4% between 3 and  $4 \text{ GeV}^2/c^4$  and 2–3% in the rest of the spectrum. As this analysis is performed under the hypothesis that the decays are described by a the SM, these values are given in order to provide the full information but are not added as systematic uncertainties.

#### 3.7.2.2 Simulation statistics

The limited statistics of the simulated samples used to determine efficiencies is considered as a source of systematic uncertainty. While it is not the dominant

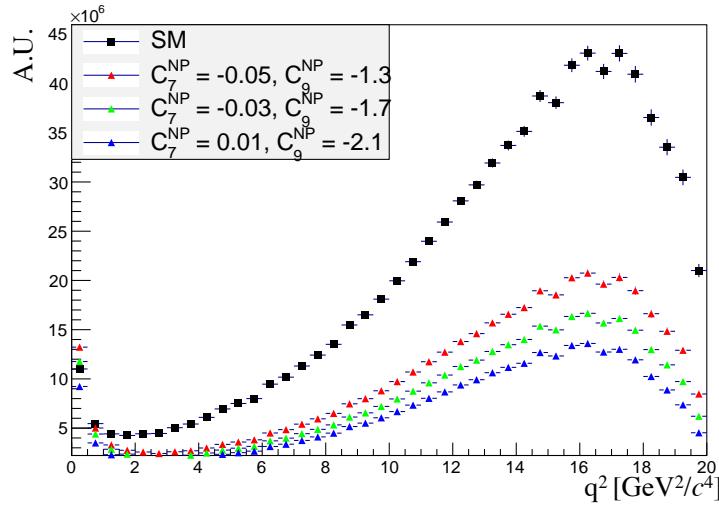


Figure 3.18: The  $q^2$  spectrum of  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  simulated events weighted with models embedding different sets of Wilson Coefficients. The black distribution corresponds to the weights used to calculate nominal efficiencies.

source, its size does not allow to completely neglect it. When reporting relative efficiency values the statistical uncertainty due to the rare and resonant channels is always considered.

### 3.7.2.3 Production polarisation and decay structure

One of the main unknown, which affects the determination of the efficiencies, is the angular structure of the decays and, connected to it, also the production polarisation, which is a parameter of the model. To assess the systematic uncertainty due to the knowledge of the production polarisation for  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decays the polarisation parameter in the model is varied within one standard deviation from the central value of the most recent LHCb measurement,  $P_b = 0.06 \pm 0.09$  [102]. The full observed difference is taken as systematic uncertainty. To assess the systematic uncertainty due to the decay structure an alternative set of form factors is used based on lattice QCD calculation [105]. The two models are compared and the full difference is taken as systematic uncertainty. In total this results in an uncertainty of  $\sim 1.3\%$  for long candidates and  $\sim 0.6\%$  for downstream candidates, mostly coming from the knowledge of the production polarisation.

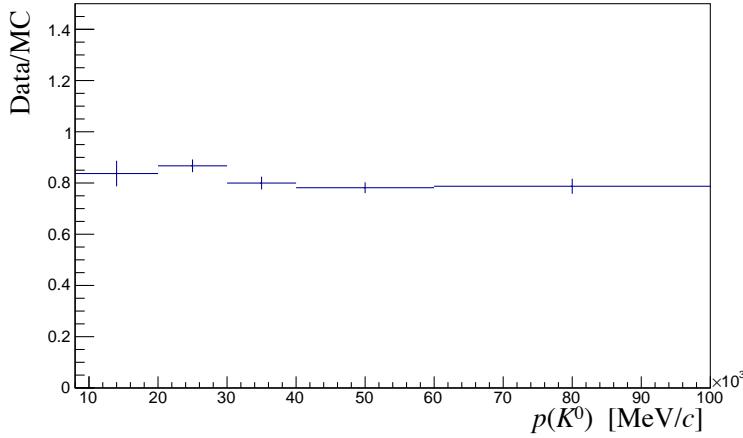


Figure 3.19: Ratio of reconstruction efficiency in data and simulation found using  $K_S$  events [107].

#### 3.7.2.4 $\Lambda_b^0$ lifetime

The  $\Lambda_b^0$  lifetime is known with limited precision. For the efficiencies' evaluation the world average value,  $1.482 \text{ ps}^{-1}$  [106], is used which is varied within one standard deviation from the measured value to asses the systematic uncertainty. Only the case where both signal and normalisation channel are varied in same direction are considered. The largest difference from the default lifetime case is taken as systematic uncertainty, which is found to range from  $\sim 0.4\%$  at low- $q^2$  to  $\sim 0.1\%$  at high- $q^2$ .

#### 3.7.2.5 Downstream candidates reconstruction efficiency

Other analysis in LHCb using particles reconstructed with downstream tracks showed that the efficiency for these candidates is not well simulated. For example, Fig. 3.19 shows the ratio between the reconstruction efficiency for downstream candidates in data and simulation found analysing  $K_S^0$  events [107]. This effect is not yet fully understood and is currently under study. It seems to be mainly due to a poor simulation of the vertexing efficiency for downstream tracks. As the analysis is performed separately for downstream and long candidates and efficiencies are calculated separately, the effect of this mis-modelling, present in both the rare and resonant chan-

nels, mostly cancels their ratio. Nevertheless, a systematic uncertainty is assessed by re-weighting simulated downstream candidates by the efficiency ratio between data and simulation found for  $K_S$  as a function of momentum (see Fig. 3.19). The efficiencies obtained using the weighted and unweighted simulation are compared and the full difference is taken as systematic uncertainty. As the discrepancy shows little dependence on momentum, dependencies due to the different momentum distributions of  $\Lambda$  and  $K_S^0$  are assumed to be negligible. This results in a  $\sim 0.4\%$  systematic uncertainty at low- $q^2$  and 1.2% at high- $q^2$ , only for downstream candidates.

### 3.7.2.6 Data-simulation discrepancies

The simulation used to calculate the efficiencies is weighted as described in Sec. 3.3.2 to improve the simulation' description of data. The influence of this procedure on the efficiency determination is checked by comparing values obtained with and without re-weighting. The effect is negligible with respect to other systematics considered.

## 3.8 Differential branching fraction extraction

In this section the differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay is calculated relative to the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  channel as a function of  $q^2$ . The values are directly obtained from the fit to the rare sample by parameterising the downstream and long yields with the following formula:

$$N(\Lambda \mu^+ \mu^-)_k = \left[ \frac{d\mathcal{B}(\Lambda \mu^+ \mu^-)/dq^2}{\mathcal{B}(J/\psi \Lambda)} \right] \cdot N(J/\psi \Lambda)_k \cdot \varepsilon_k^{\text{rel}} \cdot \frac{\Delta q^2}{\mathcal{B}(J/\psi \rightarrow \mu^+ \mu^-)}, \quad (3.15)$$

where  $k = (\text{LL}, \text{DD})$ ,  $\Delta q^2$  is the width of the  $q^2$  interval,  $\mathcal{B}(J/\psi \rightarrow \mu^+ \mu^-) = (5.93 \pm 0.06) \cdot 10^{-2}$  [2] and the only free parameter is the relative branching fraction ratio. Table 3.13 summarises the total relative efficiencies,  $\varepsilon^{\text{rel}}$ , for downstream and long candidates together with their correlated and uncorrelated uncertainties, where the correlation is intended between the downstream and long samples. On the table

Table 3.13: Absolute values of the total relative efficiency and the absolute value of the uncorrelated uncertainty ( $\sigma_{uncorr}^k$ ), together with relative values of the correlated uncertainty ( $\sigma_{corr}$ ).

| $q^2$ [GeV $^2/c^4$ ] | Eff. (DD) | $\sigma_{uncorr}^{DD}$ | Eff. (LL) | $\sigma_{uncorr}^{LL}$ | $\sigma_{corr}$ |
|-----------------------|-----------|------------------------|-----------|------------------------|-----------------|
| 0.1 – 2.0             | 0.694     | 0.058                  | 1.136     | 0.066                  | 1.0%            |
| 2.0 – 4.0             | 0.693     | 0.027                  | 0.907     | 0.047                  | 2.7%            |
| 4.0 – 6.0             | 0.699     | 0.018                  | 0.964     | 0.044                  | 2.7%            |
| 6.0 – 8.0             | 0.733     | 0.020                  | 0.953     | 0.048                  | 2.7%            |
| 11.0 – 12.5           | 1.254     | 0.032                  | 1.140     | 0.057                  | 3.4%            |
| 15.0 – 16.0           | 1.260     | 0.035                  | 1.035     | 0.060                  | 3.0%            |
| 16.0 – 18.0           | 1.163     | 0.029                  | 0.997     | 0.048                  | 1.7%            |
| 18.0 – 20.0           | 1.023     | 0.027                  | 0.782     | 0.040                  | 2.7%            |
| 1.1 – 6.0             | 0.696     | 0.032                  | 0.950     | 0.058                  | 1.0%            |
| 15.0 – 20.0           | 1.132     | 0.014                  | 0.927     | 0.031                  | 1.4%            |

the uncorrelated uncertainty corresponds to the total systematic uncertainty on the efficiency determination. The correlated uncertainty is given in percent form since it can be applied to either downstream, long candidates or their combination. This includes the PDF systematic described in Sec. 3.7.1 and the systematic due to the uncertainty on the  $J/\psi \rightarrow \mu^+\mu^-$  branching fraction.

Figure 3.20 shows the differential branching fraction obtained by fitting the downstream and long samples independently, while the combined result, obtained fitting both samples simultaneously, is shown in Fig. 3.21. Measured values are also listed in Tab. 3.14, where the statistical uncertainty on the rare channel and the total systematic uncertainty are shown separately. The statistical uncertainty is calculated using the MINOS application of the MINUIT package [108], which provides an asymmetric interval. The normalisation and systematic uncertainties are evaluated by pushing the efficiencies and normalisation yields up and down by one standard deviation and re-performing the fit. The different efficiencies used translate into a different branching fraction and the full difference with respect to the default fit is taken as systematic uncertainty in each direction.

Finally, values for the absolute branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decay are obtained by multiplying the relative values listed in Tab. 3.14 by the branching fraction of the normalisation channel,  $\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi\Lambda) = (6.3 \pm 1.3) \times 10^{-4}$  [2].

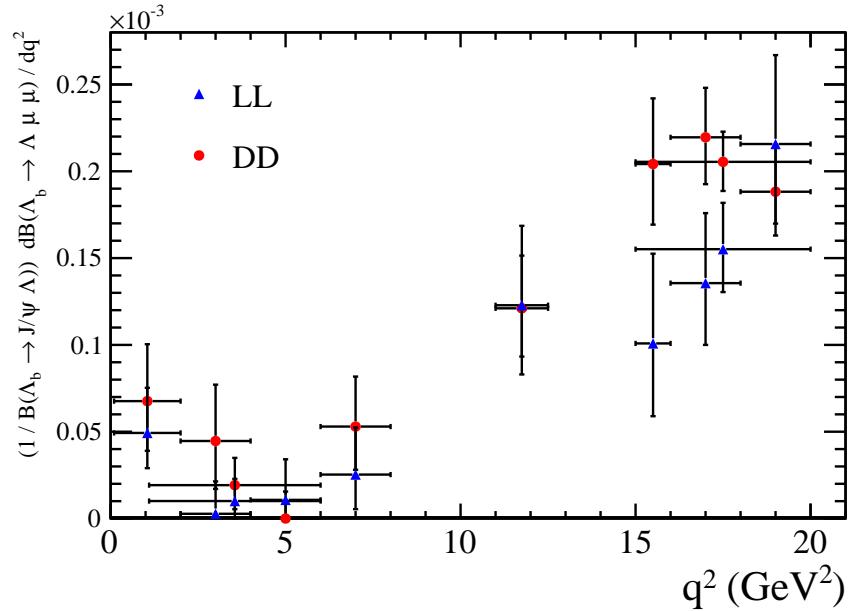


Figure 3.20: Measured values of the differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay relative to the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  decay as a function of  $q^2$  obtained fitting the downstream and long samples independently. Error bars represent the total statistical and systematic uncertainty.

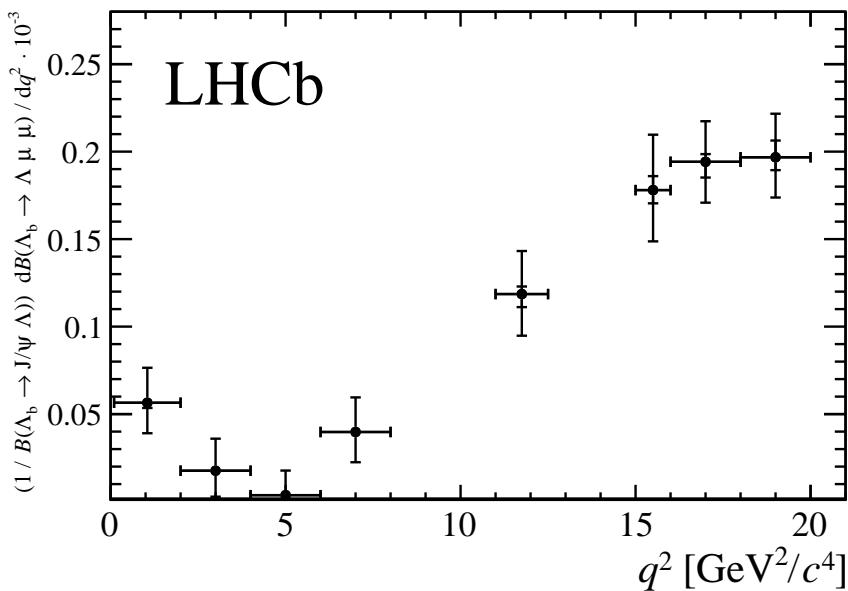


Figure 3.21: Differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay normalised to the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  mode. The inner error bar represents the systematic uncertainty and the outer error bar includes the statistical uncertainty.

Table 3.14: Measured differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decay relative to  $\Lambda_b^0 \rightarrow J/\psi\Lambda$  decays; uncertainties are statistical and systematic respectively.

| $q^2$ interval [ GeV $^2/c^4$ ] |      | $\frac{d\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-)/dq^2}{\mathcal{B}(\Lambda_b^0 \rightarrow J/\psi\Lambda)} \cdot 10^{-3}$ [( GeV $^2/c^4$ ) $^{-1}$ ] |                |
|---------------------------------|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------|
| 0.1 – 2.0                       | 0.56 | +0.20<br>–0.17                                                                                                                                                      | +0.03<br>–0.03 |
| 2.0 – 4.0                       | 0.18 | +0.18<br>–0.15                                                                                                                                                      | +0.01<br>–0.01 |
| 4.0 – 6.0                       | 0.04 | +0.14<br>–0.04                                                                                                                                                      | +0.01<br>–0.01 |
| 6.0 – 8.0                       | 0.40 | +0.20<br>–0.17                                                                                                                                                      | +0.01<br>–0.02 |
| 11.0 – 12.5                     | 1.19 | +0.24<br>–0.23                                                                                                                                                      | +0.04<br>–0.07 |
| 15.0 – 16.0                     | 1.78 | +0.31<br>–0.28                                                                                                                                                      | +0.08<br>–0.08 |
| 16.0 – 18.0                     | 1.94 | +0.23<br>–0.22                                                                                                                                                      | +0.04<br>–0.09 |
| 18.0 – 20.0                     | 1.97 | +0.23<br>–0.22                                                                                                                                                      | +0.10<br>–0.07 |
| 1.1–6.0                         | 0.14 | +0.10<br>–0.09                                                                                                                                                      | +0.01<br>–0.01 |
| 15.0–20.0                       | 1.90 | +0.14<br>–0.14                                                                                                                                                      | +0.04<br>–0.06 |

Values are shown in Fig. 3.22 and summarised in Tab. 3.15, where the uncertainty due to the knowledge of the normalisation channel, which is correlated across  $q^2$ , is shown separately. The SM predictions on the plot are obtained from Ref. [105].

Evidence for the signal is found for the first time in the interval  $0.1 < q^2 < 2.0$  GeV $^2/c^4$ , where an enhanced yield is expected due to the proximity of the photon pole and in the region between the two charmonium resonances. The uncertainty on the relative branching fraction is dominated by the size of the available data sample, while, the uncertainty on the absolute values is dominated by the precision with which the branching fraction of the normalisation channel is known. The measurement is consistent with the theoretical predictions in the high- $q^2$  region but lies below the predictions in the low- $q^2$  region. Improved predictions published after the publication of the LHCb result are reported in Appendix D, where a better agreement is found.

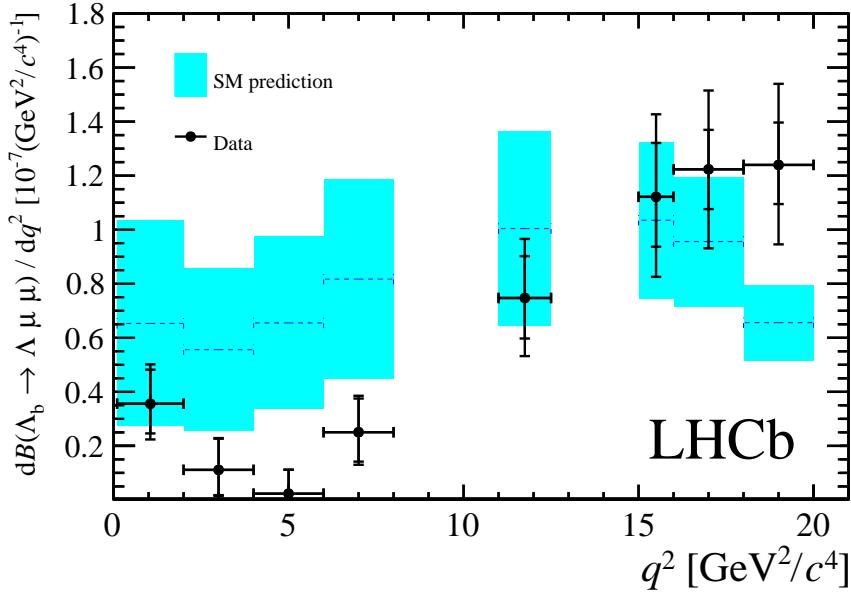


Figure 3.22: Measured  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  branching fraction as a function of  $q^2$  with SM predictions [105] superimposed. The inner error bars represent the total uncertainty on the relative branching fraction (statistical and systematic), while the outer error bar also includes the uncertainties due to the knowledge of the branching fraction of the normalisation mode.

Table 3.15: Measured differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay, where the uncertainties are statistical, systematic and due to the knowledge of the normalisation mode,  $\Lambda_b^0 \rightarrow J/\psi \Lambda$ , respectively.

| $q^2$ interval [ $\text{GeV}^2/c^4$ ] | $d\mathcal{B}(\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-)/dq^2 \cdot 10^{-7} [(\text{GeV}^2/c^4)^{-1}]$ | $+0.12$ | $+0.02$ | $\pm 0.07$ |
|---------------------------------------|----------------------------------------------------------------------------------------------------------|---------|---------|------------|
| 0.1 – 2.0                             | 0.36                                                                                                     | $-0.11$ | $-0.02$ |            |
| 2.0 – 4.0                             | 0.11                                                                                                     | $+0.12$ | $+0.01$ | $\pm 0.02$ |
| 4.0 – 6.0                             | 0.02                                                                                                     | $+0.09$ | $+0.01$ | $\pm 0.01$ |
| 6.0 – 8.0                             | 0.25                                                                                                     | $-0.11$ | $-0.01$ | $\pm 0.05$ |
| 11.0 – 12.5                           | 0.75                                                                                                     | $+0.15$ | $+0.03$ | $\pm 0.15$ |
| 15.0 – 16.0                           | 1.12                                                                                                     | $-0.18$ | $-0.05$ | $\pm 0.23$ |
| 16.0 – 18.0                           | 1.22                                                                                                     | $-0.14$ | $-0.06$ | $\pm 0.25$ |
| 18.0 – 20.0                           | 1.24                                                                                                     | $+0.14$ | $+0.06$ | $\pm 0.26$ |
| 1.1 – 6.0                             | 0.09                                                                                                     | $+0.06$ | $+0.01$ | $\pm 0.02$ |
| 15.0 – 20.0                           | 1.20                                                                                                     | $-0.09$ | $-0.04$ | $\pm 0.25$ |

# CHAPTER 4

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## Angular analysis of $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$ decays

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Neglecting the production polarisation of  $\Lambda_b^0$ , the  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decay angular distribution can be described as a function of three angles and  $q^2$ . The first two angles are the ones which are relevant for the analysis in this chapter and are defined in Fig. 4.1, where  $\theta_\ell$  is the angle between the positive (negative) muon direction in the dimuon rest frame and the dimuon system direction in the  $\Lambda_b^0$  ( $\bar{\Lambda}_b^0$ ) rest frame, and, similarly,  $\theta_h$  is defined as the angle between the proton and the  $\Lambda$  baryon directions, in the  $\Lambda$  and  $\Lambda_b^0$  rest frames. The third angle is the angle between the dimuon and  $\Lambda$  decay planes, which is integrated over in this analysis. This chapter describes a measurement of two forward-backward asymmetries in the leptonic ( $A_{\text{FB}}^\ell$ ) and in the hadronic ( $A_{\text{FB}}^h$ ) systems. These forward-backward asymmetries are defined as

$$A_{\text{FB}}^i(q^2) = \frac{\int_0^1 \frac{d^2\Gamma}{dq^2 d\cos\theta_i} d\cos\theta_i - \int_{-1}^0 \frac{d^2\Gamma}{dq^2 d\cos\theta_i} d\cos\theta_i}{d\Gamma/dq^2}, \quad (4.1)$$

where  $d^2\Gamma/dq^2 d\cos\theta_i$  is the two-dimensional differential rate and  $d\Gamma/dq^2$  is rate integrated over the angles.

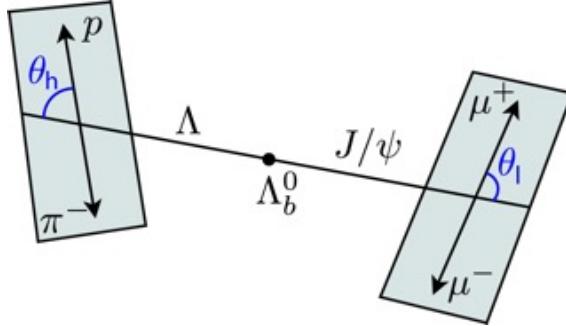


Figure 4.1: Graphical representation of the angles for the  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decay.

The  $A_{\text{FB}}^\ell$  observable was measured by LHCb also for  $B^0 \rightarrow K^{*0}\mu^+\mu^-$  decays which are going through the same quark level transition as  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decays. Instead the hadronic asymmetry,  $A_{\text{FB}}^h$ , is interesting only in the  $\Lambda_b^0$  case as it is zero by definition in the  $B^0$  case, due to the strong decay of the  $K^{*0}$ .

## 4.1 One-dimensional angular distributions

This section describes the derivation of the functional form of the differential distributions as a function of  $\cos\theta_\ell$  and  $\cos\theta_h$ , which are used to measure the observables. The content of this section is based on the calculations in Ref. [101].

For unpolarised  $\Lambda_b^0$  production, integrating over the three angles the differential branching fraction is given in Eq. 11 of Ref. [101] as

$$\frac{d\Gamma(\Lambda_b \rightarrow \Lambda \ell^+ \ell^-)}{dq^2} = \frac{v^2}{2} \cdot \left( U^{V+A} + L^{V+A} \right) + \frac{2m_\ell^2}{q^2} \cdot \frac{3}{2} \cdot \left( U^V + L^V + S^A \right), \quad (4.2)$$

and the lepton helicity angle differential distribution, given in Eq. 15, has the form

$$\begin{aligned} \frac{d\Gamma(\Lambda_b \rightarrow \Lambda \ell^+ \ell^-)}{dq^2 d\cos\theta_\ell} &= v^2 \cdot \left[ \frac{3}{8} (1 + \cos^2\theta_\ell) \cdot \frac{1}{2} U^{V+A} + \frac{3}{4} \sin^2\theta_\ell \cdot \frac{1}{2} L^{V+A} \right] \\ &- v \cdot \frac{3}{4} \cos\theta_\ell \cdot P^{VA} + \frac{2m_\ell^2}{q^2} \cdot \frac{3}{4} \cdot \left[ U^V + L^V + S^A \right]. \end{aligned} \quad (4.3)$$

In these formulas  $m_\ell$  is the mass of the lepton and  $v = \sqrt{1 - 4m_\ell^2/q^2}$ ;  $U$  denotes the unpolarised-transverse contributions,  $L$  the longitudinal contributions and  $S$  the scalar contribution. The apices  $V$  and  $A$  represent respectively vector and axial-vector currents, with  $X^{V+A} = X^V + X^A$ . The authors of Ref. [101] define then the lepton-side forward-backward asymmetry as

$$A_{\text{FB}}^\ell = -\frac{3}{2} \frac{v \cdot P^{VA}}{v^2 \cdot (U^{V+A} + L^{V+A}) + \frac{2m_\ell^2}{q^2} \cdot 3 \cdot (U^V + L^V + S^A)}. \quad (4.4)$$

For this analysis the massless leptons limit,  $m_\ell \rightarrow 0$ , is used, which is a good approximation except at very low  $q^2$ . Combining the previous equations ad taking the massless limit the differential rates simplify to

$$\frac{d\Gamma}{dq^2} = \frac{v^2}{2} \cdot (U^{V+A} + L^{V+A}) \quad (4.5)$$

and

$$\frac{d\Gamma}{dq^2 d \cos \theta_\ell} = \frac{v^2}{2} \left[ \frac{3}{8} (1 + \cos^2 \theta_\ell) U^{V+A} + A_{\text{FB}}^\ell \cos \theta_\ell (U^{V+A} + L^{V+A}) + \frac{3}{4} \sin^2 \theta_\ell (L^{V+A}) \right]. \quad (4.6)$$

Equations 4.5 and 4.6 can be then combined to achieve the form

$$\begin{aligned} \frac{d\Gamma}{dq^2 d \cos \theta_\ell} &= \frac{d\Gamma}{dq^2} \left[ \frac{3}{8} (1 + \cos^2 \theta_\ell) \frac{U^{V+A}}{U^{V+A} + L^{V+A}} + A_{\text{FB}}^\ell \cos \theta_\ell + \right. \\ &\quad \left. \frac{3}{4} \sin^2 \theta_\ell \frac{L^{V+A}}{U^{V+A} + L^{V+A}} \right]. \end{aligned} \quad (4.7)$$

The amplitude combination in the last term can be viewed as the ratio between the longitudinal and the sum of longitudinal and unpolarised contributions and therefore one can define the longitudinal fraction

$$f_L = \frac{L^{V+A}}{U^{V+A} + L^{V+A}}, \quad (4.8)$$

which leads to the functional form used in the analysis

$$\frac{d\Gamma}{dq^2 d \cos \theta_\ell} = \frac{d\Gamma}{dq^2} \left[ \frac{3}{8} (1 + \cos^2 \theta_\ell) (1 - f_L) + A_{FB}^\ell \cos \theta_\ell + \frac{3}{4} \sin^2 \theta_\ell f_L \right]. \quad (4.9)$$

Using the same steps the proton helicity distribution is given in Ref. [101] as

$$\frac{d\Gamma(\Lambda_b \rightarrow \Lambda(\rightarrow p\pi^-)\ell^+\ell^-)}{dq^2 d \cos \theta_h} = \text{Br}(\Lambda \rightarrow p\pi^-) \frac{d\Gamma(\Lambda_b \rightarrow \Lambda \ell^+\ell^-)}{dq^2} \left( \frac{1}{2} + A_{FB}^h \cos \theta_h \right), \quad (4.10)$$

and  $A_{FB}^h$  is defined as

$$A_{FB}^h = \frac{1}{2} \alpha_\Lambda P_z^\Lambda(q^2), \quad (4.11)$$

where  $P_z^\Lambda(q^2)$  is the polarisation of the daughter baryon,  $\Lambda$ , and  $\alpha_\Lambda = 0.642 \pm 0.013$  [2] is the  $\Lambda$  decay asymmetry parameter.

The above expressions assume that  $\Lambda_b^0$  is produced unpolarised, which is in agreement with the recent LHCb measurement [109]. Possible effects due to a non zero production polarisation are investigated as systematic uncertainties (see Sec. 4.5.5).

## 4.2 Multi-dimensional angular distributions

To incorporate effects of production polarisation this was introduced in the equations. In the modified version an angle  $\theta$  is defined as the angle between the  $\Lambda$  direction in the  $\Lambda_b^0$  rest frame with respect to  $\hat{n} = \hat{p}_{inc} \times \hat{p}_{\Lambda_b^0}$ , where  $\hat{p}_{inc}$  represents the direction of the incoming proton; this angle is sensitive to the production polarisation. Integrating over all the angles but  $\theta_\ell$  results in the same distribution as in the unpolarised case (Eq. 4.3). Therefore, in the case of uniform efficiency, the lepton side forward-backward asymmetry,  $A_{FB}^\ell$ , is unaffected by the production polarisation. To be able to estimate the effect of the production polarisation in the case of non-uniform efficiency, the differential distribution in  $\theta$  and  $\theta_\ell$  is derived,

which in the massless leptons limit becomes (up to a constant multiplicative factor)

$$\frac{d\Gamma(\Lambda_b \rightarrow \Lambda \ell^+ \ell^-)}{dq^2 d \cos \theta d \cos \theta_\ell} = \frac{d\Gamma}{dq^2} \left\{ \frac{3}{8} (1 + \cos^2 \theta_\ell) (1 - f_L) + A_{FB}^\ell \cos \theta_\ell + \frac{3}{4} \sin^2 \theta_\ell f_L + P_b \cos \theta \left[ -\frac{3}{4} \sin \theta_\ell^2 O_{Lp} + \frac{3}{8} (1 + \cos \theta_\ell^2) O_P \right. \right. \\ \left. \left. - \frac{3}{8} \cos \theta_\ell O_{UVA} \right] \right\}, \quad (4.12)$$

where three more observables are defined

$$O_{Lp} = \frac{L_P^V + L_P^A}{U^{V+A} + L^{V+A}}, \\ O_P = \frac{P^V + P^A}{U^{V+A} + L^{V+A}}, \\ O_{UVA} = \frac{U^{VA}}{U^{V+A} + L^{V+A}}.$$

In the massless leptons approximation two of these quantities are related to the hadron side forward-backward asymmetry as

$$\frac{1}{2} \alpha_\Lambda (O_P + O_{Lp}) = A_{FB}^h. \quad (4.13)$$

Following the same steps as for the lepton case, after integrating over all the angles but  $\theta_h$  one finds that the hadron side,  $A_{FB}^h$ , is also unaffected by the production polarisation in case of uniform efficiency and the differential distribution in  $\theta$  and  $\theta_h$  has the form

$$\frac{d\Gamma(\Lambda_b \rightarrow \Lambda \ell^+ \ell^-)}{dq^2 d(\cos \theta) d(\cos \theta_h)} = \frac{d\Gamma}{dq^2} [1 + 2A_{FB}^h \cos \theta_h + P_b (O_P - O_{Lp}) \cos \theta \\ + \alpha_\Lambda P_b (1 - 2f_L) \cos \theta \cos \theta_h]. \quad (4.14)$$

In order to use these distributions, expectations for the three additional observables, which do not enter one-dimensional distributions, are needed. Expectations are calculated using form factors and numerical inputs from Ref. [101] and are listed in Appendix A.1.

For completeness, the differential distribution in  $\cos \theta_\ell$  and  $\cos \theta_h$  has the form

$$\begin{aligned} \frac{d\Gamma(\Lambda_b \rightarrow \Lambda \ell^+ \ell^-)}{dq^2 d\cos \theta_h d\cos \theta_\ell} = & \frac{3}{8} + \frac{6}{16} \cos^2 \theta_\ell (1 - f_L) - \frac{3}{16} \cos^2 \theta_\ell f_L + A_{FB}^l \cos \theta_\ell + \\ & \left( \frac{3}{2} A_{FB}^h - \frac{3}{8} \alpha_A O_P \right) \cos \theta_h - \frac{3}{2} A_{FB}^h \cos^2 \theta_\ell \cos \theta_h - \frac{3}{16} f_L + \\ & \frac{9}{16} f_L \sin^2 \theta_\ell + \frac{9}{8} \alpha_A \cos^2 \theta_\ell \cos \theta_h O_P - \\ & \frac{3}{2} \alpha_A \cos \theta_\ell \cos \theta_h O_{UVA}. \end{aligned} \quad (4.15)$$

### 4.3 Angular resolution

This section describes a study of the angular resolution performed in order to achieve a better understanding of detector and reconstruction effects. This will be then used to study systematic uncertainties (see Sec. 4.5.5). The study is performed by analysing simulated events and comparing generated and reconstructed quantities. Figure 4.2 shows the difference between true and measured angular observables,  $\cos \theta_\ell$  and  $\cos \theta_h$ , as a function of the observables themselves. These distributions are centred at zero indicating no bias in the measurement. The spread of these distributions around the central value can be interpreted as an estimate of the angular resolution. Taking vertical slices of the plots in Fig. 4.2 one obtains approximately gaussian distributions centred at zero. These are fit with a single gaussian and its width is interpreted as the angular resolution. Table 4.1 reports the average resolutions for the two angular observables separately for long and downstream candidates. Candidates built from long tracks are characterised by a better angular resolution due to a better momentum and vertex resolution.

Table 4.1: Average angular resolutions integrated over the full interval and the full available  $q^2$ .

| Observable         | Downstream | Long  |
|--------------------|------------|-------|
| $\cos \theta_\ell$ | 0.015      | 0.010 |
| $\cos \theta_h$    | 0.066      | 0.014 |

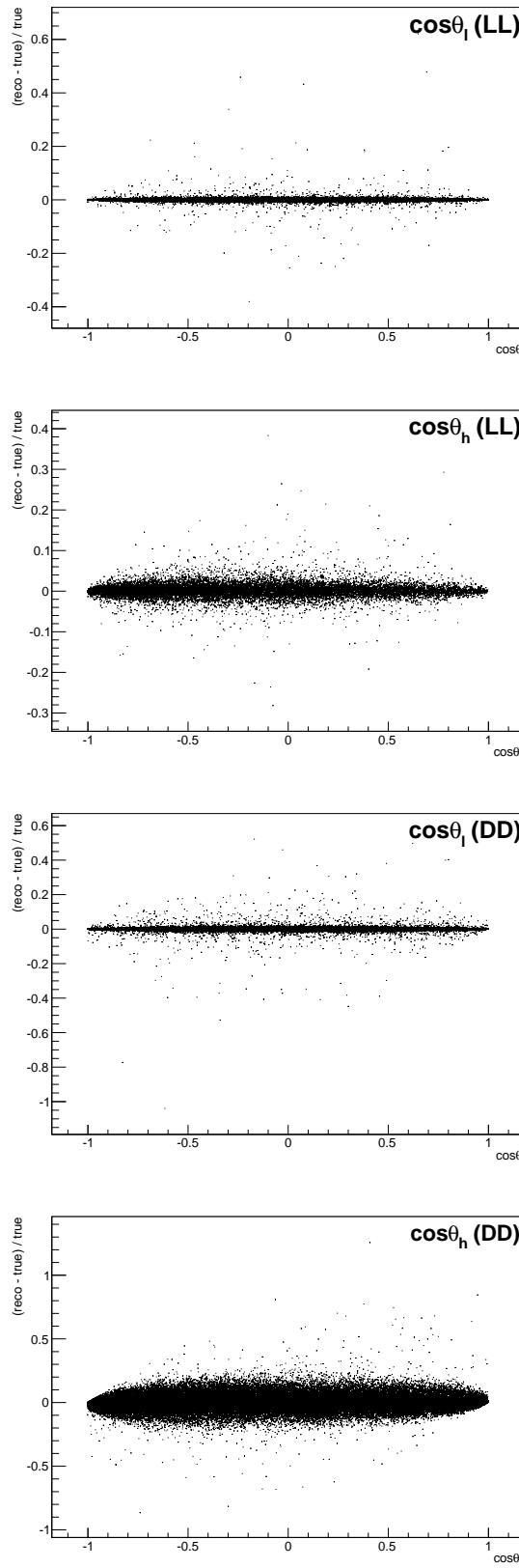


Figure 4.2: Difference between generated and reconstructed angular observables as a function of the observables themselves. From top to bottom:  $\cos\theta_\ell$  (LL),  $\cos\theta_h$  (LL),  $\cos\theta_\ell$  (DD),  $\cos\theta_h$  (DD). The spread of these distributions can be interpreted as the angular observables' resolution.

## 4.4 Fit strategy

There are physical boundaries to the values of the parameters of interests:  $A_{\text{FB}}^h$  is limited in the  $[-0.5, 0.5]$  interval and for the  $f_L$  and  $A_{\text{FB}}^\ell$  parameters the physical region, given by  $|A_{\text{FB}}^\ell| < 3/4 \cdot (f_L - 1)$ , is the triangle shown in Fig. 4.3. If the measured value is close to the border of the physical region the fit does not always converge. Therefore a “brute force” fitting technique is applied. For this purpose fit parameters are divided into two categories: parameters of interest (PoIs),  $A_{\text{FB}}^\ell$ ,  $A_{\text{FB}}^h$  and  $f_L$  and all other parameters, which are referred to as “nuisances”. The value of the Log-Likelihood ( $\log \mathcal{L}$ ) of the fit model with respect to data is evaluated in a grid of points in the PoIs’ allowed area to find the function’s minimum. A first coarse scan finds a candidate minimum and then the procedure is reiterated two more times in finer intervals around it. For each point all the nuisances are fitted using a maximum likelihood fit. Using this method the best fit point is therefore constrained inside the physical region. If the minimum of the log-likelihood is found to be outside it, the closest point on the boundary is chosen as the best fit.

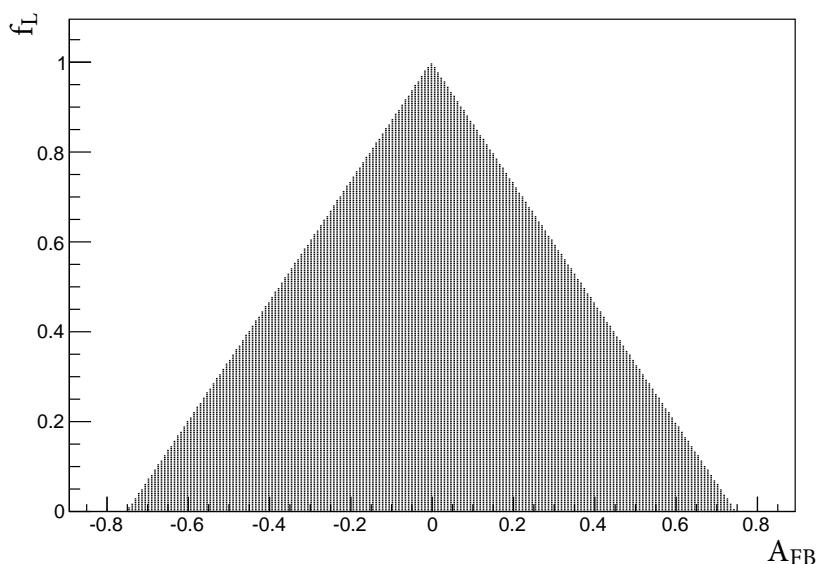


Figure 4.3: The physical  $(A_{\text{FB}}^\ell, f_L)$  parameter space. The dark region corresponds to points where the PDF is positive in the whole  $[-1, 1] \cos \theta_\ell$  interval.

