

# paper summary

## Methods

### Basic Bayesian Observer Model

- $\theta_{true} = 225$  degrees for all experiments. This is the mean of the prior, i.e. the direction around which all motions presented to subjects are centered
- Start one block  $e$  (~200 trials, 1 trial = 1 estimation task a subject)
  - Strength of the prior  $\kappa_p$  is block-specific (10,20,40 or 80 degrees) prior strength
  - create **prior distribution** as a von mises distribution  $\nu(\theta_{true}, \kappa_p)$ . Why this distribution because is the circular analogue to Gaussian distribution
    - [notice that prior distribution is also referred to as evidence distribution  $\nu(\theta_{true}, \kappa_e)$  in star methods, but I would avoid this, it generates confusion]
  - Perform Trial  $i$ 
    - Sample **sensory evidence**  $\theta_{e_i}$  from the evidence distribution. This is the actual direction of motion for this trial.
    - The sensory evidence  $\theta_{e_i}$  is also the mean of the sensory likelihood distribution i.e. the distribution of the direction of motion as it is *perceived* by the subject. This is also modeled as a von mises distribution  $\nu(\theta_{e_i}, \kappa_e)$  with the same strength  $\kappa_e = \kappa_p$  as the prior distribution.
    - Assumed that each subject has been able to learn an estimate of the prior distribution  $\nu(\theta_{true}, \kappa_{prior})_{Learned}$
    - Compute the **posterior distribution and its mode with Bayes:**

$$p(\theta_{true}, \theta_{e_i}) = \frac{p(\theta_{e_i}|\theta_{true})p(\theta_{true})L}{p(\theta_{e_i})}$$

Then the mode of this distribution is taken as the subject final estimate

$$\theta_p = \operatorname{argmax}(p(\theta_{true}, \theta_{e_i}))$$

Combining the equations above (and adding motor noise (with motion strength  $\kappa_m$ ) and lapses occurring with probability  $p_r$ , here not shown) we get the **distribution of percepts**  $\theta_p$  of one subject over all trials ( $\theta_{e_i}$  changes) for this block ( $\theta_{true}$  is fixed)

Overall, the the basic bayesian observer model has these parameters

- $\theta_{true}$  true angle
- $\kappa_p$  prior strength
- $\kappa_e$  likelihood strength
- $\kappa_m$  motion strength
- $p_r$  probability of lapses