1 Algorithm

1.1 LIS

1.2 LCS

2 Basic

2.1 mod helper function

```
int add(int i, int j) {
    if ((i += j) >= MOD)
        i -= MOD;
    return i;
}

int sub(int i, int j) {
    if ((i -= j) < 0)
        i += MOD;
    return i;
}</pre>
```

2.2 self-defined-pq-operator

```
auto cmp = [](int a, int b) {
    return a > b;
};
priority_queue<int, vector<int>, decltype(
    cmp)> pq(cmp);
```

2.3 generating all subsets

```
for (int b = 0; b < (1<<n); b++) {
   vector<int> subset;
   for (int i = 0; i < n; i++) {
      if (b&(1<<i)) subset.push_back(vc[i])
      ;
   }
}</pre>
```

2.4 memset

```
1 | memset(a, 0, sizeof(a)); // 0
2 | memset(a, 0x3f3f3f3f , sizeof(a)); // INF
```

2.5 submask enumeration

2.6 custom-hash

```
return x ^ (x >> 31);
                                                 24
                                                 25
      size_t operator()(uint64_t x) const {
          static const uint64 t FIXED RANDOM =
                                                 27
                chrono::steady clock::now().
               time since epoch().count();
          return splitmix64(x + FIXED RANDOM);
13
                                                  30
14 };
                                                 31
16 unordered_map<long long, int, custom_hash>
17 gp_hash_table<long long, int, custom_hash>
       safe_hash_table;
```

2.7 stringstream split by comma

```
1 while (std::getline(ss, segment, ',')) {
2         segments.push_back(segment);
3 }
```

3 DP

3.1 deque

```
2 遊戲 DP - O(N^2)
3 A 與 B 將進行以下的遊戲。
aN)。在 a 尚未為空時,兩位玩家輪流進行以 10 */
     下操作,從 A 開始:
7 | 從 a 的開頭或結尾移除一個元素。玩家會獲得 x
     分, 其中 x 為被移除的元素。
8 設 X 與 Y 分別為遊戲結束時 A 與 B 的總得分。
     A 會嘗試最大化 X-Y, 而 B 會嘗試最小化 X- 16
10 | 假設兩位玩家都採取最優策略,請求出最後的 X-Y
12 定義 dp[i][j] 為在區間 [i, j] 上·對於 B 來
     說的最優分數 (X-Y)。
13 */
14
15 void solve() {
    int n;
    cin >> n;
    vector<int> a(n);
    vector<vector<int>>> dp(n + 1, vector<int</pre>
        (n + 1, 0);
    for (int i = 0; i < n; ++i) {</pre>
       cin >> a[i];
```

3.2 walk

```
2 DP on graphs - O(N^3 Log K)
3| 給定一個簡單的有向圖 G, 具有 N 個頂點, 編號
      為 1, 2, ..., N。
s| 對於任意 i, j (1 ≤ i, j ≤ N) · 給定整數 a_{i,
      j},表示是否存在從頂點 i 指向頂點 j 的有
      向邊。若 a \{i,j\} = 1 \cdot 則存在邊; 若 a \{i,j\}
      i} = 0,則不存在。
  求圖中長度為 K 的不同有向路徑數目,對 10^9+7
       取模。路徑可重複通過相同邊(即允許重複
      邊)。
g 注意:當我們將鄰接矩陣 m 與 m 相乘時,得到的
      是長度為 2 的路徑數;若取 m 的 p 次方 m^{4}
      p · 則其 (i, j) 元素表示從 i 到 j 的長度
      為 p 的路徑數。
12 void solve() {
     int n, k;
     cin >> n >> k;
     vector<vector<int>> m(n, vector<int>(n))
     for (int i = 0; i < n; ++i) {</pre>
         for (int j = 0; j < n; ++j) {</pre>
            cin >> m[i][j];
     Matrix<int> mat(m);
     mat = power(mat, k);
     int ans = 0:
     for (int i = 0; i < n; ++i) {</pre>
         for (int j = 0; j < n; ++j) {</pre>
            ans += mat.mat[i][j];
            ans %= MOD;
     cout << ans << "\n";</pre>
```

3.3 grouping

```
1 /*
3 有 N 隻兔子·編號為 1,2,...,N。
s| 對於每一對 i,j (1≤i,j≤N) · 兔子 i 與 j 的相容
      度由整數 a i, j 描述。這裡 a i, i = 0 對於
      每個 i (1 \le i \le N) · 且 a_i, j = a_j, i 對於任
      意 i 與 j (1≤i, j≤N)。
7 A 將 N 隻兔子分成若干個群組。每隻兔子必須且
      僅屬於一個群組。分群後,對於每一對 i 與
     j (1≤i<j≤N), 若兔子 i 與 j 屬於同一群
      組\cdotA 即可獲得 a i,j 分。
9| 求 A 能獲得的最大總分。
11 令 cost[S] 表示將集合 S 中的所有兔子放在同一
      群組時所得到的分數。此值可在 O(2^N * N
      ^2) 時間內計算。
13 接著我們計算 dp[S],表示對集合 S 中的兔子進
      行分群時所能得到的最大分數。
  void solve() {
     int n:
     cin >> n;
     vector<vector<int>> a(n, vector<int>(n))
     vector<int> cost(1<<n, 0);</pre>
     vector<int> dp(1<<n, 0);</pre>
     for (int i = 0; i < n; ++i) {
         for (int j = 0; j < n; ++j) {
            cin >> a[i][i];
     // backtrack all subset
     for (int b = 0; b < (1 << n); ++b) {
         vector<int> subset;
        for (int i = 0; i < n; ++i) {
            if (b & (1<<i)) {</pre>
                for (const int& j : subset)
                   cost[b] += a[i][j];
               subset.pb(i);
     }
     for (int i = 0; i < (1<<n); ++i) {</pre>
        int j = ((1 << n) - 1) ^ i;
        for (int s = j; s != 0; s = (s - 1)
            dp[i^s] = max(dp[i^s], dp[i]
                 + cost[s]);
```

3.4 matching

```
2 Bitmask DP - O(N * 2^N)
 有 N 個男人和 N 個女人,分別編號為 1,2, ...,
 對於每個 i, j (1 \leq i, j \leq N) · 男人 i 和女人
      j 的相容性由整數 a[i][j] 給出。
 如果 a[i][j] = 1 則男人 i 和女人 j 是相容
 如果 a[i][i] = 0 則不是。
9|A 正在嘗試組成 N 對,每對由一個相容的男人和
      女人組成。在這裡,每個男人和每個女人必須 18
      恰好屬於一對。
 求 A 可以組成 N 對的方法數, 結果對 10^9 + 7
 定義 dp[S] 為將集合 S 中的女性與前 |S| 個男
      性配對的方法數。
 const int maxn = 21:
 const int MOD = 1e9 + 7;
 int grid[maxn][maxn];
 int dp[1 << maxn];</pre>
 void solve() {
     cin >> n:
     memset(dp, 0, sizeof(dp));
     for (int i = 0; i < n; ++i) {</pre>
         for (int j = 0; j < n; ++j) {
             cin >> grid[i][j];
     }
     dp[0] = 1;
     for (int s = 0; s < (1 << n); ++s) {
         int ps = builtin popcount(s);
         for (int w = 0; w < n; ++w) {
            if ((s & (1 << w)) || !grid[ps][</pre>
                 w]) {
                continue:
             dp[s | (1 << w)] += dp[s];
             dp[s \mid (1 << w)] \% = MOD;
     cout \langle\langle dp[(1 \langle\langle n) - 1] \langle\langle " \rangle n";
```

3.5 projects

```
2 LIS DP - O(N Log N)
3 有 n 個你可以參加的專案。對於每個專案,你知
       道其開始與結束天數以及可獲得的報酬金額
4|在同一天你最多只能參加一個專案。
  問:你最多可以賺到多少金額?
\eta dp[i] = 在第 i 天之前我們可以賺到的最大金
      額。
10 void solve() {
      int n;
      cin >> n:
      vector<array<int, 3>> vc(n);
      map<int, int> days;
      for (int i = 0; i < n; ++i) {</pre>
          int a, b, p;
          cin >> a >> b >> p;
          days[a] = days[b] = 1;
          vc[i] = {a, b, p};
      int idx = 1;
      for (auto& x : davs) {
         x.second = idx++;
      vector<int> dp(idx, 0);
      sort(vc.begin(), vc.end(), [](const
          array<int, 3>& va, const array<int,
          3>& vb) {
          if (va[1] != vb[1]) return va[1] <</pre>
          if (va[0] != vb[0]) return va[0] <</pre>
              vb[0];
          return va[2] > vb[2];
      });
      int i = 0;
      for (int d = 1; d < idx; ++d) {</pre>
          dp[d] = dp[d - 1];
          while (i < n && days[vc[i][1]] == d)</pre>
             dp[d] = max(dp[d], dp[days[vc[i
                  ][0]] - 1] + vc[i][2]);
             i++;
40
      cout << dp[idx - 1] << "\n";</pre>
```

3.6 stones

```
s | 一開始有一堆 K 顆石頭。兩位玩家輪流進行以下
      操作, 從大郎開始:
7 選擇集合 A 中的一個元素 x, 並從石堆中移除恰
      好x顆石頭。
8 當某位玩家無法進行操作時即輸掉比賽。假設兩位
      玩家都採取最優策略,請判斷誰會獲勝。
10 定義 dp[i] 表示當剩下 i 顆石頭時,是否有可能
      獲勝。
11 */
12
13 void solve() {
     int n, k;
     cin >> n >> k;
     vector<int> a(n);
     vector<bool>dp(k + 1, 0);
     for (int i = 0; i < n; ++i) {</pre>
        cin >> a[i];
     for (int i = 1; i <= k; ++i) {</pre>
        for (int x : a) {
            if (i >= x && !dp[i - x]) {
               dp[i] = 1;
29
     cout << (dp[k] ? "First" : "Second") <<</pre>
         "\n":
```

3.7 coins

```
2 機率 DP - O(N^2)
3 | 給定一個正奇數 N
4| 有 N 枚編號為 1,2,...,N 的硬幣,第 i 枚出現正
       面的機率為 p · 反面為 1-p ·
 s 已經拋擲所有硬幣,求正面數大於反面的機率。
 7|定義 dp[i][j] 為拋完前 i 枚硬幣後,得到 j 次
      正面的機率。
10 void solve() {
     int n:
      cin >> n:
      vector<double> a(n);
      vector<vector<double>> dp(n + 1, vector
          double>(n + 1, 0.0));
15
      for (int i = 0; i < n; ++i) {</pre>
16
17
         cin >> a[i];
19
      for (int i = 0; i <= n; ++i) {</pre>
20
21
         dp[i][0] = 1.0;
22
```

3.8 elevator rides

```
2 | 狀壓 DP - O(2^N)
3 有 n 個人想要搭電梯到樓頂,建築物只有一部電
      梯。你知道每個人的體重以及電梯的最大允許
      載重。最少需要搭乘多少次電梯?
s 定義 dp[S] = \{r, w\} · 其中 r 是將集合 S 中的
      所有人送到樓頂所需的最少電梯次數,w 是最
      後一次電梯所載人的總重量。
 */
 void solve() {
     int n, x;
     cin >> n >> x;
     vector<int> w(n);
     vector<pii> dp(1<<n, {INF, INF});</pre>
     for (int i = 0; i < n; ++i) {
        cin >> w[i];
     dp[0] = \{1, 0\};
     for (int b = 1; b < (1 << n); ++b) {
         for (int i = 0; i < n; ++i) {</pre>
            if (b & (1<<i)) {</pre>
                auto [r_prev, w_prev] = dp[b
                      ^ (1<<i)];
                if (w_prev + w[i] <= x) {</pre>
                    can = {r_prev, w_prev +
                        w[i]};
                else {
                    can = \{r_prev + 1, w[i]
                        ]};
                dp[b] = min(dp[b], can);
     cout << dp[(1<<n) - 1].first << "\n";</pre>
```

3.9 slimes

2 Range DP - $O(N^3)$

```
A 想要把所有史萊姆合併成一個更大的史萊姆。他
    會重複執行以下操作,直到只剩下一個史萊姆
選擇兩個相鄰的史萊姆,將它們合併成一個新的史
    萊姆。新史萊姆的大小為 x+y, 其中 x 和 y
   是合併前兩個史萊姆的大小。
這時會產生 x+v 的花費。合併時,史萊姆的相對
    位置不會改變。
請求出合併所有史萊姆所需的最小總花費。
令 dp[i][j] 表示將第 i 個到第 j 個史萊姆合併
   成一個史萊姆的最小花費。
const int maxn = 401:
const int INF = 1e18;
int dp[maxn][maxn];
int a[maxn];
int prefix[maxn + 1];
int f(int i, int j) {
   if (i + 1 == j) {
      return a[i] + a[j];
   if (i == j) {
      return 0;
   if (dp[i][j] != INF) {
      return dp[i][j];
   //cerr << i << " " << j << "\n";
   int ans = INF;
   for (int k = i; k < j; ++k) {
      ans = min(ans, f(i, k) + f(k + 1, j)
   return dp[i][j] = ans + (prefix[j + 1] -
       prefix[i]);
```

有 N 個史萊姆排成一列。最初,從左邊數來第 i

個史萊姆的大小為 ai。

3.10 digit sum

```
2 Digit DP - O(|K| * D)
3 計算在 1 到 K(含)之間·滿足其十進位數字和 為 D 的倍數的整數數量·答案對 10^9+7 取 模。
4 $ 令 dp[i][i] 表示在已確定前 i 位數字的情況
```

下,構成長度為 /K/ 的數字且目前數字和

```
mod D 等於 i 的方法數。
8 \mid const \mid int \mid MOD = 1e9 + 7;
 int dp[10001][101][2];
11 void solve() {
      string K:
      int D;
      cin >> K >> D;
      int len = K.size();
      memset(dp, 0, sizeof(dp));
      dp[0][0][1] = 1;
      for (int i = 1; i <= len; ++i) {</pre>
          int limit = K[i - 1] - '0';
          for (int s = 0; s < D; ++s) {
              for (int flag = 0; flag <= 1; ++</pre>
                   flag) {
                   int ways = dp[i - 1][s][flag]
                   if (ways == 0) continue;
                   int max_d = (flag ? limit :
                   for (int d = 0; d <= max d;</pre>
                        ++d) {
                       int rs = (s + d) \% D;
                       int rflag = (flag && d
                            == max_d ? 1 : 0);
                       dp[i][rs][rflag] += ways
                       dp[i][rs][rflag] %= MOD; 41 }
              }
      int ans = (dp[len][0][0] + dp[len
           ][0][1]) % MOD;
      ans = (ans - 1 + MOD) \% MOD;
      cout << ans << "\n";
```

3.11 sushi

```
15 const int maxn = 301;
16 double dp[maxn][maxn][maxn];
19 double dfs(int x, int y, int z) {
       if (x < 0 | | y < 0 | | z < 0) return 0;
       if (x == 0 \&\& y == 0 \&\& z == 0) return
       if (dp[x][y][z] > 0) return dp[x][y][z];
       double ans = n + x * dfs(x - 1, y, z)
                       + y * dfs(x + 1, y - 1, z)
                       + z * dfs(x, y + 1, z -
                            1);
       return dp[x][y][z] = ans / (x + y + z);
27 }
29 void solve() {
       cin >> n;
       vector<int> a(n);
       memset(dp, -1, sizeof(dp));
       vector<int> freq(4, 0);
       for (int i = 0; i < n; ++i) {</pre>
           cin >> a[i];
           freq[a[i]]++;
38
39
       cout << fixed << setprecision(10) << dfs</pre>
            (freq[1], freq[2], freq[3]) << "\n";
```

3.12 candies

```
2 | 組合 DP - O(NK)
  有 N 個小孩 · 編號為 1,2,...,N。
  他們決定將 K 顆糖果分給自己。對於每個 i (1≤i
      ≤N), 第 i 個小孩最多可以拿到 ai 顆糖果
      (包含 Ø 顆)。所有糖果都必須分完、不能
 | 請 問 有 多 少 種 分 配 糖 果 的 方 法 ? 請 將 答 案 對
     10^9+7 取模。若存在某個小孩分到的糖果數
      不同,則視為不同的分配方式。
  令 dp[i][j] 表示將 j 顆糖果分給前 i 個小孩的
     方法數。
10 */
12 void solve() {
     int n, k;
     cin >> n >> k;
     vector<int> a(n);
     vector<int> dp(k + 1, 0), S(k + 1, 0);
18
     for (int i = 0; i < n; ++i) {</pre>
        cin >> a[i];
```

```
dp[0] = 1;
for (int i = 0; i < n; ++i) {
    vector<int> new_dp(k + 1, 0);
    S[0] = dp[0];
    for (int j = 1; j <= k; ++j) {
        S[j] = (S[j - 1] + dp[j]) % MOD;
    for (int j = 0; j <= k; ++j) {</pre>
        if (j - a[i] - 1 >= 0) {
            new dp[j] = (S[j] - S[j - a[
                 i] - 1] + MOD) % MOD;
        else {
            new_dp[j] = S[j] \% MOD;
    dp = new_dp;
cout << dp[k] << "\n";</pre>
```

permutation

```
1 /*
2 抽象 DP - O(N^2)
3 | 設 N 為正整數。給定一個長度為 N-1 的字串 s ·
      字元僅包含 '‹' 與 '›'。
s| 求滿足條件的排列 (p1, p2, ..., pN) (即 1 到 N 1 | // 01 背包, 背包承重大 (1e9), 物品價值和較小
       的排列)數量,答案對 10^9+7 取模:
7 對於每個 i (1 ≤ i ≤ N-1) · 若 s 的第 i 個字
      元為 '<',則要求 pi < p {i+1};若為 '>'
      ,則要求 p i > p {i+1}。
  令 dp[i][j] 表示:在考慮前 i 個比較符號(即
      構成長度為 i+1 的排列)且最後一個元素為
     j 的有效排列數量。
12 void solve() {
     int n:
     string s;
     cin >> n >> s;
     vector<vector<int>> dp(n + 1, vector<int</pre>
         (n + 1, 0);
     vector<int> prefix(n + 1, 0);
     dp[1][0] = 1;
     for (int i = 2; i <= n; ++i) {</pre>
         for (int k = 0; k < n; ++k) {
            prefix[k + 1] = prefix[k] + dp[i]
                 - 1][k];
        for (int j = 0; j < i; ++j) {
            if (s[i - 2] == '>') {
                dp[i][j] += prefix[i - 1] -
                    prefix[j];
               dp[i][j] %= MOD;
```

```
for (int k = j; k < i - 1;
                 ++k) {
                dp[i][j] += dp[i - 1][k]
                     ];
        else {
            dp[i][j] += prefix[j];
            dp[i][j] %= MOD;
            for (int k = 0; k < j; ++k)
                dp[i][j] += dp[i - 1][k]
int ans = 0;
for (int j = 0; j < n; ++j) {
   ans += dp[n][j];
    ans %= MOD:
cout << ans << "\n";
```

3.14 Knasack2

```
(1e5)
  const int maxn = 101:
  const int maxv = 100001;
  int weight[maxn];
  int cost[maxn];
  int dp[maxv];
  void solve() {
      int n, w;
      cin >> n >> w;
       for (int i = 0; i < n; ++i) {
           cin >> weight[i] >> cost[i];
      fill(dp, dp + maxv, 1e18);
      dp[0] = 0;
       for (int i = 0; i < n; ++i) {
           for (int j = maxv - 1; j >= 0; --j)
               if (dp[j] + weight[i] <= w) {</pre>
                   dp[j + cost[i]] = min(dp[j +
                         cost[i]], dp[j] +
                        weight[i]);
25
      for (int i = maxv - 1; i >= 0; --i){
           if (dp[i] != 1e18) {
               cout << i << "\n";
```

```
return;
```

3.15 flowers

```
2 LIS DP + Segment Tree - O(N Log N)
3 有 N 朵花排成一列。對於每個 i (1 ≤ i ≤ N).
       第 i 朵花的高度與美麗分別為 h i 與 a i。
      此處 h_1, h_2, ..., h_N 兩兩互異。
 s A 會 拔 掉 一 些 花 · 使 得 剩 下 的 花 從 左 到 右 的 高 度 為
       單調遞增(嚴格遞增)。
  求剩下花的美麗值總和的最大可能值。
  令 dp[i] 表示以第 i 朵花為結尾的遞增子序列所
      能取得的最大美麗值。
12 void solve() {
     int n;
      cin >> n:
      SGT<int, MergeMax> tree(n + 1, 0);
      vector<int> h(n), b(n);
      for (int i = 0; i < n; ++i) {</pre>
         cin >> h[i]:
20
      for (int i = 0; i < n; ++i) {</pre>
21
         cin >> b[i];
23
24
      for (int i = 0; i < n; ++i) {</pre>
25
          int mx = tree.query(0, h[i]);
27
         tree.modify(h[i], mx + b[i]);
28
29
      cout << tree.query(0, n + 1) << "\n";
```

3.16 independent set

```
2 DP on Trees - O(N)
3 有一棵含 N 個頂點的樹, 頂點編號為 1,2,...,N。
    對於每個 i (1 ≤ i ≤ N-1) · 第 i 條邊連接
    頂點 x_i 和 y_i。
5 A 決定將每個頂點塗成白色或黑色,但不允許兩個
    相鄰的頂點同時為黑色。
```

```
9| 設 dp[i][j] 表示以節點 i 為根的子樹中,在節
       點 i 颜色為 j 時的塗色方案數 (例如 j=0
        表示白色 i=1 表示黑色)。
10
12 const int maxn = 100001:
13 vector<int> adj[maxn];
14 int f[maxn][2];
15 const int MOD = 1e9 + 7;
17 void dp(int u, int p) {
       for (int v : adj[u]) {
          if (v != p) {
21
               dp(v, u);
              f[u][0] = (f[v][0] + f[v][1]) %
                   MOD * f[u][0] % MOD;
              f[u][1] = f[v][0] * f[u][1] %
                   MOD;
26
28 void solve() {
      int n;
       cin >> n;
       for (int i = 0; i < n; ++i) {</pre>
          f[i][0] = f[i][1] = 1;
35
       for (int i = 0; i < n - 1; ++i) {
          int u, v;
          cin >> u >> v;
          u--, v--;
          adj[u].pb(v);
           adj[v].pb(u);
       dp(0, -1);
       cout << (f[0][0] + f[0][1]) % MOD << "\n
47 }
```

3.17 couting tower

```
1 /*
2 | 狀態機 DP - O(N)
3 | 你的任務是建造一座寬度為 2、高度為 n 的塔。
     你有無限數量寬度與高度為整數的方塊。
s \mid dp[i][0] = 高度為 i 的塔中,頂層為一個寬度為
     2 的方塊(即該層由跨越兩欄的單一方塊覆
     蓋)的塔的數量。
6 | dp [ i ] [ 1 ] = 高度為 i 的塔中,頂層在該層有兩個
     寬度為 1 的方塊(每欄各一個)的塔的數
 */
9 void solve() {
```

31

```
long long n;
cin >> n;
dp[1][0] = 1:
dp[1][1] = 1;
for(int i = 2;i<=n;i++){</pre>
    dp[i][0] = (4 * dp[i-1][0] + dp[i
          -1][1]) % mod;
    dp[i][1] = (dp[i-1][0] + 2 * dp[i
         -1][1]) % mod;
cout << (dp[n][0] + dp[n][1]) % mod <<</pre>
     endl;
```

3.18 couting numbers

1 /*

```
2 區間 DP - O(digits*10)
3 | 您的任務是計算在區間 a 到 b 之間,沒有任何相
      鄰兩位數字相同的整數的個數。
5 定義 dp[pos][prev digit][is tight][
      is started] 為從位置 pos 到結尾的有效整
6| 其中 prev digit 是位置 pos-1 的數字·
7 is tight 表示是否受原數字前綴的限制,
8 is started 表示是否已開始構成有效數字(用以
      避免計入前導零)。
11 // dp[pos][prev digit][is tight][is started]
12 int dp[20][10][2][2];
13 string s;
int f(int pos, int prev digit, bool is tight
      , bool is_started) {
     if (pos == (int)s.size()) {
         return 1;
     if (dp[pos][prev digit][is tight][
          is started] != -1) {
         return dp[pos][prev_digit][is_tight
             ][is started];
     int max d = is tight ? (s[pos] - '0') :
     for (int d = 0; d <= max d; ++d) {</pre>
         if (is started && d == prev_digit) {
         bool new is started = is started ||
             (d > 0);
         bool new_is_tight = is_tight && (d
             == max d);
         ans += f(pos + 1, d, new_is_tight,
             new is started);
```

```
return dp[pos][prev_digit][is_tight][
        is started] = ans;
int count(int x) {
    if (x < 0) return 0:
    s = to string(x);
    memset(dp, -1, sizeof(dp));
    return f(0, 0, true, false);
void solve() {
    int a, b;
    cin >> a >> b;
    int ca = count(a - 1);
    int cb = count(b);
    cout << cb - ca << "\n";
```

4 Data Structure

undo disjoint set

```
1 struct DisjointSet {
    // save() is like recursive
    // undo() is like return
    int n, fa[MXN], sz[MXN];
    vector<pair<int*,int>> h;
    vector<int> sp;
    void init(int tn) {
      for (int i=0; i<n; i++) sz[fa[i]=i]=1;</pre>
      sp.clear(); h.clear();
    void assign(int *k, int v) {
      h.PB({k, *k});
      *k=v;
    void save() { sp.PB(SZ(h)); }
    void undo() {
      assert(!sp.empty());
      int last=sp.back(); sp.pop back();
      while (SZ(h)!=last) {
        auto x=h.back(); h.pop back();
        *x.F=x.S;
    int f(int x) {
      while (fa[x]!=x) x=fa[x];
      return x;
    void uni(int x, int y) {
      x=f(x); y=f(y);
      if (x==y) return ;
      if (sz[x]<sz[y]) swap(x, y);</pre>
      assign(&sz[x], sz[x]+sz[y]);
      assign(&fa[y], x);
36 }djs;
```