#### 4.4.1 Feldman-cousins plug-in method

Physical boundaries of the parameter space could result in a wrong estimation of the uncertainties, especially if the measured value is close to the boundary. To deal with this effect the likelihood-ordering method [110] is used to estimate uncertainties and nuisance parameters are accounted for using the plug-in method [111]. This is a unified method to calculate confidence intervals and upper/lower limits, based on simulated experiments and has the advantage of having a well defined frequentist coverage.

The method is constituted by the following steps:

1. fit real data distributions with all parameters free;
2. fit real data fixing the PoIs to a value of choice while keeping nuisance parameters free;
3. generate simulated samples following the distribution given by the fit model, where all nuisance parameters are taken from the fit in point 2 and PoIs are fixed to the same value used in point 2;
4. repeat the two fits made on data (points 1 and 2) on each simulated sample: fit with all parameters free and with fixed PoIs;
5. calculate the minimum values of the Log-Likelihoods for all cases;
6. calculate the percentage of simulated experiments in which the free-to-fixed likelihood ratio is bigger than in data:  $\log \mathcal{L}_{fixed} / \log \mathcal{L}_{free} > (\log \mathcal{L}_{fixed} / \log \mathcal{L}_{free})_{data}$ ;
7. repeat the procedure for many values of the PoIs scanning around the best fit point.

The confidence interval at  $k\%$  is given by the points where the free-to-fixed likelihood ratio is bigger in data than simulation for  $(1 - k)\%$  of times. As an example, Fig. 4.4

shows the p-values obtained with the plug-in method for  $A_{\text{FB}}^h$  and  $f_L$ . A two-dimensional region can also be scanned giving a grid of p-values, which translates into two-dimensional confidence regions.

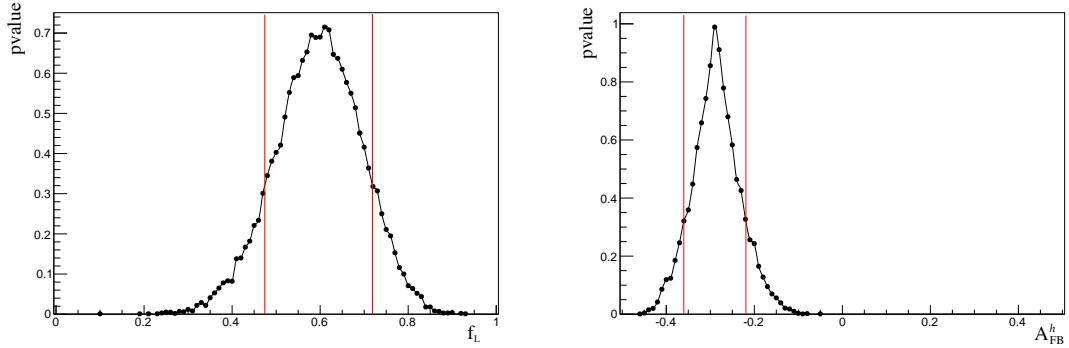


Figure 4.4: Dependence of the p-value on the values of the angular observables  $f_L$  (left) and  $A_{\text{FB}}^h$  (right) in simulated experiments. The red lines mark the points at p-value 32% corresponding to a 68% CL.

#### 4.4.2 Modelling the angular distributions

The observables are obtained from fits to one-dimensional angular distributions.

The PDFs used to model the data are defined as

$$P^k(\cos \theta_{\ell/h}) = [(1 - f_b) \cdot P_S(\cos \theta_{\ell/h}) + f_b \cdot P_B^k(\cos \theta_{\ell/h})] \times \varepsilon^k(\cos \theta_{\ell/h}), \quad (4.16)$$

where  $k = (\text{LL}, \text{DD})$ . The first term represents the signal which is modelled by the theoretical shapes,  $P_S$ , given by Eqs. 4.9 and 4.10, respectively for the lepton and hadron cases, while the second term represents the background, which is parameterised with a linear function:  $P_B^k(\cos \theta_{\ell/h}) = (c \cdot \cos \theta_{\ell/h} + q)$ . Both terms are multiplied by an acceptance function  $\varepsilon$  described in Sec. 4.4.3. Imposing the PDF normalisation the background model is left with one free parameter which is fixed by fitting candidates in the  $\Lambda_b^0$  invariant mass sideband,  $m(p\pi\mu\mu) > 5700 \text{ MeV}/c^2$ , which contains only background. Finally,  $f_b$  is the background fraction:  $f_b = B/(S+B)$ . To limit systematic effects due to the background parameterisation the fit is performed in a restricted invariant mass region around the  $\Lambda_b^0$  mass peak dominated by the

signal:  $5580 < m(p\pi\mu\mu) < 5660$  MeV/ $c^2$  (“signal region”). The background fraction,  $f_b$ , is obtained by looking at the 4-body  $m(p\pi\mu\mu)$  invariant mass distribution in a wider interval and fitting it to extract the fraction of background in the signal region. In the fit to the angular distributions this is then gaussian constrained to the obtained value. Figure 4.5 shows the angular distributions of sideband candidates for the high- $q^2$  integrated interval with overlaid the background function. Note that a different acceptance shape is used for the downstream and long samples and for each  $q^2$  interval. In summary the only free fit parameter in each of the final fits to data is the forward-backward asymmetry (and  $f_L$  in the leptonic case).

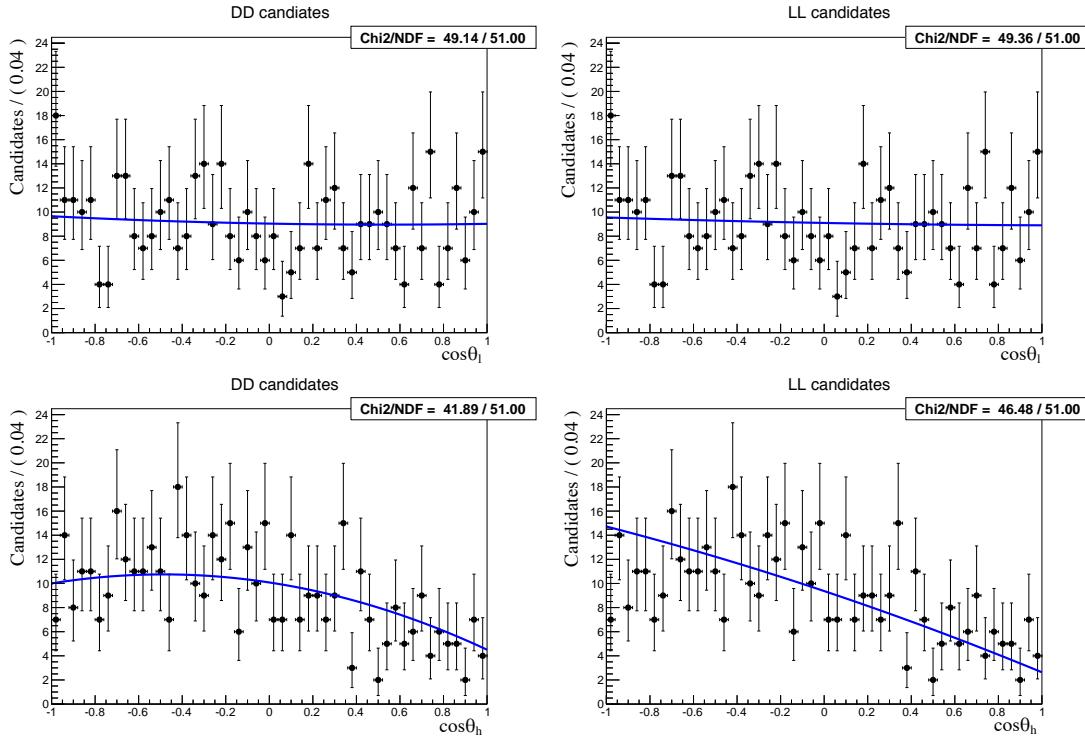


Figure 4.5: Background distribution as a function of  $\cos \theta_\ell$  (top) and  $\cos \theta_h$  (bottom) for downstream (left) and long (right) candidates in the  $15 - 20$  GeV $^2/c^4$   $q^2$  interval.

#### 4.4.3 Angular acceptance

Selection requirements on the minimum momentum of the muons can distort the  $\cos \theta_\ell$  distribution by removing candidates with extreme values of the angle. Similarly, the impact parameter requirements affect  $\cos \theta_h$  because very forward hadrons

tend to have smaller impact parameter values. While in principle one could take this into account by an additional weight, to minimise the distortion of the uncertainties estimate, the efficiency function is incorporated in the fit model. The angular efficiency is parametrised using a second-order polynomial, whose parameters are determined separately for long and downstream candidates by fitting simulated events. An independent set of parameters is obtained also for each  $q^2$  interval. These parameters are then fixed for the fits to data. Using polynomial functions allows to calculate the PDF normalisation analytically. Figure 4.6 shows the acceptance as a function of  $\cos \theta_h$  and  $\cos \theta_\ell$  for the  $15 - 20 \text{ GeV}^2/c^4$  integrated  $q^2$  interval obtained using a  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  simulated sample. For the lepton side, even though the efficiency is symmetric by construction, all parameters are left free to float, namely it is not constrained to be symmetric.

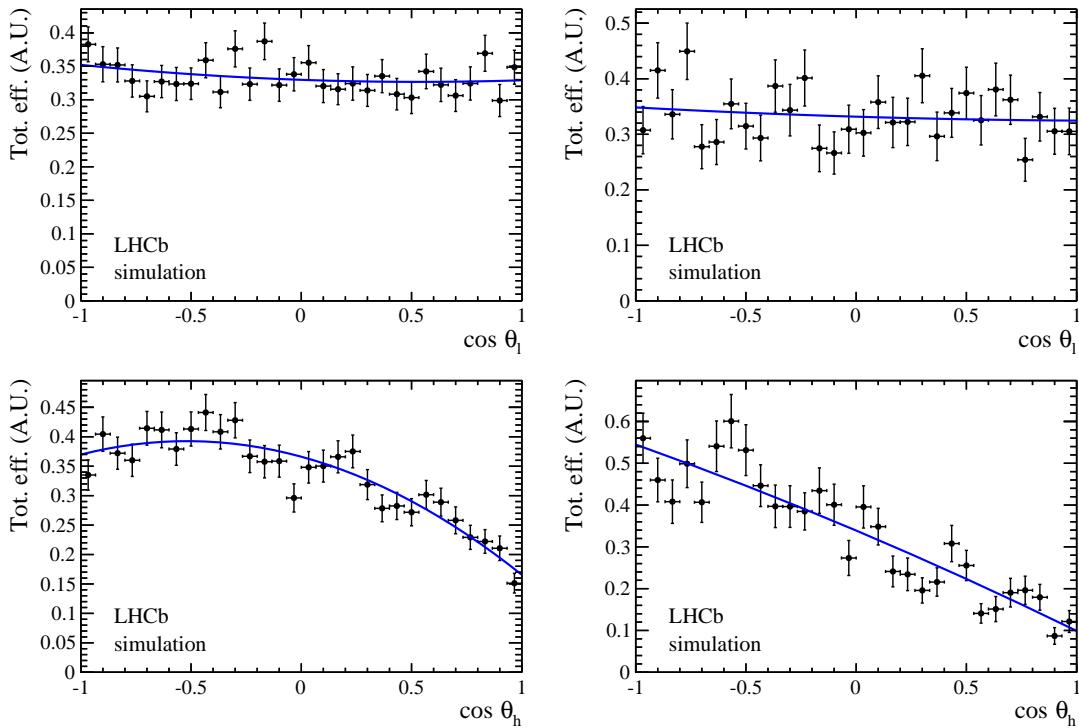


Figure 4.6: Efficiency as a function of  $\cos \theta_\ell$  (top) and  $\cos \theta_h$  (bottom) for downstream (left) and long (right) candidates in the  $15 - 20 \text{ GeV}^2/c^4$   $q^2$  interval.

#### 4.4.4 Studies on a three-dimensional fit

One other way of extracting the angular observables would be to fit at the same time both angles and also the invariant mass distribution in order to have a better handle on the level of background. In this case one can use more of the information available. On the other hand it is necessary to use a larger mass window including more background and this method involves more parameters to fit. In fact, in the 3D case in addition to the  $A_{\text{FB}}^\ell$ ,  $f_L$  and  $A_{\text{FB}}^h$  parameters, there are two background fractions and the two exponential slopes for the invariant mass background. Furthermore, to take correctly into account correlations three more observables enter the fit (see Eq. 4.12). As an high number of free parameters is difficult to constrain with the very limited statistics available, pseudo-experiments are used to check which method gives the best sensitivity. Events are generated in a 3D  $(\cos\theta_\ell, \cos\theta_h, m_{p\pi\mu\mu})$  space. The generated values of the observables are  $A_{\text{FB}}^\ell = 0$ ,  $f_L = 0.7$  and  $A_{\text{FB}}^h = -0.37$ , which are data-like values inspired to a preliminary measurement in the highest statistics interval. Also the overall statistics and the fraction of background candidates in the mass window are generated to be data-like using information from the preliminary fit to data. Each pseudo-experiment is fitted with both the 1D and 3D methods. Figure 4.7 reports distributions of parameters of interest obtained from the fit in the 1D and 3D cases. The RMS of these distributions can be taken as a measure of the sensitivity of each method. Table 4.2 lists the RMSs obtained from both methods; for all parameters of interest the 1D fit method gives a smaller RMS, hence a better sensitivity.

Table 4.2: RMS values for pseudo-experiments on the extraction of the three parameters of interests with the 1D or 3D fitting methods.

| $q^2$ [ GeV $^2/c^4$ ] | Fit type | $A_{\text{FB}}^h$ | $A_{\text{FB}}^\ell$ | $f_L$ |
|------------------------|----------|-------------------|----------------------|-------|
| 15.0 – 20.0            | 1D       | 0.070             | 0.055                | 0.099 |
|                        | 3D       | 0.092             | 0.095                | 0.153 |
| 11.0 – 12.5            | 1D       | 0.142             | 0.128                | 0.198 |
|                        | 3D       | 0.249             | 0.254                | 0.303 |

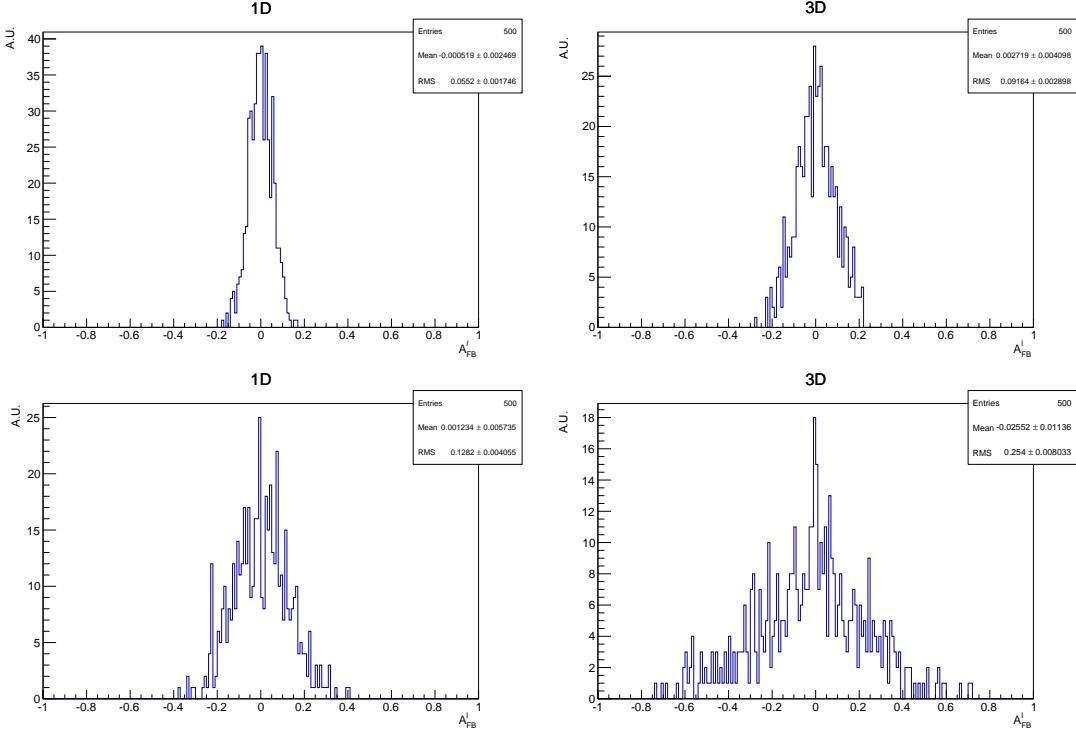


Figure 4.7: Values of the  $A_{FB}^\ell$  parameter observed in pseudo-experiments with input  $A_{FB}^\ell = 0$  using the 1D fit method (left) and the 3D one (right). Events are generated with parameters and statistics corresponding to what is observed in the highest statistics interval (top),  $15 - 20 \text{ GeV}^2/c^4$ , and in the lowest statistics one,  $11 - 12.5 \text{ GeV}^2/c^4$ .

## 4.5 Systematics uncertainties on angular observables

The following section describes the five main sources of systematic uncertainties that are considered for the angular observables measurement and, finally, results are reported in Sec. 4.7. Results are derived only for  $q^2$  intervals where the signal significance, shown in Tab. 3.6, is above 3 standard deviations. This includes all  $q^2$  intervals above the  $J/\psi$  resonance and the lowest  $q^2$  interval, where an increased yield is due to the presence of the photon pole.

### 4.5.1 Angular correlations

The angular acceptance is non-flat as a function of  $\cos \theta_\ell$  and  $\cos \theta_h$ . Therefore, while integrating the full angular distribution, terms that cancel with perfect efficiency

may remain and generate a bias in the final result. In order to deal with this effect simulated events are generated in a two-dimensional  $(\cos\theta_\ell, \cos\theta_h)$  space according to the theoretical distribution described by Eq. 4.15 multiplied by a two-dimensional efficiency function obtained from simulation. Then, one-dimensional projections are taken and fit using the default one-dimensional efficiency functions. The distributions of observed deviations from the generated value,  $\Delta x = x_{true} - x_{measured}$ , are approximately gaussian and their mean is non-zero by more than  $3\sigma$ . Therefore, the mean biases are taken as systematic uncertainties, which correspond to the absolute uncertainties  $\Delta A_{FB}^\ell = 0.032$ ,  $\Delta f_L = 0.028$ ,  $\Delta A_{FB}^h = 0.013$  independent of  $q^2$ .

#### 4.5.2 Resolution

The angular resolution could bias the observables measurement generating an asymmetric migration of events. This is especially important in the  $\cos\theta_h$  case, due to its worse resolution and considerably asymmetric distribution. Simulated experiments are used to assess this systematic. Events are generated according to the measured distributions including efficiencies. The generated events are then smeared by the angular resolution (gaussian smearing). To be conservative the case with biggest angular resolution, downstream candidates, is always used. Finally, the smeared and not-smeared distributions are fit with the same PDF. The average deviation from the default values are reported in Tab. 4.3 as a function of  $q^2$  and assigned as systematic uncertainties.

Table 4.3: Values of simulated  $\cos\theta_\ell$  and  $\cos\theta_h$  resolutions and systematic uncertainties on angular observables due to the finite resolution in bins of  $q^2$ .

| $q^2$ [GeV $^2/c^4$ ] | $\sigma_\ell$ | $\sigma_h$ | $\Delta A_{FB}^\ell$ | $\Delta f_L$ | $\Delta A_{FB}^h$ |
|-----------------------|---------------|------------|----------------------|--------------|-------------------|
| 0.1 – 2.0             | 0.0051        | 0.061      | 0.0011               | -0.0022      | -0.007            |
| 11.0 – 12.5           | 0.0055        | 0.067      | 0.0016               | -0.0051      | -0.013            |
| 15.0 – 16.0           | 0.0059        | 0.070      | 0.0006               | -0.0054      | -0.010            |
| 16.0 – 18.0           | 0.0064        | 0.070      | 0.0014               | -0.0077      | -0.010            |
| 18.0 – 20.0           | 0.0081        | 0.074      | 0.0014               | -0.0062      | -0.010            |
| 15.0 – 20.0           | 0.0066        | 0.072      | 0.0013               | -0.0076      | -0.011            |

### 4.5.3 Efficiency description

An imprecise determination of the reconstruction and selection efficiency can introduce an extra oddity and therefore bias the measurement. To asses this effect the kinematic re-weighting described in Sec. 3.3.2 is removed from the simulation and the efficiency is determined again. Simulated events are then fit using the same theoretical PDF and multiplied by the efficiency functions obtained with and without kinematical weights. As in the previous cases the average bias is taken as systematic uncertainty; results are shown in Tab. 4.4. Furthermore, the effect of the limited simulated statistics is taken into account and added to the systematic uncertainty.

Table 4.4: Values systematic uncertainties due to limited knowledge of the efficiency function on the three angular observables in bins of  $q^2$

| $q^2$ [ GeV $^2/c^4$ ] | $A_{\text{FB}}^\ell$ | $f_L$  | $A_{\text{FB}}^h$ |
|------------------------|----------------------|--------|-------------------|
| 0.1 – 2.0              | 0.0020               | 0.0440 | 0.0093            |
| 11.0 – 12.5            | 0.0069               | 0.0027 | 0.0069            |
| 15.0 – 16.0            | 0.0018               | 0.0046 | 0.0109            |
| 16.0 – 18.0            | 0.0012               | 0.0043 | 0.0159            |
| 18.0 – 20.0            | 0.0030               | 0.0017 | 0.0148            |
| 15.0 – 20.0            | 0.0002               | 0.0046 | 0.0138            |

Table 4.5: Values of systematic uncertainties due to the statistics of the simulated samples on the three angular observables in bins of  $q^2$ .

| $q^2$ [ GeV $^2/c^4$ ] | $A_{\text{FB}}^\ell$ | $f_L$   | $A_{\text{FB}}^h$ |
|------------------------|----------------------|---------|-------------------|
| 0.1 – 2.0              | 0.00151              | 0.00170 | 0.00213           |
| 11.0 – 12.5            | 0.00121              | 0.00154 | 0.00196           |
| 15.0 – 16.0            | 0.00004              | 0.00017 | 0.00103           |
| 16.0 – 18.0            | 0.00065              | 0.00246 | 0.00417           |
| 18.0 – 20.0            | 0.00023              | 0.00372 | 0.00162           |
| 15.0 – 20.0            | 0.00039              | 0.00091 | 0.00137           |

### 4.5.4 Background parameterisation

There is a certain degree of arbitrariness in the choice of a parameterisation for the background, especially for  $q^2$  intervals with low statistics. To asses possible biases

due to the choice of a specific PDF, simulated experiments are generated using the shapes obtained from fits to data and the same statistics as observed in data for each  $q^2$  interval. Each pseudo-experiment is fit with two models: the default one, a “line times efficiency” function and the efficiency function alone, corresponding to the assumption that background distributions are originally flat and only modified by the interaction with the detector. The average bias with respect to the default model is taken as systematic uncertainty; results are reported in Tab. 4.6.

Table 4.6: Values of systematic uncertainties due to the choice of background parameterisation in bins of  $q^2$ .

| $q^2$ [GeV $^2/c^4$ ] | $A_{FB}^\ell$ | $f_L$ | $A_{FB}^h$ |
|-----------------------|---------------|-------|------------|
| 0.1 – 2.0             | 0.003         | 0.049 | 0.053      |
| 11.0 – 12.5           | 0.045         | 0.034 | 0.035      |
| 15.0 – 16.0           | 0.010         | 0.038 | 0.026      |
| 16.0 – 18.0           | 0.026         | 0.036 | 0.022      |
| 18.0 – 20.0           | 0.011         | 0.031 | 0.025      |
| 15.0 – 20.0           | 0.007         | 0.014 | 0.017      |

#### 4.5.5 Polarisation

To study the effect of a non-zero  $\Lambda_b^0$  production polarisation simulated events are generated using the distributions given by Eqs. 4.12 and 4.14 as a function of the angle under study ( $\cos\theta_\ell$  or  $\cos\theta_h$ ) and  $\cos\theta$ , defined in Sec. 4.2, which is sensitive to polarisation. Similarly to the procedure used for the branching ratio measurement, events are generated varying the value of the polarisation within one standard deviation from the LHCb measurement [102]. As in the theoretical functions  $\cos\theta$  is always odd, it would always drop out when integrating over  $\theta$  in the case of perfect efficiency, yielding no bias by construction. Therefore, the generated distributions are also multiplied by the two-dimensional efficiency function. No significant bias is found.

## 4.6 $J/\psi$ cross-check

To validate the fitting procedure this is applied to the high statistics  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  sample. For this purpose events are selected with an additional requirement on the proton PID,  $\text{PID}_p > 10$ . This is needed to reduce the  $B^0 \rightarrow K_s^0 J/\psi$  background, which is particularly important for the hadronic side fit, since the  $K_s^0$  events are not distributed in a flat way in the  $\cos \theta_h$  variable and would therefore bias the fit. Figure 4.8 shows the invariant mass distributions after this requirement is applied, which can be compared with the ones in Fig. 3.12. After the PID cut there are 0.2% of  $K_s^0$  events left in the downstream sample and a fraction compatible with zero in the long sample. The signal model used for the angular fit to  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates is the same defined for the rare case and described in Sec. 4.4.2. For the background instead the higher statistics allows to leave more freedom to the fit. Therefore a second-order Chebyshev polynomial is used, where the two parameters are free to vary. As for the rare case the background fractions are gaussian-constrained to what found from the invariant mass fit. Figures 4.9 and 4.10 show fitted angular distributions for the  $J/\psi$  channel. The measured values of the observables are  $A_{\text{FB}}^\ell = -0.002^{+0.011}_{-0.011}$ ,  $A_{\text{FB}}^h = -0.402^{+0.010}_{-0.009}$  and  $f_L = 0.485^{+0.019}_{-0.020}$ , where the uncertainties are 68% Feldman-Cousins confidence intervals. The lepton side asymmetry is measured to be zero as expected for a tree level  $b \rightarrow c\bar{c}s$  process.

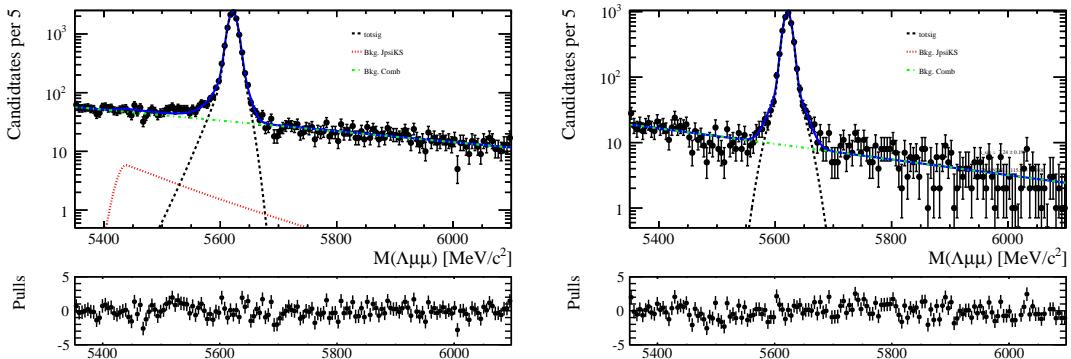


Figure 4.8: Invariant mass distribution of  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  downstream (left) and long (right) candidates with an extra proton PID cut to remove  $K_s^0$  background.

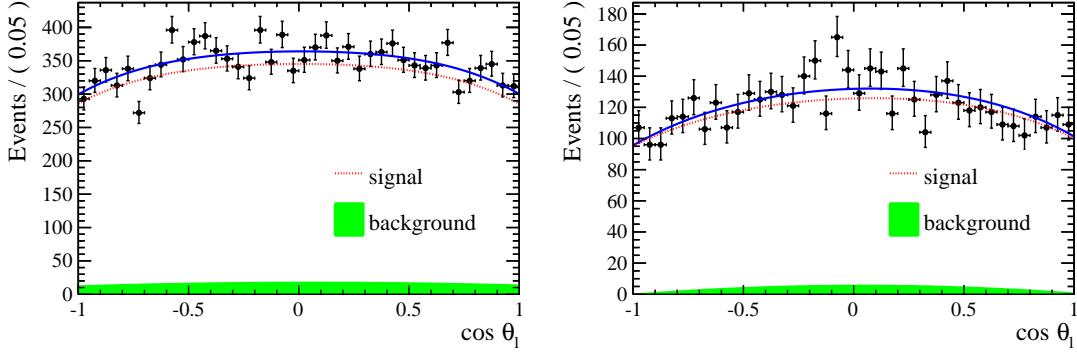


Figure 4.9: Fitted  $\cos \theta_\ell$  angular distribution for  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates reconstructed using downstream (left) and long (right) tracks.

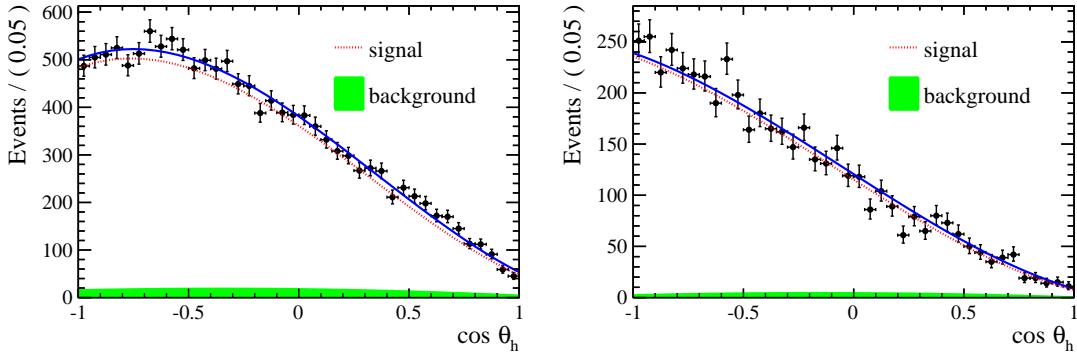


Figure 4.10: Fitted  $\cos \theta_h$  angular distribution for  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  candidates reconstructed using downstream (left) and long (right) tracks.

## 4.7 Results

Figures 4.11 and 4.12 show fits to the angular distributions for the  $15 - 20$   $\text{GeV}^2/c^4 q^2$  interval and Tab. 4.7 reports measured values of  $A_{\text{FB}}^\ell$ ,  $A_{\text{FB}}^h$  and  $f_L$  in all intervals. The asymmetries are also shown in Fig. 4.13 together with SM predictions obtained from Ref. [105]. The statistical uncertainties on these tables are obtained using the likelihood-ratio ordering method described in Sec. 4.4.1, where only one of the two observables is treated as the PoI at a time. The statistical uncertainties on  $A_{\text{FB}}^\ell$  and  $f_L$  are also reported in Fig. 4.14 as two-dimensional 68% confidence level regions, where the likelihood-ratio ordering method is applied by varying both observables at the same time and therefore taking correlations into account. Total systematic uncertainties correspond to the square root sum of the single considered sources.

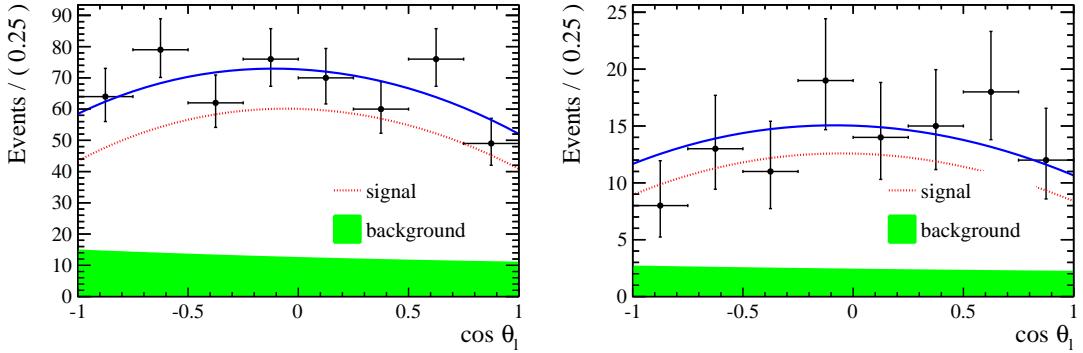


Figure 4.11: Fitted  $\cos \theta_\ell$  angular distributions for downstream (left) and long (right) candidates in the  $15 - 20 \text{ GeV}^2/c^4 q^2$  interval.

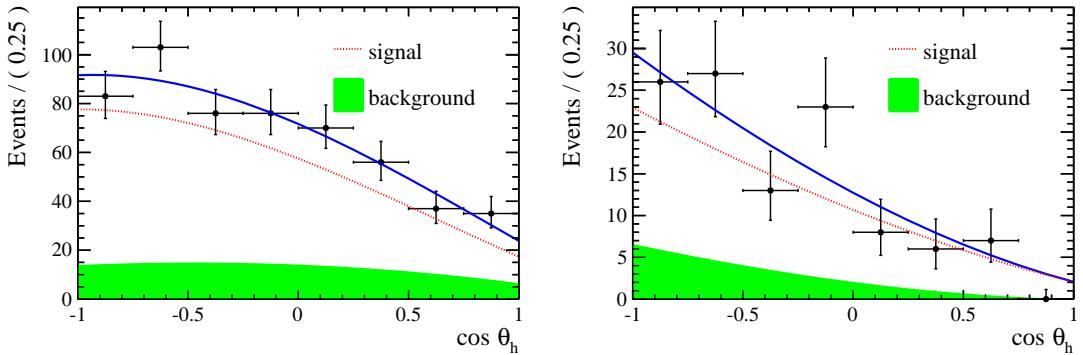


Figure 4.12: Fitted  $\cos \theta_h$  angular distributions for downstream (left) and long (right) candidates in the  $15 - 20 \text{ GeV}^2/c^4 q^2$  interval.

Table 4.7: Measured values of leptonic and hadronic angular observables; uncertainties are statistical and systematic.

| $q^2 [\text{GeV}^2/c^4]$ | $A_{\text{FB}}^\ell$             | $f_L$                           | $A_{\text{FB}}^h$                |
|--------------------------|----------------------------------|---------------------------------|----------------------------------|
| 0.1 – 2.0                | $0.37^{+0.37}_{-0.48} \pm 0.03$  | $0.56^{+0.23}_{-0.56} \pm 0.08$ | $-0.12^{+0.31}_{-0.28} \pm 0.15$ |
| 11.0 – 12.5              | $0.01^{+0.19}_{-0.18} \pm 0.06$  | $0.40^{+0.37}_{-0.36} \pm 0.06$ | $-0.50^{+0.10}_{-0.00} \pm 0.04$ |
| 15.0 – 16.0              | $-0.10^{+0.18}_{-0.16} \pm 0.03$ | $0.49^{+0.30}_{-0.30} \pm 0.05$ | $-0.19^{+0.14}_{-0.16} \pm 0.03$ |
| 16.0 – 18.0              | $-0.07^{+0.13}_{-0.12} \pm 0.04$ | $0.68^{+0.15}_{-0.21} \pm 0.05$ | $-0.44^{+0.10}_{-0.05} \pm 0.03$ |
| 18.0 – 20.0              | $0.01^{+0.15}_{-0.14} \pm 0.04$  | $0.62^{+0.24}_{-0.27} \pm 0.04$ | $-0.13^{+0.09}_{-0.12} \pm 0.03$ |
| 15.0 – 20.0              | $-0.05^{+0.09}_{-0.09} \pm 0.03$ | $0.61^{+0.11}_{-0.14} \pm 0.03$ | $-0.29^{+0.07}_{-0.07} \pm 0.03$ |

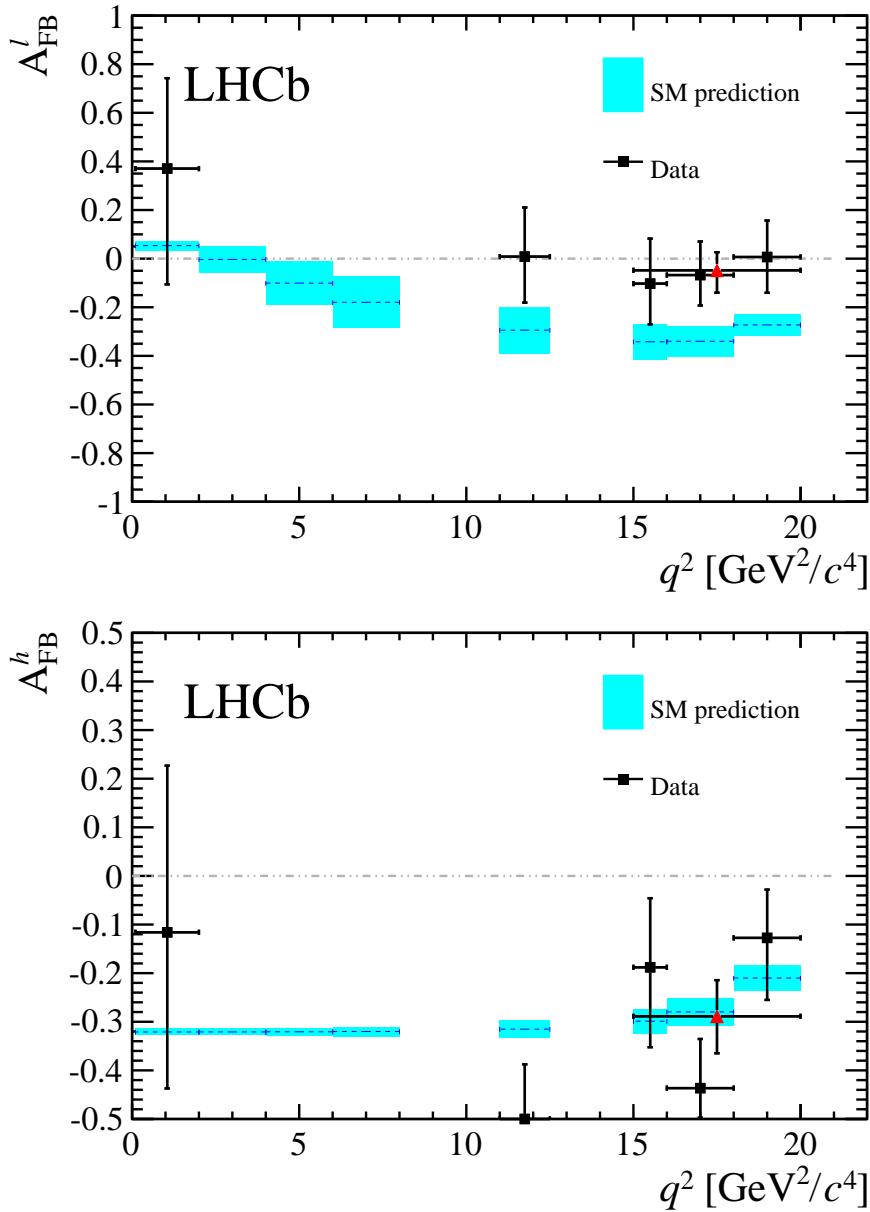


Figure 4.13: Measured values of the leptonic (top) and the hadronic (bottom) forward-backward asymmetries. Data points are only shown for  $q^2$  intervals where the signal yield is found to be statistically significant, see text for details. The (red) triangle represents the values for the  $15 < q^2 < 20$   $\text{GeV}^2/c^4$  integrated interval. Standard Model predictions are obtained from Ref. [112].

