

# Inverse Problems for Philosophers

Bridging the gap between agent-based models and behavioral data

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University of Bochum, January 2025

# Summary

1 Inverse problems for philosophers and agent-based modelers

2 A case-study of conventions: the metric signature in particle physics

- How do physicists choose which convention to use in their own papers?
- How do scientists resolve conflicting preferences in collaborations?
- How do physicists' preferences get formed?

# Why should philosophers care about data?

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- **Practical:** normative insights from models without connection to data may not be translatable into interventions/policies (abstract parameters in a computational model do not immediately connect to actionable parameters!)

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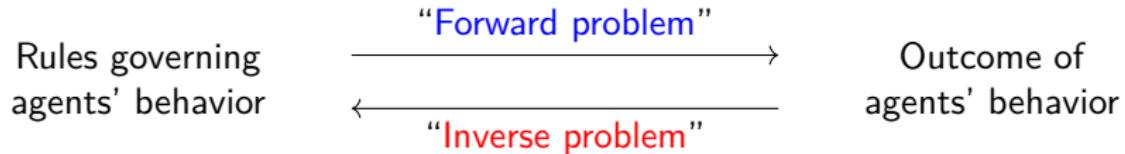
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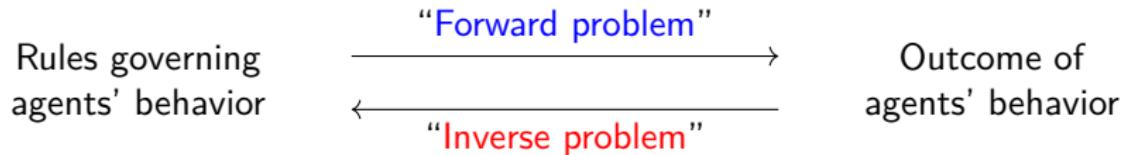
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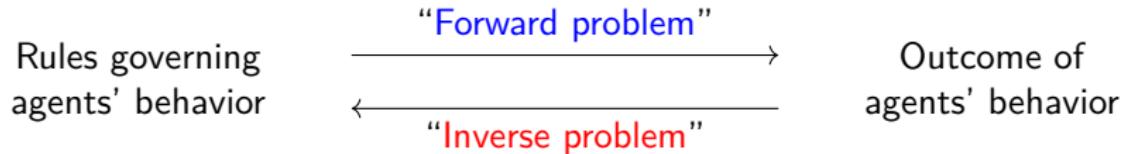
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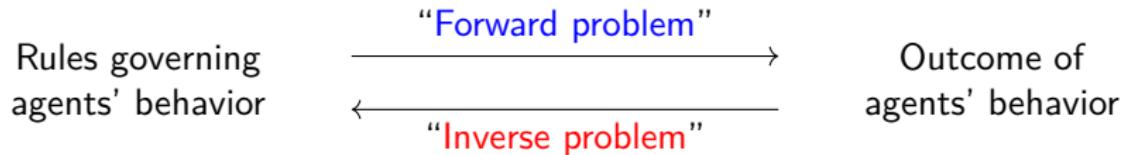
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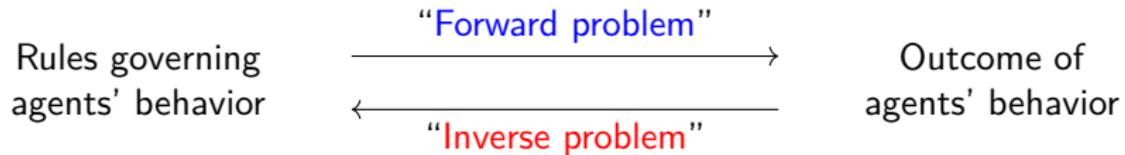
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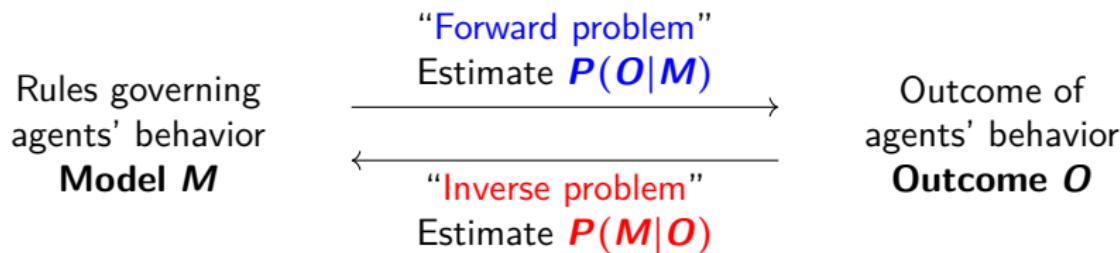
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  - ③ **Computational problems**: solving inverse problems often involves intractable computations and requires approximation schemes.

