

## f-22-jupyter-salt

April 22, 2021

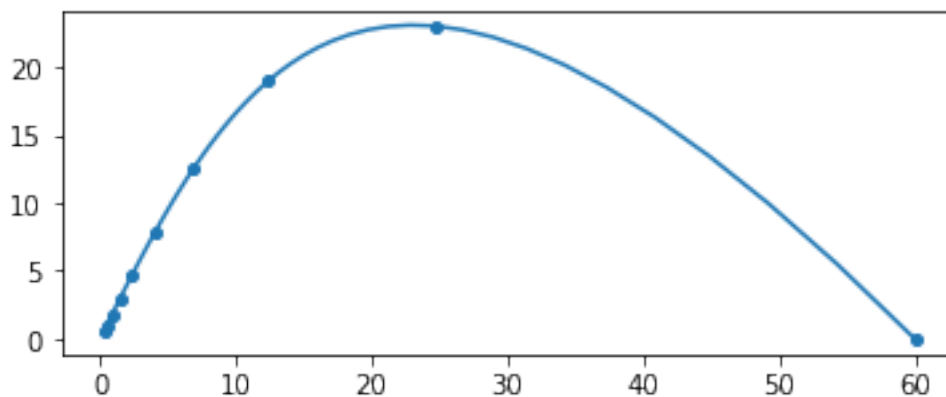
```
[1]: import matplotlib.pyplot as plt
import numpy as np
```

```
[2]: v0 = np.array([1.0, 2.0])[:, np.newaxis]
v1 = np.array([1.0, -2.0])[:, np.newaxis]
lambda0 = -1.0 / 20.0
lambda1 = -3.0 / 20.0
```

```
[3]: t = np.linspace(0, 100, 100)
løsning = (30 * v0 * np.exp(lambda0 * t)
          + 30 * v1 * np.exp(lambda1 * t))
```

```
[4]: fig, ax = plt.subplots()
ax.set_aspect('equal')
ax.plot(*løsning,
        marker='o', markevery=10, markersize=4)
```

```
[4]: [<matplotlib.lines.Line2D at 0x106fc8ca0>]
```



```
[5]: v = np.hstack([v0, v1])

def sol(r0, r1, v, lambda0, lambda1, t):
    c = np.linalg.solve(v, np.array([r0, r1])[:, np.newaxis])
```

```

return (c[0] * v[:, [0]] * np.exp(lambda0 * t)
        + c[1] * v[:, [1]] * np.exp(lambda1 * t))

```

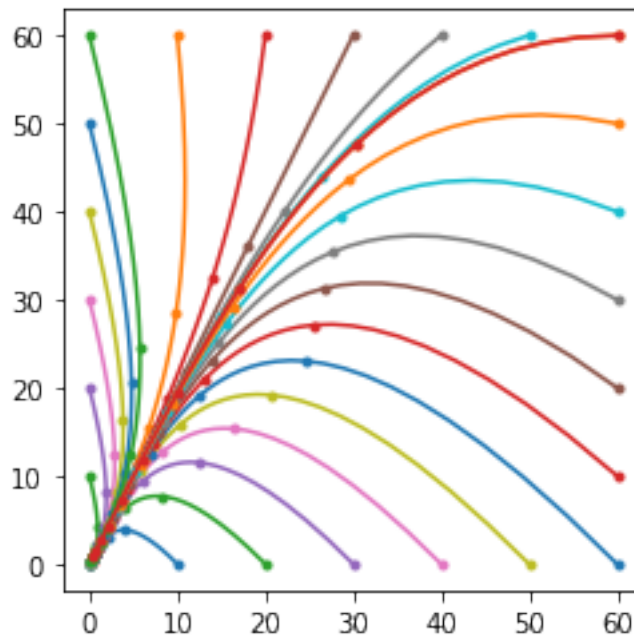
```

[6]: t = np.linspace(0, 100, 100)

marks = dict(marker='o', markevery=10, markersize=3)

fig, ax = plt.subplots()
ax.set_aspect('equal')
for s in np.linspace(10, 60, 6):
    ax.plot(*sol(s, 0, v, lambda0, lambda1, t), **marks)
    ax.plot(*sol(s, 60, v, lambda0, lambda1, t), **marks)
for s in np.linspace(10, 60, 6):
    ax.plot(*sol(0, s, v, lambda0, lambda1, t), **marks)
    ax.plot(*sol(60, s, v, lambda0, lambda1, t), **marks)

```



```

[7]: # kredsløb eksemplet

```

```

[8]: a_mat = np.array([[-2.0, -2.5],
                       [10.0, -2.0]])

```

```

[9]: # karakteristisk poly  $a x^2 + b x + c$ 

```

```

[10]: a = 1.0

```

```

[11]: b = 2.0 * (-2.0) * (-1.0)

```

```
[12]: c = (-2.0 * -2.0) - (-2.5 * 10.0)
```

```
[13]: a, b, c
```

```
[13]: (1.0, 4.0, 29.0)
```

```
[14]: # rødder  $(-b \pm \sqrt{b^2 - 4ac}) / (2a) = -b/2a \pm \sqrt{\text{diskriminant}} / 2a$ 
```

```
[15]: diskriminant = b**2 - 4*a*c
```

```
[16]: diskriminant
```

```
[16]: -100.0
```

```
[17]: -b/(2*a)
```

```
[17]: -2.0
```

```
[18]: #  $\pm i$  gange
```

```
[19]: 10 / (2*a)
```

```
[19]: 5.0
```

```
[20]: lambda0 = -2.0 + 5.0j  
lambda1 = -2.0 - 5.0j
```

```
[21]: # find en egenvektor  $v_0$ 
```

```
[22]: b_mat = a_mat - lambda0 * np.eye(2)
```

```
[23]: b_mat
```

```
[23]: array([[ 0. -5.j, -2.5+0.j],  
         [10. +0.j,  0. -5.j]])
```

```
[24]: b_mat[0, :] /= b_mat[0,0]
```

```
[25]: b_mat
```

```
[25]: array([[ 1.-0.j , -0.-0.5j],  
         [10.+0.j ,  0.-5.j ]])
```

```
[26]: b_mat[1, :] += - b_mat[1,0] * b_mat[0, :]
```

```
[27]: b_mat
```

```
[27]: array([[ 1.-0.j , -0.-0.5j],  
         [ 0.+0.j ,  0.+0.j ]])
```

[ ]: