

02-  $u=(1,-1,2)$ ,  $v=(1,2,1)$  e  $w=(-1,-1,2)$

a-  $A = \frac{1}{2} \|u \times v\|$

$$\begin{array}{c|c} \begin{array}{ccc} i & j & k \\ 1 & 2 & 1 \\ -1 & -1 & 2 \end{array} & \begin{array}{ccc} i & j \\ 1 & 2 \\ -1 & -1 \end{array} \end{array}$$

$$4i - j - k + 2k + i - 2j = 5i - 3j + k = (5, -3, 1)$$

$$A = \frac{1}{2} \|u \times v\| = \frac{1}{2} \sqrt{25+9+1} \Rightarrow A = \frac{1}{2} \sqrt{35}$$

$$b- \begin{array}{c|c} \begin{array}{ccc} 1 & -1 & 2 \\ 1 & 2 & 1 \\ -1 & -1 & 2 \end{array} & \begin{array}{ccc} 1 & -1 \\ -1 & -1 \end{array} \end{array}$$

$$\underbrace{-4 \quad -1 \quad -2}_{-4} \quad \underbrace{4 \quad 1 \quad -2}_{3} = -4 + 3 = -1$$

$$\|u \times v\| = |-1| = 1$$

$$A = \frac{1}{2} \|u \times v\| = \frac{1}{2} \cdot 1 = \frac{1}{2}$$

03-

$$(x+2)^2 + (y+1)^2 + (z-1)^2 = 9 \Rightarrow C = (-2, -1, 1)$$

$$A = (4, -2, 2)$$

$$\vec{AC} = (-2-4, -1-2, 1-2) = (-6, -3, -1) \Rightarrow \vec{AC} = (-6, -3, -1)$$

$$r = \begin{cases} x = 4 - 6t \\ y = -2 - 3t \\ z = 2 - 2t \end{cases} \Rightarrow \begin{cases} t = 1 \Rightarrow x = -2 \\ t = \frac{1}{3} \Rightarrow y = -3 \\ t = -\frac{1}{2} \Rightarrow z = 3 \end{cases}$$

|                           |                           |                          |
|---------------------------|---------------------------|--------------------------|
| $-2 = 4 - 6t$             | $-1 = -2 - 3t$            | $1 = 2 - 2t$             |
| $-6t = -2 - 4 \quad (-1)$ | $-3t = -2 + 1 \quad (-1)$ | $-2t = 2 - 1 \quad (-1)$ |
| $6t = 2 + 4$              | $3t = 2 - 1$              | $2t = -2 + 1$            |
| $6t = 6$                  | $3t = 1$                  | $2t = -1$                |
| $t = 1$                   | $t = \frac{1}{3}$         | $t = -\frac{1}{2}$       |

C não pertence a r.

04.

2-  $\alpha$  e  $\beta$  são concorrentes

b-  $\alpha: 2x + y + 2z = 5$      $\beta: 2x - y + z = -5$

$$\begin{cases} 2x + y + 2z = 5 \\ 2x - y + z = -5 \end{cases}$$

$$4x + 3z = 0 \Rightarrow x = -\frac{3}{4}z$$

$$2(-\frac{3}{4}z) + y + 2z = 5$$

$$-1.5z + y + 2z = 5$$

$$y = 5 - 0.5z$$

$$y = -0.5z + 5$$

$$r: \begin{cases} x = -\frac{3}{4}z \\ y = -0.5z + 5 \\ z = z \end{cases}$$

$\Rightarrow$  sendo  $z=t$ , então as equações paramétricas da reta que tem o ponto  $A(4, -3, 0)$  e é paralela ao vetor  $v = (3, -5, 1)$