4.2 segment tree range update (lazy 47) propagation)

```
1 // segment tree
2 // range query & range modify
3 class SGT {
      using value_t = int;
                                                  53
      using node t = pair<value t, int>;
      int n;
      vector<node_t> t;
      vector<optional<value_t>> lz;
      // [tv+1:tv+2*(tm-tl)) \rightarrow left
           subtree
      int left(int tv) { return tv + 1; }
      int right(int tv, int tl, int tm) {
                                                  57
           return tv + 2 * (tm - t1); }
                                                  58
      /** differ from case to case **/
                                                  59
      // query is "max" and modify is "add"
      node_t merge(const node_t& x, const
           node t& y) { // associative function 61
          return max(x, y);
      void update(int tv, int len, const
           value_t& x) {
          if (!\overline{lz}[tv]) \overline{lz}[tv] = x;
          else lz[tv] = lz[tv].value() + x;
          t[tv].fi = t[tv].fi + x;
      /*****************************
      void build(const vector<value t>& v, int
            tv, int tl, int tr) {
          if (tr - tl > 1) {
              int tm{(tl + tr) / 2};
              build(v, left(tv), tl, tm);
              build(v, right(tv, tl, tm), tm,
              t[tv] = merge(t[left(tv)], t[
                                                  71
                   right(tv, tl, tm)]);
          } else t[tv] = {v[t1], t1};
      void push(int tv, int tl, int tr) { //
                                                  73 };
           Lazy propagation
          if (!lz[tv]) return ;
                                                  74
          int tm{(tl + tr) / 2};
          update(left(tv), tm - tl, lz[tv].
               value());
          update(right(tv, tl, tm), tr - tm,
                                                  78
               lz[tv].value());
                                                  79
          lz[tv].reset();
      void set(int p, const value_t& x, int tv
          , int tl, int tr) {
if (tr - tl > 1) {
              push(tv, tl, tr);
                                                  83
              int tm{(tl + tr) / 2};
              if (p < tm) set(p, x, left(tv),</pre>
                   tl, tm);
              else set(p, x, right(tv, tl, tm)
                                                  86
                   , tm, tr);
                                                  87
              t[tv] = merge(t[left(tv)], t[
                                                  88
                   right(tv, tl, tm)]);
          } else t[tv].fi = x;
```

```
void rmodify(int 1, int r, const value t
           & x, int tv, int tl, int tr) {
          if (!(1 == t1 && r == tr)) {
               push(tv, tl, tr);
               int tm{(t1 + tr) / 2};
               if (r \le tm) \text{ rmodify}(1, r, x,
                   left(tv), t1, tm);
               else if (1 >= tm) rmodify(1, r,
                   x, right(tv, tl, tm), tm, tr
               else rmodify(1, tm, x, left(tv),
                    tl, tm),
                   rmodify(tm, r, x, right(tv,
                       tl, tm), tm, tr);
               t[tv] = merge(t[left(tv)], t[
                    right(tv, tl, tm)]);
          } else update(tv, tr - tl, x);
      node_t rquery(int 1, int r, int tv, int
           tl, int tr) {
          if (1 == t1 && r == tr) return t[tv
          push(tv, tl, tr);
          int tm{(t1 + tr) / 2};
          if (r <= tm) return rquery(1, r,</pre>
               left(tv), tl, tm);
          else if (1 >= tm) return rquery(1, r
                , right(tv, tl, tm), tm, tr);
          else return merge(rquery(1, tm, left
               (tv), tl, tm),
               rquery(tm, r, right(tv, tl, tm),
                    tm, tr));
68 public:
      explicit SGT(const vector<value t>& v) :
            n\{v.size()\}, t(2 * n - 1), lz(2 * n
            - 1) { build(v, 0, 0, n); }
      void set(int p, const value_t& x) { set(
           p, x, 0, 0, n); }
      void rmodify(int 1, int r, const value t
           & x) { rmodify(1, r, x, 0, 0, n); }
           // [L:r)
      node t rquery(int 1, int r) { return
           rquery(1, r, 0, 0, n); } // [L:r)
75 int main() {
      vector<long long> a = \{1, 5, 2, 4, 3\};
      SGT st(a);
      auto [val, idx] = st.rquery(0, 5);
      cout << "Initial max: " << val << " at " << idx << "\\n"; // (5, 1)
      st.rmodify(1, 4, 3); // add 3 to indices
            1..3
       tie(val, idx) = st.rquery(0, 5);
      cout << "After add: " << val << " at " << idx << "\\n"; // (8, 1)
      st.set(2, 10); // set a[2] = 10
      tie(val. idx) = st.rquerv(0, 5):
```

41

42 };

4.3 segment tree prefix sum lower 3 bound 5

1 class SGT {

int n;

```
vector<long long> t;
      int left(int tv) { return tv + 1; }
      int right(int tv, int tl, int tm) {
           return tv + 2 * (tm - tl); }
      void modify(int p, long long x, int tv,
           int tl, int tr) {
          if (tr - tl > 1) {
              int tm{(t1 + tr) / 2};
              if (p < tm) modify(p, x, left(tv</pre>
                   ), tl, tm);
              else modify(p, x, right(tv, tl,
                   tm), tm, tr);
              t[tv] = t[left(tv)] + t[right(tv
                   , tl, tm)];
          } else t[tv] = x;
      long long query(int 1, int r, int tv,
           int tl, int tr) {
          if (1 == t1 && r == tr) return t[tv
          int tm{(t1 + tr) / 2};
          if (r <= tm) return query(l, r, left</pre>
               (tv), tl, tm);
          else if (1 >= tm) return query(1, r,
                right(tv, tl, tm), tm, tr);
          else return query(1, tm, left(tv),
               t1, tm) +
              query(tm, r, right(tv, tl, tm),
                   tm, tr);
22 public:
      explicit SGT(int _n) : n{_n}, t(2 * n -
      void modify(int p, long long x) { modify
           (p, x, 0, 0, n); };
      long long query(int 1, int r) { return
           query(1, r, 0, 0, n); }
      int ps_lower_bound(long long ps) { //
           prefix sum lower bound
          if (ps > t[0]) return n;
          int tv{0}, tl{0}, tr{n};
          while (tr - tl > 1) {
              int tm{(t1 + tr) / 2};
              if (t[left(tv)] >= ps) tv = left
                   (tv), tr = tm;
              else ps -= t[left(tv)], tv =
                   right(tv, tl, tm), tl = tm;
          return tl;
36 };
```

4.4 Fenwick tree (BIT)

```
1 // 1-based
2 struct Fenwick {
```

```
vector<int> bit;
      Fenwick(int n=0): n(n), bit(n+1, 0) {}
      void update(int idx, int val) {
          for (; idx \le n; idx += idx & -idx)
               bit[idx] += val:
      int query(int idx) {
          int res = 0:
          for (; idx > 0; idx -= idx & -idx)
               res += bit[idx];
          return res;
      int query(int 1, int r) {
          return query(r) - query(1-1);
17 };
  int main() {
      Fenwick fw(n);
      for (int i = 1; i < n; ++i) {</pre>
          fw.update(i, a[i]);
      cout << fw.query(3, 7) << "\\n"; //
           range sum [3..7]
      int current = ...; // old value at idx
      int newVal = ...; // new value you want
      fw.update(idx, newVal - current);
```

4.5 Trie (Prefix tree)

```
| struct trie {
      int n = 0:
      trie *a[2];
      trie() {
          a[0] = a[1] = nullptr;
      void insert(int k) {
          trie *curr = this;
          for (int i = 63; i >= 0; --i) {
              bool bit = (k & (1LL << i)) > 0:
              if (curr->a[bit] == nullptr) {
                  curr->a[bit] = new trie();
              curr = curr->a[bit];
              curr->n++ :
      void erase(int k) {
          trie *curr = this:
          for (int i = 63; i >= 0; --i) {
              bool bit = (k & (1LL << i)) > 0;
              curr = curr->a[bit];
              curr->n--;
     }
      int query(int k) {
          trie *curr = this;
          int x = 0;
```

```
for (int i = 63; i >= 0; --i) {
    x ^= (1LL << i) & k;
    x ^= 1LL << i;
    bool bit = (k & (1LL << i)) ==
        0;
    if (curr->a[bit] == nullptr ||
        curr->a[bit]->n == 0)
        x ^= 1LL << i, bit ^= 1;
    curr = curr->a[bit];
}
return x;
```

4.6 segment tree

2 template<typename value t, class merge t>

1 // Segment tree

3 class SGT {

```
int n;
      vector<value t> t;
      value t defa;
      merge_t merge;
8 public:
      explicit SGT(int _n, value_t _defa,
           const merge t& merge = merge t{})
           : n{_n}, t(2 * n), defa{_defa},
               merge{ merge} {}
      void modify(int p, const value_t& x) {
           for (t[p += n] = x; p > 1; p >>= 1)
               t[p \gg 1] = merge(t[p], t[p ^
                    1]);
      value t query(int 1, int r) { return
           query(1, r, defa); }
      value_t query(int 1, int r, value_t init 15
           for (1 += n, r += n; 1 < r; 1 >>= 1,
                r >>= 1) {
               if (1 & 1) init = merge(init, t[
                    1++]);
               if (r & 1) init = merge(init, t
                    [--r]);
           return init:
24
25
28 // Custom merge for range minimum + index
29 struct MergeMin {
      pair<int, int> operator()(const pair<int 30</pre>
           , int>& a,
                                  const pair<int 32</pre>
                                      , int>& b) 33
                                       const {
                                                  34
           if (a.first != b.first) return (a.
               first < b.first) ? a : b;</pre>
           return (a.second < b.second) ? a : b</pre>
               ; // tie-break on index
```

4.7 BIT range update point query

```
1 // Fenwick Tree (Binary Indexed Tree) for
        Range Updates and Point Oueries
 3 template<typename T>
 4 class BIT {
  #define ALL(x) begin(x), end(x)
 6 private:
       vector<T> arr;
       int n;
       inline int lowbit(int x) { return x & (-
       void addInternal(int s, T v) {
           while (s > 0) {
11
               arr[s] += v;
12
               s -= lowbit(s);
16 public:
       void init(int n_) {
           n = n;
           arr.resize(n + 1);
           fill(ALL(arr), 0);
       void add(int 1, int r, T v) {
           // add v to interval (l, r], 1-based
           addInternal(1, -v);
           addInternal(r, v);
25
27
       T query(int x) {
           // value at index x
           T res = 0:
           while (x <= n) {
               res += arr[x];
               x += lowbit(x);
           return res;
36 #undef ALL
37 };
39 int main() {
```

32 }

```
BIT<int> bit;
                                                   explicit DSU(int n) : pa(n, -1), sz(n,
bit.init(5);
                                                   int find(int x) { // collapsing find
// add +3 to indices 1..3
                                                       return pa[x] == -1 ? x : pa[x] =
bit.add(0, 3, 3);
                                                            find(pa[x]);
// add +2 to indices 3..5
                                                   void unite(int x, int y) { // weighted
bit.add(2, 5, 2);
                                                       auto rx{find(x)}, ry{find(y)};
cout << "Value at 1 = " << bit.query(1)</pre>
                                                       if (rx == ry) return ;
     << "\n"; // expect 3
                                                       if (sz[rx] < sz[ry]) swap(rx, ry);</pre>
cout << "Value at 3 = " << bit.query(3)</pre>
                                                       pa[ry] = rx, sz[rx] += sz[ry];
     << "\n"; // expect 3+2=5
cout << "Value at 5 = " << bit.query(5)</pre>
     << "\n"; // expect 2
```

5 Geometry

5.1 using std::complex

```
1 // previous/next one
2 class PvNx {
      vector<int> pa, sz, mn, mx;
      int find(int x) { // collapsing find
          return pa[x] == -1 ? x : pa[x] =
               find(pa[x]);
      void unionn(int x, int y) { // weighted
          auto rx{find(x)}, ry{find(y)};
          if (rx == ry) return ;
          if (sz[rx] < sz[ry]) swap(rx, ry);</pre>
          pa[ry] = rx, sz[rx] += sz[ry], mn[rx]
               ] = min(mn[rx], mn[ry]), mx[rx]
               = max(mx[rx], mx[ry]);
13 public:
      explicit PvNx(int n) : pa(n + 1, -1), sz
           (n + 1, 1), mn(n + 1) \{ iota(mn.
           begin(), mn.end(), 0), mx = mn; }
      void remove(int i) { unionn(i, i + 1); }
      int prev(int i) { return mn[find(i)] -
           1; }
      int next(int i) {
          int j{mx[find(i)]};
          if (i == j) j = mx[find(j + 1)];
          return j;
      bool exist(int i) { return i == mx[find(
```