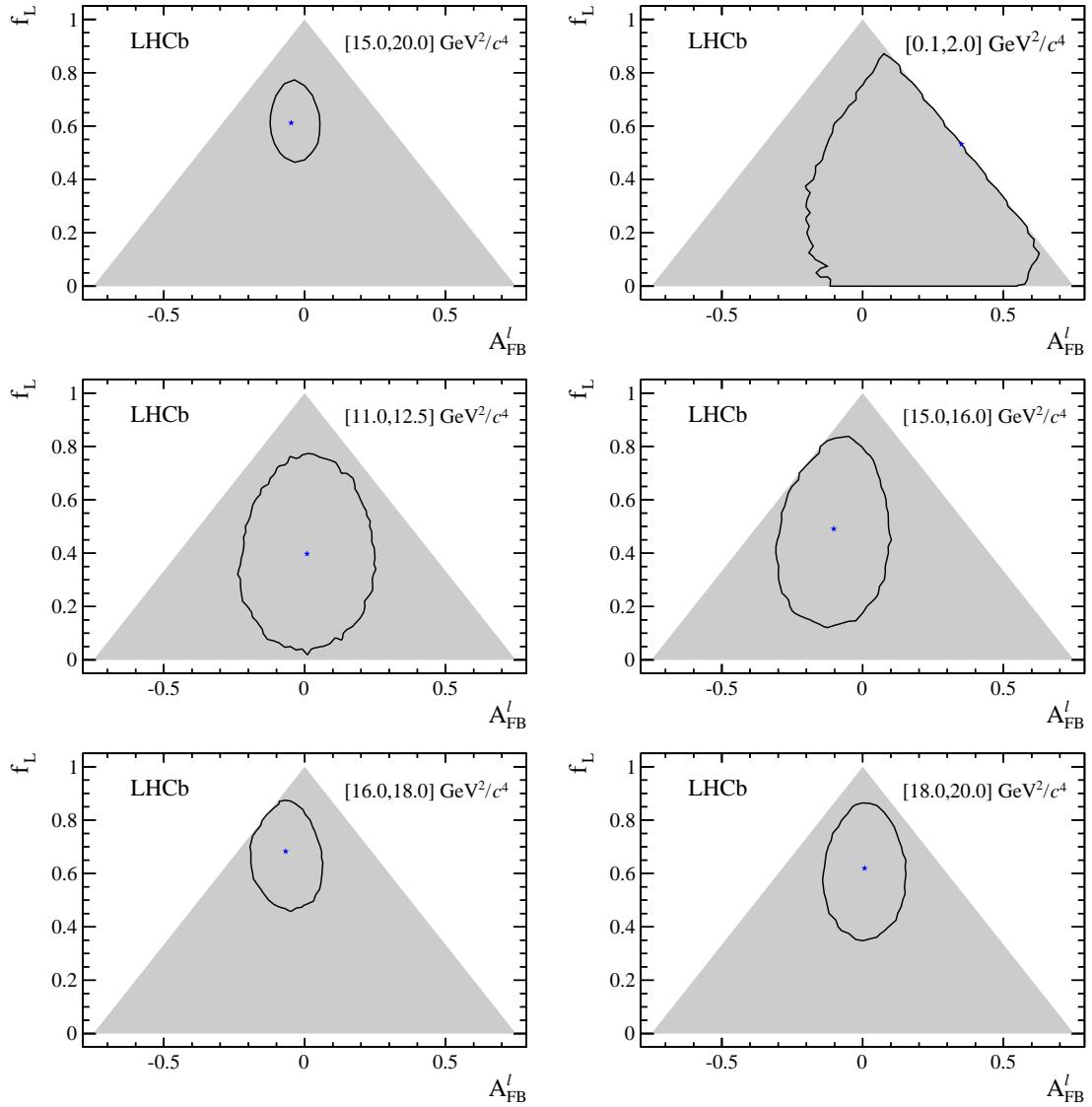


Figure 4.14: Two-dimensional 68% CL regions (black) as a function of  $A_{\text{FB}}^L$  and  $f_L$ . The shaded areas highlight the region in which the PDF is positive over the whole  $\cos \theta_\ell$  range. The best fit points are indicated by the (blue) stars.

# CHAPTER 5

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## Testing lepton flavour universality with $R_{K^{*0}}$

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Lepton Favour Universality (LFU) is the equality of the weak coupling constants for all leptons. FCNC processes, which are forbidden in the SM at tree level and happen only at loop level, are an ideal laboratory to study LFU as new physics contributing in the loops could break the flavour symmetry.

In this work  $b \rightarrow s\mu^+\mu^- (e^+e^-)$  decays are studied to test LFU between electrons and muons. In particular, the  $B^0$  meson semileptonic decays  $B^0 \rightarrow K^{*0}\ell^+\ell^-$  are considered. Figure 5.1 shows the possible Feynman diagrams producing such decays while Fig. 5.2 illustrates how these Feynman diagrams may include new particles. A series of recent LHCb measurements [31] points to a tension with SM predictions, which make these processes very interesting to better understand the nature of the discrepancy.

In order to exploit the sensitivity of loop diagrams, in 2004 Hiller and Kruger pro-

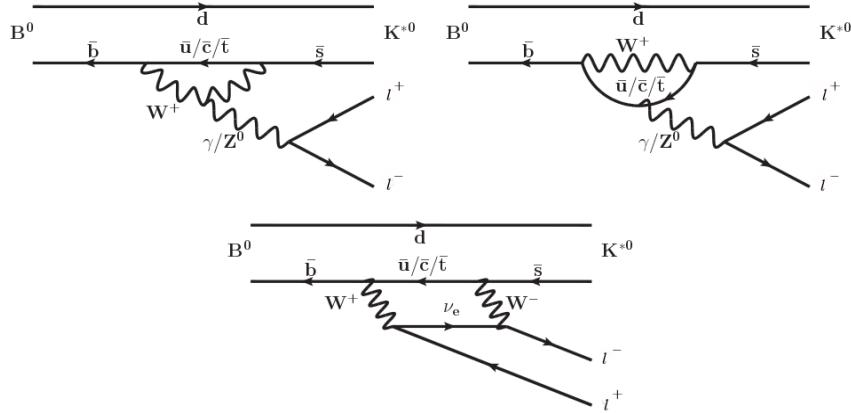


Figure 5.1: Loop diagrams producing  $B^0 \rightarrow K^{*0} \ell^+ \ell^-$  decays.

posed the measurement of the  $R_H$  ratio [113], defined as

$$R_H = \frac{\int_{4m_\mu^2}^{m_b} \frac{d\mathcal{B}(B^0 \rightarrow H \mu^+ \mu^-)}{dq^2} dq^2}{\int_{4m_\mu^2}^{m_b} \frac{d\mathcal{B}(B^0 \rightarrow H e^+ e^-)}{dq^2} dq^2}, \quad (5.1)$$

where  $H$  can be an inclusive state containing an  $s$  quark ( $X_s$ ) or an  $s$ -quark resonance like  $K$  or  $K^{*0}$ . In this quantity the differential branching fraction is integrated over the squared dilepton invariant mass,  $q^2$ , from  $q_{min}^2 = 4m_\mu^2$ , which is the threshold for the  $\mu\mu$  process, up to  $q_{max}^2 = m_b^2$ .

The advantage of using ratios of branching fractions as observables is that, in the theoretical prediction, hadronic uncertainties cancel out. Furthermore, experimentally, some of the systematic uncertainties on the ratios are reduced giving a better measurement. For example, what is measured is the number of  $\mu\mu$  and  $ee$  decays happening in a certain period of time. Then, the luminosity,  $\mathcal{L}$ , is used to obtain a cross section,  $\sigma$ , using  $R = \mathcal{L}\sigma$ , where  $R$  is the rate at which the decays occur. The luminosity measurement is usually a source of systematic uncertainty, but it appears on both sides of the ratio and therefore cancels out.

Since the SM does not distinguish between lepton flavours, the predicted value of the ratio is  $R_H = 1$ , under the assumption of massless leptons. Taking into account effects of order  $m_\mu^2/m_b^2$  Hiller and Kruger calculate that in the SM and in the full  $q^2$

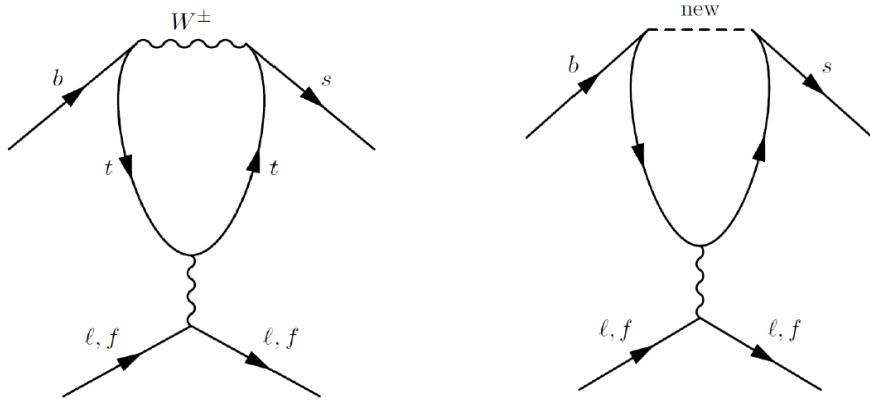


Figure 5.2: Example of penguin diagrams, on the left involving SM particles and on the right involving new possible particles.

range [113]:

$$R_{X_s} = 0.987 \pm 0.006, \quad (5.2)$$

$$R_K = 1.0000 \pm 0.0001, \quad (5.3)$$

$$R_{K^{*0}} = 0.991 \pm 0.002; \quad (5.4)$$

$$(5.5)$$

under the assumptions that:

- right-handed currents are negligible;
- (pseudo-)scalar couplings are proportional to the lepton mass;
- there are no CP-violating phases beyond the SM.

The measurement of the  $R_H$  ratios is of particular interest after the recent measurement of the branching fraction of the  $B_s^0 \rightarrow \mu^+ \mu^-$  decay [42], where no evidence of new physics was found. In fact the quantities  $(R_H - 1)$  and  $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$  remain proportional with

$$\frac{R_H - 1}{\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)} \sim 2 \cdot 10^{-5}. \quad (5.6)$$

A joint measurement of these two quantities can give much information and constrain MFV models. If  $R_H = 1$  and  $\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$  is close to the SM prediction as it is

measured to be this will allow to put strong constraints on extensions of the SM. If instead  $R_H > 1$  and the equation above is not verified, this would mean that one of the assumptions listed above are not verified, which can happen in some extensions of the SM as Super-Symmetric models with broken R-parity. A series of recent LHCb measurements [31] shows tensions with SM predictions, which makes it interesting to further investigate these processes.

## 5.1 Combining ratios

The full power of the  $R_H$  ratios in understanding new physics scenarios comes from their combinations. In Ref. [114] Hiller and Schmaltz propose the measurement of the double ratios,  $X_H = R_H/R_K$ , which not only can test LFU but also allow to disentangle the kind of new physics that lies behind. These ratios are in fact sensitive to FCNCs of right-handed currents. Furthermore, in Ref. [114] the study is extended to  $B_s^0$  decays such as  $B_s^0 \rightarrow \phi \ell^+ \ell^-$  and  $B_s^0 \rightarrow \eta \ell^+ \ell^-$ .

Parity and Lorentz invariance require that the Wilson Coefficients with left-handed chirality ( $C$ ) and their right-handed counterparts ( $C'$ ) appear in the decay amplitude of exclusive decays in determined combinations, e.g.

$$\begin{aligned} C + C' : & K, K_{\perp}^{*0}, \dots \\ C - C' : & K_0(1430), K_{\parallel}^{*0}, \dots \end{aligned} \tag{5.7}$$

where the labels for the  $K^{*0}$  meson represent its longitudinal (0), parallel ( $\parallel$ ) and perpendicular ( $\perp$ ) transversity components. The  $C$  contributions are universal to all decays and therefore  $X_H$  double ratios are sensitive to right-handed currents. In fact the  $R_H$  ratios can be expressed in terms of their deviation from unity as

$$\begin{aligned} R_K &\simeq 1 + \Delta_+, \\ R_{K_0(1430)} &\simeq 1 + \Delta_-, \\ R_{K^{*0}} &\simeq 1 + p(\Delta_- - \Delta_+) + \Delta_+, \end{aligned} \tag{5.8}$$

where the  $\Delta_{\pm}$  quantities are combinations of Wilson coefficients described in Eq. 10 of Ref. [114] and the parameter  $p$  is the polarisation of  $K^{*0}$  that in Ref. [114] is determined to be close to 1 simplifying the formula to  $R_{K^{*0}} \simeq 1 + \Delta_-$ . In particular one can observe the following correlations:

- $R_K < 1$ , as it is measured to be, and  $X_{K^{*0}} > 1$  points to dominant BSM contributions into  $C_{LR}$  (see definition in Sec. 1.5.2);
- a SM like  $R_K \sim 1$  together with  $X_{K^{*0}} \neq 1$  requires BSM with  $C_{LL} + C_{RL} \simeq 0$ ;
- $R_K \neq 1$  and  $X_{K^{*0}} \simeq 1$  corresponds to new physics in  $C_{LL}$ .

## 5.2 Experimental status

The  $R_K$  and  $R_{K^{*0}}$  ratios have been measured at the B-factories [115, 116], and  $R_K$  has been recently measured also at LHCb [117], which represents the most precise measurement to date; measured values are summarised in Tab. 5.1. The LHCb measurement manifests a  $2.6\sigma$  deviation from the SM prediction. This is particularly interesting as this discrepancy can be explained with a new physics contribution in  $C_9$  which also explains other existing tensions [53, 48, 54]. It is also worth mentioning the measurement of the  $\mathcal{B}(\bar{B}^0 \rightarrow D^{*+}\tau^-\bar{\nu}_\tau)/\mathcal{B}(\bar{B}^0 \rightarrow D^{*+}\mu^-\bar{\nu}_\mu)$  ratio which probes LFU and was measured to be  $2.1\sigma$  larger than the value expected from the assumption of lepton universality in the SM [118]. By profiting of the large dataset collected during Run-I, the LHCb experiment is expected to reduce the uncertainty on  $R_{K^{*0}}$  by at least a factor of 2 with respect to the B-factories.

Table 5.1: Experimental status of the  $R_{K^{(*)}}$  measurements.

| Ratio        | Belle                    | BaBar                            | LHCb                                |
|--------------|--------------------------|----------------------------------|-------------------------------------|
| $R_K$        | $1.06 \pm 0.48 \pm 0.05$ | $1.38^{+0.39+0.06}_{-0.41-0.07}$ | $0.745^{+0.090}_{-0.074} \pm 0.036$ |
| $R_{K^{*0}}$ | $0.93 \pm 0.46 \pm 0.12$ | $0.98^{+0.30+0.08}_{-0.31-0.08}$ | —                                   |

## 5.3 Analysis strategy

The aim of the analysis in this chapter is to measure the  $R_{K^{*0}}$  ratio using  $pp$  collision data collected by the LHCb detector in 2011 and 2012, corresponding to  $3 \text{ fb}^{-1}$  of integrated luminosity. The  $B^0 \rightarrow K^{*0}\mu^+\mu^-$  and  $B^0 \rightarrow K^{*0}e^+e^-$ , “rare channels”, are reconstructed via the  $K^{*0}$  decay into a kaon and a pion with opposite charges.

The analysis has to separate signal candidates from background candidates which have similar observed properties. The selection presented in Sec. 5.6 aims to maximise the yield while minimising the background contamination. Two types of backgrounds are identified: “peaking background” and “combinatorial background”. The first comes from the mis-reconstruction of other decays or from partially reconstructed events. This type of background, because its specific kinematic properties, usually peaks in some variable, such as the invariant mass of all final particles. Therefore these candidates can be removed using specific cuts. The combinatorial background instead comes from the random combination of particles and can be lowered selecting candidates with good-quality tracks and vertices.

To further reduce the systematic uncertainties the measurement is performed as the double ratio

$$R_{K^{*0}} = \frac{N_{B^0 \rightarrow K^{*0}\mu^+\mu^-}}{N_{B^0 \rightarrow K^{*0}J/\psi \rightarrow \mu^+\mu^-}} \cdot \frac{N_{B^0 \rightarrow K^{*0}J/\psi \rightarrow e^+e^-}}{N_{B^0 \rightarrow K^{*0}e^+e^-}} \cdot \frac{\varepsilon_{B^0 \rightarrow K^{*0}J/\psi \rightarrow \mu^+\mu^-}}{\varepsilon_{B^0 \rightarrow K^{*0}\mu^+\mu^-}} \cdot \frac{\varepsilon_{B^0 \rightarrow K^{*0}e^+e^-}}{\varepsilon_{B^0 \rightarrow K^{*0}J/\psi \rightarrow e^+e^-}}, \quad (5.9)$$

where decays reaching the same final states as the rare channels via a  $J/\psi$  resonance,  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+\ell^-)$ , also referred to as “charmonium” or “resonant” channels, are used as control samples. These decays are distinguished from the rare channel using the invariant mass of the dilepton pair. As new physics is expected not to affect tree level  $b \rightarrow c\bar{c}s$  processes the ratio between the  $J/\psi$  channels,  $r_{J/\psi}$ , is 1 and therefore  $R'_{K^{*0}} = R_{K^{*0}} \cdot r_{J/\psi} = R_{K^{*0}}$ . On the other hand using the relative efficiencies between the rare and resonant channels allows to cancel out many systematic effects resulting in a better control of systematic uncertainties.

For brevity, the rare channels will also be denoted as “ $\ell\ell$ ”, or specifically “ $ee$ ” and “ $\mu\mu$ ”, and the resonant channels as “ $J/\psi(\ell\ell)$ ”, or “ $J/\psi(ee)$ ” and “ $J/\psi(\mu\mu)$ ”.

## 5.4 Dilepton invariant mass intervals

Three  $q^2$  intervals are considered in this work:

- the “low- $q^2$ ” region between 0.0004 and 1.1  $\text{GeV}^2/c^4$ , where the  $b \rightarrow s\ell^+\ell^-$  process is dominated by the photon pole;
- the “central- $q^2$ ” region, [1.1,6.0]  $\text{GeV}^2/c^4$ ;
- the “high- $q^2$ ” region, above 15  $\text{GeV}^2/c^4$ .

The central- $q^2$  region is the most interesting place to look for new physics. In fact, at low  $q^2$  values, below 1  $\text{GeV}^2/c^4$  the photon pole dominates leaving little space for new physics to be found. The choice of the lower limit of the low- $q^2$  interval is driven by the need to reject the background due to the  $B^0 \rightarrow K^{*0}\gamma$  decay where the photon converts into electrons in the material. The lower bound of the central interval is set at 1.1  $\text{GeV}^2/c^4$ , in order to exclude the contribution from  $\phi \rightarrow \ell^+\ell^-$  decays, that can dilute new physics effects, while the upper bound is chosen to be sufficiently far away from the  $J/\psi$  radiative tail, where predictions cannot be cleanly obtained. The 6 – 15  $\text{GeV}^2/c^4$  region is characterised by the presence of the narrow peaks of the  $J/\psi$  and  $\psi(2S)$  resonances. The lower bound of the high- $q^2$  region, where the signal in the electron channel is still unobserved, is chosen to be sufficiently far from the  $\psi(2S)$  resonance. Rare and normalisation channels are selected depending on the  $q^2$  interval they fall into (for details see Sec. 5.6).

### 5.4.1 Control channels

Beyond the normalisation channels,  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-/\mu^+\mu^-)$ , extra-control channels are used to perform cross-checks and better constrain some of the background components in the electron fit; in particular,  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$ , also denoted as “ $\gamma(ee)$ ”, and  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$ , also denoted as “ $\psi(2S)(ee)$ ”. All the normalisation and control channels are distinguished depending on the  $q^2$  interval they fall into (for details see Sec. 5.6).

## 5.5 Data samples and simulation

Simulated samples are used to study the properties of backgrounds, determine efficiencies and to train a multivariate classifier. The hard interactions are generated with PYTHIA8 hadronic particles are decayed using EVTGEN and, finally, propagated into the detector using GEANT4 and reconstructed with the same software used for data. Samples are generated with both 2011 and 2012, magnet up and down conditions and are combined in the right proportions, according to the luminosities registered on data. The next section describes the corrections applied to the simulation to obtain a better description of data.

### 5.5.1 Data-simulation corrections

Since the multivariate classifier training (see Sec. 5.6.6) and the calculation of most of the efficiency components (see Sec. 5.8) are obtained from the study of simulated events it is important to verify that the simulation provides a reliable reproduction of the data. In particular it is important to match data and Monte Carlo in the kinematics of the final particles and the occupancy of the detector. The kinematics of the decays is characterised by the transverse momentum spectrum of the  $B^0$ . Discrepancies in this distribution cause also the spectra of the final particles to differ

from data and affect the efficiency determination as its value often depends on the momentum of the final particles. The occupancy of the detector is relevant as it is correlated to the invariant mass shape of the signal because of the addition of energy clusters in the electromagnetic calorimeter, which affects the electron's momenta especially when bremsstrahlung photons are emitted before the magnet. The hit multiplicity in the SPD detector is a proxy for the detector occupancy. Since it is important that these quantities are well modelled, the simulation is reweighted so that their distributions in data and simulation match. The weight is calculated using resonant  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+\ell^-)$  candidates, for which the signal peak is already visible in data after pre-selection (see Sec. 5.6). However, the data still includes a high level of background and distributions cannot be directly compared. The  $\text{\texttt{sPlot}}$  technique [69] is used to statistically subtract the background from data and obtain pure signal distributions using the invariant mass as the control variable. Figure 5.3 shows fits to the 4-body invariant mass of candidates after pre-selection. Data and simulation are then compared and the ratio between the two distributions is used to reweight the simulation. The discrepancy in the SPD hits multiplicity is solved as a first step and then the  $B^0$  transverse momentum distributions are compared between data and simulation reweighted for the SPD multiplicity only. Distributions of  $B^0$  transverse momentum and SPD multiplicity are reported in Fig. 5.4 and ratios of these distributions, which are used to reweight the simulation, are reported in Fig. 5.5. The weights for the SPD multiplicity are calculated separately for 2011 and 2012 events, because distributions are significantly different in the two years. The binnings are chosen to have approximately the same number of events in each bin to limit fluctuations. Further corrections are made by reweighting the simulation for PID efficiency using the `PIDCalib` package as described in Sec. 5.8.3 and, finally,  $ee$  samples are also reweighted for L0 trigger efficiency as described in Sec. 5.8.4. Weights are always applied throughout unless specified.

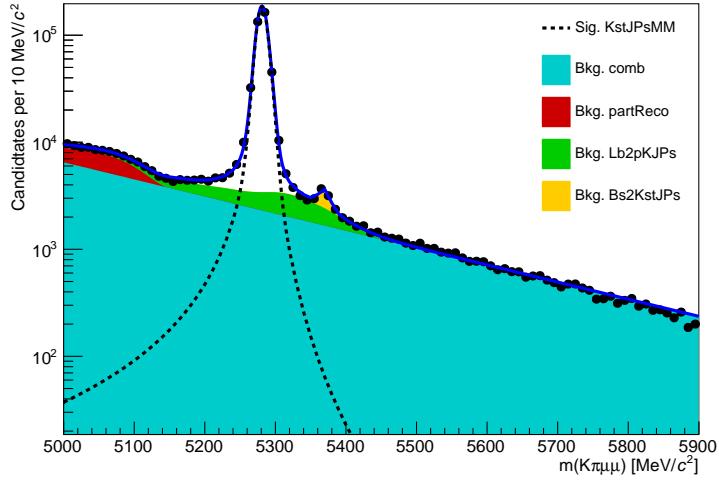


Figure 5.3: Fitted 4-body invariant mass distributions of muonic resonant candidates used to obtain  ${}_s\mathcal{W}$ eights.

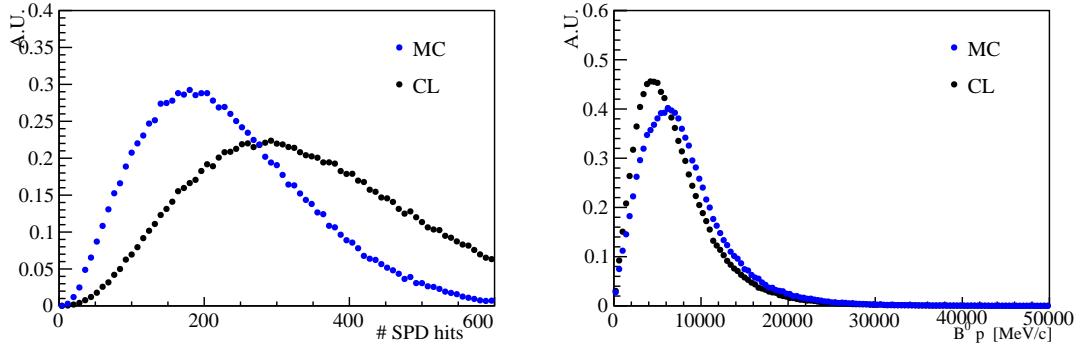


Figure 5.4: Distributions of number of SPD hits (left) and  $B^0$  transverse momentum (right) in data and MC.

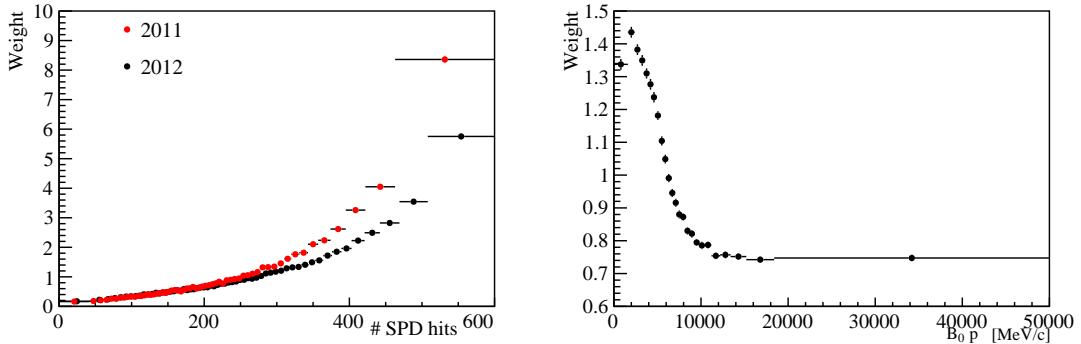


Figure 5.5: Ratios of simulated over real data distributions used to correct the simulation as a function of the number of SPD hits (left) and the  $B^0$  transverse momentum (right).

## 5.6 Selection

The selection process, described in this section, is divided into several steps:

- first of all candidates have to fall into the detector acceptance, produce hits and be selected on the basis of quality features, such as  $\chi^2$  of tracks and vertices and basic kinematic cuts. This stage is called “stripping”. Furthermore, it is required that the events are triggered by specific trigger lines and cuts are applied to remove backgrounds from specific decays. All these first three steps are referred to as “pre-selection”;
- secondly, particle identification requirements are applied to remove part of misreconstructed background and clear the way for the last step;
- in the final step a neural network is used to remove combinatorial background. Furthermore, for the electron channels, which are more challenging, the kinematic structure of the decays is also used to improve the samples’ purity.

In order to identify the  $J/\psi(\mu\mu)$  candidates a dimuon invariant mass interval of 100 MeV/ $c^2$  around the nominal  $J/\psi$  peak [2] is selected. On the other hand it is not possible to use a narrow interval around  $J/\psi(ee)$  mass peak as the invariant mass distribution is characterised by a long radiative tail at low masses due to bremsstrahlung radiation. Furthermore, a requirement on  $m(ee)$  would distort the 4-body  $m(K\pi ee)$  mass distribution which is not advisable as is important to be able to fit a wide mass range in order to constrain the backgrounds. For these reasons the interval to select  $J/\psi(ee)$  candidates is chosen to go as low as possible in  $q^2$  without overlapping with the rare channel interval. Candidates are therefore identified as  $J/\psi(ee)$  if they fall in the  $q^2$  interval  $6 < q^2 < 11$  GeV $^2/c^4$ . Similarly, candidates are identified as  $\psi(2S)(ee)$  if they fall into  $11 < q^2 < 15$  GeV $^2/c^4$  and  $\gamma(ee)$  if they fall into  $q^2 < 0.004$  GeV $^2/c^4$ . Table 5.2 summarises the requirements used to distinguish samples corresponding to different decay channels. Figure 5.6 shows two-dimensional distributions of  $q^2$  versus the 4-body invariant mass for candidates passing the full

Table 5.2: Summary of the channel categories.

| Type            | Sample                                                                   | $q^2$                                                   |
|-----------------|--------------------------------------------------------------------------|---------------------------------------------------------|
| $\mu\mu$        | $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ (low)                               | $0.0004 < q^2 < 1.1 \text{ GeV}^2/c^4$                  |
|                 | $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ (central)                           | $1.1 < q^2 < 6 \text{ GeV}^2/c^4$                       |
|                 | $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ (high)                              | $q^2 > 15 \text{ GeV}^2/c^4$                            |
|                 | $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+ \mu^-) (m(K\pi\mu\mu))$ | $ m_{\mu\mu} - m_{J/\psi}^{PDG}  < 100 \text{ MeV}/c^2$ |
| $ee$            | $B^0 \rightarrow K^{*0} e^+ e^-$ (low)                                   | $0.0004 < q^2 < 1.1 \text{ GeV}^2/c^4$                  |
|                 | $B^0 \rightarrow K^{*0} e^+ e^-$ (central)                               | $1.1 < q^2 < 6 \text{ GeV}^2/c^4$                       |
|                 | $B^0 \rightarrow K^{*0} e^+ e^-$ (high)                                  | $q^2 > 15 \text{ GeV}^2/c^4$                            |
|                 | $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+ e^-) (m(K\pi ee))$        | $6 < q^2 < 11 \text{ GeV}^2/c^4$                        |
| Control samples |                                                                          |                                                         |
|                 | $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+ e^-) (m(K\pi ee))$        | $q^2 < 0.0004 \text{ GeV}^2/c^4$                        |
|                 | $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+ e^-) (m(K\pi ee))$        | $6 < q^2 < 11 \text{ GeV}^2/c^4$                        |
|                 | $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+ e^-) (m(K\pi ee))$      | $11 < q^2 < 15 \text{ GeV}^2/c^4$                       |

selection. Horizontal bands can be clearly seen at  $q^2$  values corresponding to the  $J/\psi$  and  $\psi(2S)$  resonances. On the plot for muons it is also evident a vertical band which corresponds to the rare decay.

### 5.6.1 Trigger and Stripping

Events are triggered for the  $\mu\mu$  and the  $ee$  channels by the trigger lines reported in Tab. 5.3, where the logical *and* of L0, HLT1 and HLT2 lines is required and the logical *or* of the lines on the same level. The candidates are required to be triggered-on-signal (TOS) for most of the stages, namely it is required for the particle which triggered to be one of the particles used to build the signal candidates. Only for `LOGlobal`, used in the electron case, a trigger-independent-of-signal (TIS) is required. The `L0Muon` trigger requires hits in the muon detector, while `L0Electron` and `L0Hadron` use information from the calorimeters; `HLT1TrackAllL0` adds information from the trackers and triggers if the L0 decision is confirmed; finally, `HLT2Topo[2,3]BodyBBDT` uses a full reconstruction of the event and a neural network trained on candidates with a specific topology in order to detect specific decay structures.

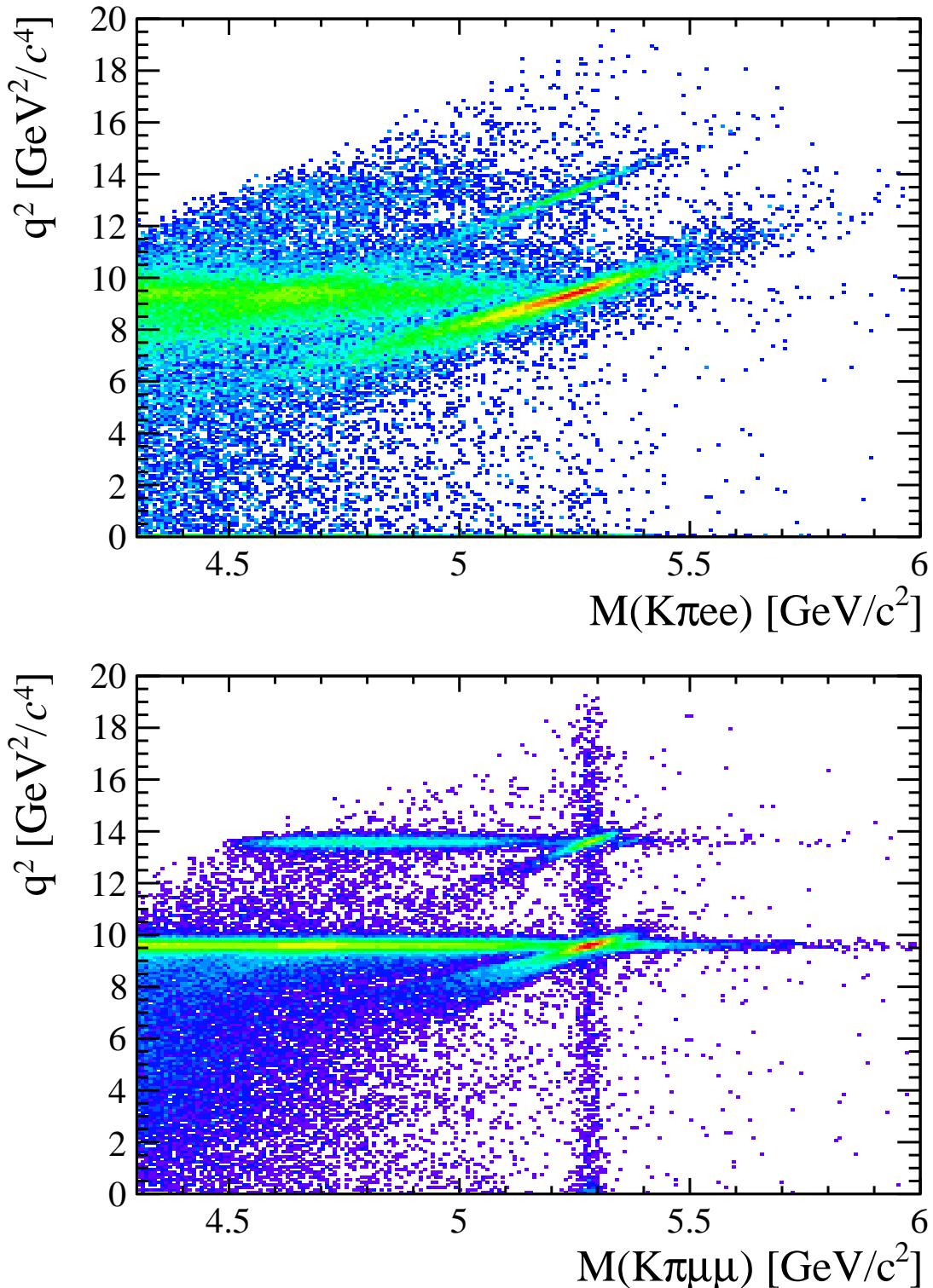


Figure 5.6: Two-dimensional distributions of  $q^2$  versus 4-body  $m(K\pi\ell\ell)$  invariant mass for the electron (top) and muon (bottom) channels in 2012 data.

Table 5.3: Summary of the trigger lines used to select the  $\mu\mu$  and the  $ee$  channels. Where not explicitly indicated, the lines are required to be TOS.

| $\mu\mu$ candidates                                                            | $ee$ candidates                                 |
|--------------------------------------------------------------------------------|-------------------------------------------------|
| L0Muon                                                                         | L0Electron<br>L0Hadron<br>L0Global (TIS)        |
| Hlt1TrackAllL0<br>Hlt1TrackMuon                                                | Hlt1TrackAllL0                                  |
| Hlt2Topo[2,4]BodyBBDT<br>Hlt2TopoMu[2,4]BodyBBDT<br>Hlt2DiMuonDetachedDecision | Hlt2Topo[2,4]BodyBBDT<br>Hlt2TopoE[2,4]BodyBBDT |

For the electron channels the L0 lines have different properties, therefore the analysis is performed separately for three categories of events, depending on the L0 trigger that fired them. These categories are defined to be exclusive in the following way:

- **L0E**: events triggered by at least one of the electrons in the signal candidate (`L0Electron_TOS`);
- **L0H**: events triggered by at least one of the hadrons in the signal candidate and not by `L0Electron` (`L0Hadron_TOS && !L0Electron_TOS`);
- **L0I**: events triggered by particles not in the signal candidate and not by the previous cases (`L0Global_TIS && !(L0Electron_TOS || L0Hadron_TOS)`).

The majority of the selected events falls in the L0E category, while the L0H category is more efficient at low  $q^2$  were the  $K^{*0}$  has more momentum. Because L0I is defined to be independent of the signal candidate, the corresponding signal efficiency is the same in the rare and resonant cases and cancels out in their ratio.

Candidates are then required to pass the kinematic and quality cuts summarised in Tab. 5.4. The meaning of the variables in the table was already explained in Sec. 3.4. Loose PID cuts are applied in preselection to limit the size of the samples, while tighter cuts are applied in a second stage. A large mass window is kept around the  $B^0$  peak in order to be able to use the sideband to train the multivariate

Table 5.4: Summary of stripping requirements.

| Particle   | Requirements                                                                                                                                                                    |
|------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $\pi$      | $\chi^2_{\text{IP}}(\text{primary}) > 9$                                                                                                                                        |
| K          | $\text{PID}_K > -5$<br>$\chi^2_{\text{IP}}(\text{primary}) > 9$<br><b>hasRICH</b>                                                                                               |
| $K^{*0}$   | $p_T > 500 \text{ MeV}/c$<br>$ m_{K\pi} - m_{K^{*0}}^{\text{PDG}}  < 300 \text{ MeV}/c^2$<br>$\chi^2_{\text{IP}}(\text{primary}) > 9$<br>Origin vertex $\chi^2/\text{ndf} < 25$ |
| $\mu$      | $p_T > 300 \text{ MeV}/c$<br>$\chi^2_{\text{IP}}(\text{primary}) > 9$<br><b>isMuon</b>                                                                                          |
| e          | $p_T > 300 \text{ MeV}/c$<br>$\chi^2_{\text{IP}}(\text{primary}) > 9$<br><b>hasCalo</b><br>$\text{PID}_e > 0$                                                                   |
| $\ell\ell$ | $m_{\ell\ell} < 5500 \text{ MeV}/c^2$<br>End vertex $\chi^2/\text{ndf} < 9$<br>Origin vertex $\chi^2$ separation $> 16$                                                         |
| $B^0$      | $\text{DIRA} > 0.9995$<br>End vertex $\chi^2/\text{ndf} < 9$<br>$\chi^2_{\text{IP}}(\text{primary}) < 25$<br>Primary vertex $\chi^2$ separation $> 100$                         |

classifier and to constrain the backgrounds. Track and vertex quality cuts are also applied using the  $\chi^2_{track}/\text{ndf}$ , `GhostProb`, and  $\chi^2_{vtx}/\text{ndf}$  variables. The `GhostProb` quantity describes the probability of a track being fake. By construction cutting at 0.4 removes  $(1 - 0.4) \cdot 100 = 60\%$  of fake tracks. For details about the definition of the variables used see Ref. [119].

