

## PROVA MATEMÁTICA DISCRETA CORREÇÃO

Prova Matemática Discreta

$$1- A = \{a, b, c, d, e\}, B = \{d, e, f, g, h, m, p\},$$

$$C = \{b, e, f, g, h, i\}$$

$$1.1) (A \cap B) = \{d, e\}$$

$$(A \cap B) \cup C = \{a, b, c, d, e, f, g, h, i\}$$

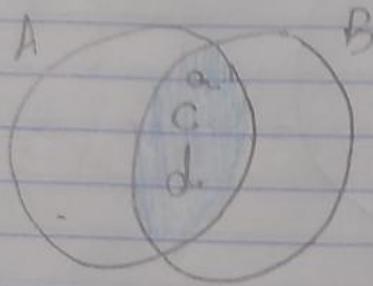
$$1.2) (A \cup B) \cap (A \cap C) = \{b, e\}$$

$$(A \cup B) = \{a, b, c, d, e, f, g, h, m, p\}$$

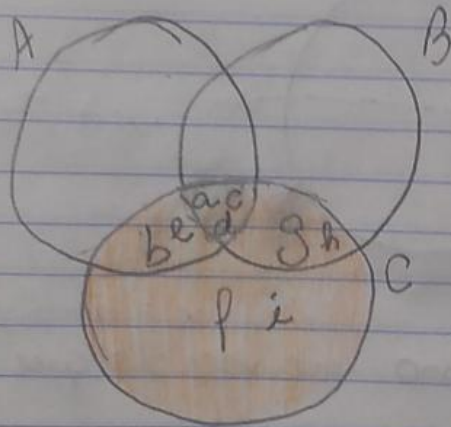
$$(A \cap C) = \{b, e\}$$

1.1) Diagramma di Venn

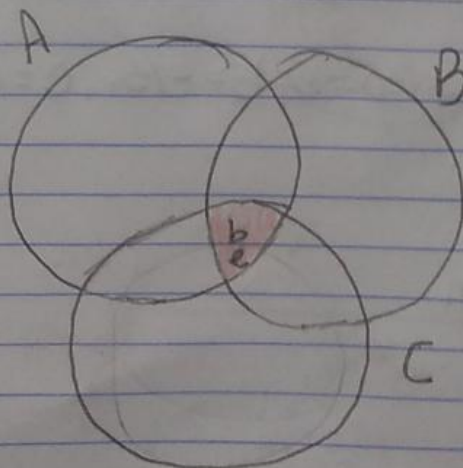
$(A \cap B)$



$(A \cap B) \cup C$



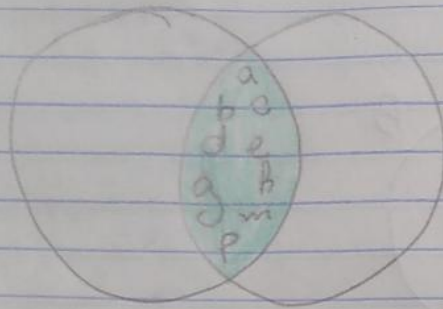
1.2)  $(A \cup B) \cap (A \cap C)$



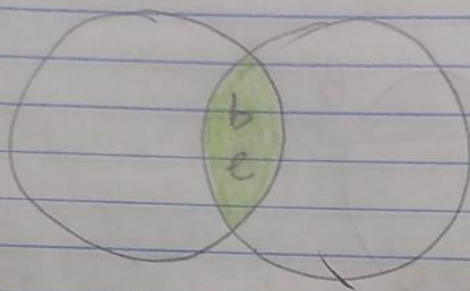
U S T Q O S S  
L M M J V S

$$\begin{array}{r} 75 \\ 15+ \\ \hline 225 \end{array}$$

$(A \cup B)$



$(A \cap C)$



2) Não necessariamente o diagrama, usei o da folha

2.1)  $A = \{10, 6, 9, 4, 7, 1, 3, 2\}$

2.2)  $B = \{30, 2, 3, 1, 5, 21, 8\}$

2.3)  $C = \{15, 33, 22, 5, 1, 7, 4\}$

2.4)  $A \cup C = \{10, 6, 9, 4, 7, 1, 3, 2, 5, 15, 33, 22\}$

2.5)  $A \cap B = \{2, 3, 1\}$

2.6)  $A \cup B \cup C = \{9, 6, 10, 30, 8, 21, 15, 33, 22, 4, 7, 5, 2, 3, 1\}$

2.7)  $(A \cup B) \cap C = \{9, 6, 10, 30, 8, 21, 2, 3, 1, 4, 7, 5\}$

2.8)  $(B \cap C) \cup (A \cap C) = \{4, 7, 5, 1\}$

3  $A = \{x \in \mathbb{N} \mid x \text{ é primo, menor do que } 25\}$

$$A = \{2, 3, 5, 7, 11, 13, 17, 19, 23\}$$

$$b = \{x \in \mathbb{R} \mid 5x^2 + 3x = 18x\} =$$

$$5x^2 + 3x - 18x = 0$$

$$5x^2 - 15x = 0$$

$$a=5, b=-15, c=0$$

$$\Delta = b^2 - 4 \cdot a \cdot c$$

$$\Delta = (-15)^2 - 4 \cdot 5 \cdot 0$$

$$\Delta = 225 - 0$$

$$\Delta = 225$$



$$x = \frac{-b \pm \sqrt{\Delta}}{2 \cdot a}$$

$$x = \frac{-(-15) \pm \sqrt{225}}{2 \cdot 5}$$