4.8 DSU remove node find prev next

one

4.9 DSU

```
1 // fast disjoint set union
2 class DSU {
3     vector<int> pa, sz;
4 public:
```

```
#include <iostream>
  #include <complex>
  #include <cmath>
  typedef std::complex<double> point;
  #define x real()
  #define y imag()
  constexpr double PI = std::acos(-1.0);
10 // conj(a) = a 的共軛, reflection of a
       across x-axis
12 // Basic operations
double dot(const point &a, const point &b) { 57
        return (std::conj(a) * b).real(); }
14 double cross(const point &a, const point &b) 59
        { return (std::conj(a) * b).imag(); }
16 // Projections / reflections / geometry
point project onto vector(const point &p,
       const point &v) {
      return v * (dot(p, v) / std::norm(v));
21 point project onto line(const point &p,
       const point &a, const point &b) {
      return a + (b - a) * (dot(p - a, b - a)
           / std::norm(b - a));
point reflect across line(const point &p,
       const point &a, const point &b) {
      return a + std::conj((p - a) / (b - a))
           * (b - a);
point intersection(const point &a, const
       point &b, const point &p, const point &q 72
      double c1 = cross(p - a, b - a), c2 =
           cross(q - a, b - a);
```

```
37 }
39 double angle ABC(const point &a, const point 81
        &b, const point &c) {
      double r = std::remainder(std::arg(a - b 83
            ) - std::arg(c - b), 2.0 * PI);
      return std::abs(r);
42 }
44 int main() {
      // sample
      point a = 2.0;
                                   // (2,0)
      point b(3.0, 7.0);
                                  // (3,7)
      std::cout << a << ' ' << b << '\n'; //
                                                    88
            (2,0)(3,7)
      std::cout << a + b << '\n';
            (5,7)
      // usage examples
      point p1(3, 2), p2(2, -7);
      std::cout << "p1 + p2 = " << p1 + p2 <<
            ' \ n'; \ // (5,-5)
      std::cout << "p1 - p2 = " << p1 - p2 <<
            '\n'; // (1,9)
      std::cout << "3.0 * p1 = " << 3.0 * p1
            << '\n'; // (9,6)
      std::cout << "p1 / 5.0 = " << p1 / 5.0
            << '\n'; // (0.6,0.4)
      // dot / cross via complex
      std::cout \langle\langle "dot(p1, p2) = " \langle\langle dot(p1, p2) \rangle\rangle
            p2) << '\n';
       std::cout << "cross(p1,p2) = " << cross(
            p1, p2) << '\n';
      // distances, angle, rotation, polar/
            cartesian
      std::cout << "squared dist = " << std::</pre>
            norm(p1 - p2) << ' / n';
      std::cout << "euclid dist = " << std::
            abs(p1 - p2) \langle\langle ' \rangle n';
      std::cout << "angle p1->p2 = " <<
            angle between(p1, p2) \langle\langle ' \rangle n' \rangle
       std::cout << "angle ABC = " << angle ABC
            (point(1,0), point(0,0), point(0,1))
             << '\n';
      // project / reflect / intersect
            examples
      point v(1, 1);
      point proj = project onto vector(p1, v);
                                                   23
      std::cout << "project p1 onto v = " <<
            proj << '\n';
      point lineA(0,0), lineB(2,0);
      std::cout << "project p1 onto line = "
            << project_onto_line(p1, lineA,
```

return (c1 * q - c2 * p) / (c1 - c2); //

34 double angle between(const point &a, const

// anale of vector b - a

return std::arg(b - a);

point &b) {

undefined if parallel (divide by

```
lineB) << ' \setminus n';
std::cout << "reflect p1 across line = "</pre>
      << reflect across line(p1, lineA,
     lineB) << ' \setminus n';
// intersection example
point r1a(0,0), r1b(1,1);
point r2a(0,1), r2b(1,0);
std::cout << "intersection = " <<</pre>
     intersection(r1a, r1b, r2a, r2b) <<
// polar/cartesian and rotation
point polar pt = std::polar(5.0, PI/4);
std::cout << "polar(5,PI/4) = " <<
     polar pt << ' \setminus n';
point rotated = p1 * std::polar(1.0, PI
     /2); // rotate p1 by 90 degrees
     about origin
std::cout << "rotate p1 by 90deg = " <<
     rotated << '\n';
return 0;
```

6 Graph

6.1 Euler tour+RMQ

```
1 // Euler Tour Technique
 2 class LCA {
       const vector<vector<int>>& adj;
       vector<int> d, first, euler{}, log2{};
       vector<vector<int>> st{};
       void dfs(int u, int w = -1, int dep = 0)
           d[u] = dep;
           first[u] = euler.size();
           euler.push back(u);
           for (auto& v : adj[u]) {
               if (v == w) continue;
13
               dfs(v, u, dep + 1);
               euler.push_back(u);
15
16
17 public:
      LCA(const vector<vector<int>>& adj, int
            root) : adj{_adj}, n{adj.size()}, d
            (n), first(n) {
           dfs(root);
20
           int tn{euler.size()};
21
           log2.resize(tn + 1);
          log2[1] = 0;
24
          for (int i{2}; i <= tn; ++i) log2[i]</pre>
                 = log2[i / 2] + 1;
           st.assign(tn, vector<int>(log2[tn] +
           for (int i{tn - 1}; i >= 0; --i) {
```

```
st[i][0] = euler[i];
               for (int j{1}; i + (1 << j) <=
                     tn; ++j) {
                    auto& x{st[i][j - 1]};
                    auto& y{st[i + (1 << (j - 1)</pre>
                         )][j - 1]};
                    st[i][j] = d[x] \leftarrow d[y] ? x
                         : у;
           }
      int operator()(int u, int v) {
           int l{first[u]}, r{first[v]};
           if (1 > r) swap(1, r);
           ++r; // make the interval left
                closed right open
           int j{log2[r - 1]};
           auto& x{st[1][j]};
           auto& y{st[r - (1 << j)][j]};</pre>
           return d[x] <= d[y] ? x : y;</pre>
46 };
48 int main() {
      int n, q;
      cin >> n >> q;
      vector<vector<int>> adj(n);
      for (int i = 1; i < n; ++i) {</pre>
           int u;
           cin >> u;
           u - - :
           adj[u].pb(i);
           adj[i].pb(u);
      LCA lca(adj, 0);
      while (q--) {
           int u, v;
           cin >> u >> v;
           u--, v--;
           cout << lca(u, v) + 1 << "\setminus \setminus n";
       return 0;
```

6.2 Prim

6.3 Eulerian cycle

size();

vector<int> res{};

m /= 2;

1 // Eulerian cycle in an undirected graph

int, int>>>& adj, int w = 0) {

int n{adj.size()}, m{};

vector<int> euler_cycle(vector<vector<pair</pre>

for (int $v\{0\}$; v < n; ++v) m += adj[v].

```
stack<pair<int, int>> stk{};
    stk.emplace(w, -1);
    vector<int> nxt(n);
    vector<bool> usd(m);
    while (!stk.empty()) {
        auto [u, i]{stk.top()};
        while (nxt[u] < adj[u].size() && usd</pre>
             [adj[u][nxt[u]].second]) ++nxt[u
        if (nxt[u] < adj[u].size()) {</pre>
            auto [v, j]{adj[u][nxt[u]]};
            ++nxt[u], usd[j] = true, stk.
                 emplace(v, j);
        } else {
            if (i != -1) res.push_back(i);
            stk.pop();
    return res;
int main() {
    int n = 4; // number of vertices
    vector<vector<pair<int, int>>> adj(n);
    // Add edges with edge IDs
    int eid = 0;
    auto add_edge = [&](int u, int v) {
        adj[u].push_back({v, eid});
        adj[v].push_back({u, eid});
        ++eid;
    };
    add_edge(0, 1);
```

6.4 Floyd-Warshall

```
1 // Floyd-Warshall algorithm
2 template<typename T>
3 vector<vector<optional<T>>> Flovd Warshall(
       const vector<vector<optional<T>>>& adj)
      const auto& n{adj.size()};
      auto d{adj};
      for (int i{0}; i < n; ++i) d[i][i] = 0;</pre>
      for (int k{0}; k < n; ++k)</pre>
          for (int i{0}; i < n; ++i)</pre>
              for (int j{0}; j < n; ++j) {</pre>
                   if (!d[i][k] || !d[k][j])
                        continue; // no value
                   if (!d[i][j] || d[i][j] > d[
                        i][k].value() + d[k][j].
                        value())
                       d[i][j] = d[i][k].value
                            () + d[k][j].value()
      return d;
```

6.5 MST

6.6 all longest path dfs

```
1 // all longest path (generalization of the
       tree diameter problem)
vector<tuple<int, int, int>> dp{};
3 // [mx1, x, mx2] the path of mx1 goes
       through x
  int dfs1(int u, int w = -1) {
      int mx{0};
      for (auto& v : adj[u])
          if (v != w) {
               auto 1{1 + dfs1(v, u)};
              mx = max(mx, 1);
               auto& [mx1, x, mx2]{dp[u]};
              if (1 >= mx1) mx2 = mx1, mx1 = 1
                   , x = v;
               else if (1 > mx2) mx2 = 1;
14
      return mx;
15
16 }
void dfs2(int u, int w = -1) {
      if (w != -1) {
          int tmx:
          { // calculate the longest path
20
               through parent
              auto& [mx1, x, mx2]{dp[w]};
              if (x != u) tmx = mx1 + 1;
               else tmx = mx2 + 1:
23
24
          { // update the path
              auto& [mx1, x, mx2]{dp[u]};
              if (tmx >= mx1) mx2 = mx1, mx1 =
                    tmx, x = w:
              else if (tmx > mx2) mx2 = tmx;
      for (auto& v : adj[u])
          if (v != w) dfs2(v, u);
32
33 }
34 void all_longest_path() {
      dfs1(0), dfs2(0);
```

6.7 all longest path top sort

```
1  // all longest path in DAG
2  // 1. topological sort
3  vector<int> in(n, 0);
  for (int i = 0; i < m; ++i) {
      int a, b, w;
      cin >> a >> b >> w;
      adj[a].emplace_back(b, w);
      in[b]++;
}

vector<int> topo; // sequence of top sort
queue<int> q;
  for (int i = 0; i < n; ++i) {
      if (in[i] == 0) {
            q.push(i);
      }
}</pre>
```

67

```
24 }
18 while (!q.empty()) {
      int pa = q.front();
      q.pop();
      topo.push back(pa);
      for (auto& [child, w] : adj[pa]) {
          in[child]--;
          if (in[child] == 0) {
              q.push(child);
30 // all longest path
31 vector<int> dist(n, INT MIN);
32 vector<vector<int>> parents(n);
33 dist[0] = process[0];
  for (int u : topo) {
      for (auto& [v, w] : adj[u]) {
          if (dist[v] < dist[u] + process[v] + 12</pre>
               dist[v] = dist[u] + process[v] +
              parents[v] = {u};
          else if (dist[v] == dist[u] +
               process[v] + w) {
               parents[v].push_back(u);
45
47 cout << dist[n - 1];
```

6.8 Dijkstra

```
1 // Dijkstra algorithm
2 template<typename T>
3 vector<optional<T>> Dijkstra(const vector
      vector<pair<int, T>>>& adj, int s) {
     const auto& n{adj.size()};
     vector<optional<T>>> d(n, nullopt);
     d[s] = 0;
     vector<bool> found(n, false);
     using pq t = pair<T, int>;
     priority_queue<pq_t, vector<pq_t>,
          greater<pq_t>> pq{};
     pq.emplace(0, s);
     while (!pq.empty()) {
         auto [_, u]{pq.top()}; pq.pop();
         if (found[u]) continue;
         found[u] = true;
         for (auto& [v, w] : adj[u])
             if (!d[v] || d[v] > d[u].value()
                 d[v] = d[u].value() + w;
                 pq.emplace(d[v].value(), v);
     return d;
```

6.9 binary lifting

vector<int> log2;

vector<vector<int>> an{};

const vector<vector<int>>& adj;

1 // binary liftina

int n;
vector<int> d;

2 class LCA {

```
void dfs(int u, int w = -1, int dep = 0)
          d[u] = dep;
          an[u][0] = w;
          for (int i{1}; i <= log2[n - 1] &&
              an[u][i - 1] != -1; ++i)
              an[u][i] = an[an[u][i - 1]][i -
                  1]; // 走 2^(i-1) 再走 2^(i
                   -1) 步
          // 因為計算 an 會用到祖先的資訊,所
               以先計算再繼續往下
          for (auto& v : adj[u]) {
              if (v == w) continue; // parent
              dfs(v, u, dep + 1);
  public:
      LCA(const vector<vector<int>>& _adj, int
      : adj{_adj}, n{adj.size()}, d(n), log2(n
          \log 2[1] = 0;
          for (int i{2}; i < log2.size(); ++i)</pre>
               log2[i] = log2[i / 2] + 1;
          an.assign(n, vector<int>(log2[n - 1]
               + 1, -1));
          dfs(root);
      int operator()(int u, int v) {
          if (d[u] > d[v]) swap(u, v);
          for (int i{log2[d[v] - d[u]]}; i >=
              0: --i)
              if (d[v] - d[u] >= (1 << i)) v =
                   an[v][i];
          // v 先走到跟 u 同高度
          if (u == v) return u;
          for (int i{log2[d[u]]}; i >= 0; --i)
              if (an[u][i] != an[v][i]) u = an
                  [u][i], v = an[v][i];
          // u, v 一起走到 Lca(u, v) 的下方
          return an[u][0];
          // 回傳 Lca(u, v)
43 };
  int main() {
     int n, q;
```

```
cin >> n >> q;
vector<vector<int>>> adj(n);

for (int i = 1; i < n; ++i) {
    int u;
    cin >> u;
    u--;
    adj[u].pb(i);
    adj[i].pb(u);
}

// adj, root
LCA lca(adj, 0);

while (q--) {
    int u, v;
    cin >> u >> v;
    u--, v--;
    cout << lca(u, v) + 1 << "\\n";
}
return 0;
}</pre>
```