# Bayesian inference for inverse problems

- Both forward models and inverse problems have a stochastic/probabilistic component (random initialization, partially random decisions; uncertainty quantification...)
- We appeal to **probabilities** and **Bayesian inference**.



$$P(M|O) = \frac{P(O|M) \overbrace{P(M)}^{\text{Prior}}}{P(O)} \quad (1)$$

# Model comparison and parameter estimation

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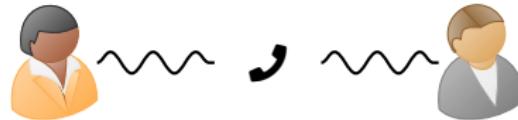
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A case-study of conventions: the metric signature in particle physics

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  - Example: left-hand or right-hand traffic.
  - Language! “The syllable ‘big’ could have meant ‘small’ for all we care, and the red light could have meant ‘go’” (Quine, foreword to Lewis 1969)

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Most often: idealized formal models or controlled experiments. Few studies in naturalistic settings!

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- Both choices are legitimate, as long as one remains consistent.

# A heated debate

 **the finite physicist** @FinitePhysicist · 1 mai  
(-, +, +, +) metric signature people are insane.

"Cook the pizza for  $\sqrt{-30^2}$  minutes" statements by the **utterly deranged**

🕒 14      ⏱ 26      ❤️ 230      📖 22 k      📄 ↗

# A heated debate

 **Cliff Burgess** ✅ @CburgessCliff · 10 août 2023  
When her family finds you use the wrong **metric**...

 **Enez Özen** ✅ @Enezator · 10 août 2023  
Every pleasure in life has a price

 0:00 / 0:32

 **the finite physicist** @Fini  
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"Cook the pizza for  $\sqrt{-1}$ : deranged

**Will Kinney** ✅ @WKCosmo · 12 oct. 2022  
Be sure to check your kids' candy this year. Just found this metric inside a Snickers bar.



0 / 0:32



3 k

L. Gautheron (IZWT, ENS) Inverse Problems for Philosophers 24/01/2025 12 / 41

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**Greg Trayling** @GregTrayling · 27 avr.

Metric convention reveal parties for graduating physics majors, hear me out.

0 1 t 8 1k

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# A heated debate



Superconformal Hassaan  
@Hassaan\_PHY

...

This is a small post to argue that  $(-+++)$  metric is objectively better than the  $(+---)$  metric. Before starting, let me mention that I studied QFT in the  $(+---)$  metric (from Peskin and Schroeder).

1/17

#Physics #scicomm

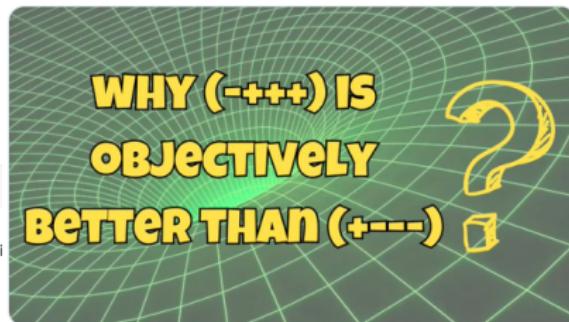
Traduire le post



Greg Trayling @GregTrayling · Metric convention reveal part out.