$$x = \frac{15 \pm 15}{10} \rightarrow x' = \frac{30}{10} = 3$$

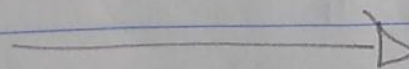
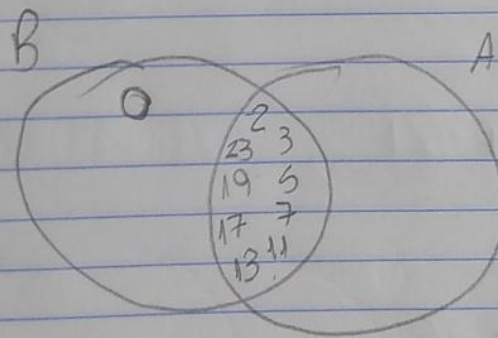
$$x'' = \frac{15 - 15}{10} = \frac{0}{10} = 0$$

$$B \cup A = \{0, 2, 3, 5, 7, 11, 13, 17, 19, 23\}$$

$$(B \cup A) \cap A = \{2, 3, 5, 7, 11, 13, 17, 19, 23\}$$

$$A = \{2, 3, 5, 7, 11, 13, 17, 19, 23\}$$

$$B = \{0, 3\}$$



$$\begin{array}{r} 21 \\ \times 4 \\ \hline 84 \end{array}$$

$$\begin{array}{r} 18 \\ \times 6 \\ \hline 108 \end{array}$$

$$\begin{array}{r} 38 \\ \times 4 \\ \hline 152 \end{array}$$

4 - Determinar  $x$  e  $y$  tal que

$$\begin{cases} \frac{1}{2}x + 5y = 2y + 2 \\ -7x + \frac{3}{4}y + \frac{1}{3}x = -5 \end{cases}$$



$$\begin{cases} \frac{1}{2}x + 5y - 2y = 2 \times 2 \longrightarrow x + 3y = 4 \\ -7x + \frac{1}{3}x + \frac{3}{4}y = -5 \end{cases}$$



$$\begin{cases} x + 10y - 4y = 4 \\ -21x + 3x + \frac{3}{4}y = -5 \end{cases}$$

$$\begin{cases} x + 10y - 4y = 4 \\ -18x + \frac{3}{4}y = -5 \end{cases}$$

$$\begin{array}{r} 318 \\ \times 4 \\ \hline 72 \end{array}$$

$$\begin{array}{r} 180 \\ - 72 \\ \hline 108 \end{array}$$

$$\begin{array}{r} 5108 \\ \times 4 \\ \hline 432 \end{array}$$

data  
fecha

☐ D ☐ S ☐ T ☐ Q ☐ Q ☐ S ☐ S  
☐ S ☐ L ☐ M ☐ M ☐ J ☐ V ☐ S

$$\begin{cases} 18x + 108y = 72 \\ -18x + \frac{3}{4}y = -5 \end{cases} \rightarrow \begin{cases} 18x + 108y = 72 \\ 18x = 72 - 108y \\ 18x = 72 - 108 \left( \frac{72}{410} \right) \end{cases}$$

$$108y + \frac{3}{4}y = 72 - 5 \quad 18x = 72 - \frac{7776}{410}$$

$$\frac{432y + 12y}{4} = 72 \quad 18x = 72 - 7776$$

$$410y = 72 \quad 18x = 7704$$

$$y = \frac{72}{410} \quad x = \frac{7704}{18}$$

$$x = 428$$

$$\begin{array}{r} 46 \\ 206 \\ 41 \\ 1 \end{array}$$