### 5.6.2 PID

After pre-selection there still are high levels of background. In particular, as the ID of kaons and pions are not constrained, the samples still contain both ID combinations for most candidates, therefore tighter PID requirements are applied. In the LHCb analysis framework the particle identification probability can be quantified using the “`ProbNN`” variables [120]. These variables are the output of a neural network which takes as input information from the calorimeters, the RICH detectors the muon system and the tracking system. Unlike the DLL variables (see Sec. 2.8) the `ProbNN` are bound from 0 to 1 and can be directly interpreted as probabilities; *e.g.* `ProbNNk` corresponds to the probability for a reconstructed particle to be a kaon.

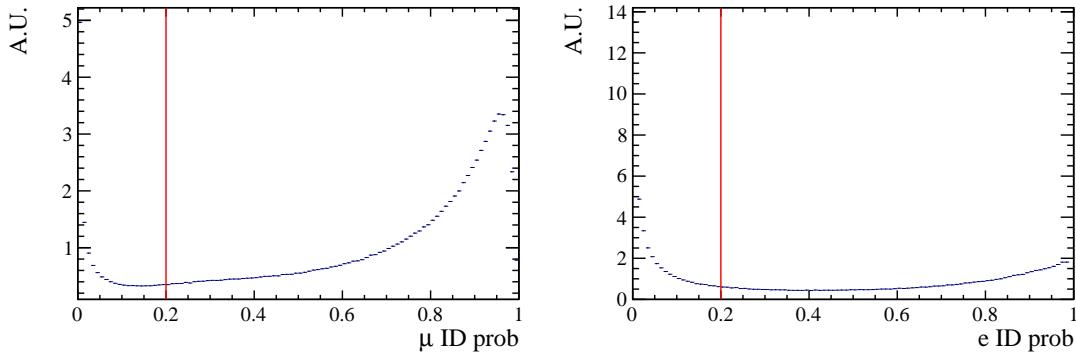


Figure 5.7: Correct ID probability distributions for muons (left) and electron (right) in 2012 data.

Figure 5.7 shows correct ID probability distributions for electrons and muons in data, while Fig. 5.8 shows the probabilities of correct identification and mis-identification of kaons and pions in a two-dimensional plane. These plots are characterised by clear peaks at maximal ID probability and minimal mis-ID probability, corresponding

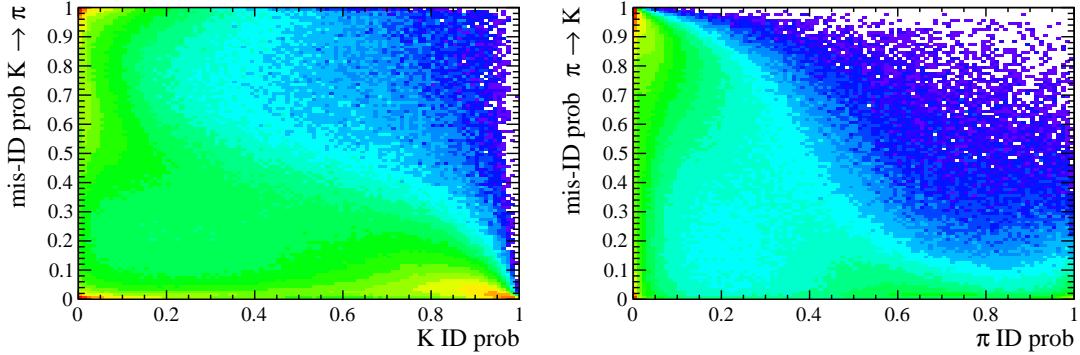


Figure 5.8: On the horizontal axis of these plots is shown the correct ID probabilities for kaons (left) and pions (right), while the vertical axis show the mis-ID probability.

to particles to which a well defined identification can be assigned. In order to maximise the power of the PID requirements probabilities of correct ID and mis-ID are combined using the following cuts:

$$\begin{aligned} \pi &\rightarrow \text{ProbNNpi} \times (1 - \text{ProbNNk}) \times (1 - \text{ProbNNp}) > 0.1 \\ K &\rightarrow \text{ProbNNk} \times (1 - \text{ProbNNp}) > 0.05 \\ \mu &\rightarrow \min(\text{ProbNNmu}, \text{ProbNNmu}) > 0.2 \\ e &\rightarrow \min(\text{ProbNNe}, \text{ProbNNe}) > 0.2 \end{aligned}$$

In the first formula, for example, `ProbNNpi` is the probability of correctly identifying the pion as a pion, while `ProbNNk` is the probability of mistaking it for a kaon. Therefore by maximising the quantity “`ProbNNpi` × (1 - `ProbNNk`)”, one can maximise the correct ID probability and minimise at the same time the mis-ID probability.

### 5.6.3 Peaking backgrounds

Backgrounds due to specific decays usually peak in some variable because of their distinctive kinematic properties and therefore they can be removed without significant efficiency loss for the signal. The following sections describe the main sources of peaking background. The same requirements are applied to the muon and electron channels, unless specified differently.

### 5.6.3.1 Charmonium vetoes

Charmonium resonances such as  $J/\psi$  and  $\psi(2S)$  peak in  $q^2$ . The choice of  $q^2$  binning described in Sec. 5.4 constitutes a natural veto for these decays. Simulated events are used to check if resonant candidates leak inside the  $q^2$  intervals chosen for the rare channel analysis. For the muonic channels the leakage is negligible as the peaks are sharper due to a better resolution and muons emit fewer bremsstrahlung photons, resulting in shorter radiative tails. The electron channels are instead characterised by a worse resolution and at the same time electrons can radiate several bremsstrahlung photons, yielding long tails at low  $q^2$ . Analysing simulated events it was found that 1.3 – 2% (depending on the trigger category) of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  candidates leak into the  $1.1 < q^2 < 6$   $\text{GeV}^2/c^4$  interval and 1.8% of  $\psi(2S)$  events leak above 15  $\text{GeV}^2/c^4$ . The contribution from these candidates is modelled in the fit.

### 5.6.3.2 $\phi$ veto

It can happen that a kaon from the decay  $B_s \rightarrow \phi\ell^+\ell^-$ , where the  $\phi$  decays in two kaons, is mis-identified as a pion and therefore causes the  $\phi$  to be reconstructed as a  $K^{*0}$ . This results in a candidate with a value of  $m(K\pi)$  that is less than the nominal  $K^{*0}$  mass but still high enough to pass the selection requirements. Figure 5.9 shows the plot of  $m(K\pi)$  versus  $m(K\pi\mu\mu)$ , where the kaon mass hypothesis is assigned to the pion. A peak can clearly be seen around the  $(B_s^0, \phi)$  mass. To remove this background only candidates with  $m_{K(\pi \rightarrow K)} > 1040$   $\text{MeV}/c^2$  are selected. This results in a  $\sim 98\%$  background rejection while keeping a  $\sim 99\%$  signal efficiency.  $B_s^0$  decays such as  $B_s \rightarrow \phi K^{*0}$  could also constitute a background when  $\phi$  decays into two leptons but the branching fraction of this decay is small compared to the previous case. Furthermore, this contribution is already taken into account by the choice of the  $q^2$  intervals (see Sec. 5.4).

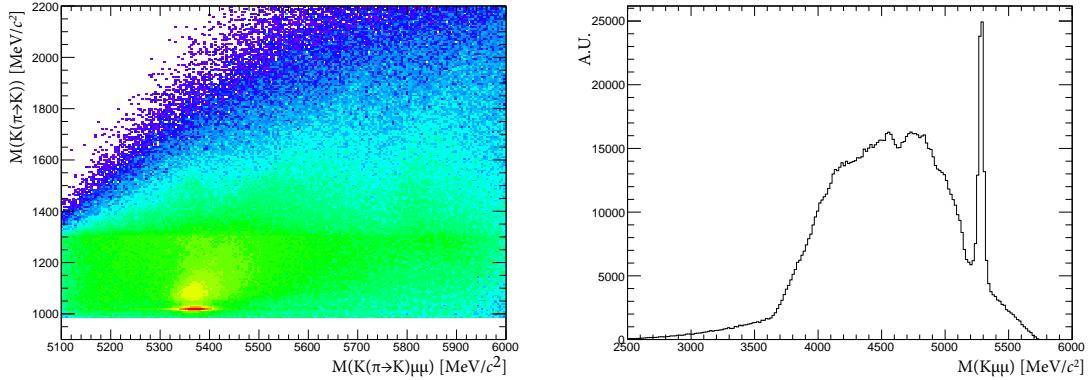


Figure 5.9: (left) Distribution of data candidates as a function of the variables ( $m_{K(\pi \rightarrow K)}$ ) and ( $m_{K(\pi \rightarrow K)\mu\mu}$ ), where  $\pi \rightarrow K$  means that the kaon mass hypothesis is given to the pion. (right) The invariant mass distribution of the three-body system ( $K\mu\mu$ ), where the peak due to the  $B^+ \rightarrow K^+\mu^+\mu^-$  decay is visible.

#### 5.6.3.3 $B^+ \rightarrow K^+\ell^+\ell^-$ plus a random pion

$B^+ \rightarrow K^+\ell^+\ell^-$  decays can contaminate the upper  $B^0$  mass sideband if they are combined with a soft pion from somewhere else in the event and therefore reconstructed as a  $B^0$  decay. Similarly a kaon can be mis-identified as a pion and combined with an other kaon in the event. Figure 5.9 shows the invariant mass distribution of the three-body ( $K\mu^+\mu^-$ ) system,  $m(K\mu\mu)$ . This is characterised by a narrow peak at the  $B^+$  mass. Since these candidates have  $m(K\pi\ell\ell) > 5380$  MeV/ $c^2$  there is no contribution under the  $B^0$  peak, but they can cause problems when using sidebands candidates to train the neural network. An effective veto for this decay was found to be  $\max(m_{K\ell\ell}, m_{(K \rightarrow \pi)\ell\ell}) < 5100$  MeV/ $c^2$ , which results in a  $\sim 95\%$  background rejection while keeping  $\sim 99\%$  signal efficiency.

#### 5.6.3.4 $\Lambda_b$ decays

$\Lambda_b^0 \rightarrow J/\psi \Lambda$  decays are unlikely to be reconstructed as  $B^0 \rightarrow K^{*0}\ell^+\ell^-$  because the  $\Lambda$  is long-lived and decays further in the detector with a separate vertex. Nevertheless, simulated events were used to check how many candidates fall into the  $B^0$  samples, which results to be negligible. Instead,  $\Lambda_b^0 \rightarrow J/\psi pK$  decays can contribute more

easily, when the proton is mis-identified as a kaon, since the  $m(pK)$  is above the  $\Lambda$  threshold and therefore they must come from  $\Lambda^*$  resonances, which are not long-lived. This background is already reduced by the PID requirements but a non-negligible contribution is still expected, and cannot be easily removed due to its broad shape. It is therefore modelled in the fit.

### 5.6.3.5 $B^0 \rightarrow (D^- \rightarrow K e^- \bar{\nu}) e^+ \nu$

The  $B^0 \rightarrow D^- e^+ \nu$  decay, where the  $D^-$  in turn decays semileptonically to  $K^{*0} e^- \nu$  has the same final particles as the  $B^0 \rightarrow K^{*0} e^+ e^-$  decay plus two neutrinos which are not reconstructed. This decay has a branching ratio four orders of magnitude larger than  $B^0 \rightarrow K^{*0} e^+ e^-$  in the low- $q^2$  region and it may pass the selection requirements when the two neutrinos carry a low momentum. To lower the level of this background the angle  $\theta_\ell$  is used, which is defined as the angle between the direction of the  $e^+$  ( $e^-$ ) in the di-electron rest frame and the direction of the di-electron in the  $B^0$  ( $\bar{B}^0$ ) rest frame. Low momentum neutrinos demand the  $D^-$  and the  $e^+$  to be almost back-to-back in the  $B^0$  rest frame giving the  $e^+$  a relatively large energy compared to the  $e^-$ . As a consequence, the direction of the  $e^+$  is close to the direction of the di-electron pair, thus the  $\theta_\ell$  angle is close to zero. In fact the distribution of background candidates, obtained imposing the invariant mass cut  $m(K\pi ee) < 4800 \text{ MeV}/c^2$ , is asymmetric towards extreme  $\cos \theta_\ell$  values as it can be seen in Fig. 5.10. The cut is chosen to be  $|\cos \theta_\ell| < 0.8$ , but it is not applied in the high- $q^2$  case as the variable loses its discriminating power. In the muon channels the background from  $B^0 \rightarrow (D^- \rightarrow K \mu^- \bar{\nu}) \mu^+ \nu$  decays remains outside of the invariant mass window used for the fits.

### 5.6.3.6 $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+ e^-)$

For the low- $q^2$  region, a potentially dangerous peaking background is due to the  $B^0 \rightarrow K^{*0} \gamma$  decay followed by a conversion of the photon in the detector. The

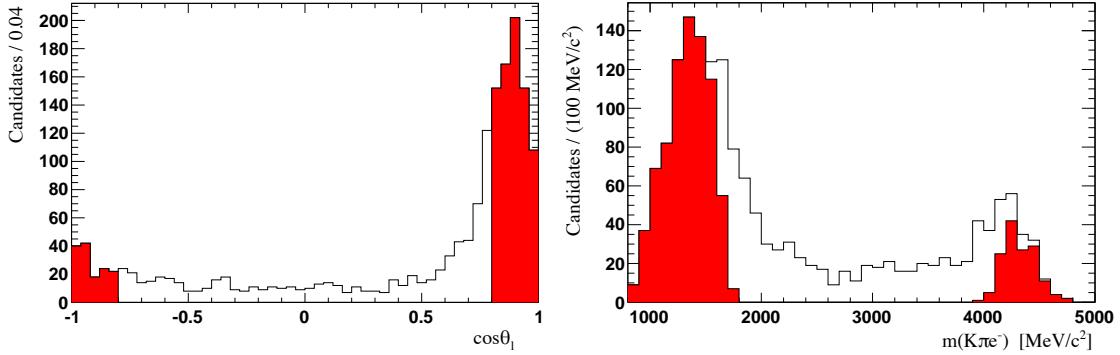


Figure 5.10: Distribution of (left)  $\cos \theta_\ell$  and of (right) the  $m(K\pi e^-)$  invariant mass, where the  $B^0 \rightarrow (D^- \rightarrow K e^- \bar{\nu}) e^+ \nu$  background is selected by requiring  $m(K\pi ee) < 4800$  MeV/ $c^2$ . The red distribution highlights candidates with  $|\cos \theta_\ell| > 0.8$ .

branching fraction of  $B^0 \rightarrow K^{*0} \gamma$  has been measured to be  $\mathcal{B} = (4.33 \pm 0.15) \times 10^{-5}$  and when the photon converts to an electron and a positron has similar characteristics to  $B^0 \rightarrow K^{*0} e^+ e^-$ . In LHCb around 40% of the photons convert before the calorimeter. Although only a small fraction of these,  $\sim 10\%$ , converts in the VeLo and are reconstructed as long tracks, the resulting  $B^0$  mass should peak under that of the signal, making it a dangerous background. To veto this signal-like background an effective veto is given by the choice of the lower bound for the low- $q^2$  interval that corresponds to  $m(ee) = 20$  MeV/ $c^2$ . Furthermore, the  $e^+ e^-$  pair from  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+ e^-)$  has a vertex at the point of conversion of the photon, but it may still be reconstructed as originating from the  $B^0$  decay if the  $e^+ e^-$  vertex is determined with a large uncertainty. Therefore a requirement is applied on the uncertainty of the reconstructed  $z$ -coordinate of the  $e^+ e^-$  pair:  $\sigma_z(e^+ e^-) < 30$  mm. Then, simulation is used to predict the contamination from  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+ e^-)$  decays in the signal region which is found to be  $(3.2 \pm 1.6)\%$ .

### 5.6.3.7 Other peaking backgrounds

Contamination from  $B^0 \rightarrow K^{*0}\eta$  and  $B^0 \rightarrow K^{*0}\pi^0$  where  $\eta$  and the pion decay into two photons was considered and found to be small. Furthermore, a potentially dangerous background could come from candidates where the identity of the kaon and the pion are swapped as these candidates peak under the signal. Their contri-

bution is found to be small, 0.5%, however the effect of their modelling into the fit is taken into account in the systematic uncertainties. Finally, charmonium decays where the identity of the kaon, or the pion, and one of the muons are swapped is are rejected by requiring that the hadron- $\mu$  invariant mass  $m((h \rightarrow \mu)\mu)$ , where the muon mass hypothesis is assigned to the hadron, is not compatible with a  $J/\psi$  ( $\psi(2S)$ ) resonance:  $|m((h \rightarrow \mu)\mu) - m_{J/\psi,(\psi(2S))}| > 60 \text{ MeV}/c^2$ .

### 5.6.4 Partially-reconstructed background

Partially-reconstructed candidates are defined as decays where one or more particles in the final state are not reconstructed, resulting in  $m(K\pi\ell\ell)$  values smaller than the mass of the  $B^0$ , but with tails that can still contaminate the signal sample. Sources of partially-reconstructed background are decays involving higher hadronic states such as  $B^0 \rightarrow (Y \rightarrow K\pi X)(J/\psi \rightarrow e^+e^-)$ , where  $X$  represents one or more not reconstructed particles. The  $Y$  state can be a  $K^*$  resonance as well as  $D$  mesons that decays semileptonically as explained in the previous sections. For the resonant channels, an additional source of partially-reconstructed background comes from decays of higher  $c\bar{c}$  resonances,  $B^0 \rightarrow (K^{*0} \rightarrow K\pi)(Y \rightarrow (J/\psi \rightarrow e^+e^-)X)$ . To reject this backgrounds the 4-body invariant mass  $m(K\pi\ell\ell)$  is recalculated using `DecayTreeFitter` with a vertex constraint. For the resonant case this also includes a  $J/\psi$  mass constraint to the dilepton pair; in this case the 4-body mass is denoted as  $m(K\pi\ell\ell)_{J/\psi}$ . This constraint pushes partially-reconstructed candidates towards low  $m(K\pi\ell\ell)_{J/\psi}$  values, resulting in no contamination above 5150 MeV/ $c^2$ . This requirement is implicitly applied for the muon channels by the definition of the invariant mass fit-windows. The requirement  $m(K\pi\ell\ell)_{J/\psi(\psi(2S))} > 5150 \text{ MeV}/c^2$  is instead explicitly applied to select the  $J/\psi(ee)$  and  $\psi(2S)(ee)$  samples. However, the vertex constraint alone is not sufficient to cleanup the electron rare channels. Furthermore, to correctly model the long radiative tail of the mass shapes, a fit region that extends down to 4500 MeV/ $c^2$  is needed. As a consequence the partially-reconstructed background is still relevant for the electron rare channels and extends

below the signal peak. For this reason this background is modelled in the fit for the rare channels (for details see Sec. 5.7.2.2).

### 5.6.5 Bremsstrahlung corrected mass

For the electron channels it is particularly difficult to separate partially-reconstructed and combinatorial background from the long radiative tail of the signal. An additional handle against these backgrounds is provided by the analysis of the kinematics of the decay. In fact for the  $B^0$  daughters, the  $K^{*0}$  and the dielectron, the momentum components orthogonal to the flight direction<sup>1</sup> of the  $B^0$  meson,  $p_T$ , should cancel out as described by the sketch shown in Fig. 5.11.

The ratio between the  $p_T$  of the  $K^{*0}$  and the dielectron pair,  $\alpha = p_T(K^{*0})/p_T(e^+e^-)$ , can be used to check this hypothesis. When  $\alpha$  deviates from one, some energy is missing in the final state. For signal candidates, the missing energy is most likely carried away by bremsstrahlung photons emitted by the electrons. Therefore we can use  $\alpha$  to correct the electron momentum as  $p_{\text{corr}}(e^+e^-) = \alpha \cdot p(e^+e^-)$ . Since bremsstrahlung photons are emitted in the direction of the electron, the same  $\alpha$  correction can be also applied to the longitudinal component of the dielectron momentum. In contrast, the missing particles in partially-reconstructed background candidates are not necessarily emitted in the direction of the electrons, and therefore

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<sup>1</sup>The flight direction is defined using the primary and the decay vertices.

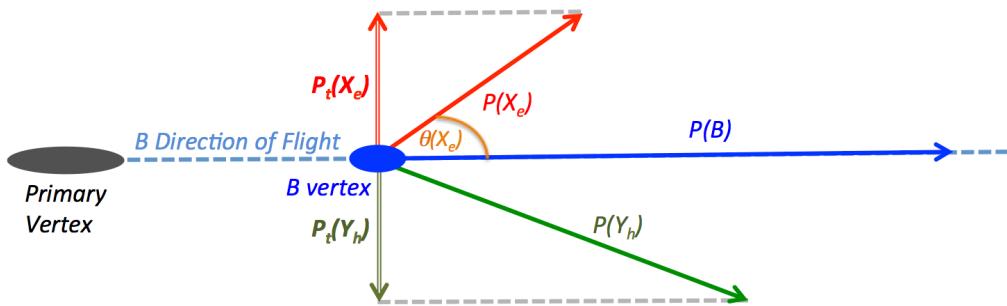


Figure 5.11: Schematic of the kinematic of a  $B \rightarrow Y_h X_e$  decay, highlighting the quantities relevant for the definition of the bremsstrahlung correction factor,  $\alpha$ .

this correction does not work properly. A similar argument applies to the combinatorial background.

The corrected momenta can be used to re-calculate the invariant mass of the  $B^0$  candidate, which in the following will be called Bremsstrahlung Corrected Mass,  $m_{\text{BCM}}$ . The resolution of  $m_{\text{BCM}}$  depends on the quality of the vertex reconstruction and on the  $B^0$  lifetime, and degrades as a function of  $q^2$ . Figure 5.12 shows the dependence of the  $B^0 \chi_{\text{FD}}^2$  (flight distance  $\chi^2$ ) as a function of  $m_{\text{BCM}}$  in the considered  $q^2$  regions.

As the correction does not work properly for backgrounds this leads the candidates to spread out making  $m_{\text{BCM}}$  a discriminating variable between signal and background. A two-dimensional cut is adopted

$$m_{\text{BCM}} > a_{\text{BCM}} + b_{\text{BCM}} \cdot \log(\chi_{\text{FD}}^2),$$

where the  $a_{\text{BCM}}$  and  $b_{\text{BCM}}$  coefficients are optimised as described in Sec. 5.6.7. No cut is applied at high- $q^2$  because the variable loses discriminating power nor on the muon channels for which the bremsstrahlung radiation is negligible.

### 5.6.6 Multivariate analysis

The final selection is performed using a neural network classifier based on the NEUROBAYES package [79, 80]. The multivariate analysis is intended to remove some combinatorial background and obtain a clearer signal peak. In order to avoid biases, a  $k$ -fold approach is adopted to train and optimise the classifier, using  $k = 10$ . This method consists in dividing the samples in  $k$  equally sized subsamples;  $k$  classifiers are then trained and optimised each on  $(k - 1)$  samples and applied to the  $k$ th one. This approach ensures that a classifier is never applied to the candidates used for its training. Each classifier is trained on half of the candidates included in the  $(k - 1)$  samples and optimised using the other half, which ensures that candidates used for training are not used for optimisation.

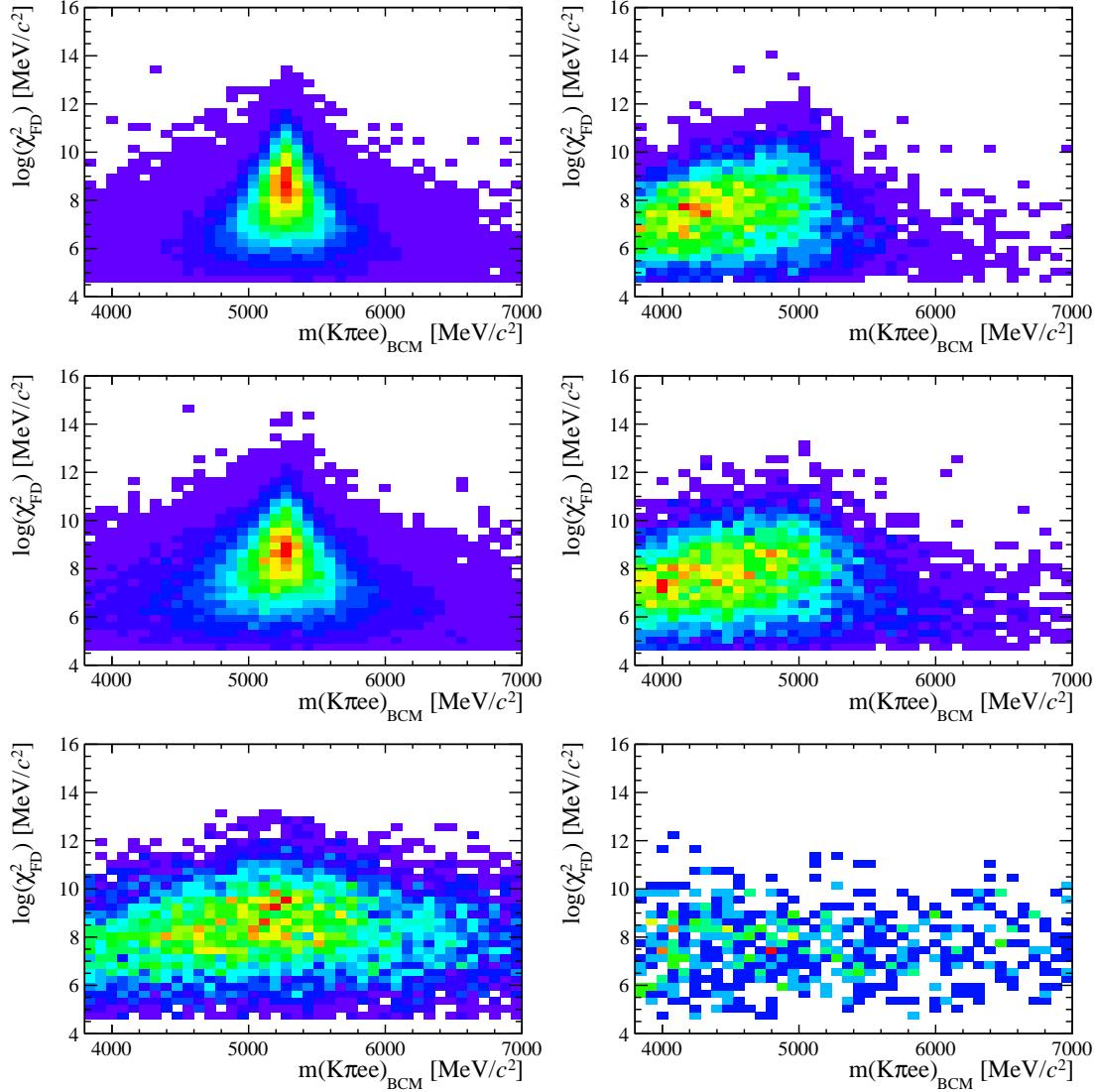


Figure 5.12: Two-dimensional distribution of  $\chi^2_{FD}$  vs.  $m_{BCM}$  for (left)  $B^0 \rightarrow K^{*0} e^+ e^-$  signal and (right) partially-reconstructed background. From top to bottom the low-, central- and high- $q^2$  intervals.

### Samples:

Representative samples of the signal and background are needed to train the classifier. For the signal, fully reconstructed  $B^0 \rightarrow K^{*0} \mu^+ \mu^-$  and  $B^0 \rightarrow K^{*0} e^+ e^-$  simulated events can be used. Instead a sample representative of the background can be obtained using real data candidates in the upper  $B^0$  sideband:  $m(K\pi\mu\mu) > 5400$  MeV/ $c^2$  and  $m(K\pi ee) > 5600$  MeV/ $c^2$ . The lower sideband is not used in the training as it contains a significant fraction of mis-reconstructed background. All pre-selection requirements are applied to the background samples used for the

Table 5.5: List of variables used as inputs for the neural-network training.

| Particle   | Variables                                                                                                                |
|------------|--------------------------------------------------------------------------------------------------------------------------|
| $B^0$      | $p_T$ , $\chi_{\text{IP}}^2$ , $\chi_{\text{FD}}^2$ , $\chi_{vtx}^2/\text{ndf}$ , DIRA, $\chi_{\text{DTF}}^2/\text{ndf}$ |
| $K^{*0}$   | $p_T$ , $\chi_{\text{IP}}^2$ , $\chi_{\text{FD}}^2$ , $\chi_{vtx}^2/\text{ndf}$ , DIRA                                   |
| $h$        | $\min, \max(p_{T,K}, p_{T,\pi})$ , $\min, \max(\chi_{\text{IP},K}^2, \chi_{\text{IP},\pi}^2)$                            |
| $\ell\ell$ | $p_T$ , $\chi_{\text{IP}}^2$ , $\chi_{\text{FD}}^2$ , $\chi_{vtx}^2/\text{ndf}$ , DIRA                                   |
| $\ell$     | $\min, \max(p_{T,\ell^+}, p_{T,\ell^-})$ , $\min, \max(\chi_{\text{IP},\ell^+}^2, \chi_{\text{IP},\ell^-}^2)$            |

training. As L0 and PID variables are not well described in simulation these cuts are not applied to the simulation but their effect is taken into account by event weights. An approximately equal number of signal and background candidates is used for the training which corresponds to about  $10^3$  electron and  $10^4$  muon candidates.

### Training:

The neural network input consists of 24 variables carrying information about the kinematic of the decays and the quality of tracks and vertices. All the variables used are listed in Tab. 5.5. The single most discriminating variable is the  $\chi^2$  of a kinematic fit that constrains the decay product of the  $B^0$ , the  $K^{*0}$  and the dimuon, to originate from their respective vertices. Other variables that contribute significantly are the  $\chi_{\text{IP}}^2$  of  $J/\psi$  and  $K^{*0}$ , the transverse momentum of the  $B^0$  and the pointing direction (DIRA) of the reconstructed  $B^0$  to the primary vertex.

Figure 5.13 shows neural network output distributions for signal and background.

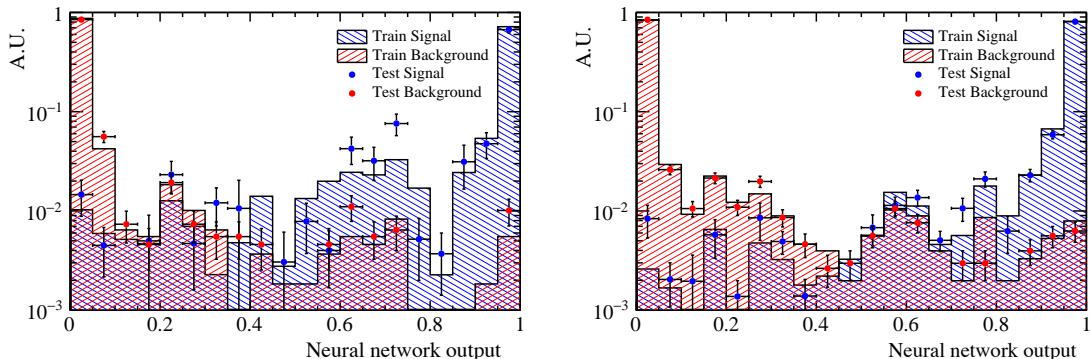


Figure 5.13: Neural network output distributions for training (solid) and test (stripes) samples, for simulated signal (blue) and data sideband (red) candidates. For the electron (left) and muon (right) training.

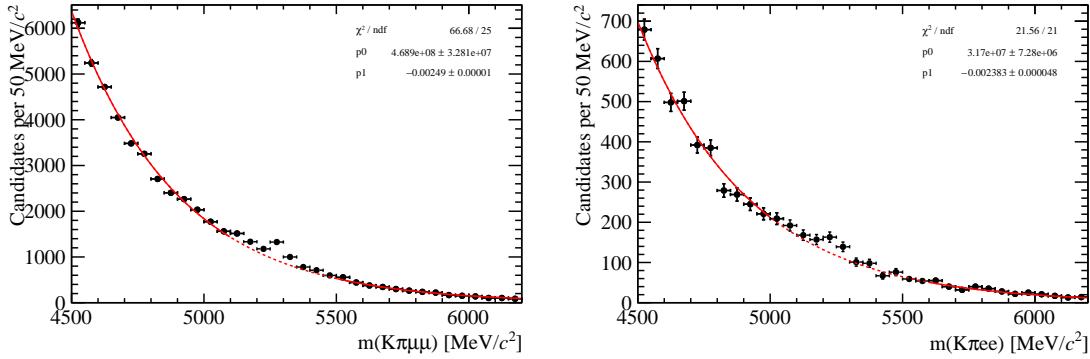


Figure 5.14: Fit to the data sidebands performed to estimate the amount of residual background in the signal mass window for (left) muons and (right) electrons. The region corresponding to the dashed line is excluded from the fit.

On this plot the distributions from the test samples are also overlaid in order to check for overtraining. The distributions follow the same shape but with different fluctuations indicating no significant overtraining. In general it can be concluded that the neural network is able to separate signal from background and that the training converged properly.

It can happen that too much information is given to the classifier, which becomes able to calculate the invariant mass of the candidates from its inputs. This could generate fake peaks and it is therefore important to check for correlations between the 4-body invariant mass and the neural-network output. Figure 5.15 reports the average neural-network output as a function of the 4-body mass for sideband data and simulated signal candidates. The distributions are flat showing that no significant correlation is present.

### 5.6.7 Optimisation

In order to optimise the requirements on the  $m_{\text{BCM}}$  and the neural network output the expected signal significance,  $N_S/\sqrt{N_S + N_B}$ , is maximised, where  $N_S$  ( $N_B$ ) is number of rare signal (background) candidates. When the BCM requirement is applied, the optimisation is performed in a three-dimensional space ( $t_{\text{MVA}}$ ,  $a_{\text{BCM}}$ ,  $b_{\text{BCM}}$ ), where  $t_{\text{MVA}}$  is the neural-network output threshold below which a candidate

is considered background, and  $a_{\text{BCM}}$  and  $b_{\text{BCM}}$  are the parameters of the BCM cut described in Sec. 5.6.5. Otherwise, only the MVA cut is optimised (this is the case for all muons samples and the high- $q^2$  electron sample).

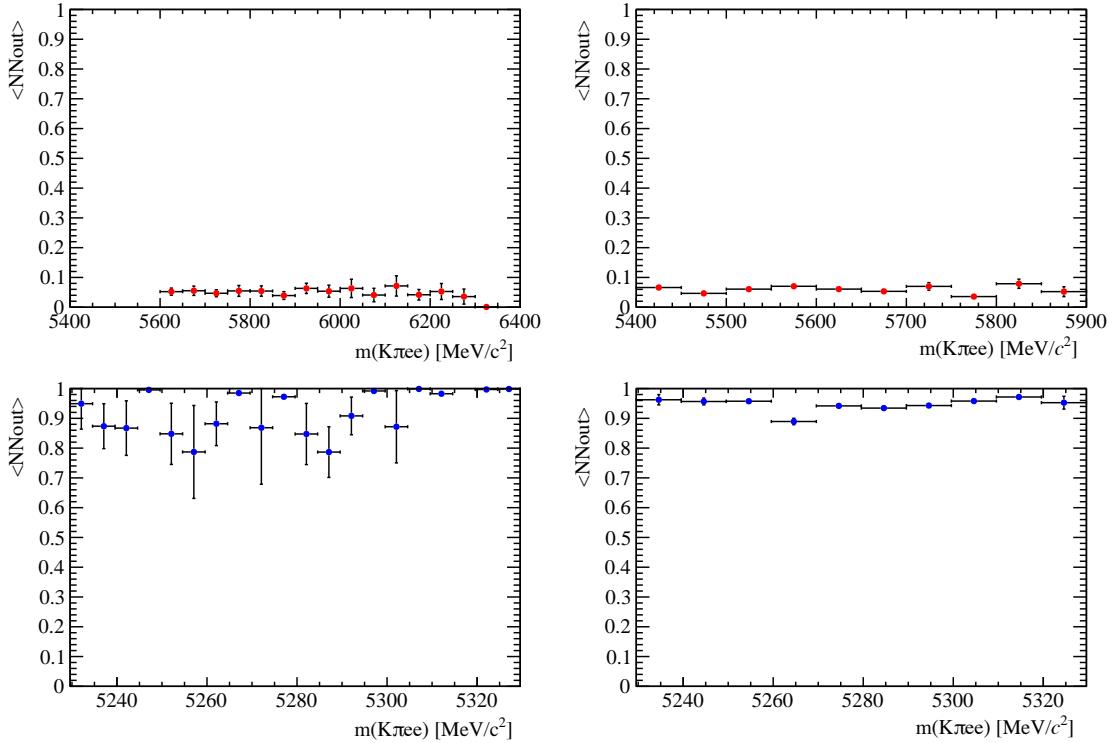


Figure 5.15: Average value of neural network output as a function of 4-body invariant mass for data sideband (top) and simulated signal (bottom) candidates for the electron (left) and muon (right) trainings.