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  - ➊ How do scientists decide which convention to use in a paper?
  - ➋ How do they resolve conflicting preferences in collaborations?
  - ➌ What factors shape scientists' preferences?

- Data collected from **Inspire HEP** (authorship/citation metadata) and **arXiv** (LaTeX source)
- Categories: hep-th (high-energy physics theory), hep-ph (phenomenology), gr-qc (gravitation and cosmology), astro-ph (astrophysics)
- 22 500 papers classified according to their metric signature (mostly plus or mostly minus) using regular expressions.

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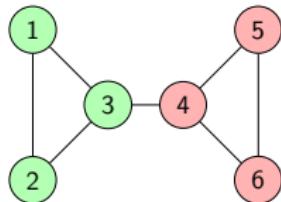
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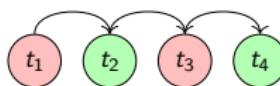
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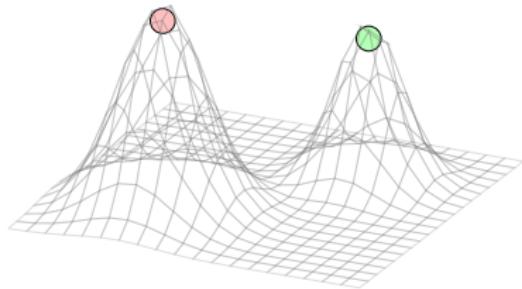
**Social consistency**  
(coordination costs)



**Individual consistency**  
(switching costs)



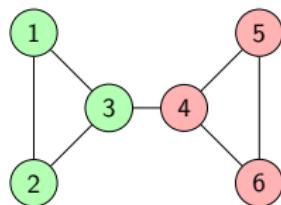
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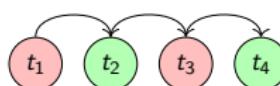
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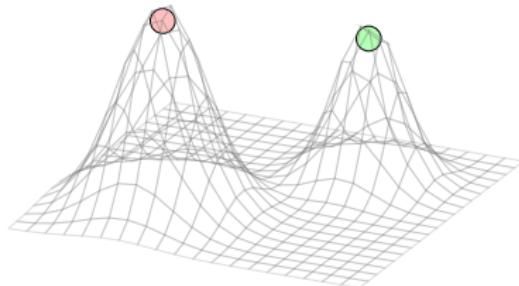
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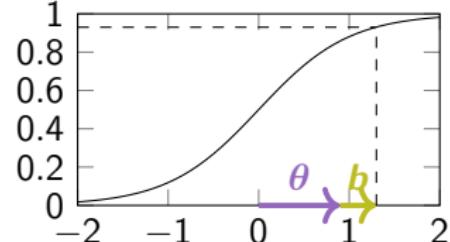


⇒ Are these involved in the context of the metric signature?

# Individual and contextual consistency

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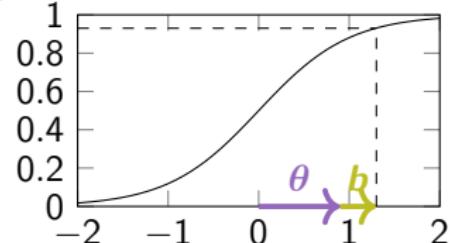
$$P(\sigma_d = +1 | \theta(\text{👤}), b(c_d)) = f(\underbrace{\theta(\text{👤})}_{\text{Author's preference}} + \underbrace{b(c_d)}_{\text{Effect of research area}})$$



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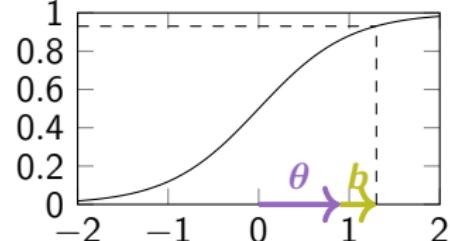