6.10 topological sort

```
1 // topological sort 1
2 optional<vector<int>> top_sort(vector<vector</pre>
      <int>>& adj) {
      vector<int> res{};
      int n{static_cast<int>(adj.size())};
      vector<int> cnt(n, 0); // predecessor
      for (int u = 0; u < n; ++u)</pre>
          for (auto& v : adj[u]) ++cnt[v];
      queue<int> qu{};
      for (int u = 0; u < n; ++u) if (!cnt[u])</pre>
            qu.push(u);
      while (!qu.empty()) {
          auto u = qu.front();
          qu.pop();
          res.push back(u);
          for (auto& v : adj[u])
              if (!--cnt[v]) qu.push(v);
      if (res.size() != adj.size()) return
           nullopt:
      return res:
```

6.11 tree diameter

```
int diam = 0;

int dfs(int u, int p = -1) {
   int mx = 0;
   for (int v : adj[u]) {
      if (v != p) {
```

```
int len = 1 + dfs(v, u);
diam = max(diam, mx + len);
mx = max(mx, len);
}

return mx;
```

6.12 all longest path

```
int fir[maxn]; // Length of the Longest
       downward path from u into its subtree.
1 int sec[maxn]; // Length of the second
       longest downward path from u
  int res[maxn];
  void dfs1(int u, int p) {
      for (int v : adj[u]) {
          if (v != p) {
               dfs1(v, u);
               if (fir[v] + 1 > fir[u]) {
                   sec[u] = fir[u];
11
                   fir[u] = fir[v] + 1;
12
13
               else if (fir[v] + 1 > sec[u]) {
                   sec[u] = fir[v] + 1;
14
15
16
17
  // to p: the best path length that comes
       from the parent's side
void dfs2(int u, int p, int to_p) {
      res[u] = max(to_p, fir[u]);
24
      for (int v : adj[u]) {
           if (v != p) {
               if (fir[v] + 1 == fir[u]) {
27
                   dfs2(v, u, max(to_p, sec[u])
                        + 1);
               else {
29
                   dfs2(v, u, res[u] + 1);
30
31
32
36 // usage
37 dfs1(1, 0);
38 dfs2(1, 0, 0);
39 // Now res[i] is the maximum distance from
       node i to any other node
40 for (int i = 1; i <= n; i++) {
      cout << res[i] << " ";
```

6.13 tree diameter (len,end)

```
| array<int, 2> dfs(int u, int w = -1) {
      array < int, 2 > mx{0, u}; // {length,}
           farthest leaf}
      for (auto& v : adj[u]) {
          if (v == w) continue;
          auto [len, leaf]{dfs(v, u)};
          mx = max(mx, \{len + 1, leaf\});
      return mx;
11 array<int, 3> tree_diameter(int a = 0) {
      auto b{dfs(a)[1]};
                              // farthest node
            from 'a'
      auto [1, c]{dfs(b)};
                              // farthest node
           from 'b'
      return {1, b, c};
                              // {diameter
           length, endpoint1, endpoint2}
```

6.14 Bellman-Ford

```
1 // Bellman-Ford algorithm
2 template<typename T>
3 optional<vector<optional<T>>> Bellman Ford(
      const vector<vector<pair<int, T>>>& adj,
     const auto& n{adi.size()}:
     vector<optional<T>> d(n, nullopt);
     d[s] = 0:
     queue<int> qu{}, qu2{};
     vector<bool> in(n, false), in2(n, false)
     qu.push(s), in[s] = true;
     for (int i{0}; i < n; ++i) { // at most</pre>
          n-1 edges
         while (!qu.empty()) {
             int u{qu.front()};
             qu.pop(), in[u] = false;
             for (auto& [v, w] : adj[u])
                 if (!d[v] | | d[v] > d[u].
                      value() + w) { // relax
                     d[v] = d[u].value() + w;
                     if (!in2[v]) qu2.push(v)
                          , in2[v] = true;
         qu.swap(qu2), in.swap(in2);
     if (qu.empty()) return d;
     return nullopt; // if negative cycle
```

7 Language

7.1 CNF

1 #define MAXN 55

struct CNF{

```
int s,x,y;//s->xy \mid s->x, if y==-1
    int cost;
    CNF(){}
    CNF(int s,int x,int y,int c):s(s),x(x),y(y
        ),cost(c){}
8 int state; //規則數量
9| map<char, int> rule; // 每個字元對應到的規則
       小寫字母為終端字符
  vector<CNF> cnf;
  void init(){
    state=0;
    rule.clear();
    cnf.clear():
  void add to cnf(char s,const string &p,int
    //加入一個s -> 的文法,代價為cost
   if(rule.find(s)==rule.end())rule[s]=state
    for(auto c:p)if(rule.find(c)==rule.end())
         rule[c]=state++;
    if(p.size()==1){
      cnf.push_back(CNF(rule[s],rule[p[0]],-1,
           cost));
    }else{
      int left=rule[s];
      int sz=p.size();
      for(int i=0;i<sz-2;++i){</pre>
        cnf.push back(CNF(left,rule[p[i]],
            state,0));
       left=state++;
      cnf.push back(CNF(left,rule[p[sz-2]],
           rule[p[sz-1]],cost));
32 vector<long long> dp[MAXN][MAXN];
33 | vector < bool > neg INF[MAXN][MAXN];//如果花費
       是負的可能會有無限小的情形
34 void relax(int 1.int r.const CNF &c.long
       long cost,bool neg c=0){
    if(!neg_INF[1][r][c.s]&&(neg_INF[1][r][c.x
         ]||cost<dp[1][r][c.s])){
      if(neg_c||neg_INF[1][r][c.x]){
        dp[1][r][c.s]=0;
        neg_INF[1][r][c.s]=true;
      }else dp[l][r][c.s]=cost;
  void bellman(int l,int r,int n){
   for(int k=1:k<=state:++k)</pre>
      for(auto c:cnf)
        if(c.y==-1)relax(l,r,c,dp[l][r][c.x]+c
             .cost,k==n);
```

```
47 | void cyk(const vector<int> &tok){
    for(int i=0;i<(int)tok.size();++i){</pre>
      for(int i=0:i<(int)tok.size():++i){</pre>
         dp[i][j]=vector<long long>(state+1,
         neg INF[i][j]=vector<bool>(state+1,
              false);
53
      dp[i][i][tok[i]]=0;
54
      bellman(i,i,tok.size());
    for(int r=1;r<(int)tok.size();++r){</pre>
      for(int l=r-1;l>=0;--1){
         for(int k=1;k<r;++k)</pre>
           for(auto c:cnf)
             if(~c.y)relax(1,r,c,dp[1][k][c.x]+
                  dp[k+1][r][c.y]+c.cost);
         bellman(l,r,tok.size());
63
64 }
```

8 Number Theory

8.1 Linear Sieve

```
// Calculate the smallest divisor of
    integers in [2, maxn) in O(maxn)

vector<int> min_div{[] {
    constexpr int maxn = 400000 + 10;

vector<int> v(maxn), p;

for (int i = 2; i < maxn; ++i) {
    if (!v[i]) {
        v[i] = i;
        p.push_back(i);
    }

for (int j = 0; p[j] * i < maxn; ++j
    ) {
        v[p[j] * i] = p[j];
        if (p[j] == v[i]) break;
    }

return v;
}
</pre>
```

8.2 C(n,m)

8.3 derangement (Principle of Inclusion-Exclusion)

```
1 // 1. Principle of Inclusion-Exclusion
2 // n! = n! * Σ (from k=0 to n) [((-1)^k) / (k!)]

3 
4 mint c = 1;
5 for (int i = 1; i <= n; i++) {
    c = (c * i) + (i % 2 == 1 ? -1 : 1);
    cout << c.val() << ' ';
8 }
```

8.4 matrix template (with fast power)

```
i template < class T> struct Matrix {
      T **mat; int a, b;
      Matrix() : a(0), b(0) {}
      Matrix(int a , int b ) : a(a ), b(b ) {
          int i, j;
           mat = new T*[a];
          for (i = 0; i < a; ++i) {
               mat[i] = new T[b];
               for (j = 0; j < b; ++j){
                   mat[i][j] = 0;
13
      Matrix(const vector<vector<T>>& vt) {
           int i, j;
           *this = Matrix((int)vt.size(), (int)
                vt[0].size());
           for (i = 0; i < a; ++i) {</pre>
               for (j = 0; j < b; ++j) {
                   mat[i][j] = vt[i][j];
23
24
      Matrix operator*(const Matrix& m) {
           int i, j, k;
           assert(b == m.a):
           Matrix r(a, m.b);
           for (i = 0; i < a; ++i) {</pre>
               for (j = 0; j < m.b; ++j) {</pre>
                   for (k = 0; k < b; ++k) {
                        r.mat[i][j] += mul(mat[i
                             ][k], m.mat[k][j]);
                        r.mat[i][j] %= MOD;
38
           return r;
39
      Matrix& operator*=(const Matrix& m) {
40
41
           return *this = (*this) * m;
```

8.5 Sieve of Eratosthenes (with big num)

```
1 const int MX = 100000;
  bool np[MX + 1];
  vector<int> prime numbers;
  int init = []() {
      np[0] = np[1] = true;
      for (int i = 2; i <= MX; i++) {
          if (!np[i]) {
              prime_numbers.push_back(i);
              for (int j = i; j <= MX / i; j</pre>
                  ++) { // 避免溢出的写法
                  np[i * j] = true;
          }
      return 0;
16 }();
18 bool is_prime(long long n) {
      if (n <= MX) {
          return !np[n];
      for (long long p : prime_numbers) {
          if (p * p > n) {
              break;
          if (n % p == 0) {
              return false;
      return true;
```

8.6 mod inv

8.7 derangement (DP)

8.8 fast power

8.9 first and second mex

8.10 Chinese Remainder Theorem

8.11 mod inv (not prime)

```
/* exists when a and mod are coprime */
/* but mod is not prime */
long long MI(long long a, long long mod) {
    return power_mod(a, euler_phi(mod) - 1,
    mod);
}
```

8.12 Euler Totient precompute

8.13 mod inv (not coprime)

```
/* a and mod are not coprime */
long long MI(long long a, long long mod) {
    long long d, x, y;
    extEcu(a, mod, d, x, y);
    return d == 1 ? (x + mod) % mod : -1;
}
```

8.14 Euler Totient

```
int euler_phi(int n) {
   int res{n};
   for (int i{2}; i * i <= n; ++i) {
      if (n % i) continue;
      while (n % i == 0) n /= i;
      res = res / i * (i - 1);
   }
   if (n > 1) res = res / n * (n - 1);
   return res;
}
```

8.15 C(n,k) mod inverse

```
fac[0] = 1;
for (int i = 1; i <= n; ++i) {
    fac[i] = fac[i - 1] * i % MOD;
}
inv_fac[n] = power_mod(fac[n], MOD - 2, MOD)
inv_fac[i] = inv_fac[i + 1] * (i + 1) %
MOD;
}
// C(n, k) = fac[n] * inv_fac[k] * inv_fac[n - k];</pre>
```

8.16 擴展歐基里德

```
1  /* solve x, y for ax + by = gcd(a, b) = g */
2  template < typename T >
3  void extEcu(T a, T b, T &g, T &x, T &y) {
    if (b) extEcu(b, a % b, g, y, x), y -= x
        * (a / b);
5  else g = a, x = 1, y = 0;
6 }
```

8.17 Sieve of Eratosthenes

8.18 C(n,k) DP

| class Solution {

9.1 Z

String

```
c = i;
               int l = p[i] - 1;
              if(1 \% 2 == 0) cnt += 1 / 2;
               else cnt += 1 / 2 + 1:
          return cnt;
23
25 };
  9.3 AC 自動機
1 template < char L='a', char R='z'>
  class ac automaton{
    struct joe{
      int next[R-L+1],fail,efl,ed,cnt_dp,vis;
      joe():ed(0),cnt dp(0),vis(0){
        for(int i=0;i<=R-L;++i)next[i]=0;</pre>
    };
  public:
    std::vector<ioe> S:
    std::vector<int> q;
    int qs,qe,vt;
```

if (i <= box r) {

i + 1):

i + z[i] {

box r = i + z[i];

int countSubstrings(string s) {

ch = ch + c + "#";

int c = 0, r = 0, cnt = 0;

if(i + p[i] > r) {

r = i + p[i];

for(int i = 0; i < 12; i++) {</pre>

], r - i): 1;

p[i] = (i < r)? min(p[2 * c - i)

while(i + p[i] < 12 && i - p[i]