The number of signal candidates accepted by a given requirement is determined using a data-driven method. Firstly,  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+\ell^-)$  candidates selected with all the requirements except for the MVA, and BCM cuts are fitted to determine the total yield. This number is then scaled by the ratio between the signal and  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+\ell^-)$  branching fractions and the efficiency ratio:

$$N_S = N_{J/\psi(\ell\ell)} \cdot \frac{\mathcal{B}(S)}{\mathcal{B}(B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+\ell^-))} \cdot \frac{\varepsilon_S}{\varepsilon_{J/\psi(\ell\ell)}} .$$

The number of background candidates is also derived from data by fitting the background in the lower and upper mass sidebands with an exponential function, and extrapolating the residual yield in the signal region (Fig. 5.14). Because the back-

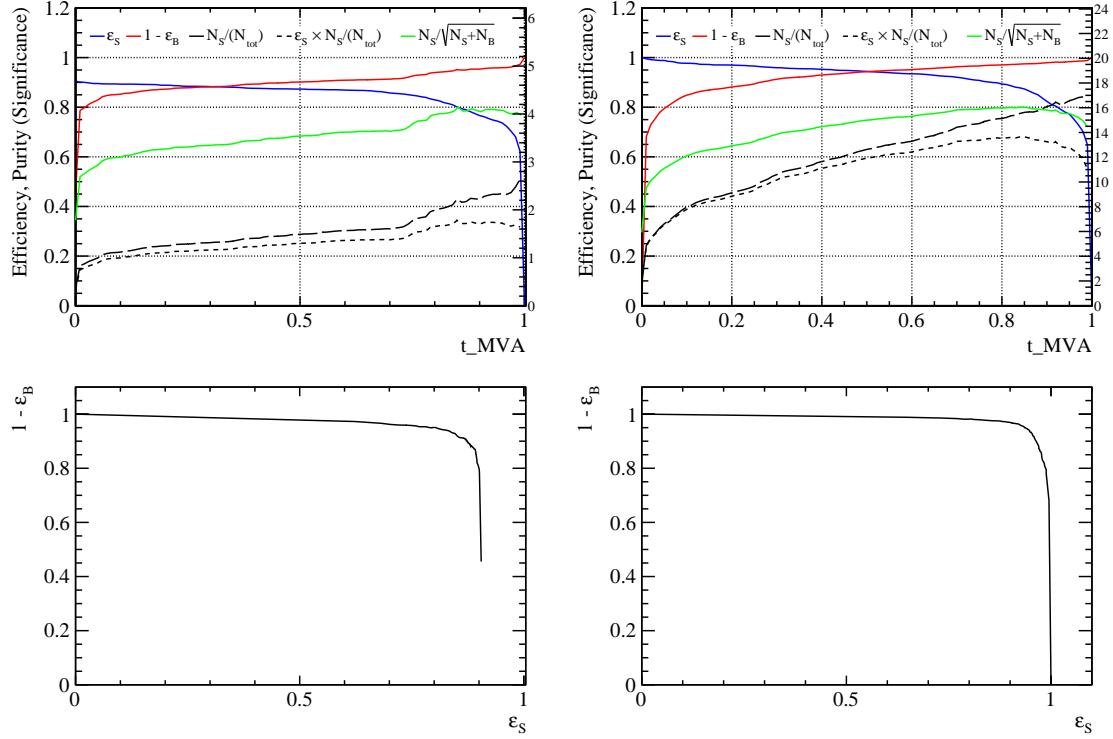


Figure 5.16: (top) Dependence of figure-of-merit on the requirement on neural network output. (bottom) Signal efficiency versus background rejection. Plots correspond to the electron (left) and muons (right) samples.

ground shape changes as a function of the requirement that is being optimised, the sidebands are refitted for each considered cut value.

The cut optimisation is performed in a signal mass window of  $\pm 100$  MeV/ $c^2$  around the nominal  $B^0$  mass for muons, and between 5000 and 5400 MeV/ $c^2$  for electrons. The average result of the  $k$  optimisations is taken as the nominal requirement. The variation of the signal and background efficiency, signal purity and figure-of-merit as a function of the neural-network output requirement for the central- $q^2$  is shown in Fig. 5.16 together with curves of the background rejection as a function of the signal efficiency. After full selection about  $\sim 3\%$  of events still contain multiple candidates which are removed at random keeping only a single candidate per event.

### 5.6.8 Selection summary

Table 5.6 summarises the requirements applied for each sample after stripping.

Table 5.6: Summary of the selection requirements. The last column indicates to which  $q^2$  intervals the requirement is applied.

| Type            |                                      | Requirement                                                                             | $q^2$               |
|-----------------|--------------------------------------|-----------------------------------------------------------------------------------------|---------------------|
| Quality         | All tracks                           | $\chi^2/\text{ndf} < 3$<br>$\text{GhostProb} < 0.4$                                     | all<br>all          |
|                 | ID                                   | $ m(K\pi) - m_{K^{*0}}^{\text{PDG}}  < 100 \text{ MeV}/c^2$                             | all                 |
| PID             | $K$                                  | $\text{ProbNNk} \cdot (1 - \text{ProbNNp}) > 0.05$                                      | all                 |
|                 | $\pi$                                | $\text{ProbNNpi} \cdot (1 - \text{ProbNNk}) \cdot (1 - \text{ProbNNp}) > 0.1$           | all                 |
|                 | $\mu$                                | $\text{ProbNNmu} > 0.2$                                                                 | all $\mu\mu$        |
|                 | $e$                                  | $\text{ProbNNe} > 0.2$                                                                  | all $ee$            |
| BKG             | Swap                                 | $ m((h \rightarrow \mu)\mu) - m_{J/\psi,(\psi(2S))}^{\text{PDG}}  > 60 \text{ MeV}/c^2$ | all                 |
|                 | $B^+ \rightarrow K^+\ell^+\ell^-$    | $\max(m(K\ell\ell), m((\pi \rightarrow K)\ell\ell)) < 5.1 \text{ GeV}/c^2$              | all                 |
|                 | $B_s^0 \rightarrow \phi\ell^+\ell^-$ | $m(K(\pi \rightarrow K)) > 1040 \text{ MeV}/c^2$                                        | all                 |
|                 | $B^0 \rightarrow D^-e^+\nu$          | $ \cos \theta_\ell  < 0.8$                                                              | except high-        |
|                 | $B^0 \rightarrow K^{*0}\gamma$       | $\sigma_z(e^+e^-) < 30 \text{ mm}$                                                      | except $\gamma(ee)$ |
|                 | Comb                                 | $\text{NNout} > 0.68$                                                                   | $\mu\mu$ low-       |
|                 |                                      | $\text{NNout} > 0.64$                                                                   | $ee$ low-           |
|                 |                                      | $\text{NNout} > 0.85$                                                                   | $\mu\mu$ central-   |
|                 |                                      | $\text{NNout} > 0.97$                                                                   | $ee$ central-       |
|                 |                                      | $\text{NNout} > 0.40$                                                                   | $\mu\mu$ high-      |
|                 |                                      | $\text{NNout} > 0.93$                                                                   | $ee$ high-          |
|                 |                                      | $\text{NNout} > 0.06$                                                                   | $J/\psi(\mu\mu)$    |
|                 |                                      | $\text{NNout} > 0.20$                                                                   | $J/\psi(ee)$        |
|                 | Part-reco                            | $\text{NNout} > 0.16$                                                                   | $\gamma(ee)$        |
|                 |                                      | $\text{NNout} > 0.68$                                                                   | $\psi(2S)(ee)$      |
| Comb, part-reco | Part-reco                            | $m(K\pi\ell\ell)_{J/\psi} > 5150 \text{ MeV}/c^2$                                       | $J/\psi(ee)$        |
|                 | Comb, part-reco                      | $m_{\text{BCM}} > 4680 + 31 \cdot \log(\chi_{\text{FD}}^2)$                             | $ee$ low-           |
|                 |                                      | $m_{\text{BCM}} > 4437 + 64 \cdot \log(\chi_{\text{FD}}^2)$                             | $ee$ central-       |
|                 |                                      | $m_{\text{BCM}} > 3380 + 140 \cdot \log(\chi_{\text{FD}}^2)$                            | $\gamma(ee)$        |

## 5.7 Invariant mass fits

The signal yields are obtained using a simultaneous unbinned maximum likelihood fit to the 4-body invariant mass,  $m(K\pi\ell\ell)$ , of the rare, normalisation and control samples. The simultaneous fit allows to share parameters *e.g.* those describing data-simulation differences. The yields of the rare channels are parameterised as a function of the corresponding  $J/\psi$  yields as

$$N_{\ell\ell}(r_{\ell\ell}, N_{J/\psi}) = N_{J/\psi} \cdot \varepsilon^{\text{rel}} \cdot r_{\ell\ell}, \quad (5.10)$$

where  $\varepsilon^{\text{rel}}$  is the relative efficiency between the rare and resonant channels (given in Tab. 5.10). Consequently,  $r_{\ell\ell}$  corresponds to the efficiency corrected ratio between the raw rare and resonant yields:

$$r_{\ell\ell} = \frac{N_{\ell\ell}/\varepsilon^{\ell\ell}}{N_{J/\psi}/\varepsilon^{J/\psi(\ell\ell)}}. \quad (5.11)$$

The two ratios,  $r_{ee}$  and  $r_{\mu\mu}$ , are then used to determine the  $R_{K^{*0}}$  quantity, as described in Sec. 5.10. The following subsections contain a description of the line shapes used to model the signal and background components in each sample.

### 5.7.1 Muon channels

For the rare and resonant  $\mu\mu$  channels the fitted variable is the  $m(K\pi\mu\mu)$  invariant mass coming from a kinematic fit where all vertices are required to point to their mother particle. In the resonant case it is beneficial to also constrain the dimuon mass to the known  $J/\psi$  mass; in this case the invariant mass is referred to as  $m(K\pi\mu\mu)_{J/\psi}$ . The effect of the kinematical constraint is to improve the mass resolution by roughly a factor of 2, which results in a more stable fit. Furthermore, partially reconstructed background candidates are pushed away from the  $B^0$  peak towards low invariant mass values. The mass spectrum is fitted in the range 5150 – 5800 MeV/ $c^2$  with the lower limit chosen to totally exclude the partially

reconstructed background. As it is not needed to model partially reconstructed backgrounds in the fit this also eliminates the systematic uncertainties associated with the knowledge of their shape.

### 5.7.1.1 $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+\mu^-)$ PDF

The signal PDF adopted to describe the reconstructed 4-body invariant mass of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+\mu^-)$  candidates is the sum of a Double Crystal Ball [104] (DCB) function with opposite-side tails and a Gaussian function with a common mean,  $\mu$ :

$$\mathcal{P}_{\text{sig}}(m|\vec{\lambda}) = f_{\text{CB1}} \cdot \mathcal{P}_{\text{CB}}(m|\mu, \sigma_1, \alpha_1, n_1) + \\ f_{\text{CB2}} \cdot \mathcal{P}_{\text{CB}}(m|\mu, \sigma_2, \alpha_2, n_2) + (1 - f_{\text{CB1}} - f_{\text{CB2}}) \cdot \mathcal{P}_{\text{Gauss}}(m|\mu, \sigma_3),$$

where  $f_{\text{CB}i}$  is the relative fraction of candidates falling in the  $i^{\text{th}}$  Crystal Ball function,  $\sigma_i$  is the width,  $\alpha_i$  and  $n_i$  are the parameters controlling the power law tail of each CB, and  $\sigma_3$  is the width of the Gaussian function.

As a first step, the parameters of the signal PDF are extracted by fitting the  $m(K\pi\mu\mu)_{J/\psi}$  distribution of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+\mu^-)$  simulated candidates; parameters are then fixed for the fit to the data. Figure 5.17 shows the fitted simulated distribution for the normalisation channel, while fits or the rare channel in the three  $q^2$  bins are reported in Appendix E. In order to account for possible discrepancies in the invariant mass distribution between data and simulation, the mass is allowed to shift,  $\mu \rightarrow \mu + m'$ , and the widths are allowed to scale,  $\sigma_i \rightarrow c \cdot \sigma_i$ , where the scale factor  $c$  is common between the three  $\sigma$ s.

In summary, the signal PDF for the  $J/\psi(\mu\mu)$  channel fit on data is defined as

$$\mathcal{P}_{J/\psi(\mu\mu)}(m|m', c) = f_{\text{CB1}} \cdot \mathcal{P}_{\text{CB}}(m|m', c) + f_{\text{CB2}} \cdot \mathcal{P}_{\text{CB}}(m|m', c) + \\ (1 - f_{\text{CB1}} - f_{\text{CB2}}) \cdot \mathcal{P}_{\text{Gauss}}(m|m', c).$$

where the only free parameters are the mass shift,  $m'$  and the width scale factor,  $c$ .

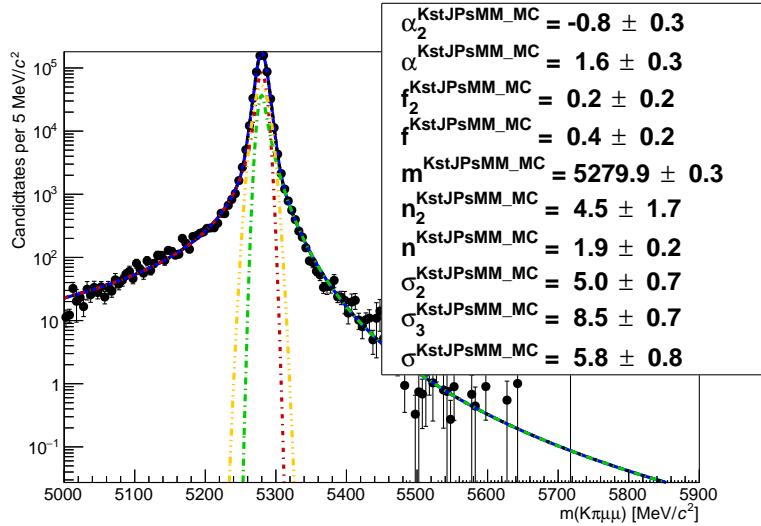


Figure 5.17: Fitted  $m(K\pi\mu\mu)_{J/\psi}$  mass spectrum for  $K^{*0}J/\psi$  simulated events.

The following backgrounds are considered:

- *Combinatorial*: modelled with an exponential function;
- $\Lambda_b^0 \rightarrow pK(J/\psi \rightarrow \mu^+\mu^-)$ : described using fully reconstructed simulated events to which the full selection is applied; this distribution has a broad shape under the signal peak and is smoothed using the `RooKeysPdf` class of the `ROOFIT` [121] package;
- $B_s^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+\mu^-)$ : described using the same PDF adopted for the signal, but a different central value,  $\mu$ , which is set at the  $B_s^0$  nominal mass. The same shift  $m'$  is used as for the signal.

### 5.7.1.2 $B^0 \rightarrow K^{*0}\mu^+\mu^-$ PDF

The signal PDF adopted to describe the reconstructed 4-body invariant mass of the rare  $B^0 \rightarrow K^{*0}\mu^+\mu^-$  candidates is a DCB function with opposite-side tails with a common mean,  $\mu$ . The parameters of the PDF are fixed to values obtained by fitting simulated candidates, separately in each  $q^2$  interval. As for the charmonium channel, the mass is allowed to shift and the widths are allowed to scale with a

common factor:

$$\mathcal{P}_{\text{mm},q^2}(m|m'_{q^2}, c_{q^2}) = f_{\text{core},q^2} \cdot \mathcal{P}_{\text{CB}}(m|m'_{q^2}, c_{q^2}) + (1 - f_{\text{core},q^2}) \cdot \mathcal{P}_{\text{CB}}(m|m'_{q^2}, c_{q^2}).$$

where  $f_{\text{core},q^2}$  is the relative fraction of candidates falling in the first Crystal Ball function,  $m'_{q^2}$  is the mass shift and  $c_{q^2}$  is the width scale. The subscript “ $q^2$ ” indicates that independent parameters are used for each  $q^2$  interval. The background is described by an exponential function in all the three  $q^2$  intervals.

### 5.7.1.3 Summary

In summary, the free parameters of the simultaneous fit to the  $J/\psi(\mu\mu)$  and  $\mu\mu$  candidates are the signal and background yields, the combinatorial background slopes, the mass shifts and the width scales. Figure 5.19 shows the results of the fit to the rare and resonant  $\mu\mu$  candidates. Values of the fitted parameters are reported on the plots.

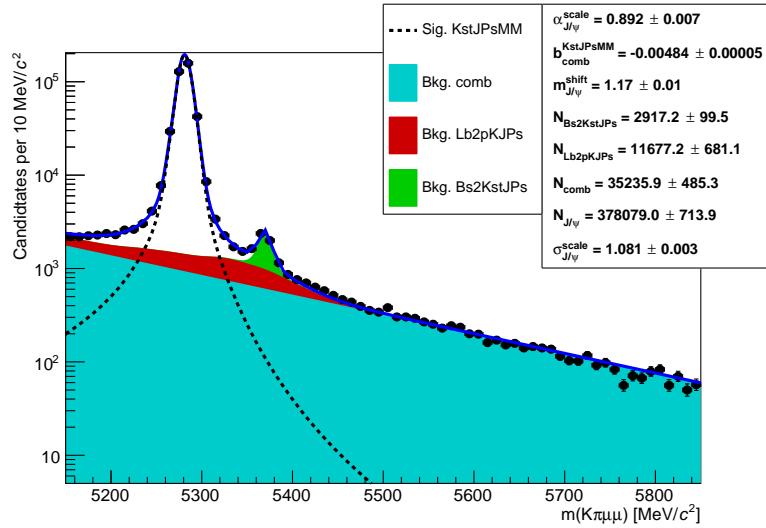


Figure 5.18: Fitted  $m(K\pi\mu\mu)_{J/\psi}$  invariant mass distribution for  $J/\psi(\mu\mu)$  candidates in logarithmic scale. Dashed black lines represent the signal PDFs and filled shapes the background components.

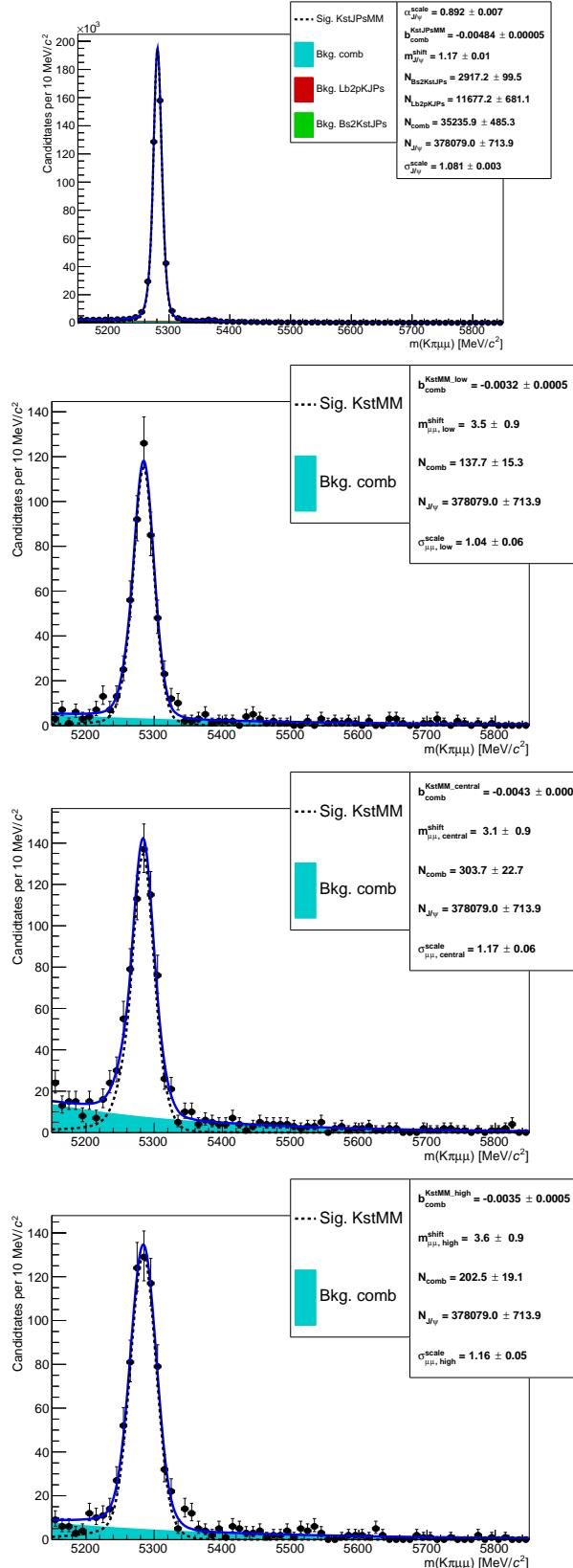


Figure 5.19: From top to bottom fitted  $m(K\pi\mu\mu)_{J/\psi}$  invariant mass distributions for  $J/\psi(\mu\mu)$  candidates and fitted  $m(K\pi\mu\mu)$  distributions for rare candidates in the low-, central- and high- $q^2$  intervals. Dashed black lines represent the signal PDFs and filled shapes the background components.

### 5.7.2 Electron channels

Also in the electron case the fitted variable is the 4-body invariant mass coming from a kinematic fit. In general, this does not include constraints to intermediate resonances, unless specified. When constraints to intermediate resonances are applied the invariant mass is referred to as  $m(K\pi ee)_R$ , where  $R = J/\psi$  or  $\psi(2S)$ . A simultaneous fit to the 4-body invariant mass of the  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  and  $B^0 \rightarrow K^{*0}e^+e^-$  channels and across the three trigger categories defined in Sec. 5.6.1 is performed. For each trigger category, the  $J/\psi(ee)$  and  $ee$  yields are extracted from the following signal channel categories:

- $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$ , with a  $J/\psi$  mass constraint,  $m(K\pi ee)_{J/\psi}$ ;
- $B^0 \rightarrow K^{*0}e^+e^-$  in the three  $q^2$  intervals.

Extra control channels are fit simultaneously:

- $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$  to constrain the yield of partially-reconstructed background in the low- $q^2$  and the leakage of  $B^0 \rightarrow K^{*0}\gamma$  into the low- $q^2$ ;
- $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$ , without the  $J/\psi$  mass constraint, to constrain the leakage into the central- $q^2$  and the parameters that model residual data-simulation discrepancies;
- $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$ , with a  $\psi(2S)$  mass constraint,  $m(K\pi ee)_{\psi}$ , to constrain the leakage to lower and higher  $q^2$  values.

When fitting the variable without a  $J/\psi$  mass constraint it is important to fit a wider mass range to better constrain the parameters modelling the radiative tail and the backgrounds; therefore a mass window [4500,6200] MeV/ $c^2$  is used. The lower limit is given by the point in which the  $q^2$  cut (at 6 GeV $^2/c^4$  to separate the rare and resonant channels) starts to affect the 4-body invariant mass distribution.

The invariant mass distributions are different depending on the L0 line that triggered the event and also on the number of bremsstrahlung photons recovered. Therefore, our samples are divided in three trigger categories, as described in Sec. 5.6.1, and three bremsstrahlung categories defined as:

- $0\gamma$ : candidates with no photons recovered;
- $1\gamma$ : candidates with one photon from either of the electrons;
- $2\gamma$ : candidates with more than one recovered photon.

All samples are fitted simultaneously, which allows a better use of the available statistics as the simultaneous fit gathers information from the three categories at the same time. Furthermore, using this method the results for the three categories are naturally combined in a single  $r_{ee}$  ratio. The PDFs used to fit the invariant mass distributions are described in the following sections.

### 5.7.2.1 Signal PDFs for the electron channels

As for the muon channels, simulated candidates are fitted first to constrain the shape parameters for the subsequent fit to data. The signal PDFs are built using the following method:

- Simulated  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow ee)$  and  $B^0 \rightarrow K^{*0}ee$  candidates are divided in each trigger and bremsstrahlung category and an independent fit is performed to each sample. A different fit is also performed for each  $q^2$  interval. It is important to use independent signal tail parameters for each  $q^2$  interval because, as can be seen in Fig. 5.20, the invariant mass distributions can be significantly different.
- For each trigger category a PDF is built as the sum of the three PDFs of the

Table 5.7: Percentages of events with 0, 1 and 2 emitted photons in the three trigger categories, obtained from simulated events.

| Trigger                                               | $0\gamma$ (%) | $1\gamma$ (%) | $2\gamma$ (%) |
|-------------------------------------------------------|---------------|---------------|---------------|
| $B^0 \rightarrow K^{*0}e^+e^-$ low- $q^2$             |               |               |               |
| L0E                                                   | 34.2          | 56.0          | 9.8           |
| L0H                                                   | 27.8          | 58.1          | 14.2          |
| L0I                                                   | 31.7          | 56.9          | 11.4          |
| $B^0 \rightarrow K^{*0}e^+e^-$ central- $q^2$         |               |               |               |
| L0E                                                   | 29.2          | 50.0          | 20.8          |
| L0H                                                   | 23.6          | 50.5          | 26.0          |
| L0I                                                   | 28.5          | 49.9          | 21.6          |
| $B^0 \rightarrow K^{*0}e^+e^-$ high- $q^2$            |               |               |               |
| L0E                                                   | 20.6          | 51.2          | 28.2          |
| L0I                                                   | 10.0          | 53.8          | 36.2          |
| $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$   |               |               |               |
| L0E                                                   | 40.4          | 59.6          | –             |
| L0H                                                   | 32.2          | 67.8          | –             |
| L0I                                                   | 39.3          | 60.7          | –             |
| $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$   |               |               |               |
| L0E                                                   | 29.0          | 50.1          | 20.8          |
| L0H                                                   | 18.9          | 51.3          | 29.8          |
| L0I                                                   | 26.9          | 51.7          | 21.4          |
| $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$ |               |               |               |
| L0E                                                   | 27.2          | 51.3          | 21.5          |
| L0H                                                   | 17.4          | 51.5          | 31.2          |
| L0I                                                   | 22.0          | 55.0          | 23.0          |

bremsstrahlung categories:

$$\mathcal{P}^{\text{L0}}(m) = f_{0\gamma}^{\text{L0}} \cdot \mathcal{P}_{0\gamma}^{\text{L0}}(m) + f_{1\gamma}^{\text{L0}} \cdot \mathcal{P}_{1\gamma}^{\text{L0}}(m) + (1 - f_{0\gamma}^{\text{L0}} - f_{1\gamma}^{\text{L0}}) \cdot \mathcal{P}_{2\gamma}^{\text{L0}}(m), \quad (5.12)$$

where the  $\mathcal{P}(m)_{n\gamma}^{\text{L0}}$  functions are the chosen PDFs for the trigger and bremsstrahlung categories and the  $f_{n\gamma}^{\text{L0}}$  parameters are the relative fractions of events falling in each category.

- Most parameters are fixed (details later) and the combined PDF,  $\mathcal{P}_{\text{sig}}(m)$ , is used to fit real data divided only in trigger categories.

The distribution of the  $m(K\pi ee)$  mass in the  $0\gamma$  category is characterised by a sharp tail on the righthand side and is described with a Crystal Ball function (CB),

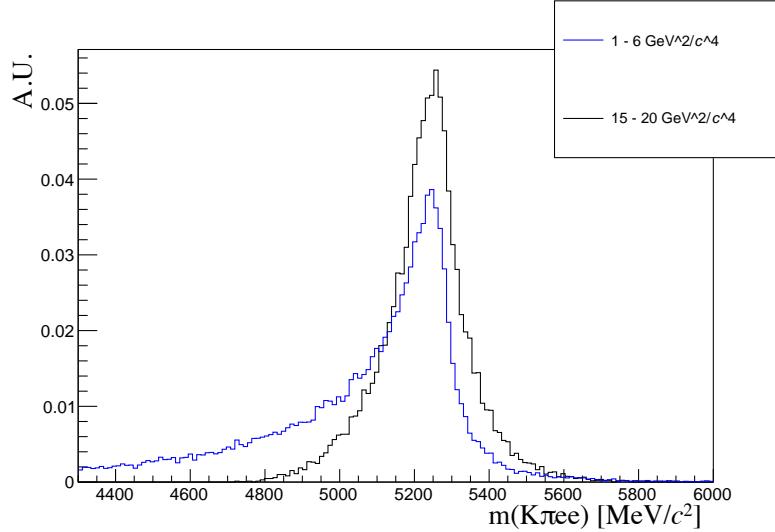


Figure 5.20: Simulated  $m(K\pi ee)$  invariant mass in the  $[1.1, 6]$  and  $[15, 20]$   $\text{GeV}^2/c^4 q^2$  intervals.

while the  $1\gamma$  and  $2\gamma$  categories are modelled using the sum of a Crystal Ball and a Gaussian function (CBG) with independent parameters. In all the bremsstrahlung categories the distribution of the 4-body invariant mass with the  $J/\psi$  mass constraint,  $m(K\pi ee)_{J/\psi}$ , is modelled using the sum of a DCB and a Gaussian functions as done for the muon fit. To account for possible data-simulation discrepancies, the mass (widths) of each trigger PDF is allowed to shift (scale), similarly to the muon channels. However, due to the larger background contamination these parameters are shared between the rare and the  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  control sample.

The  $f_{n\gamma}^{L0}$  fractions have been shown to be in good agreement between resonant data and simulation and therefore they are fixed to the simulated values, separately for the normalisation channel and each  $q^2$  interval. Table 5.7 lists the percentages of candidates with 0, 1 and 2 recovered photons for each trigger category.

In summary the signal PDF for the fit on data is defined as:

$$\begin{aligned} \mathcal{P}_{sig}(m; c, m') &= \sum_{L0} [f_{0\gamma}^{L0} \cdot \mathcal{P}_{0\gamma}^{L0}(m; c, m') \\ &\quad + f_{1\gamma}^{L0} \cdot \mathcal{P}_{1\gamma}^{L0}(m; c, m') + (1 - f_{0\gamma}^{L0} - f_{1\gamma}^{L0}) \cdot \mathcal{P}_{2\gamma}^{L0}(m; c, m')] \end{aligned} \quad (5.13)$$

where the free parameters are:  $c$ , the widths' scaling factors, and  $m'$ , the mass shifts.

### 5.7.2.2 Background PDFs for the electron channels

This section reports the background components considered for each fitted sample.

$$B^0 \rightarrow K^{*0} e^+ e^- \text{ low-}q^2$$

- *Combinatorial*: described using an exponential function; the yield and slope parameters are free to vary in the fit;
- *Partially-reconstructed* (hadronic): the shape is obtained from a  $K_1^+(1270)$  simulated sample smoothed with a `RooKeysPdf`; the simulated distribution is shown in Fig. 5.21. The fraction of partially-reconstructed candidates with respect to the signal ones is expected to be very similar to that found in  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+ e^-)$  and therefore the normalisation is constrained as:

$$N_{e^+ e^-, \text{low}}^{\text{part-reco}} = N_{e^+ e^-} \cdot \frac{N_{\gamma(ee)}^{\text{part-reco}}}{N_{\gamma(ee)}},$$

where  $N_{\gamma(ee)}^{\text{part-reco(hadronic)}}/N_{\gamma(ee)}$  is the fraction of hadronic partially-reconstructed background candidates relative to the signal yield in the  $\gamma(ee)$  channel;

- $B^0 \rightarrow K^{*0}\gamma$  *leakage*: the leakage from the  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+ e^-)$  decay into the low- $q^2$  region is modelled using simulated candidates that pass the low- $q^2$  requirements. The distribution, smoothed with a `RooKeysPdf`, is shown in Fig. 5.21 and the normalisation is constrained to the  $\gamma(ee)$  yield,  $N_{\gamma(ee)}$ , as:

$$N_{e^+ e^-, \text{low}}^{\text{leak}} = N_{\gamma(ee)} \cdot f_{\gamma(ee)}^{\text{leak, MC}},$$

where  $f_{\gamma(ee)}^{\text{leak, MC}}$  is the fraction of  $\gamma(ee)$  simulated candidates which leaks in the low- $q^2$  region.

$B^0 \rightarrow K^{*0}e^+e^-$  central- $q^2$

- *Combinatorial*: described using an exponential function; the yield and slope parameters are free to vary in the fit.
- *Partially-reconstructed* (hadronic): modelled using simulation as described for the low- $q^2$  but in this case the normalisation is left free to vary.
- $B^0 \rightarrow K^{*0}J/\psi$  leakage: the leakage from the  $J/\psi$  radiative tail into the central- $q^2$  interval is modelled by selecting simulated  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  candidates which pass the central- $q^2$  requirements and smoothing the distributions with a kernel density estimation method; the simulated distribution is shown in Fig. 5.21. The normalisation is constrained to the  $J/\psi(ee)$  yield,  $N_{J/\psi(ee)}$ , as:

$$N_{e^+e^-,\text{central}}^{\text{leak}} = N_{J/\psi(ee)} \cdot f_{J/\psi(ee)}^{\text{leak, MC}},$$

where  $f_{J/\psi(ee)}^{\text{leak, MC}}$  is the fraction of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  simulated candidates reconstructed in the central- $q^2$  interval.

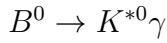
$B^0 \rightarrow K^{*0}e^+e^-$  high- $q^2$

- *Combinatorial*: modelled using a shape obtained by reversing the neural network requirement on data, which has the effect of selecting background candidates instead of signal ones. Figure 5.22 shows the invariant mass distributions for different anti-cuts on the electron and muon samples at high- $q^2$ . The shapes are very similar between the two samples and as a function of the cut value. In order to have a larger statistics, the shape is taken from the muon sample with a tight anti-MVA cut,  $\text{NNout} < 0.1$ , and smoothed with a `RooKeysPdf`;
- *Partially-reconstructed* (hadronic): modelled using simulation as described for the previous intervals; the normalisation is left free to vary.
- $B^0 \rightarrow K^{*0}\psi(2S)$  leakage: the leakage from the  $\psi(2S)$  radiative tail is modelled using simulated  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  candidates which pass the the

high- $q^2$  requirements. The normalisation is constrained to the  $\psi(2S)(ee)$  yield,  $N_{\psi(2S)(ee)}$  as:

$$N_{e^+e^-,\text{high}}^{\text{leak}} = N_{\psi(2S)(ee)} \cdot f_{\psi(2S)(ee)}^{\text{leak, MC}},$$

where  $f_{\psi(2S)(ee)}^{\text{leak, MC}}$  is the fraction of  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  simulated candidates leaking into the high- $q^2$  interval.



- *Combinatorial*: described using an exponential function; the yield and slope parameters are free to vary in the fit;
- *Partially-reconstructed* (hadronic): modelled using simulation as described for the previous intervals; the normalisation is left free to vary and used to constrain the fraction of partially-reconstructed candidates in the low- $q^2$  interval.
- $B^0 \rightarrow K^{*0}e^+e^-$  leakage: as the  $K^{*0}\gamma$  was added to the low- $q^2$  also the low- $q^2$  leakage is added to  $K^*\gamma$ . The yield is constrained to the  $N_{ee}^{\text{low}}$  yield.



The following backgrounds are considered for the fits to the invariant mass of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  candidates:

- *Combinatorial*: described using an exponential function. The yield and slope parameters are free to vary in the fit;
- $\Lambda_b^0 \rightarrow pK(J/\psi \rightarrow e^+e^-)$ : described using simulated candidates to which the full selection is applied. This distribution, which is shown in Fig. 5.21, has a broad shape under the signal peak and is smoothed using a `RooKeysPdf`. The normalisation is fixed to the  $\Lambda_b^0 \rightarrow pK(J/\psi \rightarrow \mu^+\mu^-)$  yield returned by the muon fit after correcting for efficiency differences between final states with muons and electrons.

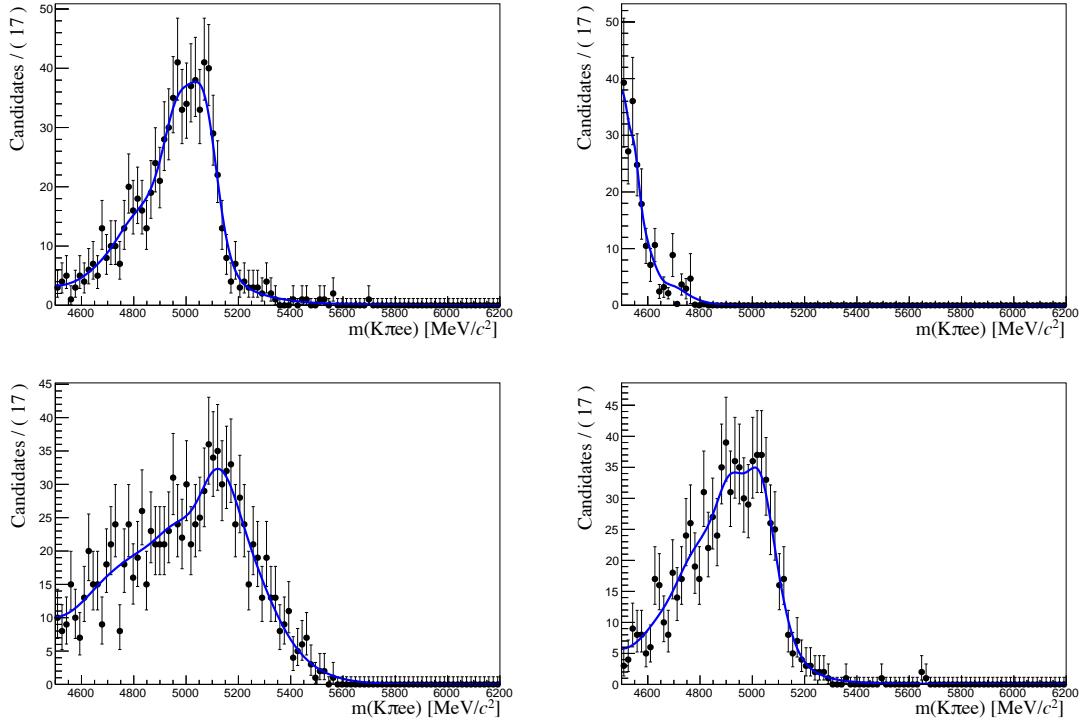


Figure 5.21: Distributions of the  $m(K\pi ee)$  invariant mass of: decays involving higher  $K^{*0}$  resonances (top left), the  $J/\psi$  leakage into the central- $q^2$  interval (top right),  $\Lambda_b^0$  decays (bottom left) and  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$  decays (bottom right).

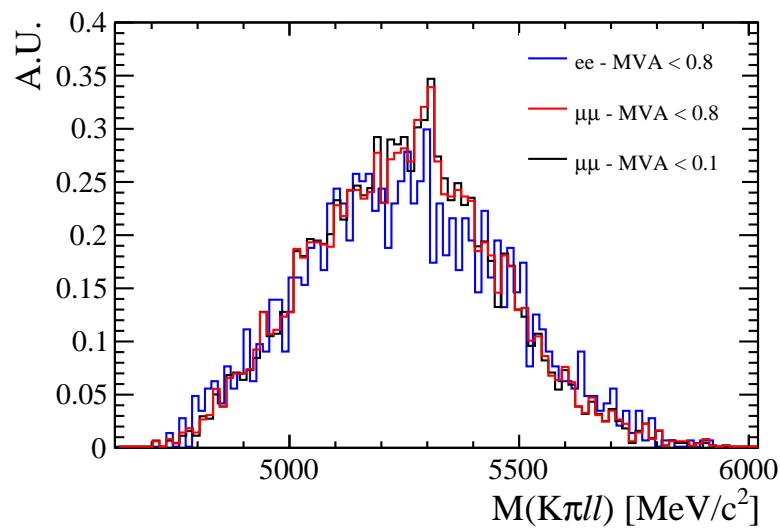


Figure 5.22: Distributions of the  $m(K\pi\ell\ell)$  invariant mass for  $B^0 \rightarrow K^{*0}\ell^+\ell^-$  candidates selected with a reversed cut on the neural network output.

- $B_s^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$ : described using the same PDF adopted for the signal, but a different central value,  $m_0$ , which is set at the  $B_s^0$  nominal mass. The normalisation is fixed to the  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+\mu^-)$  yield returned by the muon fit after correcting for efficiency differences between final states with muons and electrons;

The  $J/\psi$  mass constraint has the effect of pushing the partially-reconstructed background away from the peak outside the fit window. The  $J/\psi$  control sample is selected using the requirement that the 4-body mass constrained using `DecaTreeFitter` is above 5150 MeV/ $c$ , which explicitly removes the partially-reconstructed background; this cut does not produce significant distortion to the unconstrained invariant mass distribution in the considered window. For these reasons this background does not need to be modelled in either of these cases. For the fit to  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  candidates, which includes a  $\psi(2S)$  mass constraint, only the combinatorial background is considered and described using an exponential function.