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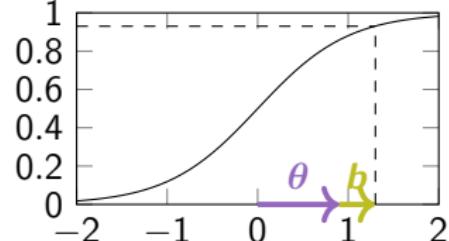


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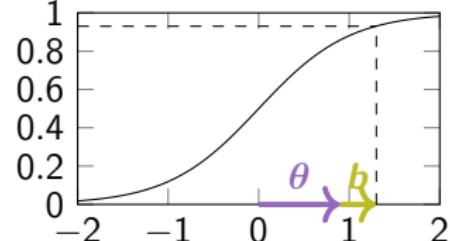
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Author's preference      Effect of research area



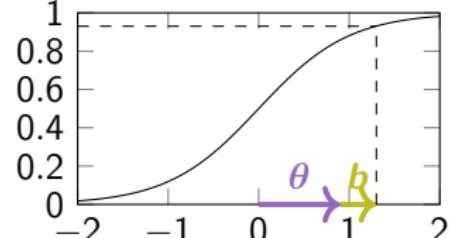
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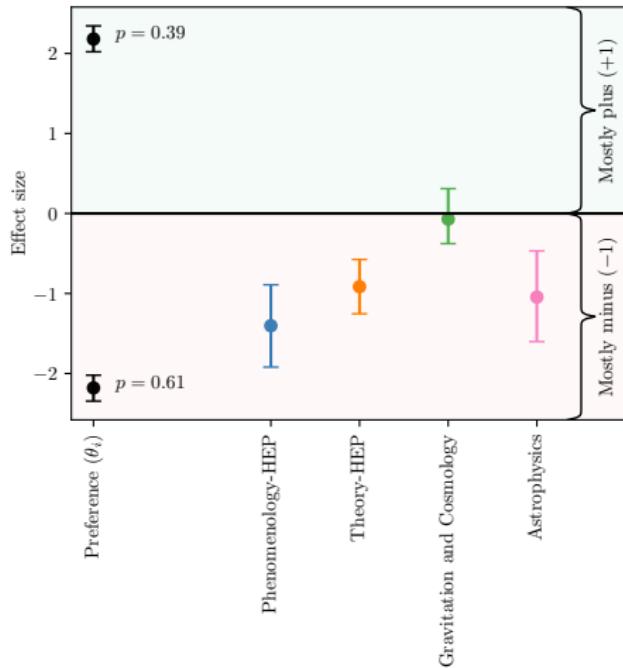
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- If  $|\theta| \gg |b|$ , individual preferences dominate the need to adapt to a given research area
- “Item-response model”: recover invisible traits/factors that may account for observed behaviors.
- **Given physicists' choices in their solo-authored papers, we can infer back  $\theta$  and  $b$  using Bayesian inference.**

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**Figure:** Individual consistency (preferences) matter the most, but adaptation to the context also occurs.

# Individual and contextual consistency

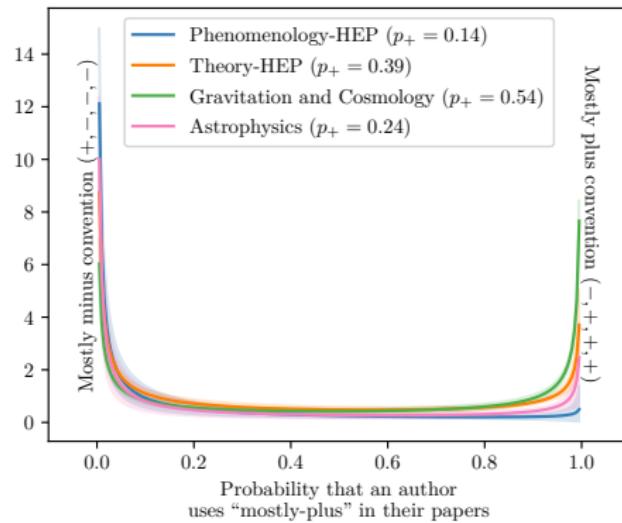


Figure: Physicists tend to always be using the same convention

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- We can assume different preference aggregation strategies  $(A_k)$ :

