SIGMA POLYNOMIAL PROBLEM

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Problem: Given an non-zero, n-variable, complex-valued polynomial of finite degree $\mathcal{P}$, prove that $\mathcal{P}(m, \sigma(m), \ldots, \sigma_{n-1}(m))$ is not identically zero at all values of m for $m \in \mathbb{N}$.