### 5.7.2.3 Summary of the fit to the electron samples

In summary, the free parameters in the fit to data are:

- the  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$ ,  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  and  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$  yields in each trigger category;
- the  $r_{ee}$  ratio common to all trigger categories; one for the low, one for the central- and one for the high- $q^2$  region;
- one mass shift,  $m'$ , and one width scale factor,  $c$ , for the signal PDF common between  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  and  $B^0 \rightarrow K^{*0}e^+e^-$  in all intervals, but different for the three trigger categories and for  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  and  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$ ;

- the yield and slope, when applicable (e.g. no slope at high- $q^2$ ), of the combinatorial background in each trigger category and for each channel;
- the yield of the backgrounds when not constrained or fixed as described in the previous section.

Fits to simulated  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  candidates are shown in Appendix E, while fits to real candidates are shown in Fig. 5.23 for the normalisation channel, in Fig. 5.24 for the rare channel and in Fig. 5.25 for the control channels. For simplicity the latter two figures show the sum of the three trigger categories, while the separate plots are reported in Appendix F, where fitted parameters are also reported on the plots. In the high- $q^2$  interval, above  $15 \text{ GeV}^2/c^4$ , the efficiency for the L0Hadron trigger becomes very low as the  $K^{*0}$  has very low momentum. In this region only 9 candidates are found spread in the interval  $4500 < m(K\pi ee) < 6000 \text{ MeV}/c^2$ . Therefore only L0E and L0I triggered events are fitted for this region.

### 5.7.3 Event yields

Table 5.8 reports raw yields obtained from the fits described in the previous subsections. The values for the rare channels and  $\gamma(ee)$  are not parameters free to vary in the fits but, as described in Sec. 5.7, they are parameterised as a function of the number of resonant candidates found and the ratios  $r_{ee}$  and  $r_{\mu\mu}$  between the resonant and rare branching fractions; the values in the tables are derived from the ratios.

Table 5.8: Summary of the raw yields obtained from the invariant mass fits. The uncertainty is statistical.

| Sample   | $\gamma(ee)$ | $J/\psi(ee)$     | $\psi(2S)(ee)$ |
|----------|--------------|------------------|----------------|
| $\mu\mu$ | –            | $373755 \pm 641$ | –              |
| $ee$ L0E | $614 \pm 35$ | $42797 \pm 260$  | $2701 \pm 62$  |
| $ee$ L0H | $262 \pm 24$ | $3680 \pm 79$    | $58 \pm 10$    |
| $ee$ L0I | $382 \pm 39$ | $10804 \pm 138$  | $569 \pm 32$   |

| Sample   | low- $q^2$   | central- $q^2$ | high- $q^2$  |
|----------|--------------|----------------|--------------|
| $\mu\mu$ | $475 \pm 24$ | $636 \pm 29$   | $679 \pm 29$ |
| $ee$ L0E | $117 \pm 12$ | $89 \pm 13$    | $158 \pm 26$ |
| $ee$ L0H | $44 \pm 8$   | $18 \pm 7$     | –            |
| $ee$ L0I | $72 \pm 11$  | $38 \pm 9$     | $52 \pm 13$  |

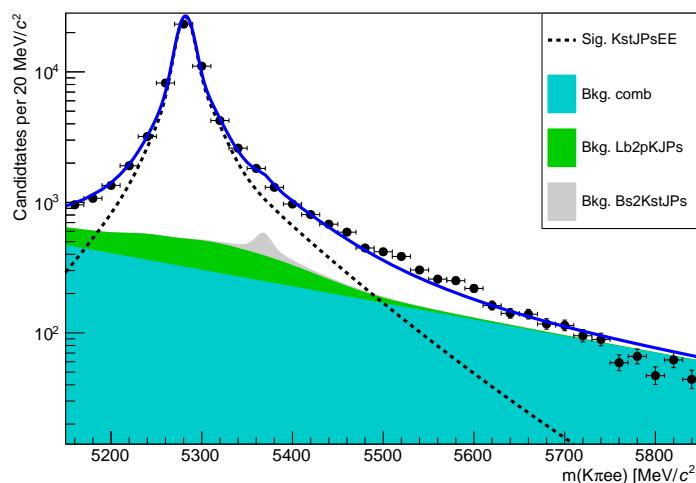


Figure 5.23: Fit to the mass constrained invariant mass,  $m(K\pi ee)_{J/\psi}$ , of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  candidates. The dashed black line represents the signal and the shaded shapes the backgrounds.

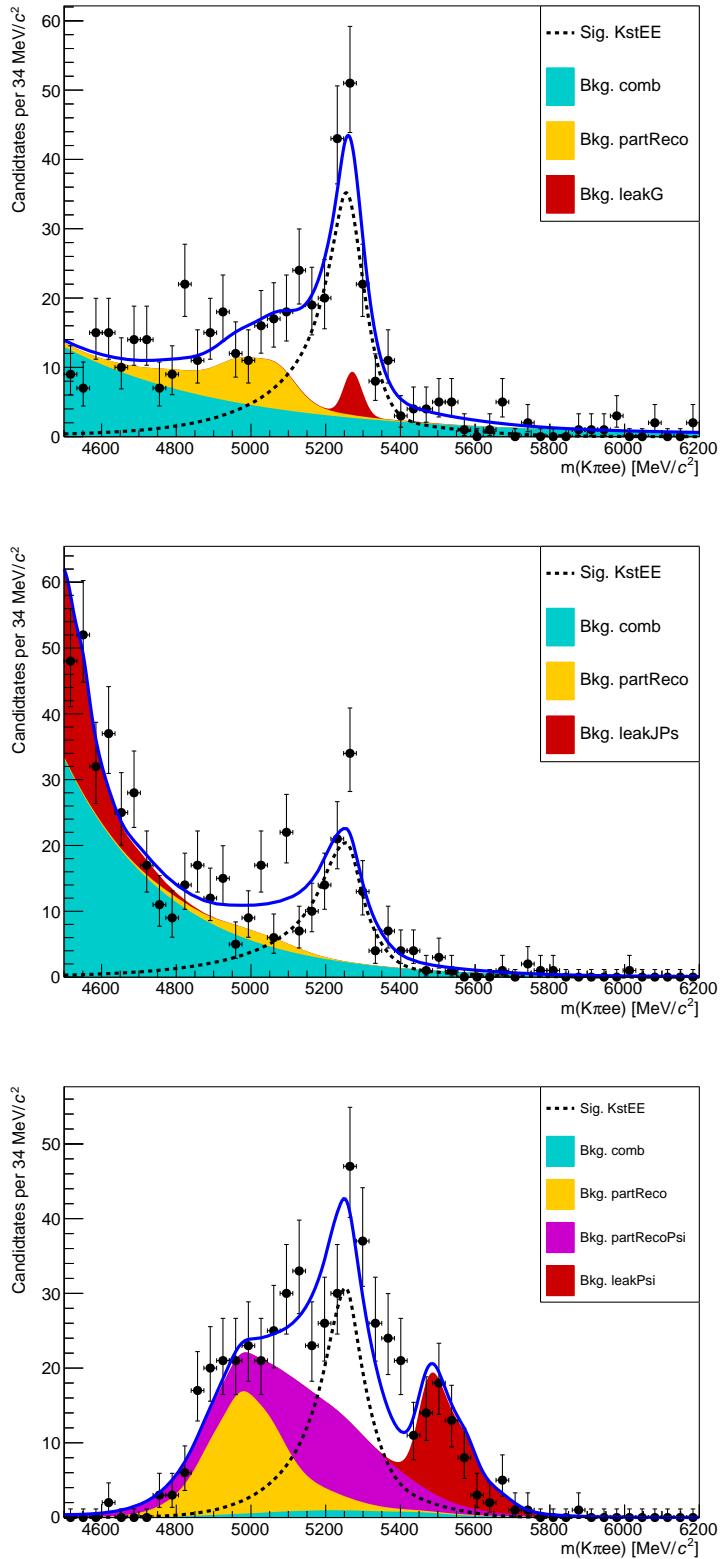


Figure 5.24: Fit to the  $m(K\pi ee)$  invariant mass of  $B^0 \rightarrow K^{*0}e^+e^-$  candidates. From top to bottom for the low-, central- and high- $q^2$  intervals. The dashed black line represents the signal and the shaded shapes the backgrounds.

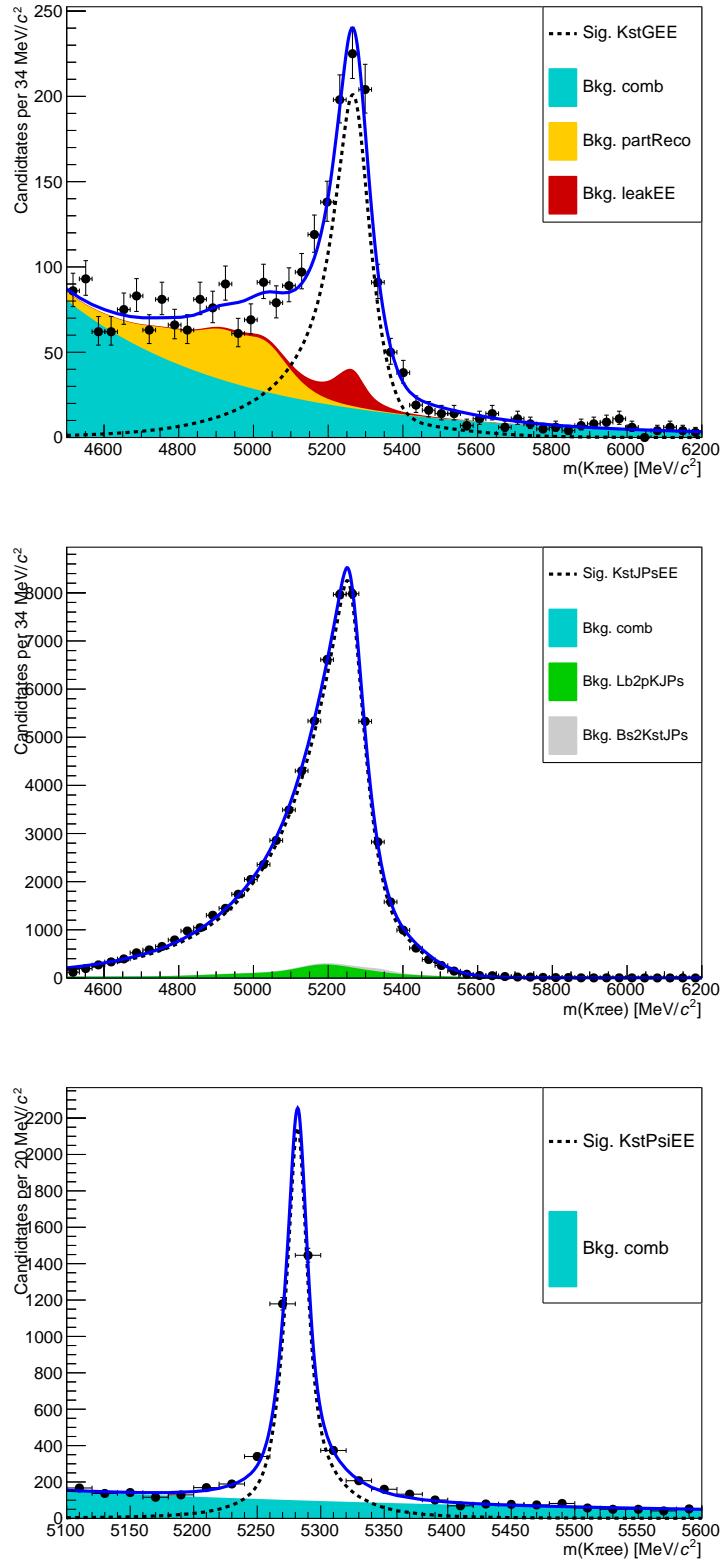


Figure 5.25: Fit to the  $m(K\pi ee)$  invariant mass of control channel candidates. From top to bottom: the invariant mass distribution without mass constraint of  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$  and  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  candidates and the constrained invariant mass,  $m(K\pi ee)_\psi$ , of  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  candidates. The dashed black line represents the signal and the shaded shapes the backgrounds.

## 5.8 Efficiency

The efficiency for each of the decay channels is calculated according to the formula

$$\varepsilon^{tot} = \varepsilon^{\text{geom}} \cdot \varepsilon^{\text{reco|geom}} \cdot \varepsilon^{\text{PID|reco}} \cdot \varepsilon^{\text{trig|PID}} \cdot \varepsilon^{\text{MVA|trig}} \cdot \varepsilon^{\text{BCM|MVA}},$$

where the first term is the efficiency to have final state particles in the LHCb detector acceptance; the second term ( $\varepsilon^{\text{reco|geom}}$ ) carries information on reconstruction and stripping efficiency; the third ( $\varepsilon^{\text{PID|reco}}$ ) corresponds to the efficiency of the PID requirements; the fourth ( $\varepsilon^{\text{trig|PID}}$ ) handles the trigger efficiency for those events which are selected by the pre-selection process; and, finally, the latter term deals with the efficiency of the neural network classifier. Geometric, reconstruction, trigger, MVA and BCM efficiencies are evaluated using simulated data samples with the trigger efficiency for  $B^0 \rightarrow K^{*0}J/\psi$  being cross-checked using the data-driven TISTOS method as described in Sec. 3.6.3. The PID efficiency is calculated with a data-driven method as described in Sec. 5.8.3.

Absolute efficiencies for the muon and electron normalisation channel are reported in Tab. 5.9 and relative efficiencies between the rare and resonant channel,  $\varepsilon^{\ell\ell}/\varepsilon^{J/\psi(\ell\ell)}$ , are listed in Tab. 5.10; these are the efficiencies which are used in the fit.

Table 5.9: Absolute efficiencies for the resonant  $ee$  and  $\mu\mu$  channels.

| $\varepsilon$                    | $\mu\mu$            | $ee$                |                     |                     |
|----------------------------------|---------------------|---------------------|---------------------|---------------------|
|                                  |                     | L0E                 | L0H                 | L0I                 |
| $\varepsilon^{\text{geom}}$      | $0.1598 \pm 0.0005$ |                     | $0.1589 \pm 0.0005$ |                     |
| $\varepsilon^{\text{reco geom}}$ | $0.0947 \pm 0.0001$ |                     | $0.0603 \pm 0.0001$ |                     |
| $\varepsilon^{\text{PID reco}}$  | $0.8148 \pm 0.0000$ |                     | $0.8222 \pm 0.0000$ |                     |
| $\varepsilon^{\text{trig PID}}$  | $0.7511 \pm 0.0005$ | $0.1939 \pm 0.0005$ | $0.0163 \pm 0.0002$ | $0.0707 \pm 0.0003$ |
| $\varepsilon^{\text{MVA trig}}$  | $0.8944 \pm 0.0004$ | $0.8597 \pm 0.0007$ | $0.8983 \pm 0.0006$ | $0.8276 \pm 0.0017$ |
| $\varepsilon^{\text{Total}}$     | $0.0083 \pm 0.0000$ | $0.0013 \pm 0.0000$ | $0.0001 \pm 0.0000$ | $0.0005 \pm 0.0000$ |

Table 5.10: Relative efficiencies,  $\varepsilon^{rel} = \varepsilon^{\ell\ell}/\varepsilon^{J/\psi(\ell\ell)}$ , for the  $ee$  and  $\mu\mu$  channels in the central and high  $q^2$  intervals.

| $\varepsilon$                   | $\mu\mu$            | $ee$                |                     |                     |
|---------------------------------|---------------------|---------------------|---------------------|---------------------|
|                                 |                     | L0E                 | L0H                 | L0I                 |
| <b>low-<math>q^2</math></b>     |                     |                     |                     |                     |
| $\varepsilon^{geom}$            | $1.0200 \pm 0.0091$ |                     | $1.0429 \pm 0.0084$ |                     |
| $\varepsilon^{reco geom}$       | $0.1309 \pm 0.0010$ |                     | $0.1961 \pm 0.0007$ |                     |
| $\varepsilon^{PID reco}$        | $0.9861 \pm 0.0003$ |                     | $0.9718 \pm 0.0001$ |                     |
| $\varepsilon^{trig PID}$        | $0.8103 \pm 0.0048$ | $0.6478 \pm 0.0058$ | $2.5556 \pm 0.0455$ | $1.2748 \pm 0.0139$ |
| $\varepsilon^{MVA trig}$        | $0.9528 \pm 0.0024$ | $0.9568 \pm 0.0014$ | $0.9570 \pm 0.0013$ | $0.9463 \pm 0.0030$ |
| $\varepsilon^{BCM MVA}$         | –                   | $0.9394 \pm 0.0014$ | $0.9492 \pm 0.0013$ | $0.9590 \pm 0.0023$ |
| $\varepsilon^{tot}$             | $0.7810 \pm 0.0168$ | $0.5809 \pm 0.0097$ | $2.2685 \pm 0.0514$ | $1.1073 \pm 0.0200$ |
| <b>central-<math>q^2</math></b> |                     |                     |                     |                     |
| $\varepsilon^{geom}$            | $1.0200 \pm 0.0091$ |                     | $1.0429 \pm 0.0084$ |                     |
| $\varepsilon^{reco geom}$       | $0.1891 \pm 0.0012$ |                     | $0.1580 \pm 0.0006$ |                     |
| $\varepsilon^{PID reco}$        | $0.9784 \pm 0.0002$ |                     | $0.9672 \pm 0.0001$ |                     |
| $\varepsilon^{trig PID}$        | $0.8925 \pm 0.0038$ | $0.7909 \pm 0.0069$ | $2.1344 \pm 0.0439$ | $1.1208 \pm 0.0141$ |
| $\varepsilon^{MVA trig}$        | $0.9068 \pm 0.0024$ | $0.8397 \pm 0.0024$ | $0.8512 \pm 0.0022$ | $0.7946 \pm 0.0054$ |
| $\varepsilon^{BCM MVA}$         | –                   | $0.8960 \pm 0.0020$ | $0.8978 \pm 0.0020$ | $0.9283 \pm 0.0037$ |
| $\varepsilon^{tot}$             | $0.7171 \pm 0.0124$ | $0.8145 \pm 0.0157$ | $2.2235 \pm 0.0595$ | $1.0542 \pm 0.0236$ |
| <b>high-<math>q^2</math></b>    |                     |                     |                     |                     |
| $\varepsilon^{geom}$            | $1.0200 \pm 0.0091$ |                     | $1.0429 \pm 0.0084$ |                     |
| $\varepsilon^{reco geom}$       | $0.1172 \pm 0.0009$ |                     | $0.0530 \pm 0.0003$ |                     |
| $\varepsilon^{PID reco}$        | $1.0286 \pm 0.0001$ |                     | $1.0113 \pm 0.0002$ |                     |
| $\varepsilon^{trig PID}$        | $1.1122 \pm 0.0038$ | $1.5639 \pm 0.0148$ | –                   | $0.8090 \pm 0.0195$ |
| $\varepsilon^{MVA trig}$        | $0.8986 \pm 0.0027$ | $0.8228 \pm 0.0036$ | –                   | $0.7201 \pm 0.0115$ |
| $\varepsilon^{tot}$             | $0.7843 \pm 0.0155$ | $0.6063 \pm 0.0131$ | –                   | $0.2745 \pm 0.0095$ |

### 5.8.1 Geometric efficiency

In order to save disk space, simulated samples only contain decays with final daughters in the LHCb detector acceptance, which can therefore be reconstructed. This corresponds to the requirement for each of the final particles' momenta to have an angle between 10 and 400 mrad from the beam line direction. The efficiency of this cuts is obtained using a generator level simulated sample.

### 5.8.2 Reconstruction efficiency and bin migration

The reconstruction efficiency is here defined as the efficiency to reconstruct each decay channel given that its daughters are into the geometrical acceptance of the detector. This includes both the probability that the final particles generate observable signatures and the efficiency of all the pre-selection requirements described in Sec. 5.6, including those aimed to remove peaking backgrounds. The efficiency of the PID cuts is kept separate as it is known to be not well simulated, while there are reliable data-driven methods which can be used to extract it (see Sec. 5.8.3).

#### 5.8.2.1 Bin migration

It can happen that events generated in a  $q^2$  interval are reconstructed in a different one, this is referred to as “bin migration” and can be due to two different effects. First of all, as the resolution of real detectors is not perfect, candidates close to the bins’ edges of the considered intervals can fall on the wrong side of the edge. This effect is only important in case of non-flat true distributions, as the amount of bin migration in the two directions is different. The second possible source of bin migration are systematic effects due, for example, to the presence of bremsstrahlung photons that cannot be recovered. It is particularly important to take into account the bin migration for the electron channels case because more photons are radiated from the final state and the mass resolution is worse. Figure 5.26 shows the response

matrix for simulated  $B^0 \rightarrow K^{*0} e^+ e^-$  events, which represents the correlation between reconstructed and generated  $q^2$ . In the ideal case of perfect resolution this plot would look like a diagonal line and in the case where no bias is present its slope would be 1. Table 5.11 lists the net amounts of bin migration,  $M_{net}$ , in the considered  $q^2$  intervals defined as:

$$M_{net} = N(\text{in} \rightarrow \text{in}) + N(\text{out} \rightarrow \text{in}) - N(\text{in} \rightarrow \text{out}) \quad (5.14)$$

where  $N(\text{in} \rightarrow \text{in})$  is the number of candidates that are generated and reconstructed inside the considered interval,  $N(\text{out} \rightarrow \text{in})$  the number of candidates that are generated outside the interval but reconstructed inside and  $N(\text{in} \rightarrow \text{out})$  the number of candidates generated inside that fall outside. The reconstruction efficiency is calculated comparing generated and reconstructed samples and therefore already includes bin migration effects. Nevertheless, it is useful to single out this component to better assess the corresponding systematic uncertainty.

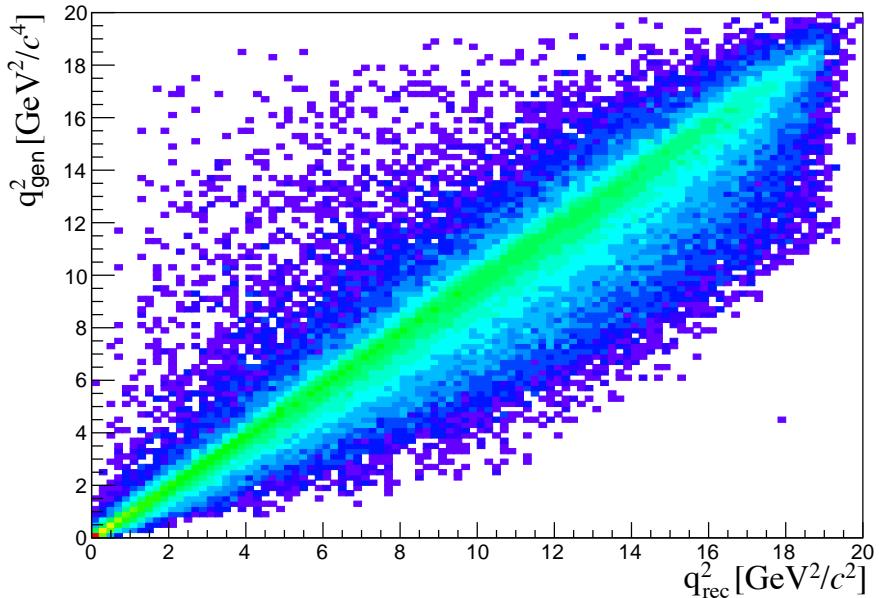


Figure 5.26: Generated versus reconstructed  $q^2$  for simulated  $B^0 \rightarrow K^{*0} e^+ e^-$  events.

### 5.8.3 PID efficiency

The simulation is known not to reliably describe particle ID variables and therefore a data-driven method is used to obtain this efficiency component. This is done using the `PIDCalib` package described in Sec. 2.8.1. Furthermore, the same method is used to weight the simulation in order to calculate the MVA and trigger efficiencies. The `PIDCalib` package allows to divide the phase-space in intervals of quantities relevant for the determination of the PID efficiency and obtain a data-driven efficiency for each interval. For this analysis the phase-space is divided in equi-populated bins of momentum and pseudorapidity of the particle under study. Figure 5.27 shows performance tables for pions, kaons, muons and electrons. Once the efficiency tables are obtained for each particle, the total efficiency is calculated for each candidate as the product of the four final particles efficiencies.  $\varepsilon = \varepsilon_K \cdot \varepsilon_\pi \cdot \varepsilon_{\ell_1} \cdot \varepsilon_{\ell_2}$ . Finally, as the decay channel under study generally has different kinematical distributions than the calibration sample, the total efficiency is found by averaging over simulated events, namely

$$\varepsilon_{PID} = \frac{1}{N} \sum_i^N \varepsilon_K(p_K^i, \eta_K^i) \cdot \varepsilon_\pi(p_\pi^i, \eta_\pi^i) \cdot \varepsilon_\ell(p_{\ell_1}^i, \eta_{\ell_1}^i) \cdot \varepsilon_K(p_{\ell_2}^i, \eta_{\ell_2}^i) \quad (5.15)$$

### 5.8.4 Trigger efficiency

While the trigger efficiency for the muon channels is calculated using simulated events, for the electron channels a combination of simulation and data-driven methods is used. The efficiency of the software stage, HLT, is always obtained from

Table 5.11: Net bin migration amounts ( $M_{net}$ ) in the considered  $q^2$  intervals. Positive values indicate “net in”, negative values “net out”.

| <b>Sample</b> | <b>low-<math>q^2</math></b> | <b>central-<math>q^2</math></b> | <b><math>J/\psi</math></b> | <b>high-<math>q^2</math></b> |
|---------------|-----------------------------|---------------------------------|----------------------------|------------------------------|
| $\mu\mu$      | $0.0002 \pm 0.0001$         | $-0.0021 \pm 0.0003$            | $0.0032 \pm 0.0004$        | $-0.0012 \pm 0.0000$         |
| $ee$          | $0.0268 \pm 0.0005$         | $0.0663 \pm 0.0009$             | $-0.4277 \pm 0.0048$       | $-0.0445 \pm 0.0003$         |

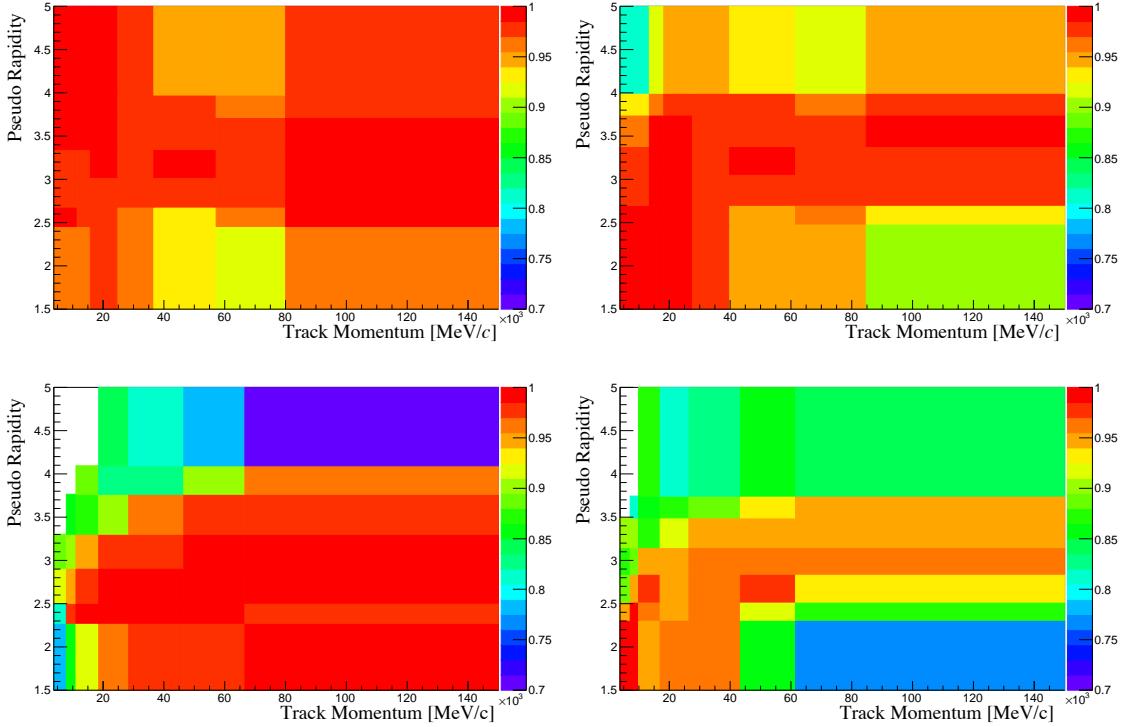


Figure 5.27: Performance tables obtained with data-driven methods for pions (top left), kaons (top right), muons (bottom left) and electrons (bottom right).

simulation, while the efficiency of the hardware stage, L0, is obtained using a data-driven method as described in the next subsection. For both muon and electron channels it is possible to use the resonant sample to cross-check the efficiency obtained using the simulation, as explained in Sec. 5.8.4.2.

#### 5.8.4.1 Electron triggers

For the electron channels data is fitted separately in three trigger categories: L0E, L0H and L0I and therefore the efficiency is calculated separately for each category. While the HLT (1 and 2) efficiency is always derived using simulated events, the L0Electron and L0Hadron efficiencies cannot be reliably modelled in simulation. In fact data-simulation discrepancies are caused by the ageing of the calorimeters, which is not simulated. The ageing modifies the response of the calorimeters with time, which affects the L0 trigger efficiency. Therefore, this must be calibrated using data driven-methods.

Tables of efficiencies are obtained applying the TISTOS method to a calibration sample. For each trigger category these tables contain the efficiency as a function of the  $p_T$  of the considered particle and are given for different calorimeter regions as these have different properties (e.g. cell size) due to the different position with respect to the beam line. The considered regions are the inner and outer HCAL, and the inner, middle and outer ECAL. Figure 5.28 shows data-driven efficiencies for the L0Electron trigger in the three ECAL regions.

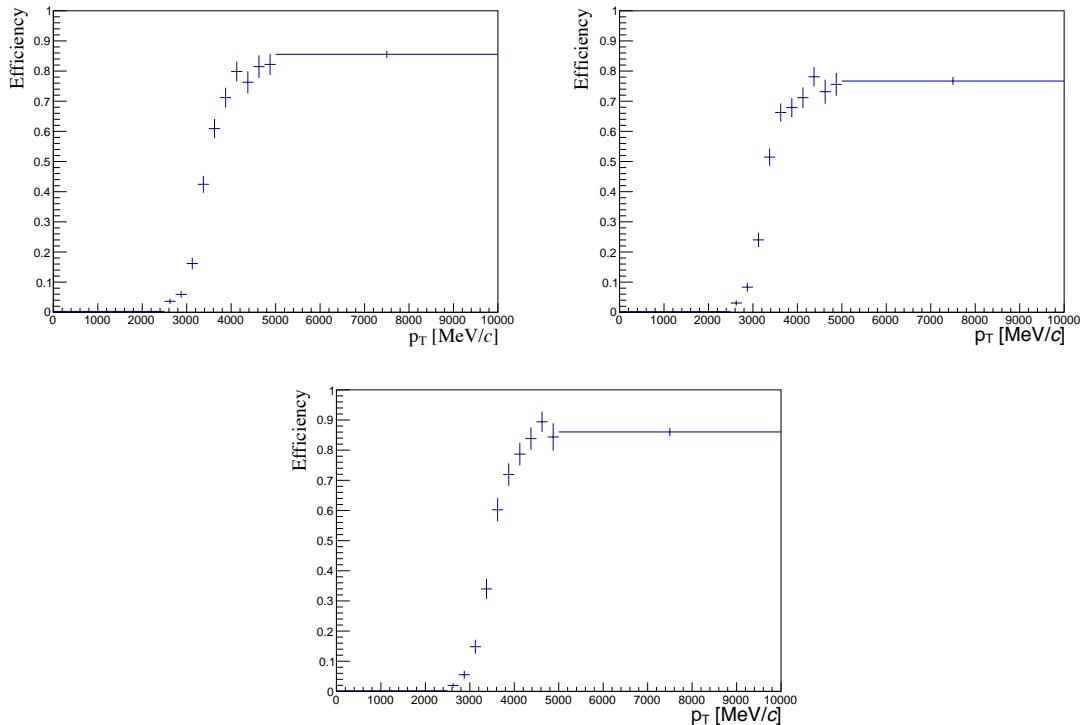


Figure 5.28: Data-driven L0Electron trigger efficiencies as a function of the transverse momentum of the electrons for the three ECAL regions: inner (top left), middle (top right) and outer (bottom).

The probabilities of an event being triggered by L0Electron or L0Hadron are calculated for each candidate as:

$$P_{L0E} = \varepsilon(e^+) + \varepsilon(e^-) - \varepsilon(e^+)\varepsilon(e^-) \text{ and } P_{L0H} = \varepsilon(\pi) + \varepsilon(K) - \varepsilon(\pi)\varepsilon(K).$$

The probability of TIS trigger is defined to be independent of the signal and therefore must be the same in the rare and resonant channels and cancel in their ratio.

Then event by event efficiencies for the three trigger categories are defined to be exclusive in the following way:

- L0E:  $\varepsilon^{L0E} = P_{L0E}$ , namely the probability that at least one electron triggered;
- L0H:  $\varepsilon^{L0H} = P_{L0H} \cdot (1 - P_{L0E})$ , namely the probability that at least one hadron triggered but none of the electrons;
- L0I:  $\varepsilon^{L0I} = (1 - P_{L0H}) \cdot (1 - P_{L0E})$ , namely the probability that neither the hadrons or the electrons in the candidate triggered. Note that in this case  $\varepsilon^{L0I}$  does not correspond to the efficiency of TIS trigger but to the probability that the event does not fall into the L0E or L0H categories.

Finally, as in the PID case, the total efficiency is found averaging over all events of a simulated sample:

$$\varepsilon^{\text{trg}} = \frac{1}{N} \sum_i^N \varepsilon^{\text{trg}}(p_T^i), \quad (5.16)$$

where “trg” is a label indicating the trigger category under consideration.

#### 5.8.4.2 TISTOS cross-check

The efficiency obtained using the simulation is cross-checked applying the TISTOS method, already described in Sec. 3.6.3, to resonant data. For this purpose a sample of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+ \ell^-)$  candidates triggered independent-of-signal (TIS) is used as control sample. As data also contains non negligible amounts of background a narrow interval around the peak, dominated by the signal, is selected and the  $s\mathcal{P}\text{lot}$  method is used to remove residual background in the data sample. Results are shown in Tab. 5.12, where the efficiency obtained using the TISTOS method is compared between data and simulation. These are found to be in agreement for the muon channel, while they show deviations in the electron channels. In particular a significant discrepancy is found, for the L0I category, for which the procedure explained in Sec. 5.8.4.1 does not ensure a correct calibration. The table also reports

Table 5.12: Trigger efficiencies obtained using the TISTOS method on simulated and real  $B^0 \rightarrow K^{*0} J/\psi (\rightarrow \ell^+ \ell^-)$  decays.

| Sample                      | MC                | Data              | Correction factor |
|-----------------------------|-------------------|-------------------|-------------------|
| $J/\psi \rightarrow \mu\mu$ | $0.797 \pm 0.002$ | $0.803 \pm 0.004$ | 1.0073            |
| $J/\psi \rightarrow ee$ L0E | $0.268 \pm 0.002$ | $0.255 \pm 0.004$ | 0.9536            |
| $J/\psi \rightarrow ee$ L0H | $0.028 \pm 0.001$ | $0.026 \pm 0.002$ | 0.9269            |
| $J/\psi \rightarrow ee$ L0I | $0.017 \pm 0.001$ | $0.011 \pm 0.001$ | 0.6760            |

a correction factor obtained according to the formula

$$f = 1 + \frac{\varepsilon_{data}^{\text{TISTOS}} - \varepsilon_{MC}^{\text{TISTOS}}}{\varepsilon_{MC}^{\text{TISTOS}}}, \quad (5.17)$$

which can be used to correct the absolute resonant yields. On the other hand, even though discrepancies are present, they should cancel out in the ratio between the rare and  $J/\psi$  channels; only the residual discrepancy on this ratio, due to the different  $q^2$ , is relevant for the measurement of  $R_{K^{*0}}$ . In order to check if discrepancies cancel out we need to obtain a data-driven efficiency also for the rare channels. To do this the TISTOS efficiency obtained on  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+ \ell^-)$  candidates must be reweighted for the difference in the kinematics between the rare and resonant channels. This is done by determining the TISTOS efficiency as function of the maximum  $p_T$  of the particles that fired L0 (the leptons for L0Electron and L0Muon, the kaon and the pion for L0Hadron, and all final state particles for L0Global). Results are shown in Fig. 5.29 and used to re-weight the distribution of rare simulated candidates. The ratios  $\varepsilon_{\ell\ell}^{tistos}/\varepsilon_{J/\psi}^{tistos}$  obtained using the data-driven method and simulation are compared and found to be fully compatible. This means that, even though the TISTOS correction has an effect on the absolute efficiency of each channel, this becomes negligible on their ratio. Therefore, no correction due to this effect is applied for the calculation of the  $R_{K^{*0}}$  ratio.

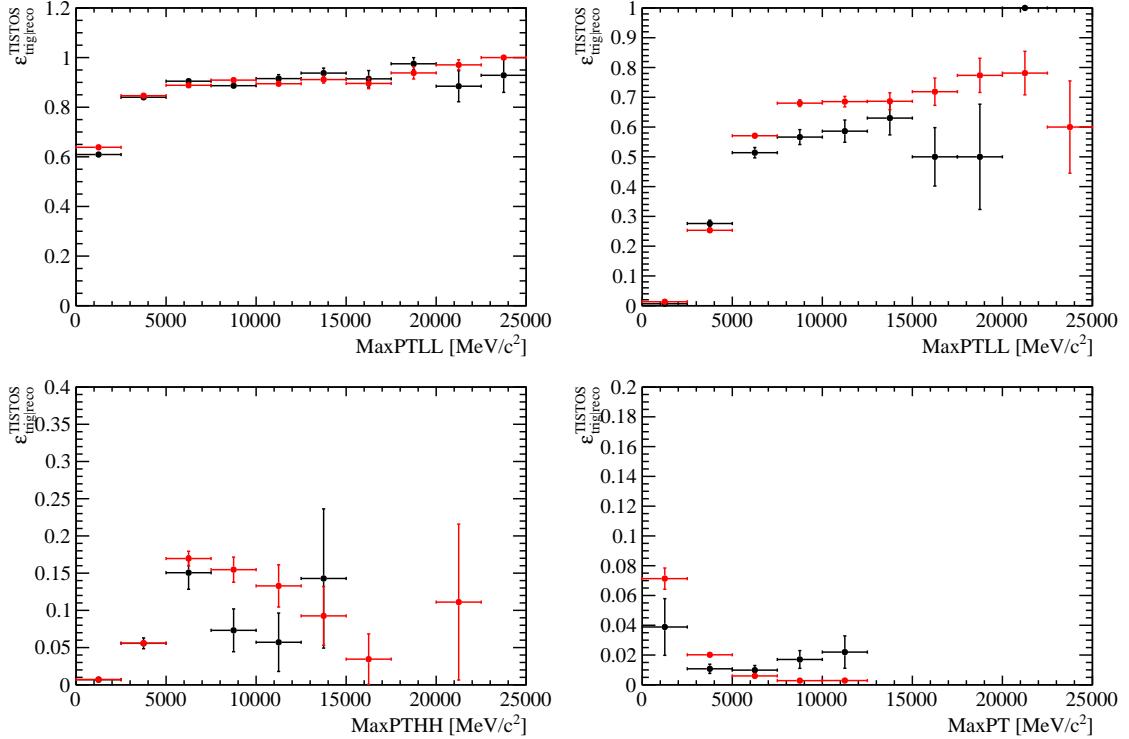


Figure 5.29: Trigger efficiency obtained applying the TISTOS method on  $B^0 \rightarrow J/\psi K^{*0}$  candidates as a function of the maximum  $p_T$  of the two muons (top left) of the two electrons for the L0E category (top right), the maximum  $p_T$  of  $K$  and  $\pi$  for L0H (bottom left) and the maximum  $p_T$  of all the final particles for L0I (bottom right).