- p[i]]) p[i]++;

>= 0 && ch[i + p[i]] == ch[i 46]

string ch = "#";

for(char c: s) {

vector<int> p(12);

int 11 = s.size(), 12 = 11 * 2 + 1;

box l = i;

z[i]++;

z[0] = n;

return z;

public:

manacher

z[i] = min(z[i - box 1], box r -

while (i + z[i] < n && s[z[i]] == s[

```
ac_automaton():S(1),qs(0),qe(0),vt(0){}
    void clear(){
      a.clear():
      S.resize(1);
      for(int i=0;i<=R-L;++i)S[0].next[i]=0;</pre>
      S[0].cnt dp=S[0].vis=qs=qe=vt=0;
    void insert(const char *s){
21
      int o=0:
      for(int i=0,id;s[i];++i){
        id=s[i]-L;
        if(!S[o].next[id]){
          S.push_back(joe());
          S[o].next[id]=S.size()-1;
        o=S[o].next[id];
30
      ++S[o].ed;
31
    void build_fail(){
      S[0].fail=S[0].efl=-1;
      q.clear();
      q.push back(0);
      ++qe;
      while(qs!=qe){
        int pa=q[qs++],id,t;
        for(int i=0;i<=R-L;++i){</pre>
          t=S[pa].next[i];
          if(!t)continue;
          id=S[pa].fail;
          while(~id&&!S[id].next[i])id=S[id].
               fail;
          S[t].fail=~id?S[id].next[i]:0;
          S[t].efl=S[S[t].fail].ed?S[t].fail:S
               [S[t].fail].efl;
          q.push back(t);
          ++qe;
48
49
    /*DP出每個前綴在字串s出現的次數並傳回所有
         字串被s匹配成功的次數O(N+M)*/
    int match 0(const char *s){
      int ans=0,id,p=0,i;
      for(i=0;s[i];++i){
        id=s[i]-L;
        while(!S[p].next[id]&&p)p=S[p].fail;
        if(!S[p].next[id])continue;
        p=S[p].next[id];
        ++S[p].cnt_dp;/*匹配成功則它所有後綴都
59
             可以被匹配(DP計算)*/
60
      for(i=qe-1;i>=0;--i){
61
        ans+=S[q[i]].cnt_dp*S[q[i]].ed;
62
63
        if(~S[q[i]].fail)S[S[q[i]].fail].
             cnt dp+=S[q[i]].cnt dp;
65
      return ans;
66
    /*多串匹配走efL邊並傳回所有字串被s匹配成功
```

的 次 數 O(N*M^1.5)*/

int ans=0,id,p=0,t;

id=s[i]-L;

for(int i=0;s[i];++i){

int match 1(const char *s)const{

```
73
        if(!S[p].next[id])continue;
74
        p=S[p].next[id];
75
        if(S[p].ed)ans+=S[p].ed;
76
        for(t=S[p].efl;~t;t=S[t].efl){
          ans+=S[t].ed;/*因為都走efl邊所以保證
77
               匹配成功*/
78
79
80
      return ans;
81
    /*枚舉(s的子字串nA)的所有相異字串各恰一次
         並傳回次數O(N*M^(1/3))*/
    int match_2(const char *s){
84
      int ans=0,id,p=0,t;
85
      ++vt;
86
      /*把戳記vt+=1,只要vt沒溢位,所有S[p].
           vis==vt就會變成false
       這種利用vt的方法可以0(1)歸零vis陣列*/
      for(int i=0;s[i];++i){
        id=s[i]-L;
        while(!S[p].next[id]&&p)p=S[p].fail;
        if(!S[p].next[id])continue;
        p=S[p].next[id];
        if(S[p].ed&&S[p].vis!=vt){
          S[p].vis=vt;
          ans+=S[p].ed;
        for(t=S[p].efl;~t&&S[t].vis!=vt;t=S[t
             1.ef1){
          S[t].vis=vt;
          ans+=S[t].ed;/*因為都走efL邊所以保證
               匹配成功*/
100
101
102
      return ans;
103
    /*把AC自動機變成真的自動機*/
104
    void evolution(){
106
      for(qs=1;qs!=qe;){
107
        int p=q[qs++];
        for(int i=0;i<=R-L;++i)</pre>
108
          if(S[p].next[i]==0)S[p].next[i]=S[S[
109
              p].fail].next[i];
110
111
112 };
```

while(!S[p].next[id]&&p)p=S[p].fail;

9.4 KMP

```
cnt = pi[cnt - 1];
    if (pattern[cnt] == b) {
        cnt++;
    pi[i] = cnt;
}
vector<int> pos;
cnt = 0;
for (int i = 0; i < text.size(); i++) {</pre>
    char b = text[i];
    while (cnt && pattern[cnt] != b) {
        cnt = pi[cnt - 1];
    if (pattern[cnt] == b) {
        cnt++;
    if (cnt == m) {
        pos.push_back(i - m + 1);
        cnt = pi[cnt - 1];
return pos;
```

9.5 suffix array lcp

```
| #define radix_sort(x,y){\
    for(i=0;i<A;++i)c[i]=0;\</pre>
    for(i=0;i<n;++i)c[x[y[i]]]++;\</pre>
    for(i=1;i<A;++i)c[i]+=c[i-1];\</pre>
    for(i=n-1;~i;--i)sa[--c[x[y[i]]]]=y[i];\
  #define AC(r,a,b)\
    r[a]!=r[b]||a+k>=n||r[a+k]!=r[b+k]
   void suffix_array(const char *s,int n,int *
       sa,int *rank,int *tmp,int *c){
    int A='z'+1,i,k,id=0;
    for(i=0;i<n;++i)rank[tmp[i]=i]=s[i];</pre>
    radix sort(rank,tmp);
    for(k=1;id<n-1;k<<=1){</pre>
      for(id=0,i=n-k;i<n;++i)tmp[id++]=i;</pre>
      for(i=0;i<n;++i)</pre>
        if(sa[i]>=k)tmp[id++]=sa[i]-k;
      radix sort(rank,tmp);
      swap(rank,tmp);
      for(rank[sa[0]]=id=0,i=1;i<n;++i)</pre>
        rank[sa[i]]=id+=AC(tmp,sa[i-1],sa[i]);
      A=id+1;
24 //h: 高度數組 sa:後綴數組 rank:排名
void suffix_array_lcp(const char *s,int len,
       int *h,int *sa,int *rank){
    for(int i=0;i<len;++i)rank[sa[i]]=i;</pre>
    for(int i=0,k=0;i<len;++i){</pre>
      if(rank[i]==0)continue;
      if(k)--k;
      while(s[i+k]==s[sa[rank[i]-1]+k])++k;
      h[rank[i]]=k;
    h[0]=0;// h[k]=lcp(sa[k],sa[k-1]);
```

9.6 hash

34 }

```
1 #define MAXN 1000000
  #define mod 1073676287
  /*mod 必須要是質數*/
  typedef long long T;
 char s[MAXN+5];
6 T h[MAXN+5];/*hash陣列*/
  T h base[MAXN+5];/*h base[n]=(prime^n)%mod*/
  void hash init(int len,T prime){
    h base[0]=1;
    for(int i=1;i<=len;++i){</pre>
      h[i]=(h[i-1]*prime+s[i-1])%mod;
      h_base[i]=(h_base[i-1]*prime)%mod;
15 T get_hash(int l,int r){/*閉區間寫法・設編號
       為0 ~ Len-1*/
    return (h[r+1]-(h[1]*h_base[r-1+1])%mod+
         mod)%mod;
17 }
```

9.7 minimal string rotation

```
| int min_string_rotation(const string &s){
| int n=s.size(),i=0,j=1,k=0; | while(i<n&&j<n&&k<n){
| int t=s[(i+k)%n]-s[(j+k)%n]; | ++k; | if(t){
| if(t>0)i+=k; | else j+=k; | if(i==j)++j; | k=0; | } | } | return min(i,j);//最小循環表示法起始位置
```

9.8 reverseBWT

```
const int MAXN = 305, MAXC = 'Z';
int ranks[MAXN], tots[MAXC], first[MAXC];
void rankBWT(const string &bw){
   memset(ranks,0,sizeof(int)*bw.size());
   memset(tots,0,sizeof(tots);
   for(size_t i=0;i<bw.size();++i)
      ranks[i] = tots[int(bw[i])]++;
}
void firstCol(){
   memset(first,0,sizeof(first));
   int tot = 0;
   for(int c='A';c<='Z';++c){
   if(!tots[c]) continue;</pre>
```

10 default

10.1 debug

10.2 template

```
1 // alias g++='g++ -std=c++14 -fsanitize=
       undefined -Wall -Wextra -Wshadow -D
       LOCAL'
  #include <bits/stdc++.h>
  using namespace std;
  #ifdef LOCAL
7 void dbg() { cerr << '\\n'; }</pre>
  template < class T, class ... U> void dbg(T a,
       U ...b) { cerr << a << ' ', dbg(b...); }
  template < class T> void org(T 1, T r) { while
        (1 != r) cerr << *1++ << ' '; cerr <<
       \\n'; }
10 #define debug(args...) (dbg("#> (" + string)
       (#args) + ") = (", args, ")"))
11 #define orange(args...) (cerr << "#> [" +
       string(#args) + ") = ", org(args))
#pragma GCC optimize("03,unroll-loops")
```

```
14 #pragma GCC target("avx2,bmi,bmi2,lzcnt,
       popcnt")
#define debug(...) ((void)0)
16 #define orange(...) ((void)0)
17 #endif
19 #define int long long
20 #define pii pair<int, int>
21 #define ff first
22 #define ss second
23 #define pb push back
24 #define SPEEDY ios_base::sync_with_stdio(
       false); cin.tie(0); cout.tie(0);
26 void solve() {
27
28 }
30 signed main() {
      SPEEDY;
33
      return 0;
34 }
```

13

11 other

11.1 Nim game

```
ı a1^a2^a3^...^an != 0 ? A win : B win
```

11.2 找小於 n 所有出現的 1 數量

```
1 current == 0 higher * factor
2 current == 1 higher * factor + lower + 1
3 other current (higher + 1) * factor
```

2 other language

12.1 python heap

```
import heapq

heap = [7,1,2,2]
heapq.heapify(heap)
print(heap) # [1, 2, 2, 7]
heapq.heappush(heap, 5)
print(heap) # [1, 2, 2, 7, 5]
print(heapq.heappop(heap)) # 1
print(heap) # [2, 2, 5, 7]
```

12

13

20

21

22

23

24

25

44

47

48

52

53

58 # 遞迴分解

59 def factor(n, out):

else:

if n == 1:

隨機多項式 (x^2 + c) mod n

起始點

while d == 1:

if d == n:

if d > 1 and d < n:

return d

if is probable prime(n):

out.append(n)

找到非平凡因數

c = random.randrange(1, n-1)

x = random.randrange(2, n-1)

 $\rightarrow f(x)$

-> f(f(y)), 走兩步

y = (pow(y, 2, n) + c) % n

計算兩者差的 acd

d = gcd(abs(x - y), n)

失敗就重試 break

隨機挑選常數 c

while True:

y = x

d = 1

12.2 java

12.2.1 文件操作

```
i import java.io.*;
 import java.util.*;
 import iava.math.*:
 import java.text.*;
 public class Main{
   public static void main(String args[]){
       throws FileNotFoundException.
        IOException
     Scanner sc = new Scanner(new FileReader(
          "a.in"));
     PrintWriter pw = new PrintWriter(new
         FileWriter("a.out"));
     int n,m;
     n=sc.nextInt();//读入下一个INT
     m=sc.nextInt();
     for(ci=1: ci<=c: ++ci){</pre>
       pw.println("Case #"+ci+": easy for
           output"):
     pw.close();//关闭流并释放,这个很重要,
          否则是没有输出的
     sc.close();// 关闭流并释放
```

12.2.2 优先队列

```
1 | PriorityQueue queue = new PriorityQueue( 1,
      new Comparator(){
   public int compare( Point a, Point b ){
   if(a.x < b.x | | a.x == b.x && a.y < b.y)
   else if( a.x == b.x && a.y == b.y )
     return 0:
   else return 1;
9 });
```

12.2.3 Map

```
1 | Map map = new HashMap();
2 map.put("sa","dd");
3 String str = map.get("sa").toString;
for(Object obj : map.keySet()){
   Object value = map.get(obj );
```

12.2.4 sort

```
static class cmp implements Comparator{
  public int compare(Object o1,Object o2){
  BigInteger b1=(BigInteger)o1;
  BigInteger b2=(BigInteger)o2;
  return b1.compareTo(b2);
public static void main(String[] args)
     throws IOException{
  Scanner cin = new Scanner(System.in);
  n=cin.nextInt();
  BigInteger[] seg = new BigInteger[n];
  for (int i=0;i<n;i++)</pre>
  seg[i]=cin.nextBigInteger();
  Arrays.sort(seg, new cmp());
```

