# Exercises Lecture 6 Introduction to Artificial Intelligence (IAI)

#### Exercise 1

Consider the claims

- 1. If the sun shines then it is true that I get wet if it rains.
- 2. If the sun shines then it is summer.
- 3. It is not summer
- 4. Therefore, I get wet if the sun shines.
- a) A proposition symbol represents something that can be either true or false. In claim 1., 2., 3. and 4. above, there are several statements like "the sun shines" that can be either true or false. Define a propositional symbol for each of these statements.
- b) Translate 1., 2., 3., and 4. to propositional logic sentences using your proposition symbols from a).
- c) Does the conjunction of 1., 2. and 3. entail the conclusion in 4 (why / why not)?

## Exercise 2 (adapted from RN03 7.8)

Decide whether each of the following sentences is valid, unsatisfiable, or neither. Verify your decisions using truth tables or equivalence rules.

- a)  $Smoke \Rightarrow Smoke$
- b)  $Smoke \Rightarrow Fire$
- c)  $(Smoke \Rightarrow Fire) \Rightarrow (\neg Smoke \Rightarrow \neg Fire)$
- d) Smoke  $\vee$  Fire  $\vee \neg$ Fire
- e)  $((Smoke \land Heat) \Rightarrow Fire) \Leftrightarrow ((Smoke \Rightarrow Fire) \lor (Heat \Rightarrow Fire))$
- f)  $(Smoke \Rightarrow Fire) \Rightarrow ((Smoke \land Heat) \Rightarrow Fire)$
- g)  $Big \vee Dumb \vee (Big \Rightarrow Dumb)$
- h) ( $Big \wedge Dumb$ )  $\vee \neg Dumb$

## Exercise 3 (adapted from RN03 7.4)

Argue for the correctness of each of the following assertions:

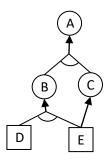
- a)  $\alpha$  is valid if and only if  $True \models \alpha$ .
- b) For any  $\alpha$ , False  $\models \alpha$ .
- c)  $\alpha \models \beta$  if and only if the sentence  $(\alpha \Rightarrow \beta)$  is valid.
- d)  $\alpha \equiv \beta$  if and only if the sentence  $(\alpha \Leftrightarrow \beta)$  is valid.
- e)  $\alpha \models \beta$  if and only if the sentence  $(\alpha \land \neg \beta)$  is unsatisfiable.

#### **Exercise 4**

- a) Translate the sentence  $\neg(a \Rightarrow b) \land (a \lor b \Leftrightarrow (c \Rightarrow b))$  to CNF
- b) Use resolution to prove  $\neg(a \Rightarrow b) \land (a \lor b \Leftrightarrow (c \Rightarrow b)) \models \neg c$

### **Mandatory assignment**

During the lecture 4 you learned that the forward-chaining algorithm can be used to efficiently entail propositions from a knowledge-base of definite clauses. In the textbook, a different approach called backward-chaining is discussed. This algorithm works backward from the query. If the query is known to be true, then no work is needed, otherwise it tries to prove the query by proving its premises true (by backward-chaining). Consider the following AND-OR graph of a knowledge-base *KB*:



If we were to query the *KB* for A using backward-chaining, we would first have to prove B and C. C can be proven because it is implied by E which is a known fact, and B can be proven because it is implied by D and E which are known facts. Since we have proven B and C we can conclude A.

- 1) In which situations can it be an advantage to do backward-chaining rather than forward-chaining?
- 2) Professor Smart has implemented the following backward-chaining algorithm:

function PL-BC-ENTAILS(KB, q) returns true or false inputs: KB, the knowledge base, a set of propositional definite clauses q, the query, a propositional symbol if q is known to be true in KB then return true for each clause c in KB where q is in c.Conclusion do if Check-All(KB, c.Premise) then return true return false

Given the following *KB* of definite clauses:

- $F \wedge E \Rightarrow D$
- $E \Rightarrow B$
- $B \wedge E \wedge G \Rightarrow C$
- $C \Rightarrow G$
- $D \wedge B \wedge C \Rightarrow A$
- $\bullet \Rightarrow F$
- $\bullet \Rightarrow E$

Can professor Smart's algorithm answer  $KB \models A$ ? If yes, explain how the algorithm induces the answer. If no, explain in words where the problem lies and extend professor Smart's pseudocode with a solution.