### 5.8.5 Neural networks and BCM efficiencies

The neural network and BCM efficiencies are evaluated from fully weighted simulated samples, and separately for each trigger category for the electron channels. In order to check for biases one can compare the efficiency obtained for  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+\ell^-)$  decays with the one obtained for rare  $B^0 \rightarrow K^{*0}\ell^+\ell^-$  decays selected in the same  $q^2$  region used for the resonant case. The ratio between the two should be close to unity with small deviations due the fact that the  $q^2$  interval width is finite and the events are distributed differently inside the interval. This ratio is found to be  $0.997 \pm 0.004$  for the  $\mu\mu$  channels and on average  $0.981 \pm 0.005$  for the  $ee$  channels. Values for the electron channels show a small deviation from unity due to the very large  $q^2$  interval used to select the resonant channel ( $6 - 11$  GeV $^2/c^4$ ).

Table 5.13: Summary of the relative percent systematic uncertainties on  $R_{K^{*0}}$ .

| Source                                      | low- $q^2$ (%) | central- $q^2$ (%) | high- $q^2$ (%) |
|---------------------------------------------|----------------|--------------------|-----------------|
| Signal shape                                | 1.65           | 1.10               | 2.92            |
| Bremsstrahlung categories                   | 0.04           | 0.06               | 0.37            |
| Swap                                        | 0.30           | 0.12               | 0.13            |
| $\Lambda_b^0 \rightarrow p K \ell^+ \ell^-$ | 0.25           | 0.28               | 0.77            |
| Combinatorial                               | 0.00           | 0.02               | 8.02            |
| $J/\psi$ leakage                            | 0.06           | 0.01               | 0.10            |
| $\psi(2S)$ leakage                          | 0.03           | 0.01               | 2.00            |
| RooKeysPdf ( $\rho = 1.1$ )                 | 0.11           | 0.28               | 0.14            |
| RooKeysPdf ( $\rho = 1.3$ )                 | 0.10           | 0.24               | 0.49            |
| Efficiency                                  | 0.65           | 0.74               | 0.83            |
| TISTOS                                      | 2.47           | 2.30               | 2.80            |
| Bin migration                               | 0.69           | 1.43               | 1.19            |

## 5.9 Systematic uncertainties

This section describes the main sources of systematic uncertainty considered. Other sources, which would matter in measurements of absolute quantities, cancel in the ratio between the rare and resonant channels. A list of the systematic uncertainties that are considered and their effect on the  $R_{K^{*0}}$  ratio is summarised in Tab. 5.13. The total uncertainty is evaluated by summing in quadrature the single components. These studies are preliminary.

### 5.9.1 Choice of signal and background PDFs

There is a certain arbitrariness in the choice of PDFs to model signal and background contributions in the invariant mass fits, which could translate into a bias on the final result. The systematic uncertainty due to the parameterisation of line shapes is studied in the following ways.

For the signal PDF:

- *Shape*: in the electron channels the PDF is changed from a Crystal Ball and Gaussian to a Double Crystal Ball. Modifying the PDF has a negligible effect in the muon modes, while it affects the electron ones. Furthermore the data-simulation discrepancy parameters ( $m'$  and  $c$ ) are constrained using the  $B^0 \rightarrow K^{*0}(\gamma \rightarrow e^+e^-)$  sample instead of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$ .
- *Bremsstrahlung categories*: gaussian constraints are applied to the relative fractions of the bremsstrahlung categories, instead of fixing them to the values observed on simulation.

For the background PDFs:

- *Swaps*: a component that describes candidates where the particle identities are swapped is added both to the muon and electron resonant fits, and constrained to the number of candidates expected from simulation.
- $\Lambda_b^0 \rightarrow pK J/\psi (\rightarrow e^+e^-)$ : the normalisation is left free to vary.
- *Combinatorial*: the PDF is changed from an exponential to an anti-MVA cut distribution; the opposite is done for the high- $q^2$  interval, where the anti-MVA shape is the nominal one.
- $\Lambda_b^0 \rightarrow pK \ell^+ \ell^-$ : this background is added to the fit to the rare channel and returns zero yield for both the muon and the electron samples. Therefore this yields no systematic uncertainty.
- *Leakage*: gaussian constraints are applied to the amounts of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)$  leakage in the central- $q^2$  region and to the  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  leakage in the high- $q^2$  region, which are fixed in the default fit.

Furthermore in all case where a simulated sample is used to obtain background shapes and smoothed to obtain a PDF the kernel of the density estimation is varied by  $\pm 0.1$  from the value used in the nominal fit.

### 5.9.2 Efficiency determination

The statistical uncertainty on the efficiency determination due to the simulated or calibration sample sizes is taken as the corresponding systematic uncertainty. A further source of systematic uncertainty associated to the trigger efficiency is estimated using the data-simulation differences observed in Sec. 5.8.4.2. Ratios of efficiencies for the rare to resonant decays are found to be compatible between the electron and muon modes, indicating that the effect on  $R_{K^{*0}}$  is negligible, but the statistical precision on the determinations is taken as an extra systematic uncertainty.

### 5.9.3 Bin migration

The determination of the reconstruction efficiency is affected by the knowledge of the amount of bin migration as explained in Sec. 5.8.2. This amount depends on the shape of the  $q^2$  distribution, which in turn depends on the simulated  $B^0 \rightarrow K^{*0}e^+e^-$  decay model. In order to asses this systematic, simulated samples are generated using different models corresponding to different form factors [122, 123]. The  $q^2$  distributions obtained using each model are compared with the ones obtained using the default one [124]. Figure 5.30 shows normalised ratios between these  $q^2$  distributions and the default one, which are used to reweight the simulation. The amount of bin migration is calculated using the simulation reweighted to reproduce each model; Table 5.14 lists the percent variations obtained. The largest difference between two values is taken as systematic uncertainty.

Table 5.14: Percent variation on the bin migration amount obtained using different form factors models.

| Model             | low- $q^2$ | central- $q^2$ | central- $q^2$ |
|-------------------|------------|----------------|----------------|
| Ball-Zwicky       | -0.3       | 1.0            | 0.2            |
| Colangelo 2pt QCD | 0.4        | 0.4            | 0.8            |
| Melikhov lattice  | 0.1        | -0.4           | -0.4           |

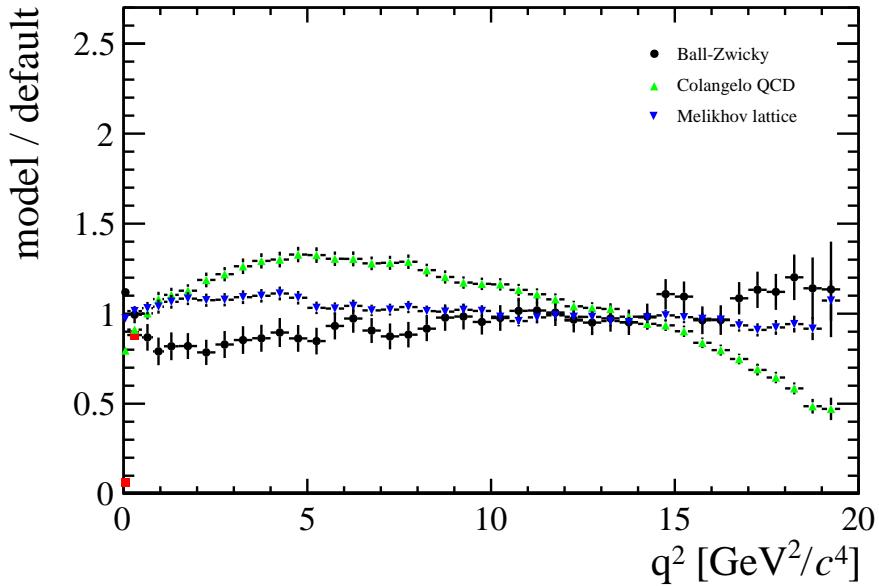


Figure 5.30: Ratios between the  $q^2$  distributions obtained using different form factors models with respect to the default model.

## 5.10 Result extraction and validation

This section presents the procedure to obtain the  $R_{K^{*0}}$  ratio together with methods to validate the robustness of the analysis.

### 5.10.1 $r_{J/\psi}$ sanity check

In order to cross-check the analysis procedure, the ratio between the measured branching ratio of the electron and muon resonant channels is calculated:

$$r_{J/\psi} = \frac{\mathcal{B}(B^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+\mu^-))}{\mathcal{B}(B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-))} = \frac{\varepsilon_{J/\psi(\mu\mu)} \cdot N_{B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-)}}{\varepsilon_{J/\psi(ee)} \cdot N_{B^0 \rightarrow K^{*0}(J/\psi \rightarrow \mu^+\mu^-)}}. \quad (5.18)$$

Compared with absolute branching fractions calculations, the determination of  $r_{J/\psi}$  represents a better sanity test as it is not affected by uncertainties due to the knowledge of the amount of collected luminosity or of the fragmentation fraction: the probability for a  $b$  quark to produce a  $B^0$  meson. These quantities come with large uncertainties but they cancel in the  $r_{J/\psi}$  ratio. As new physics is expected not to

affect tree level  $b \rightarrow c\bar{c}s$  processes the ratio between the  $J/\psi$  channels should be 1, while deviations from unity would signal unaccounted systematic effects.

### 5.10.2 $\mathcal{B}(B^0 \rightarrow K^{*0}\gamma)$

As a further check, the  $B^0 \rightarrow K^{*0}\gamma$  branching fraction can be determined using the ratio

$$r_\gamma = \frac{\mathcal{B}(B^0 \rightarrow K^{*0}\gamma)}{\mathcal{B}(B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+e^-))} = \frac{N_{\gamma(ee)}}{N_{J/\psi(ee)}} \cdot \frac{\varepsilon_{J/\psi(ee)}}{\varepsilon_{\gamma(ee)}}.$$

This is an interesting cross-check as it involves only electrons that are those that could be more easily affected by systematics effects due to the more complex reconstruction process. The measured value can be compared with the one reported in the Review of Particle Physics,  $(4.33 \pm 0.15) \times 10^{-5}$  [2].

### 5.10.3 $R_{K^{*0}}$

The ratio  $R_{K^{*0}}$  is calculated by dividing the  $r_{ee}$  and  $r_{\mu\mu}$  parameters described in Sec. 5.7. These ratios are direct parameters of the fit but they can also be built from the yields in Tab. 5.8 and the efficiencies in Tab. 5.10. In summary the definition of the  $R_{K^{*0}}$  ratio is the following:

$$R_{K^{*0}} = \frac{r_{ee}}{r_{\mu\mu}} = \frac{N_{ee}}{N_{J/\psi(ee)}} \cdot \frac{N_{J/\psi(\mu\mu)}}{N_{\mu\mu}} \cdot \frac{\varepsilon_{J/\psi(ee)}}{\varepsilon_{ee}} \cdot \frac{\varepsilon_{\mu\mu}}{\varepsilon_{J/\psi(\mu\mu)}}. \quad (5.19)$$

As the electron ratio,  $r_{ee}$ , is a shared parameter in the simultaneous fit across the three trigger categories its value is already a combination of the three samples. Results are still blinded.

# CHAPTER 6

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## Conclusions

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In this work rare decays were analysed in order to look for hints of new physics using data collected by the LHCb detector at centre-of-mass energies of 7 and 8 TeV and corresponding to a total integrated luminosity of  $3.0 \text{ fb}^{-1}$ .

First, a measurement of the differential branching fraction of the rare  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay was performed together with the first measurement of angular observables for this decay. Evidence for the signal was found for the first time in the  $q^2$  region between the two charmonium resonances and below the square of the  $J/\psi$  mass, in particular in the  $0.1 < q^2 < 2.0 \text{ GeV}^2/c^4$  interval, where an increased yield is expected due to the vicinity of the photon pole. Due to a larger data sample and a better control of systematic effects, the uncertainty on the measurement in the  $15 < q^2 < 20 \text{ GeV}^2/c^4$  interval are reduced by approximately a factor of three with respect to the previous LHCb measurements. The branching fraction measurements are compatible with SM predictions in the high- $q^2$  region, above the square of the  $J/\psi$  mass, but lie below the predictions in the low- $q^2$  region. Furthermore, an

angular analysis of  $\Lambda_b^0 \rightarrow \Lambda\mu^+\mu^-$  decays is performed, where two forward-backward asymmetries, in the  $p\pi$  and dimuon systems, are measured. The measurements of the  $A_{\text{FB}}^h$  observable are in good agreement with the SM predictions, while for the  $A_{\text{FB}}^\ell$  observable they are consistently above the predictions. Following the publication of these studies improved predictions were produced, which are reported in Appendix D and show a better agreement with the measurement. Theoretical values are now compatible with the branching fraction measurements at low- $q^2$  and overestimate the experimental values at high- $q^2$ . The situation regarding the angular observables is unchanged but the significance of the existing discrepancies is enhanced due to the improved uncertainties on the predicted values.

Secondly, an analysis is set up to test flavour universality between electrons and muons exploiting rare decays. A set of requirements is defined to select the rare and normalisation,  $B^0 \rightarrow K^{*0}\ell^+\ell^-$  and  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow \ell^+\ell^-)$  modes in both electron and muons channels, which includes the definition of a multivariate classifier. The efficiency of the selection requirements are evaluated for all channels. A study of the possible backgrounds is performed, which results in a set of requirements to lower their yield in the selected samples and a set of PDFs to model the remaining contributions in the invariant mass fits. Preliminary fits to the 4-body invariant mass distributions of all channels are performed. Finally, a preliminary study of the systematic uncertainties is presented and a procedure to calculate the result and validate its robustness is defined. The results are currently blinded.



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# APPENDIX A

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## Decay models

---

### A.1 $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$ distribution

The  $q^2$  and angular dependancies of the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decays are modelled based on Ref. [101], where the angular distribution for unpolarised  $\Lambda_b^0$  production is defined as

$$\begin{aligned} W(\theta_\ell, \theta_B, \chi) &\propto \sum_{\lambda_1, \lambda_2, \lambda_j, \lambda'_j, J, J', m, m', \lambda_\Lambda, \lambda'_\Lambda, \lambda_p} h_{\lambda_1 \lambda_2}^m(J) h_{\lambda_1 \lambda_2}^{m'}(J') e^{i(\lambda_j - \lambda'_j)\chi} \\ &\times \delta_{\lambda_j - \lambda_\Lambda, \lambda'_j - \lambda'_\Lambda} \delta_{J, J'} d_{\lambda_j, \lambda_1 - \lambda_2}^J(\theta_\ell) d_{\lambda'_j, \lambda_1 - \lambda_2}^{J'}(\theta_\ell) H_{\lambda_\Lambda \lambda_j}^m(J) H_{\lambda'_\Lambda \lambda'_j}^{m'\dagger}(J') \\ &\times d_{\lambda_\Lambda \lambda_p}^{1/2}(\theta_B) d_{\lambda'_\Lambda \lambda_p}^{1/2}(\theta_B) h_{\lambda_p 0}^B h_{\lambda_p 0}^{B\dagger}. \end{aligned} \quad (\text{A.1})$$

In this formula  $\theta_\ell$  and  $\theta_B$  correspond to the lepton and proton helicity angles,  $\chi$  is angle between dimuon and  $\Lambda$  decay planes (for unpolarised production we are sensitive only to difference in azimuthal angles),  $d_{i,j}^J$  are Wigner d-functions and  $h$ ,  $h^B$  and  $H$  are helicity amplitudes for virtual dimuon,  $\Lambda$  and  $\Lambda_b^0$  decays. The sum runs over all possible helicities with the dimuon being allowed in spin 0 and 1 states ( $J$  and  $J'$ ). The  $m$  and  $m'$  indices run over the vector and axial-vector current contributions.

The production polarisation is introduced by removing  $e^{i(\lambda_j - \lambda'_j)\chi}$  from the expression, swapping small Wigner d-functions  $d_{i,j}^J$  to the corresponding capital ones  $D_{i,j}^J$  which are related as

$$D_{i,j}^J(\theta, \phi) = d_{i,j}^J(\theta) e^{i\phi(i-j)} \quad (\text{A.2})$$

and substitute spin density matrix for  $\delta_{\lambda_j - \lambda_\Lambda, \lambda'_j - \lambda'_\Lambda} \delta_{JJ'}$ . The spin density matrix itself is given by

$$\rho_{\lambda_j - \lambda_\Lambda, \lambda'_j - \lambda'_\Lambda} = \frac{1}{2} \begin{pmatrix} 1 + P_b \cos \theta & P_b \sin \theta \\ P_b \sin \theta & 1 - P_b \cos \theta \end{pmatrix}. \quad (\text{A.3})$$

Those changes lead to the formula

$$\begin{aligned} W(\theta\ell, \theta_B, \chi) &\propto \sum_{\lambda_1, \lambda_2, \lambda_j, \lambda'_j, J, J', m, m', \lambda_\Lambda, \lambda'_\Lambda, \lambda_p} h_{\lambda_1 \lambda_2}^m(J) h_{\lambda_1 \lambda_2}^{m'}(J') \\ &\times \rho_{\lambda_j - \lambda_\Lambda, \lambda'_j - \lambda'_\Lambda} D_{\lambda_j, \lambda_1 - \lambda_2}^J(\theta\ell, \phi_L) D_{\lambda'_j, \lambda_1 - \lambda_2}^{J'}(\theta\ell, \phi_L) H_{\lambda_\Lambda \lambda_j}^m(J) H_{\lambda'_\Lambda \lambda'_j}^{m'\dagger}(J') \\ &\times D_{\lambda_\Lambda \lambda_p}^{1/2}(\theta_B, \phi_B) D_{\lambda'_\Lambda \lambda_p}^{1/2}(\theta_B, \phi_B) h_{\lambda_p 0}^B h_{\lambda_p 0}^{B\dagger}. \end{aligned} \quad (\text{A.4})$$

The lepton amplitudes come directly from Ref. [101], eq. 3. The  $\Lambda$  decay amplitudes are related to the  $\Lambda$  decay asymmetry parameter as

$$\alpha_\Lambda = \frac{|h_{\frac{1}{2}0}^B|^2 - |h_{-\frac{1}{2}0}^B|^2}{|h_{\frac{1}{2}0}^B|^2 + |h_{-\frac{1}{2}0}^B|^2}. \quad (\text{A.5})$$

Finally, the  $\Lambda_b^0$  decay amplitudes receive contributions from vector and axial-vector currents and can be written as

$$H_{\lambda_2, \lambda_j}^m = H_{\lambda_2, \lambda_j}^{Vm} - H_{\lambda_2, \lambda_j}^{Am}. \quad (\text{A.6})$$

Finally, the remaining amplitudes are expressed in terms of form factors (Ref. [101], eq. C6) as

$$\begin{aligned} H_{\frac{1}{2}t}^{Vm} &= \sqrt{\frac{Q_+}{q^2}} \left( M_- F_1^{Vm} + \frac{q^2}{M_1} F_3^{Vm} \right), \\ H_{\frac{1}{2}1}^{Vm} &= \sqrt{2Q_-} \left( F_1^{Vm} + \frac{M_+}{M_1} F_2^{Vm} \right), \\ H_{\frac{1}{2}0}^{Vm} &= \sqrt{\frac{Q_-}{q^2}} \left( M_+ F_1^{Vm} + \frac{q^2}{M_1} F_2^{Vm} \right), \\ H_{\frac{1}{2}t}^{Am} &= \sqrt{\frac{Q_-}{q^2}} \left( M_+ F_1^{Am} - \frac{q^2}{M_1} F_3^{Am} \right), \\ H_{\frac{1}{2}1}^{Am} &= \sqrt{2Q_+} \left( F_1^{Am} - \frac{M_-}{M_1} F_2^{Am} \right), \\ H_{\frac{1}{2}0}^{Am} &= \sqrt{\frac{Q_+}{q^2}} \left( M_- F_1^{Am} - \frac{q^2}{M_1} F_2^{Am} \right), \end{aligned} \quad (\text{A.7})$$

where  $M_\pm = M_1 \pm M_2$ ,  $Q_\pm = M_\pm^2 - q^2$ . The form factors  $F$  are expressed in

terms of dimensionless quantities in eqs. C8 and C9 in Ref. [101]. In our actual implementation form factors calculated in the covariant quark model [101] are used and for the numerical values of the Wilson coefficients Ref. [101] is used.

To assess effect of different form factors on efficiency calculations, an alternative set of form factors is implemented, based on the LQCD calculation from Ref. [105]. The form factors relations are found by comparing eqs. 66 and 68 in Ref. [101] to eq. 51 in Ref. [105]. Denoting LQCD form factors by  $F_i^L$  and dimensionless covariant quark model ones by  $f_i^{XX}$  we have

$$\begin{aligned} f_1^V &= c_\gamma(F_1^L + F_2^L), \\ f_2^V &= -2c_\gamma F_2^L, \\ f_3^V &= c_v(F_1^L + F_2^L), \\ f_1^A &= c_\gamma(F_1^L - F_2^L), \\ f_2^A &= -2c_\gamma F_2^L, \\ f_3^A &= -c_v(F_1^L - F_2^L), \\ f_1^{TV} &= c_\sigma F_2^L, \\ f_2^{TV} &= -c_\sigma F_1^L, \\ f_1^{TA} &= c_\sigma F_2^L, \\ f_2^{TA} &= -c_\sigma F_1^L, \end{aligned}$$

where

$$\begin{aligned} c_\gamma &= 1 - \frac{\alpha_s(\mu^2)}{\pi} \left[ \frac{4}{3} + \ln\left(\frac{\mu}{m_b}\right) \right], \\ c_v &= \frac{2}{3} \frac{\alpha_s(\mu^2)}{\pi}, \\ c_\sigma &= 1 - \frac{\alpha_s(\mu^2)}{\pi} \left[ \frac{4}{3} + \frac{5}{3} \ln\left(\frac{\mu}{m_b}\right) \right]. \end{aligned} \quad (\text{A.8})$$

In the calculations  $\mu = m_b$  is used. For the strong coupling constant, we start from the world average value at the  $Z$  mass,  $\alpha_s(m_Z^2) = 0.1185 \pm 0.0006$  [2], and we translate it to the scale  $m_b^2$  by

$$\alpha_s(\mu^2) = \frac{\alpha_s(m_Z^2)}{1 + \frac{\alpha_s(m_Z^2)}{12\pi} (33 - 2n_f) \ln\left(\frac{\mu^2}{m_Z^2}\right)}, \quad (\text{A.9})$$

where  $n_f = 5$ . The LQCD form factors  $F_1^L$  and  $F_2^L$  can be then taken directly from Ref. [105] and plugged into the code implementing the calculation from Ref. [101].

## A.2 Two-dimensional angular distribution parameters

Expectations values for parameters in the two-dimensional angular distribution for the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay calculated using form factors and numerical inputs from Ref. [101].

| $q^2$ [GeV $^2/c^2$ ] | $A_{FB}^\ell$ | $P_z^\Lambda$ | $f_L$ | $O_P$  | $O_{Lp}$ | $O_{UVA}$ |
|-----------------------|---------------|---------------|-------|--------|----------|-----------|
| 0.1 – 2.0             | 0.082         | -0.9998       | 0.537 | -0.463 | -0.537   | 0.055     |
| 2.0 – 4.0             | -0.032        | -0.9996       | 0.858 | -0.142 | -0.857   | -0.021    |
| 4.0 – 6.0             | -0.153        | -0.9991       | 0.752 | -0.247 | -0.752   | -0.102    |
| V.0 – VA.5            | -0.348        | -0.9834       | 0.508 | -0.478 | -0.505   | -0.239    |
| 15.0 – 16.0           | -0.384        | -0.9374       | 0.428 | -0.524 | -0.413   | -0.280    |
| 16.0 – 18.0           | -0.377        | -0.8807       | 0.399 | -0.513 | -0.368   | -0.294    |
| 18.0 – 20.0           | -0.297        | -0.6640       | 0.361 | -0.404 | -0.260   | -0.314    |
| 1.0 – 6.0             | -0.040        | -0.9994       | 0.830 | -0.170 | -0.830   | -0.027    |
| 15.0 – 20.0           | -0.339        | -0.7830       | 0.385 | -0.461 | -0.3A    | -0.302    |

Table A.1: Prediction for angular observables entering two-dimensional angular distributions. Prediction is based on covariant quark model form factors from Ref. [101].

## A.3 $\Lambda_b^0 \rightarrow J/\psi \Lambda$ distribution

The angular distribution of the  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  decay is modelled using Ref. [125]. The differential rate is written as

$$w(\Omega, \Omega_1, \Omega_2) = \frac{1}{(4\pi)} \sum_{i=0}^{3} \sum_{i=1}^{19} f_{1i} f_{2i}(P_b, \alpha_\Lambda) F_i(\theta, \theta_1, \theta_2, \phi_1, \phi_2), \quad (\text{A.10})$$

The expression uses four observables (angles) and depends on four complex amplitudes  $a_+, a_-, b_+, b_-$  and two real valued parameters for the production polarisation,  $P_b$ , and the  $\Lambda$  decay asymmetry,  $\alpha_\Lambda$ . The angle  $\theta$  is the angle of the  $\Lambda$  momentum in  $\Lambda_b^0$  rest frame with respect to the vector  $\vec{n} = \frac{\vec{p}_{inc} \times \vec{p}_{\Lambda_b^0}}{|\vec{p}_{inc} \times \vec{p}_{\Lambda_b^0}|}$ , where  $\vec{p}_{inc}$  and  $\vec{p}_{\Lambda_b^0}$  are the momenta of incident proton and  $\Lambda_b^0$  in the center of mass system. The angles  $\theta_1$  and  $\phi_1$  are polar and azimuthal angle of the proton coming from the  $\Lambda$  decay in the  $\Lambda$  rest frame with axis defined as  $z_1 \uparrow\uparrow \vec{p}_\Lambda$ ,  $y_1 \uparrow\uparrow \vec{n} \times \vec{p}_\Lambda$ . Finally, the angles  $\theta_2$  and  $\phi_2$  are the angles of the momenta of the muons in  $J/\psi$  rest frame with axes defined as  $z_2 \uparrow\uparrow \vec{p}_{J/\psi}$ ,  $y_2 \uparrow\uparrow \vec{n} \times \vec{p}_{J/\psi}$ .

The distribution depends on the  $\Lambda$  decay asymmetry parameter,  $\alpha_\Lambda$ , the production polarisation  $P_b$  and four complex amplitudes. The  $\alpha_\Lambda$  is measured to be  $0.642 \pm 0.013$  for  $\Lambda$ . The production polarisation  $P_b$  and magnitudes of  $a_+, a_-, b_+$  and  $b_-$  are

measured in Ref. [109]. Phases are not measured therefore, as default all phases are set to zero and then they are randomly varied to calculate the systematic uncertainty.

## APPENDIX B

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### Data-simulation comparison

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This appendix reports a comparison between distributions in data and simulated  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  events. In the plots what is labeled as “Data” is real data in a 20 MeV interval around the  $\Lambda_b^0$  mass, where a sideband subtraction technique to remove background. “Side” is real data for masses above 6 GeV containing mostly combinatorial background. These can be compared to the previous sample to see which variables differ the most. “MC” corresponds to Pythia8  $\Lambda_b^0 \rightarrow J/\psi \Lambda$  simulated events. Finally, the label “MC fully W” refers to the same simulated sample but weighted for the  $\Lambda_b^0$  and  $\Lambda$  kinematics (Sec. 3.3.2) and the decay model (Sec. 3.3.1). Distributions are shown separately for long and downstream events.

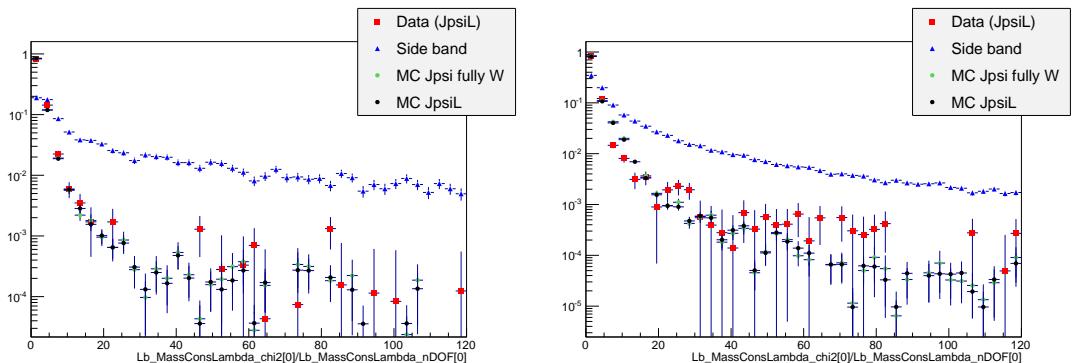


Figure B.1: Distributions of  $\chi^2/NdF$  of the kinematic fit in data and simulation for LL (left) and DD (right) events.

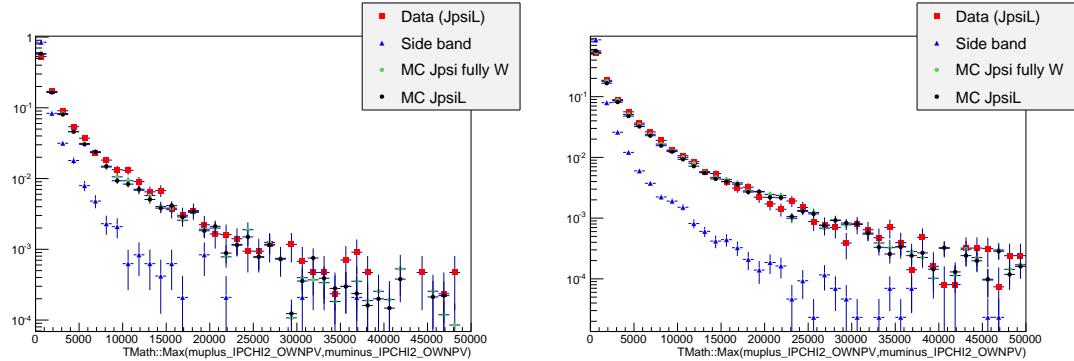


Figure B.2: Distributions of maximum muon  $IP\chi^2$  variable in data and simulation for LL (left) and DD (right) events.

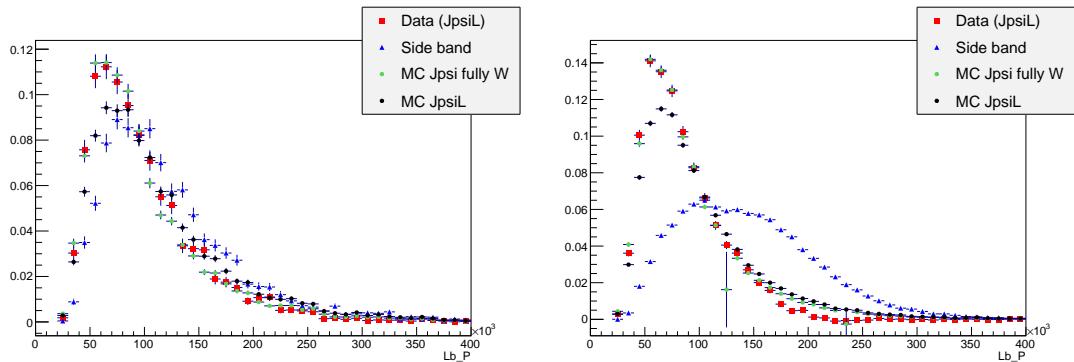


Figure B.3: Distributions of  $\Lambda_b^0$  momentum variable in data and simulation for LL (left) and DD (right) events.

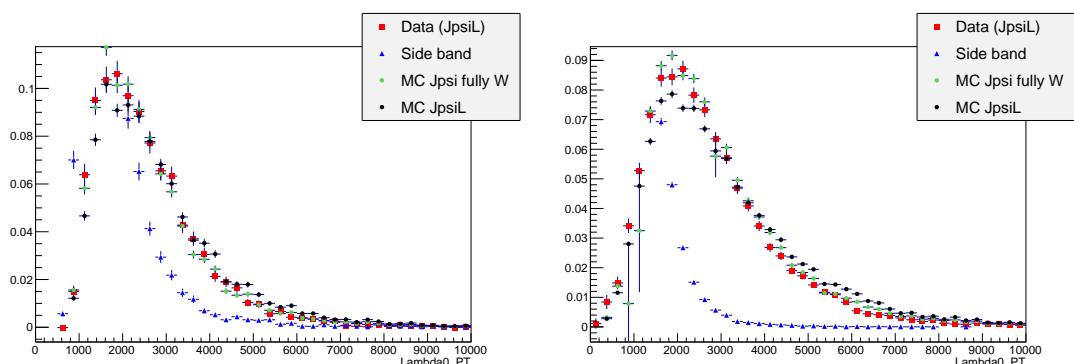


Figure B.4: Distributions of  $\Lambda$  transverse momentum variable in MC, data signal and data background for LL (left) and DD (right) events.

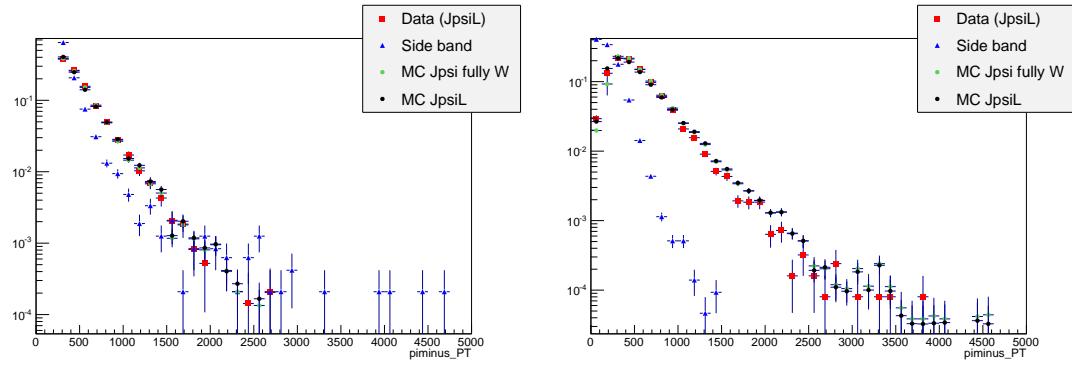


Figure B.5: Distributions of pion transverse momentum variable in data and simulation for LL (left) and DD (right) events.

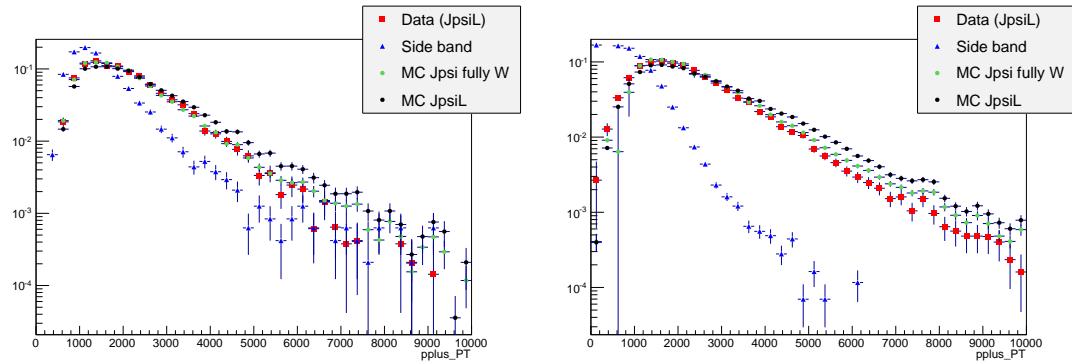


Figure B.6: Distributions of proton transverse momentum variable in data and simulation for LL (left) and DD (right) events.

## APPENDIX C

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### Systematic uncertainties on the efficiency calculation for the $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$ branching fraction analysis.