12.3 python output

```
i hello = 'Hello'
  world = 7122
  print(f'{hello} {world}') # Hello 7122
  import math
  print(f'PI is approximately {math.pi:.3f}.')
  # PI is approximately 3.142.
  print('AAA {} BBB "{}!"'.format('Jin', 'Kela
       ′))
  # AAA Jin BBB "Kela!"
12 hello = 'hello, world\n'
13 hellos = repr(hello)
14 print(hellos) # 'hello, world\n'
|v| = 40000
print(repr((x, y, ('spam', 'eggs'))))
19 # "(32.5, 40000, ('spam', 'eggs'))"
21 | x = 7
22 print(eval('3 * x')) # 21
```

12.4 pvthon 大數因數分解

```
il # 大數因數分解 (使用 Pollard's Rho 與 Miller
     -Rabin)
 import sys, random
 from math import gcd
 # Miller-Rabin 檢定(機率性質數判定)
 def is probable prime(n, k=12):
    if n < 2:
        return False
     # 先檢查一些小質數
```

```
small primes =
                                                        d = pollards rho(n)
                                              65
          [2,3,5,7,11,13,17,19,23,29]
                                                        while d is None or d == n: # 偶爾失
                                              66
      for p in small primes:
                                                             敗就重試
          if n % p == 0:
                                                            d = pollards_rho(n)
                                              67
             return n == p
                                              68
                                                        factor(d, out)
      # 把 n-1 寫成 d * 2^s
                                              69
                                                        factor(n // d, out)
      d = n - 1
                                              70
     s = 0
                                                def main():
      while d % 2 == 0:
                                                    data = sys.stdin.read().strip().split()
         d //= 2
                                                    if not data:
          s += 1
                                                        return
      # 重複 k 次隨機測試
                                                    #每個 token 當作一個數字
      for _ in range(k):
                                                     for token in data:
          a = random.randrange(2, n - 1) # 隨
                                                        try:
                                                            n = int(token)
               機挑一個測試基數
                                              79
                                                        except:
          x = pow(a, d, n)
                                                            continue
          if x == 1 or x == n - 1:
                                                        if n <= 1:
             continue
                                                            print(n)
          composite = True
                                              83
                                                            continue
          for in range(s - 1):
                                                        facs = []
             x = pow(x, 2, n)
                                              85
                                                        factor(n, facs)
             if x == n - 1:
                                                        facs.sort()
                                              86
                 composite = False
                                                        #輸出因數
                 break
          if composite:
                                                        print(" ".join(str(x) for x in facs)
             return False
      return True
                                              90 if name == " main ":
36 # Pollard's Rho 演算法(找非平凡因數)
                                                    random.seed() # 使用系統時間作為隨機種
37 def pollards rho(n):
      if n % 2 == 0:
                                                     main()
          return 2
      if n % 3 == 0:
          return 3
```

12.5 decimal

```
川# 使用 decimal 模組來處理高精度小數運算
                               2 from decimal import *
                               3 setcontext(Context(prec=MAX_PREC, Emax=
                                     MAX EMAX, rounding=ROUND FLOOR))
                                4 print(Decimal(input()) * Decimal(input()))
x = (pow(x, 2, n) + c) % n # x 6 | # 將小數轉成分數‧方便做近似或理論分析‧且可
                                      以限制分母大小。
y = (pow(y, 2, n) + c) % n # y
                               7 from fractions import Fraction
                               8 Fraction('3.14159').limit denominator(10).
                                     numerator # 22
                               10 # 設定精確度
                               11 from decimal import Decimal, getcontext
                               13 # 精確位數設定
                               14 getcontext().prec = 70
                               16 n = 100
                               17 | # 指定n 為 高 精 確 度 的 物 件
                               n = Decimal(n)
                               19 n /= 7
                               20 print(n)
                               22 # 將小數轉成分數
                               23 from fractions import Fraction
```

```
25 | n = 1.5654
26 | # 建立一個轉換物件
27 | n = Fraction(n)
28
29 | print(n)
```

12.6 python 大數排序

12.7 python 大數計算 2

```
1 # 單行輸入
2 # format : n1, operation, n2
3 from sys import stdin
  data = stdin.read().splitlines()
 limit = len(data)
8 | i = 0
10 while(i < limit):</pre>
      a, operation, b = map(str, data[i].split
           ())
      a, b = int(a), int(b)
      i += 1
      if(operation == '+'):
          print(int(a + b))
      elif(operation == '-'):
          print(int(a - b))
      elif(operation == '*'):
          print(int(a * b))
      else:
          print(int(a // b))
```

12.8 python input

```
1  ans = sum(map(float, input().split()))
2  # input: 1.1 2.2 3.3 4.4 5.5
3  print(ans) # 16.5
4
5  (n, m) = map(int, input().split()) # 300 200
6  print(n * m) # 60000
7  Arr = list(map(int, input().split()))
9  # input: 1 2 3 4 5
10  print(Arr) # [1, 2, 3, 4, 5]
```

12.9 python 大數計算

13 zformula

13.1 formula

13.1.1 Pick 公式

給定頂點坐標均是整點的簡單多邊形·面積 = 內部格點數 + 邊上格點數/2-1

13.1.2 圖論

- 1. 對於平面圖 $\cdot F = E V + C + 1 \cdot C$ 是連通分量數 2. 對於平面圖 $\cdot E < 3V 6$
- 3. 對於連通圖 G·最大獨立點集的大小設為 I(G)·最大 匹配大小設為 M(G)·最小點覆蓋設為 Cv(G)·最小 邊覆蓋設為 Ce(G)。對於任意連通圖:

(a)
$$I(G) + Cv(G) = |V|$$

(b) $M(G) + Ce(G) = |V|$

- 對於連滿一分圖:
 - (a) I(G) = Cv(G)

```
(b) M(G) = Ce(G)
5. 最大權閉合圖:
```

```
\begin{array}{ll} \text{(a)} & C(u,v) = \infty, (u,v) \in E \\ \text{(b)} & C(S,v) = W_v, W_v > 0 \\ \text{(c)} & C(v,T) = -W_v, W_v < 0 \\ \text{(d)} & \operatorname{ans} = \sum_{W_v > 0} W_v - flow(S,T) \end{array}
```

6. 最大密度子圖:

```
人名及丁國 . (a) 求 \max\left(\frac{W_e + W_v}{|V'|}\right) , e \in E' , v \in V' (b) U = \sum_{v \in V} 2W_v + \sum_{e \in E} W_e (c) C(u,v) = W_{(u,v)}, (u,v) \in E · 雙向邊 (d) C(S,v) = U, v \in V
```

(e) $D_u = \sum_{(u,v) \in E} W_{(u,v)}$ (f) $C(v,T) = U + 2g - D_v - 2W_v, v \in V$ (g) 二分搜 g: $l = 0, r = U, eps = 1/n^2$ if $(U \times |V| - flow(S,T))/2 > 0$ l = midelse r = mid

- (h) ans= $min_cut(S,T)$ (i) |E| = 0 要特殊判斷
- 7 沈團・
 - (a) 點數大於 3 的環都要有一條弦
 - (b) 完美消除序列從後往前依次給每個點染色·給每個點染上可以染的最小顏色
 - (c) 最大團大小 = 色數
 - (d) 最大獨立集: 完美消除序列從前往後能選就選
 - (e) 最小團覆蓋: 最大獨立集的點和他延伸的邊構成
 - (f) 區間圖是弦圖
 - (g) 區間圖的完美消除序列: 將區間按造又端點由 小到大排序
 - (h) 區間圖染色: 用線段樹做

13.1.3 dinic 特殊圖複雜度

```
1. 單位流:O\left(\min\left(V^{3/2},E^{1/2}\right)E\right)
2. 二分圖:O\left(V^{1/2}E\right)
```

13.1.4 0-1 分數規劃

```
x_i = \{0,1\} \cdot x_i 可能會有其他限制 · 求 max\left(rac{\sum B_i x_i}{\sum C_i x_i}
ight)
```

- 1. $D(i,q) = B_i q \times C_i$
- 2. $f(g) = \sum D(i, g)x_i$
- 3. f(g) = 0 時 g 為最佳解 f(g) < 0 沒有意義
- 4. 因為 f(g) 單調可以二分搜 g
- 5. 或用 Dinkelbach 通常比較快

```
1 binary_search(){
2    while(r-1>eps){
3        g=(1+r)/2;
4    for(i:所有元素)D[i]=B[i]-g*C[i];//D(i,g)
5    找出一組合法x[i]使f(g)最大;
6    if(f(g)>0) l=g;
7    else r=g;
```

13.1.5 學長公式

11 Dinkelbach(){

Ans=g;

p=0,q=0; for(i:所有元素)

return Ans;

13

14

17

22 23 }

g=任意狀態(通常設為0);

}while(abs(Ans-g)>EPS);

找出一組合法x[i]使f(g)最大;

if(x[i])p+=B[i],q+=C[i];

g=p/q;//更新解·注意q=0的情况

```
1. \sum_{d|n} \phi(n) = n
```

2. $g(n) = \sum_{d|n} f(d) = f(n) = \sum_{d|n} \mu(d) \times g(n/d)$

for(i:所有元素)D[i]=B[i]-g*C[i];//D(i,g)

- 3. Harmonic series $H_n = \ln(n) + \gamma + 1/(2n) 1/(12n^2) + 1/(120n^4)$
- 4. $\gamma = 0.57721566490153286060651209008240243104215$
- 5. 格雷碼 = $n \oplus (n >> 1)$
- 6. $SG(A+B) = SG(A) \oplus SG(B)$
- 7. 選轉矩陣 $M(\theta) = \begin{pmatrix} cos\theta & -sin\theta \\ sin\theta & cos\theta \end{pmatrix}$

13.1.6 基本數論

- 1. $\sum_{d|n} \mu(n) = [n == 1]$
- 2. $g(m) = \sum_{d|m} f(d) \Leftrightarrow f(m) = \sum_{d|m} \mu(d) \times g(m/d)$
- 4. $\sum_{i=1}^{n} \sum_{j=1}^{n} lcm(i,j) = n \sum_{d|n} d \times \phi(d)$

13.1.7 排組公式

- 1. k 卡特蘭 $\frac{C_n^{kn}}{n(k-1)+1} \cdot C_m^n = \frac{n!}{m!(n-m)!}$
- 2. $H(n,m) \cong x_1 + x_2 \dots + x_n = k, num = C_k^{n+k-1}$
- 3. Stirling number of 2^{nd} , n 人分 k 組方法數目
 - (a) S(0,0) = S(n,n) = 1
 - (b) S(n,0) = 0
 - (c) S(n,k) = kS(n-1,k) + S(n-1,k-1)
- 4. Bell number, n 人分任意多組方法數目

 - (a) $B_0=1$ (b) $B_n=\sum_{i=0}^n S(n,i)$ (c) $B_{n+1}=\sum_{k=0}^n C_k^n B_k$ (d) $B_{p+n}\equiv B_n+B_{n+1}modp$, p is prime (e) $B_pm_+n\equiv mB_n+B_{n+1}modp$, p is prime (f) From $B_0:1,1,2,5,15,52$
 - 203, 877, 4140, 21147, 115975
- 5. Derangement, 錯排, 沒有人在自己位置上
 - (a) $D_n = n!(1 \frac{1}{1!} + \frac{1}{2!} \frac{1}{3!} \dots + (-1)^n \frac{1}{n!})$ (b) $D_n = (n-1)(D_{n-1} + D_{n-2}), D_0 =$
 - $1, D_1 = 0$
 - (c) From $D_0: 1, 0, 1, 2, 9, 44$, 265, 1854, 14833, 133496
- 6. Binomial Equality
 - (a) $\sum_{k} {r \choose m+k} {s \choose n-k} = {r+s \choose m+n}$
 - (b) $\sum_{k} {i \choose m+k} {s \choose n+k} = {i+s \choose l-m+n}$

 - (b) $\sum_{k} \binom{l+k}{m+k} \binom{n+k}{n} = \binom{l-m+n}{k}$ (c) $\sum_{k} \binom{l}{m+k} \binom{s-k}{n} \binom{-1}{k} = (-1)^{l+m} \binom{s-m}{n-l}$ (d) $\sum_{k \le l} \binom{l-k}{m} \binom{s}{k-n} (-1)^{k} = (-1)^{l+m} \binom{s-m-1}{l-n-m}$ (e) $\sum_{0 \le k \le l} \binom{l-k}{m} \binom{q+k}{n} = \binom{l+q+1}{m+n+1}$ (f) $\binom{r}{k} = (-1)^{k} \binom{k-r-1}{k}$

 - (g) $\binom{r}{m}\binom{m}{k} = \binom{r}{k}\binom{r-k}{m-k}$
 - (h) $\sum_{k \le n} {r+k \choose k} = {r+n+1 \choose n}$
 - (i) $\sum_{0 \le k \le n} {k \choose m} = {n+1 \choose m+1}$
 - (j) $\sum_{k \le m} {m+r \choose k} x^k y^k$
 - $\sum_{k \le m} {\binom{-r}{k}} (-x)^k (x+y)^{m-k}$

