## Chapter 4/5 Homework 3

# ${\bf Lucas~Gallegos} \\ {\bf ME~397~- Introduction~to~Robot~Modeling~and~Control} \\$

November 1, 2018

**Problem 1.** Derive the Jacobian for your previous RRP robot symbolically.

#### Solution

$$J = \begin{pmatrix} -d_3 \cos(\theta_2) \sin(\theta_1) & -d_3 \cos(\theta_1) \sin(\theta_2) & \cos(\theta_1) \cos(\theta_2) \\ d_3 \cos(\theta_1) \cos(\theta_2) & -d_3 \sin(\theta_1) \sin(\theta_2) & \cos(\theta_2) \sin(\theta_1) \\ 0 & d_3 \cos(\theta_2) & \sin(\theta_2) \\ 0 & \sin(\theta_1) & 0 \\ 0 & -\cos(\theta_1) & 0 \end{pmatrix}$$

• The DH parameters for this problem were found in the previous homework assignment. Using these DH Parameters, along with equations in the textbook, I solved the forward kinematics symbolically to compute the Jacobian Matrix symbolically. This can be found in the MATLAB script titled "hw3 rrp symbolic.m".

Table 1: DH Parameters for planar RRR Robot

**Problem 2.** Derive the Jacobian for a planar RRR manipulator.

#### Solution

$$J = \begin{pmatrix} -L_2 \sin{(\theta_1 + \theta_2)} - L_1 \sin{(\theta_1)} - L_3 \sin{(\theta_1 + \theta_2 + \theta_3)} & -L_2 \sin{(\theta_1 + \theta_2)} - L_3 \sin{(\theta_1 + \theta_2 + \theta_3)} & -L_3 \sin{(\theta_1 + \theta_2 + \theta_3)} \\ L_2 \cos{(\theta_1 + \theta_2)} + L_1 \cos{(\theta_1)} + L_3 \cos{(\theta_1 + \theta_2 + \theta_3)} & L_2 \cos{(\theta_1 + \theta_2)} + L_3 \cos{(\theta_1 + \theta_2 + \theta_3)} & L_3 \cos{(\theta_1 + \theta_2 + \theta_3)} \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 \end{pmatrix}$$

• Using the DH Parameters for a planar RRR robot shown in Table 1, along with equations in the textbook, I solved the forward kinematics symbolically to compute the Jacobian Matrix symbolically. This can be found in the MATLAB script titled "hw3 rrr symbolic.m".

**Problem 3.** Animate a planar RRR robot and the RRP and 7DOF robots from the previous homework assignment using any trajectory.

### Solution

• I employed a quintic polynomial trajectory. See the attached .avi videos.