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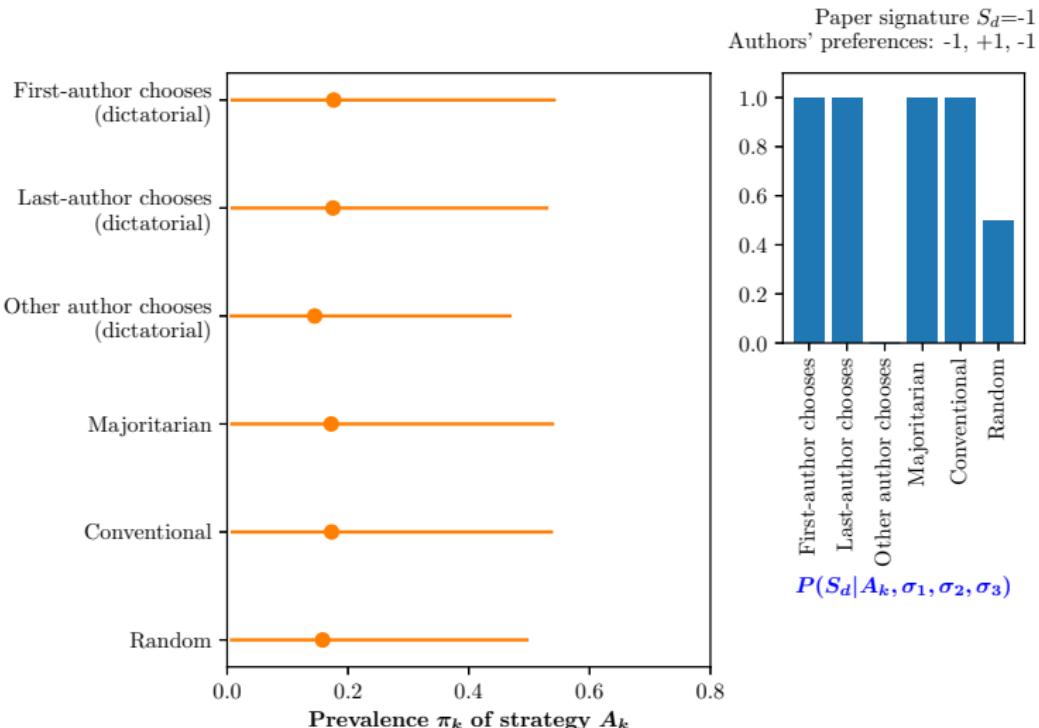
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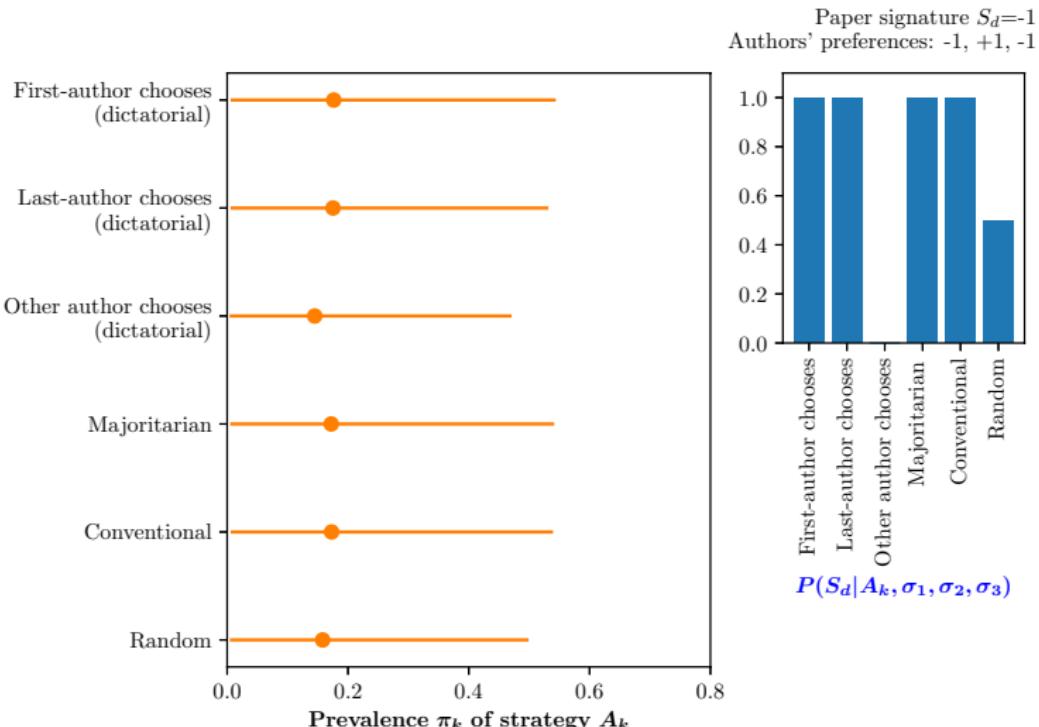