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This appendix reports systematic uncertainties on absolute and relative efficiencies for the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  branching fraction analysis.

| $q^2$ [ GeV $^2/c^4$ ] | Lifetime | Decay Model | Polarisation |
|------------------------|----------|-------------|--------------|
| 0.1-2.0                | 0.003%   | 0.059%      | 0.145%       |
| 2.0-4.0                | 0.007%   | 0.156%      | 0.145%       |
| 4.0-6.0                | 0.002%   | 0.156%      | 0.144%       |
| 6.0-8.0                | 0.003%   | 0.080%      | 0.144%       |
| 11.0-12.5              | 0.012%   | 0.101%      | 0.144%       |
| 15.0-16.0              | 0.007%   | 0.050%      | 0.144%       |
| 16.0-18.0              | 0.002%   | 0.059%      | 0.145%       |
| 18.0-20.0              | 0.009%   | 0.016%      | 0.145%       |
| 1.1-6.0                | 0.005%   | 0.651%      | 0.144%       |
| 15.0-20.0              | 0.007%   | 0.088%      | 0.144%       |

Table C.1: Absolute values of systematic uncertainties on relative geometric efficiency.

| $q^2$ [ GeV $^2/c^4$ ] | Lifetime | Decay Model | Polarisation |
|------------------------|----------|-------------|--------------|
| 0.1-2.0                | 0.007%   | 0.004%      | 0.008%       |
| 2.0-4.0                | 0.006%   | 0.001%      | 0.009%       |
| 4.0-6.0                | 0.009%   | 0.003%      | 0.008%       |
| 6.0-8.0                | 0.008%   | 0.005%      | 0.008%       |
| 11.0-12.5              | 0.010%   | 0.005%      | 0.009%       |
| 15.0-16.0              | 0.004%   | 0.006%      | 0.008%       |
| 16.0-18.0              | 0.003%   | 0.010%      | 0.010%       |
| 18.0-20.0              | 0.004%   | 0.011%      | 0.008%       |
| 1.1-6.0                | 0.009%   | 0.043%      | 0.010%       |
| 15.0-20.0              | 0.005%   | 0.072%      | 0.009%       |

Table C.2: Absolute values of systematic uncertainties on relative detection efficiency.

| $q^2$ [ GeV $^2/c^4$ ] | Downstream |        |              | Long     |        |              |
|------------------------|------------|--------|--------------|----------|--------|--------------|
|                        | Lifetime   | Model  | Polarisation | Lifetime | Model  | Polarisation |
| 0.1-2.0                | 0.350%     | 0.234% | 0.463%       | 0.066%   | 0.264% | 1.081%       |
| 2.0-4.0                | 0.170%     | 0.640% | 0.488%       | 0.005%   | 0.953% | 1.088%       |
| 4.0-6.0                | 0.073%     | 0.514% | 0.465%       | 0.052%   | 1.607% | 1.087%       |
| 6.0-8.0                | 0.054%     | 0.298% | 0.458%       | 0.011%   | 1.517% | 1.075%       |
| 11.0-12.5              | 0.043%     | 0.030% | 0.469%       | 0.025%   | 0.187% | 1.080%       |
| 15.0-16.0              | 0.078%     | 0.499% | 0.462%       | 0.030%   | 0.110% | 1.082%       |
| 16.0-18.0              | 0.100%     | 0.215% | 0.477%       | 0.021%   | 0.412% | 1.078%       |
| 18.0-20.0              | 0.130%     | 0.044% | 0.471%       | 0.034%   | 0.216% | 1.079%       |
| 1.1-6.0                | 0.137%     | 0.279% | 0.460%       | 0.025%   | 0.656% | 1.078%       |
| 15.0-20.0              | 0.107%     | 0.511% | 0.460%       | 0.016%   | 0.742% | 1.077%       |

Table C.3: Absolute values of systematic uncertainties on relative reconstruction efficiency for long and downstream candidates.

| $q^2$ [ GeV $^2/c^4$ ] | Downstream |        |              | Long     |        |              |
|------------------------|------------|--------|--------------|----------|--------|--------------|
|                        | Lifetime   | Model  | Polarisation | Lifetime | Model  | Polarisation |
| 0.1-2.0                | 0.038%     | 0.226% | 0.070%       | 0.003%   | 0.061% | 0.117%       |
| 2.0-4.0                | 0.009%     | 0.091% | 0.034%       | 0.020%   | 0.072% | 0.076%       |
| 4.0-6.0                | 0.028%     | 0.162% | 0.058%       | 0.018%   | 0.165% | 0.040%       |
| 6.0-8.0                | 0.005%     | 0.080% | 0.075%       | 0.041%   | 0.035% | 0.053%       |
| 11.0-12.5              | 0.002%     | 0.207% | 0.079%       | 0.002%   | 0.148% | 0.076%       |
| 15.0-16.0              | 0.036%     | 0.094% | 0.035%       | 0.022%   | 0.021% | 0.089%       |
| 16.0-18.0              | 0.023%     | 0.027% | 0.029%       | 0.023%   | 0.003% | 0.031%       |
| 18.0-20.0              | 0.017%     | 0.145% | 0.034%       | 0.008%   | 0.199% | 0.063%       |
| 1.1-6.0                | 0.024%     | 0.215% | 0.029%       | 0.012%   | 0.733% | 0.051%       |
| 15.0-20.0              | 0.025%     | 0.220% | 0.031%       | 0.004%   | 0.108% | 0.029%       |

Table C.4: Absolute values of systematic uncertainties on relative trigger efficiency for long and downstream candidates.

| $q^2$ [GeV $^2/c^4$ ] | Downstream |        |              | Long     |        |              |
|-----------------------|------------|--------|--------------|----------|--------|--------------|
|                       | Lifetime   | Model  | Polarisation | Lifetime | Model  | Polarisation |
| 0.1-2.0               | 0.022%     | 0.019% | 0.025%       | 0.060%   | 0.106% | 0.072%       |
| 2.0-4.0               | 0.127%     | 0.267% | 0.017%       | 0.095%   | 0.002% | 0.031%       |
| 4.0-6.0               | 0.116%     | 0.106% | 0.045%       | 0.081%   | 0.139% | 0.119%       |
| 6.0-8.0               | 0.111%     | 0.186% | 0.020%       | 0.085%   | 0.387% | 0.047%       |
| 11.0-12.5             | 0.008%     | 0.056% | 0.017%       | 0.057%   | 0.030% | 0.027%       |
| 15.0-16.0             | 0.002%     | 0.004% | 0.066%       | 0.070%   | 0.124% | 0.023%       |
| 16.0-18.0             | 0.024%     | 0.088% | 0.027%       | 0.068%   | 0.105% | 0.023%       |
| 18.0-20.0             | 0.031%     | 0.050% | 0.027%       | 0.180%   | 0.506% | 0.077%       |
| 1.1-6.0               | 0.118%     | 0.164% | 0.037%       | 0.080%   | 0.183% | 0.058%       |
| 15.0-20.0             | 0.001%     | 0.125% | 0.037%       | 0.102%   | 0.541% | 0.034%       |

Table C.5: Absolute values of systematic uncertainties on relative MVA efficiency for long and downstream candidates.

| $q^2$ [GeV $^2/c^4$ ] | Reconstruction | Trigger | MVA    |
|-----------------------|----------------|---------|--------|
| 0.1-2.0               | 0.612%         | 0.250%  | 0.173% |
| 2.0-4.0               | 0.515%         | 0.246%  | 0.223% |
| 4.0-6.0               | 0.408%         | 0.180%  | 0.272% |
| 6.0-8.0               | 0.412%         | 0.090%  | 0.218% |
| 11.0-12.5             | 0.175%         | 0.047%  | 0.103% |
| 15.0-16.0             | 0.962%         | 0.010%  | 0.141% |
| 16.0-18.0             | 1.173%         | 0.037%  | 0.103% |
| 18.0-20.0             | 1.557%         | 0.050%  | 0.122% |
| 1.1-6.0               | 0.475%         | 0.220%  | 0.246% |
| 15.0-20.0             | 1.254%         | 0.040%  | 0.083% |

Table C.6: Values of DD vertexing systematic uncertainties on relative reconstruction, trigger and MVA efficiencies for downstream candidates.

## APPENDIX D

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### Improved predictions for $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$ observables.

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The publication of the results included in this thesis triggered interest in the theory community, which produced improved lattice calculations and predictions [126]. This section reports the measured quantities with the new predictions overlaid as reported in Ref. [126].

|                                                    | <b>Prediction</b>    | <b>Measurement</b>     |
|----------------------------------------------------|----------------------|------------------------|
| $\langle d\mathcal{B}/dq^2 \rangle_{[15, 20]}$     | $0.756 \pm 0.070$    | $1.20 \pm 0.27$        |
| $\langle F_L \rangle_{[15, 20]}$                   | $0.409 \pm 0.013$    | $0.61^{+0.11}_{-0.14}$ |
| $\langle A_{\text{FB}}^\ell \rangle_{[15, 20]}$    | $-0.350 \pm 0.013$   | $-0.05 \pm 0.09$       |
| $\langle A_{\text{FB}}^\Lambda \rangle_{[15, 20]}$ | $-0.2710 \pm 0.0092$ | $-0.29 \pm 0.08$       |

Table D.1: Comparison of predictions for the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  observables with the LHCb data presented in this thesis in the interval  $[15, 20]$   $\text{GeV}^2/c^4$ , where the measurement is most precise.

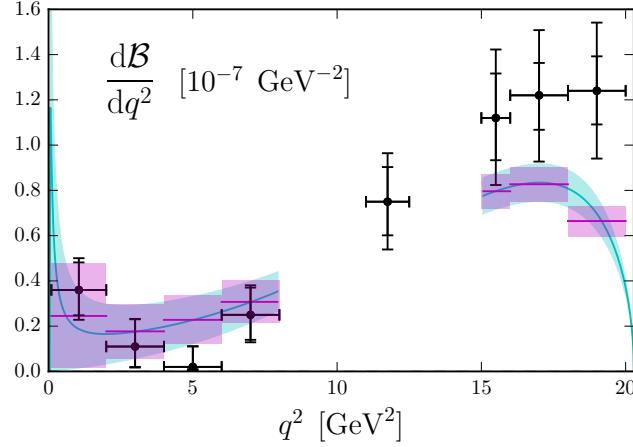


Figure D.1: Measurement of the differential branching fraction of the  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$  decay as a function of  $q^2$  already presented in Ch. 3 with improved Standard Model predictions from Ref. [126] overlaid.

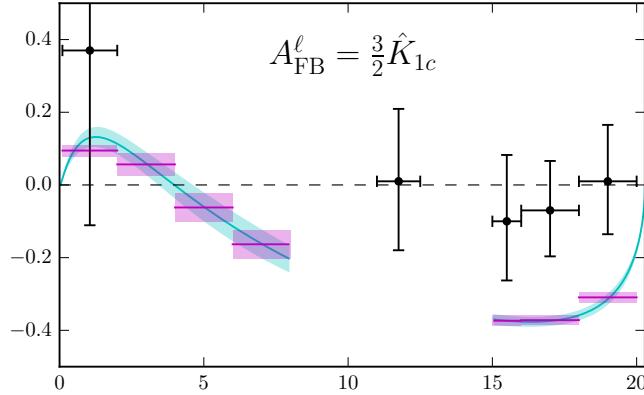


Figure D.2: Measurement of the lepton side forward-backward asymmetry,  $A_{FB}^\ell$ , as a function of  $q^2$  already presented in Ch. 4 with improved Standard Model predictions from Ref. [126] overlaid.

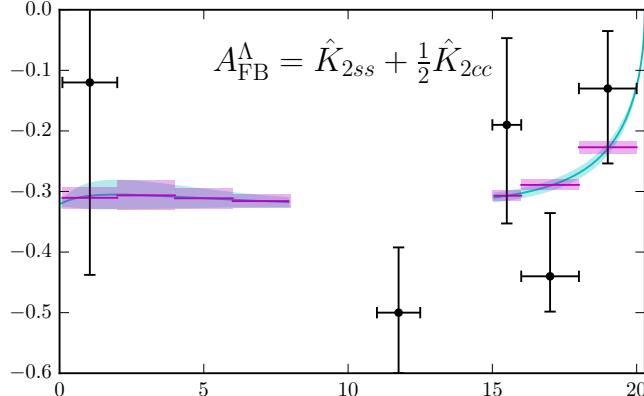


Figure D.3: Measurement of the hadron side forward-backward asymmetry,  $A_{FB}^h$ , as a function of  $q^2$  already presented in Ch. 4 with improved Standard Model predictions from Ref. [126] overlaid.

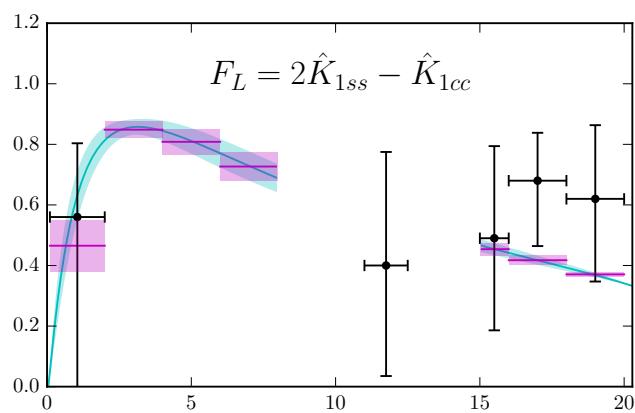


Figure D.4: Measurement of the fraction of longitudinally polarised dimuons,  $f_L$ , as a function of  $q^2$  already presented in Ch. 4 with improved Standard Model predictions from Ref. [126] overlaid.

## APPENDIX E

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### Invariant mass fits to $B^0 \rightarrow K^{*0}\ell^+\ell^-$ simulated candidates

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This appendix contains fits to the  $m(K\pi\mu\mu)$  and  $m(K\pi ee)$  invariant mass of  $B^0 \rightarrow K^{*0}\ell^+\ell^-$  simulated candidates used to constrain parameters in the fit to data.

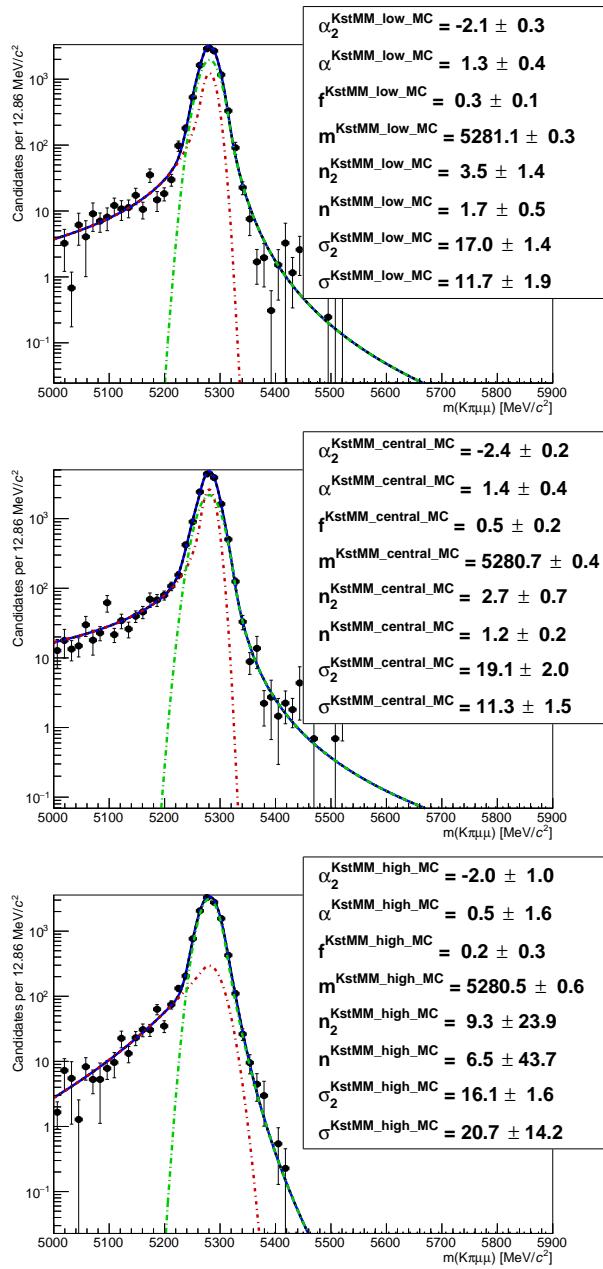


Figure E.1: Fitted  $m(K\pi\mu\mu)$  mass spectrum for simulated events in the low (top), central (medium) and high (bottom)  $q^2$  intervals.

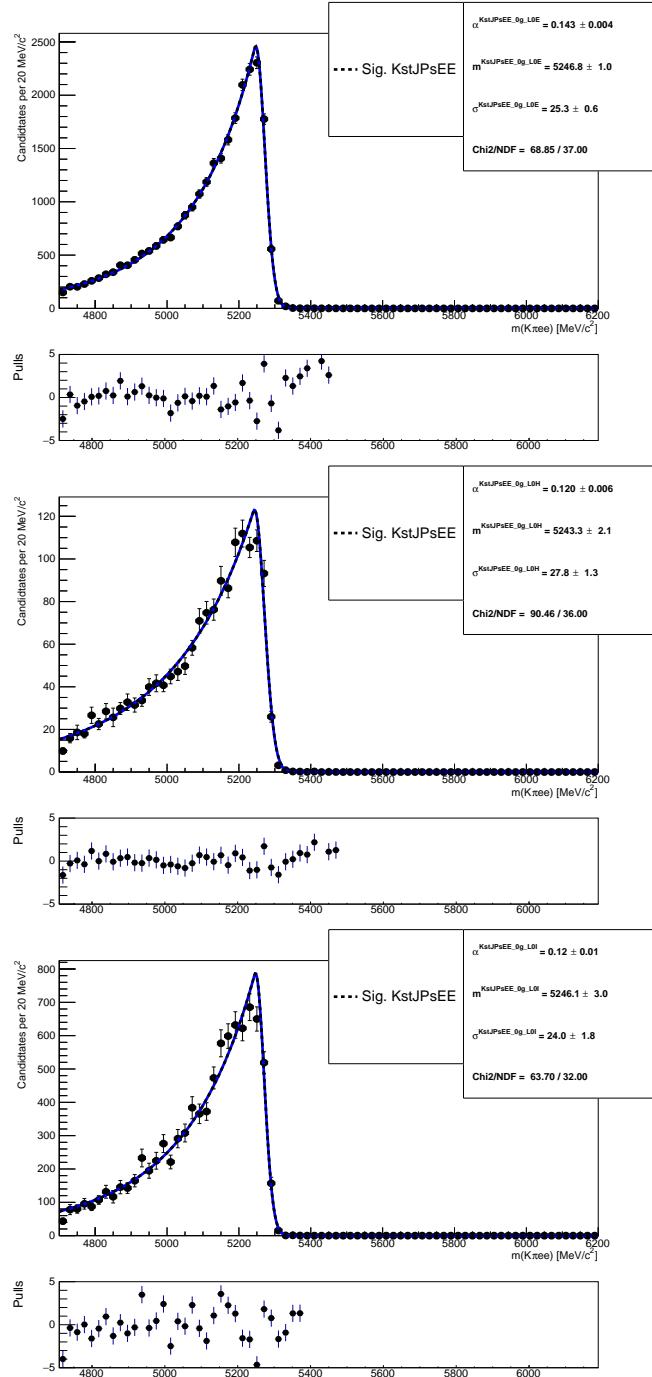


Figure E.2: Fitted  $m(K\pi ee)$  mass spectrum of  $B^0 \rightarrow K^{*0} J/\psi (J/\psi \rightarrow ee)$  simulated events in the three trigger categories and no photon emitted.

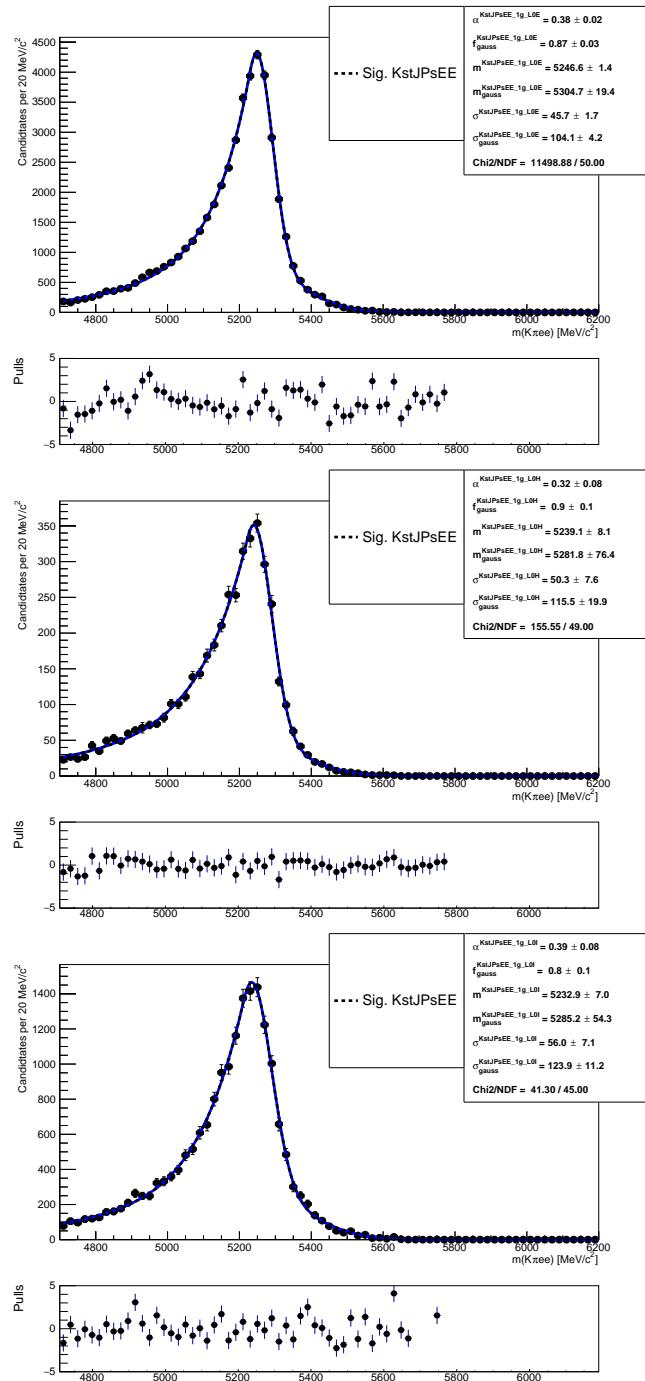


Figure E.3: Fitted  $m(K\pi ee)$  mass spectrum of  $B^0 \rightarrow K^{*0} J/\psi (J/\psi \rightarrow ee)$  simulated events in the three trigger categories and one photon emitted.

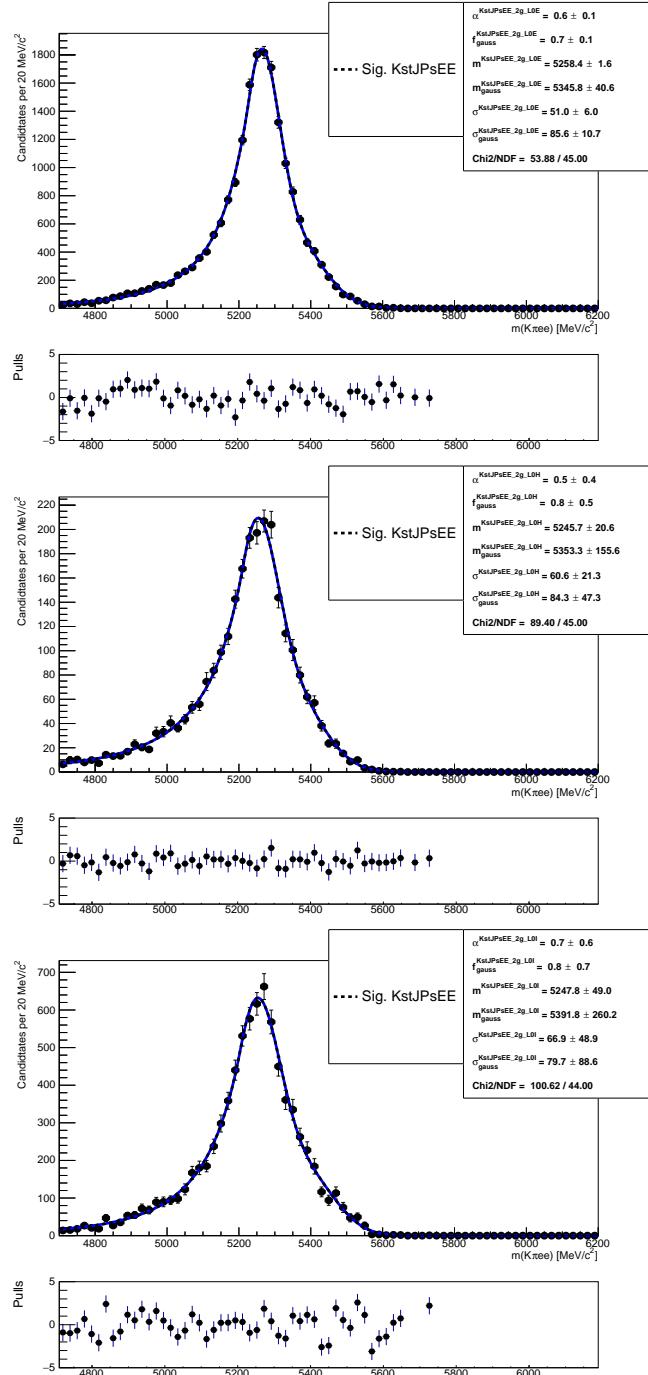


Figure E.4: Fitted  $m(K\pi ee)$  mass spectrum of  $B^0 \rightarrow K^{*0} J/\psi (J/\psi \rightarrow ee)$  simulated events in the three trigger categories and two photons emitted.

## APPENDIX F

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### Invariant mass fits to $B^0 \rightarrow K^{*0}e^+e^-$ candidates divided in trigger categories

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This appendix contains fits to the  $m(K\pi ee)$  invariant mass of rare and control channel candidates separately in the tree trigger categories. Each trigger category is always fit with its own PDF but in the main text only their sum is shown for simplicity.

213 APPENDIX F. INVARIANT MASS FITS TO  $B^0 \rightarrow K^{*0} E^+ E^-$  CANDIDATES DIVIDED IN TRIGGER CATEGORIES

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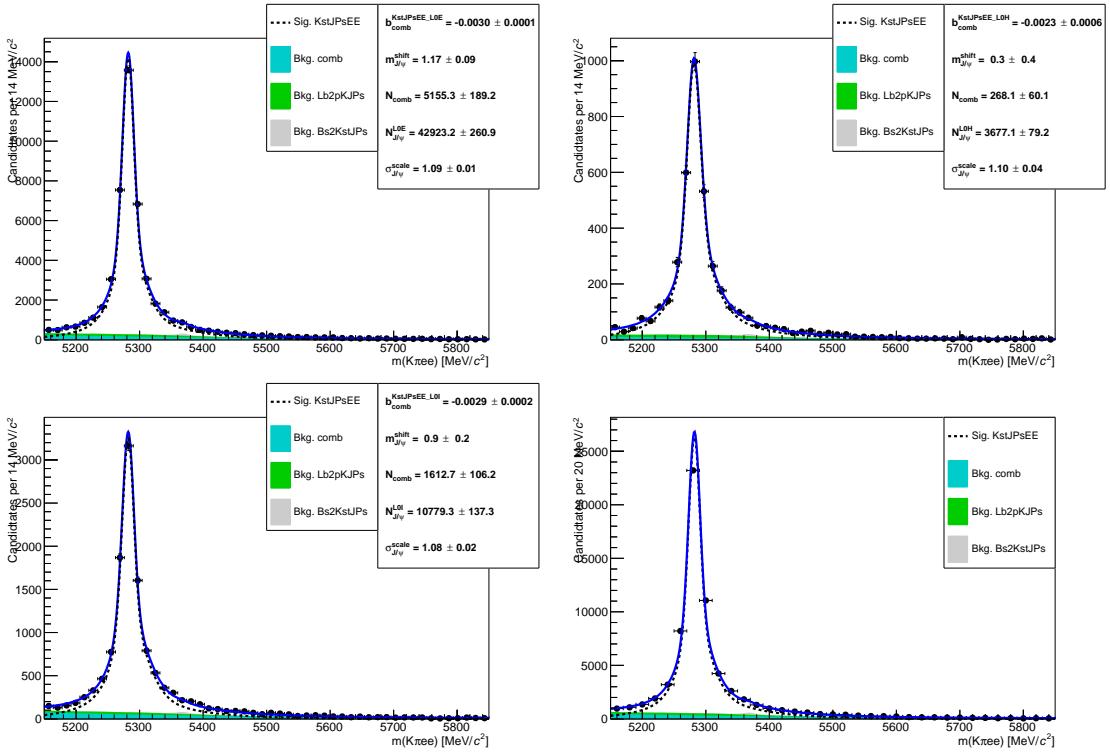


Figure F.1: Fit to the  $m(K\pi ee)$  invariant mass of  $B^0 \rightarrow K^{*0}(J/\psi \rightarrow e^+ e^-)$  candidates in the three trigger categories (L0E, L0H and L0I) separately, and (bottom right) combined. The dashed black line (shaded shapes) represents the signal (background) PDF.

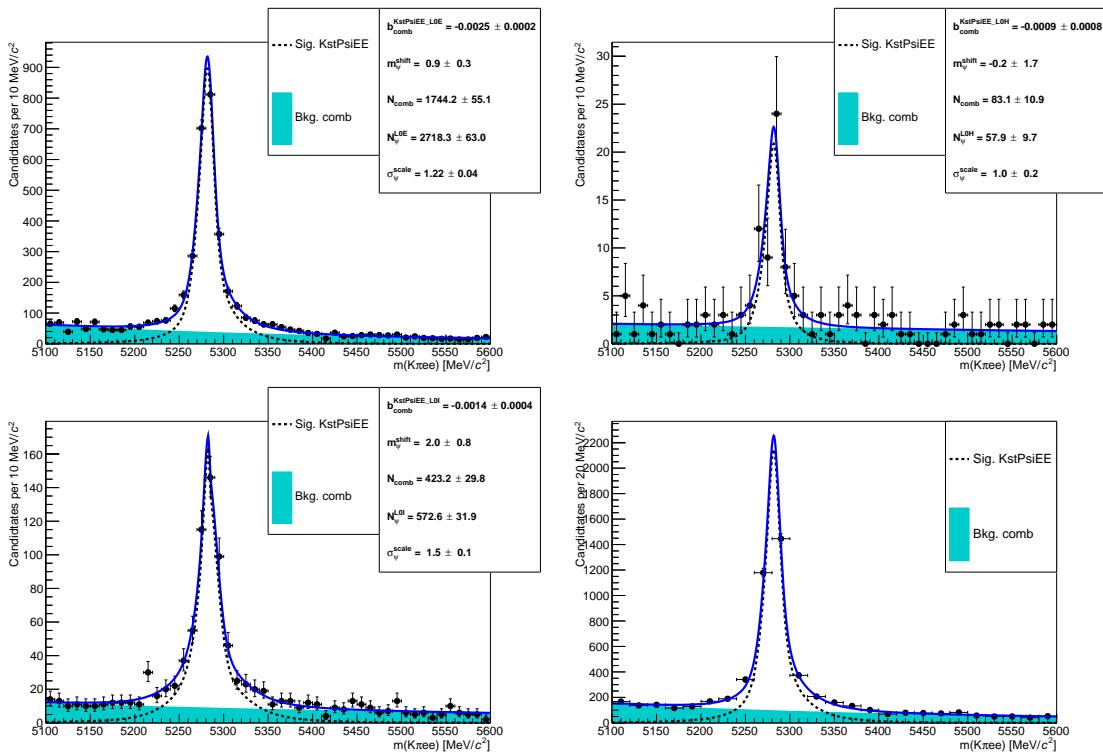


Figure F.2: Fit to the  $m(K\pi ee)$  invariant mass of  $B^0 \rightarrow K^{*0}(\psi(2S) \rightarrow e^+e^-)$  candidates in the three trigger categories (L0E, L0H and L0I) separately, and (bottom right) combined. The dashed black line (shaded shapes) represents the signal (background) PDF.

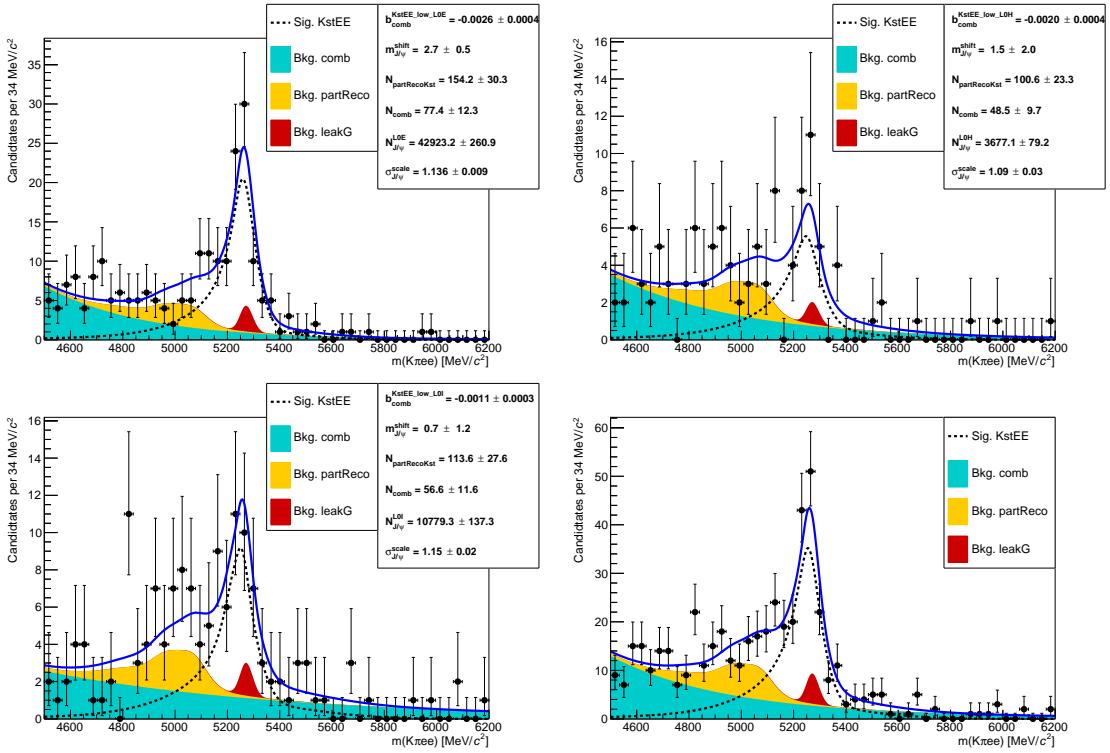


Figure F.3: Fit to the  $m(K\pi ee)$  invariant mass of  $B^0 \rightarrow K^{*0} e^+ e^-$  candidates at low- $q^2$  in the three trigger categories (L0E, L0H and L0I) separately, and (bottom right) combined. The dashed black line (shaded shapes) represents the signal (background) PDF.

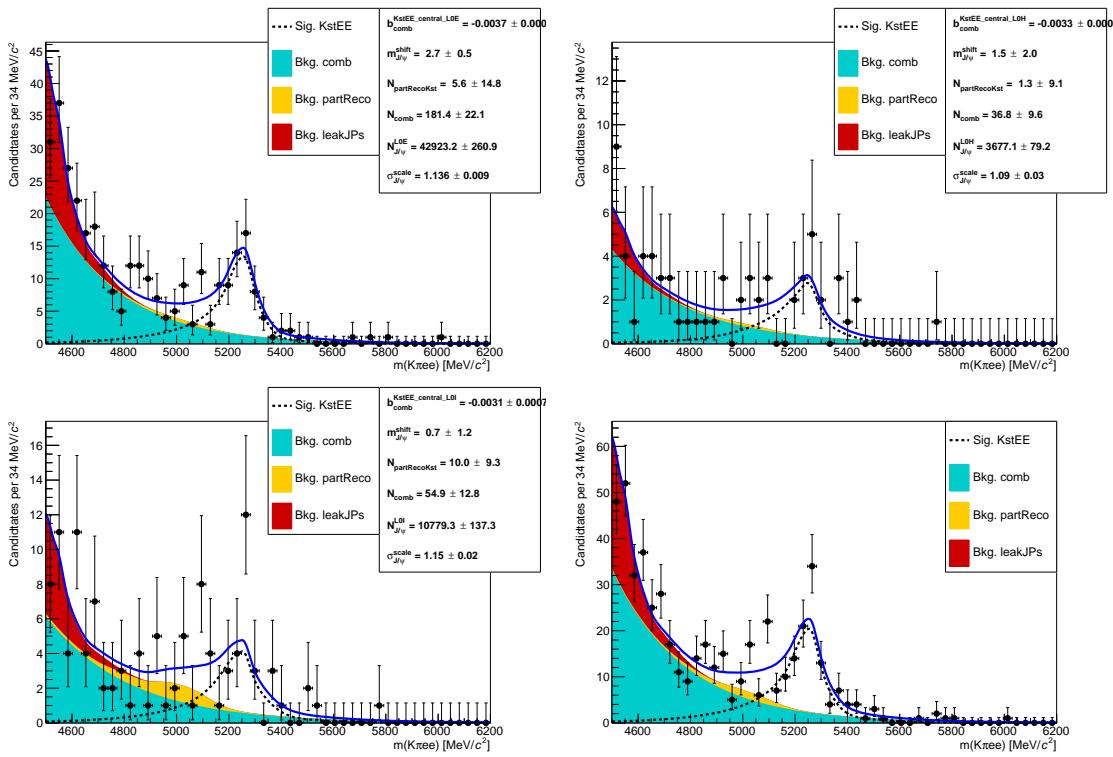


Figure F.4: Fit to the  $m(K\pi ee)$  invariant mass of  $B^0 \rightarrow K^{*0} e^+ e^-$  candidates at central- $q^2$  in the three trigger categories (L0E, L0H and L0I) separately, and (bottom right) combined. The dashed black line (shaded shapes) represents the signal (background) PDF.

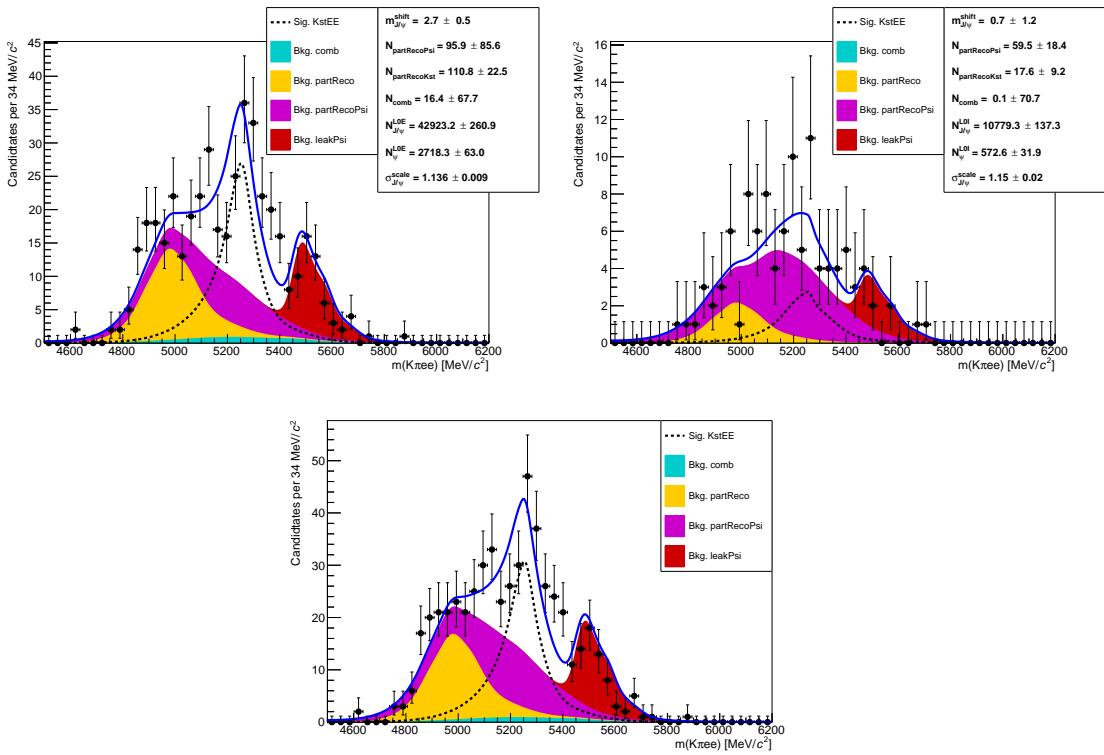


Figure F.5: Fit to the  $m(K\pi ee)$  invariant mass of  $B^0 \rightarrow K^{*0} e^+ e^-$  candidates at high- $q^2$  in the L0E and L0I trigger categories (top) separately, and (bottom) combined. The dashed black line (shaded shapes) represents the signal (background) PDF.