13.1.8 冪次, 冪次和

- 1. $a^{b} P = a^{b} \varphi(p) + \varphi(p)$, $b > \varphi(p)$
- 2. $1^3 + 2^3 + 3^3 + \ldots + n^3 = \frac{n^4}{4} + \frac{n^3}{2} + \frac{n^2}{4}$
- 3. $1^4 + 2^4 + 3^4 + \ldots + n^4 = \frac{n^5}{5} + \frac{n^4}{2} + \frac{n^3}{3} \frac{n}{30}$
- 4. $1^5 + 2^5 + 3^5 + \ldots + n^5 = \frac{n^6}{6} + \frac{n^5}{2} + \frac{5n^4}{12} \frac{n^2}{12}$
- 5. $0^k + 1^k + 2^k + \ldots + n^k = P(k), P(k) =$ $\frac{(n+1)^{k+1} - \sum_{i=0}^{k-1} C_i^{k+1} P(i)}{k+1}, P(0) = n+1$
- 6. $\sum_{k=0}^{m-1} k^n = \frac{1}{n+1} \sum_{k=0}^n C_k^{n+1} B_k m^{n+1-k}$
- 7. $\sum_{j=0}^{m} C_j^{m+1} B_j = 0, B_0 = 1$
- 8. 除了 $B_1 = -1/2$ · 剩下的奇數項都是 0
- 9. $B_2 = 1/6, B_4 = -1/30, B_6 = 1/42, B_8 =$ $-1/30, B_{10} = 5/66, B_{12} = -691/2730, B_{14} =$ $7/6, B_{16} = -3617/510, B_{18}$ $43867/798, B_{20} = -174611/330,$

13.1.9 Burnside's lemma

- 1. $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$
- 2. $X^g = t^{c(g)}$
- 3. G 表示有幾種轉法, X^g 表示在那種轉法下, 有幾種 是會保持對稱的,t 是顏色數,c(g) 是循環節不動的
- 4. 正立方體塗三顏色,轉0有36個元素不變, 轉 90 有 6 種, 每種有 33 不變, 180 有 3 × $3^4 \cdot 120$ (角) 有 8 × $3^2 \cdot 180$ (邊) 有 6 × $3^3 \cdot$ 全部 $\frac{1}{24} \left(3^6 + 6 \times 3^3 + 3 \times 3^4 + 8 \times 3^2 + 6 \times 3^3 \right) = \frac{1}{57}$

13.1.10 Count on a tree

- 1. Rooted tree: $s_{n+1} = \frac{1}{n} \sum_{i=1}^{n} (i \times a_i \times a_i)$ $\sum_{i=1}^{\lfloor n/i \rfloor} a_{n+1-i \times j})$
- 2. Unrooted tree:
 - (a) Odd: $a_n \sum_{i=1}^{n/2} a_i a_{n-i}$
 - (b) Even: $Odd + \frac{1}{2}a_{n/2}(a_{n/2} + 1)$
- 3. Spanning Tree
 - (a) 完全圖 $n^n 2$
 - (b) 般 圖 (Kirchhoff's theorem)M[i][i] = $degree(V_i), M[i][j] = -1, if have E(i, j), 0$ if no edge. delete any one row and col in A, ans = det(A)

13.1.11 循環小數轉分數

若 x = 0.ā · 則

$$x = \underbrace{\frac{a}{99 \dots 9}}_{k \text{ digits}}$$

其中a 為循環節 $\cdot k$ 為循環節的位數

2. 例子:

$$0.\overline{37} = \frac{37}{99}$$

$$0.\overline{5} = \frac{5}{9}$$

13.1.12 循環小數轉分數

1. 純循環小數: 若 $x = 0.\overline{a}$, 其中a 為循環節、長度為

$$x = \underbrace{\frac{a}{99 \dots 9}}_{k \text{ digits}}$$

$$0.\overline{37} = \frac{37}{99}, \quad 0.\overline{5} = \frac{5}{9}$$

2. 混循環小數:若 $x = 0.b\overline{a}$,其中b為前綴、長度m, a 為循環節、長度 k:

$$x = \frac{(b \cdot 10^k + a) - b}{10^m (10^k - 1)}$$

例:

$$0.12\overline{3} = \frac{(12 \cdot 10^1 + 3) - 12}{10^2(10^1 - 1)} = \frac{123 - 12}{100 \cdot 9} = \frac{111}{900} = \frac{37}{300}$$

13.1.13 常見級數與組合公式

1. 平方和公式:

$$1^{2} + 2^{2} + \dots + n^{2} = \frac{n(n+1)(2n+1)}{6}$$

$$4^{2} + 6^{2} + \dots + (2n)^{2} = \frac{(2n)(n+1)(2n+1)}{3}$$

$$1^{2} + 3^{2} + \dots + (2n+1)^{2} = \frac{n(2n-1)(2n+1)}{3}$$

2. 立方和公式:

$$1^{3} + 2^{3} + \dots + n^{3} = \frac{n^{4} + 2n^{3} + n^{2}}{4}$$

3. 四次方和公式:

$$1^4 + 2^4 + \dots + n^4 = \frac{6n^5 + 15n^4 + 10n^3 - n}{30}$$

4. 五次方和公式:

$$1^5 + 2^5 + \dots + n^5 = \frac{2n^6 + 6n^5 + 5n^4 - n^2}{12}$$

5. 六次方和公式:

$$1^{6} + 2^{6} + \dots + n^{6} = \frac{6n^{7} + 21n^{6} + 21n^{5} - 7n^{3} + n}{49}$$

6. 七次方和公式:

$$1^7 + 2^7 + \dots + n^7 = \frac{3n^8 + 12n^7 + 14n^6 - 7n^4 + 2n^2}{24}$$

7. 八次方和公式:

$$= \frac{1^8 + 2^8 + \dots + n^8}{90}$$

8. 九次方和公式:

$$= \frac{1^9 + 2^9 + \dots + n^9}{20}$$

9. 十次方和公式:

$$= \frac{1^{10} + 2^{10} + \dots + n^{1}}{66}$$

10. 等比級數:

$$S = a \cdot \frac{r^n - 1}{r - 1}$$

11. 二項式係數恆等式:

$$\binom{n}{0} + \binom{n}{1} + \dots + \binom{n}{n} = 2^n$$

$$\binom{n}{1} + \binom{n}{2} + \dots + \binom{n}{n} = 2^n - 1$$

$$\binom{n}{1} + \binom{n}{3} + \dots + \binom{n}{n-k} = 2^{n-1}$$

- 12. 分配問題 (玩具分給小孩):
 - (a) n 個玩具 $\cdot k$ 位小孩 \cdot 可以有人沒拿到:

$$\binom{n+k-1}{n} = \binom{n+k-1}{k-1}$$

(b) n 個玩具, k 位小孩,每個人至少一個:

$$\binom{n-1}{k-1}$$

13.1.14 位元運算

(a) 位元條件:

$$(x+k) & (y+k) = 0$$

(b) 加法恆等式 (利用 XOR 與 AND):

$$a + b = (a \oplus b) + 2 \cdot (a \& b)$$

(c) OR 與 AND 的關係:

$$a \mid b = a + b - (a \& b)$$

(d) 交換兩數:

$$a = a \oplus b$$
, $b = a \oplus b$, $a = a \oplus b$

(e) 取得最低位的 1:

$$x \& (-x)$$

(f) 清除最低位的1:

$$x \& (x-1)$$

13.1.15 數論公式

13. Bezout's identity:

$$ax + by = \gcd(a, b)$$
 (必定存在整數解 x, y)

14. 模指數運算(冪的冪):

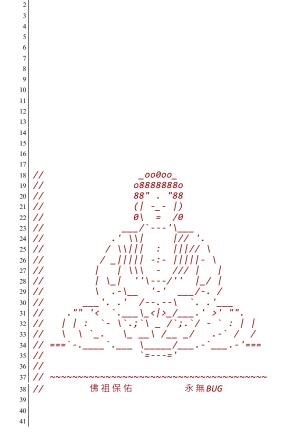
$$a^{b^c} \equiv a^{\operatorname{power_mod}(b,c,\operatorname{MOD}-1)} \pmod{\operatorname{MOD}}$$

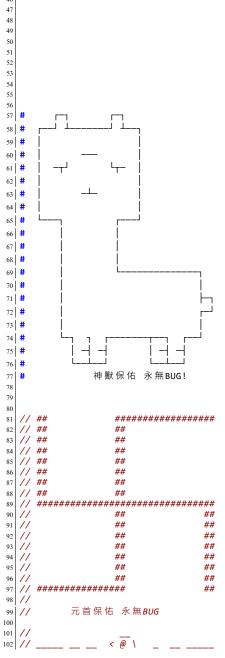
海龍公式:

$${\rm Area} = \sqrt{s(s-a)(s-b)(s-c)}, \quad s = \frac{a+b+c}{2}$$

14 Интернационал

14.1 保佑







ACM ICPC		3.13 permutation	4	7	Lang 7.1	guage CNF	10 10	11 other 1 11.1 Nim game
Team Reference BogoSort	-	3.15 flowers	4 4 4 5	8	Num 8.1 8.2 8.3	Linear Sieve	10 10 10	11.2 找小於 n 所有出現的 1 數量 . 1 12 other language
Contents	4	Data Structure 4.1 undo disjoint set 4.2 segment tree range update (lazy propagation) 4.3 segment tree prefix sum lower	5 5		8.4	Inclusion-Exclusion) matrix template (with fast power)	10	12.2.1 文件操作
1 Algorithm 1.1 LIS	1 1 1	bound	6 6 6 6			Chinese Remainder Theorem	11 11 11 11	12.4 python 大數因數分解 <
 2.1 mod helper function 2.2 self-defined-pq-operator 2.3 generating all subsets 2.4 memset 2.5 submask enumeration 2.6 custom-hash 2.7 stringstream split by comma . 	1 1 1 1 5 1 1 6	 4.8 DSU remove node find prev next one	7 7 7 7		8.12 8.13 8.14 8.15 8.16 8.17	Euler Totient precompute mod inv (not coprime) Euler Totient	11 11 11 11 11 12	12.9 python 大數計算
2.7 stringstream spiit by comma . 3 DP 3.1 deque	1 6 1 1 2 2 2 2 2 2 3 3 3 3 3	6.1 Euler tour+RMQ	7 7 8 8 8 8 8 8 9 9	9	Strir	Z	12 12 12 13 13	13.1.4 0-1 分數規劃
3.11 sushi	3	6.13 tree diameter (len,end) 6.14 Bellman-Ford	10 10			debug		14 Интернационал 1 14.1 保佑 1

ACM ICPC Judge Test BogoSort

C++ Resource Test

```
#include <bits/stdc++.h>
using namespace std;

namespace system_test {

const size_t KB = 1024;
const size_t MB = KB * 1024;
const size_t GB = MB * 1024;

size_t block_size, bound;
void stack_size_dfs(size_t depth = 1) {
```

```
if (depth >= bound)
                                                   return diff.count();
    return;
                                               36 }
 int8_t ptr[block_size]; // 若無法編譯將
                                               37
                                                 void runtime_error_1() {
      block size 改成常數
                                                   // Segmentation fault
  memset(ptr, 'a', block_size);
                                                   int *ptr = nullptr;
  cout << depth << endl;</pre>
                                                   *(ptr + 7122) = 7122;
 stack_size_dfs(depth + 1);
                                               42 }
                                               44 void runtime_error_2() {
void stack_size_and_runtime_error(size_t
                                                  // Segmentation fault
    block_size, size_t bound = 1024) {
                                                   int *ptr = (int *)memset;
  system_test::block_size = block_size;
                                                   *ptr = 7122;
 system_test::bound = bound;
                                               48
 stack size dfs();
                                                 void runtime error 3() {
                                                  // munmap_chunk(): invalid pointer
double speed(int iter num) {
                                                   int *ptr = (int *)memset;
  const int block_size = 1024;
                                                   delete ptr;
  volatile int A[block_size];
  auto begin = chrono::high_resolution_clock
      ::now();
                                                 void runtime_error_4() {
  while (iter num--)
                                                   // free(): invalid pointer
    for (int j = 0; j < block size; ++j)</pre>
                                                   int *ptr = new int[7122];
      A[j] += j;
                                                   ptr += 1;
  auto end = chrono::high_resolution_clock::
                                                   delete[] ptr;
                                               61 }
  chrono::duration<double> diff = end -
                                               62
      begin;
```

```
63 | void runtime_error_5() {
    // maybe illegal instruction
    int a = 7122, b = 0;
    cout << (a / b) << endl;</pre>
67 }
  void runtime error 6() {
    // floating point exception
    volatile int a = 7122, b = 0;
    cout << (a / b) << endl;</pre>
73 }
  void runtime_error_7() {
    // call to abort.
    assert(false);
78 }
80 } // namespace system_test
82 #include <sys/resource.h>
void print_stack_limit() { // only work in
       Linux
    struct rlimit 1;
    getrlimit(RLIMIT_STACK, &1);
    cout << "stack size = " << l.rlim cur << "</pre>
86
          byte" << endl;</pre>
87 }
```