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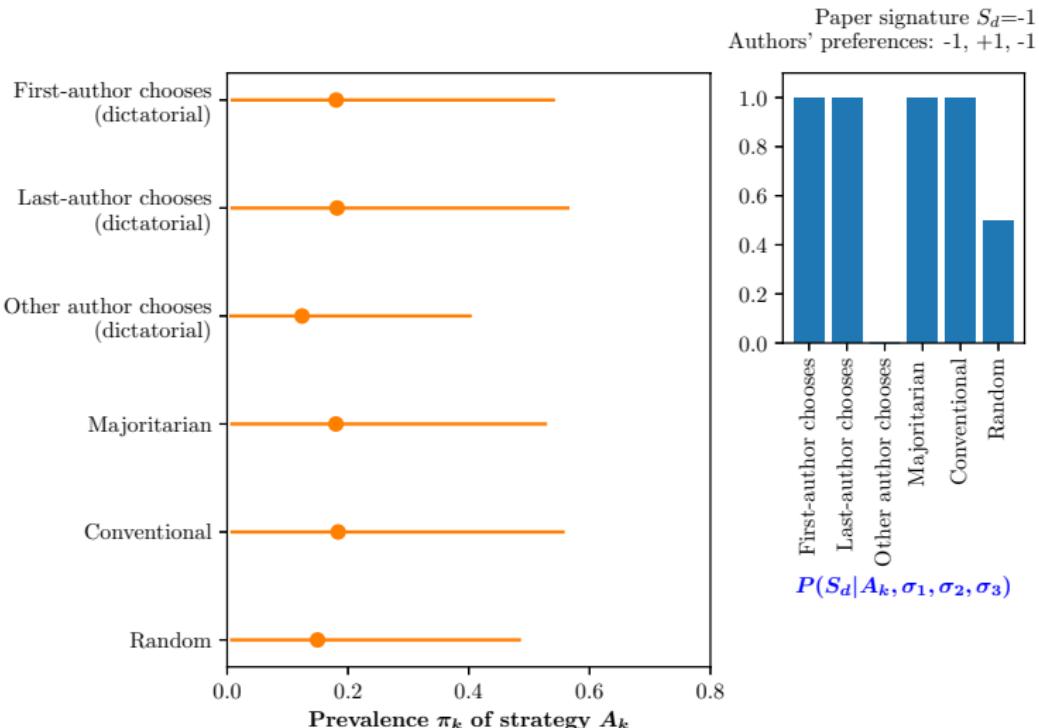
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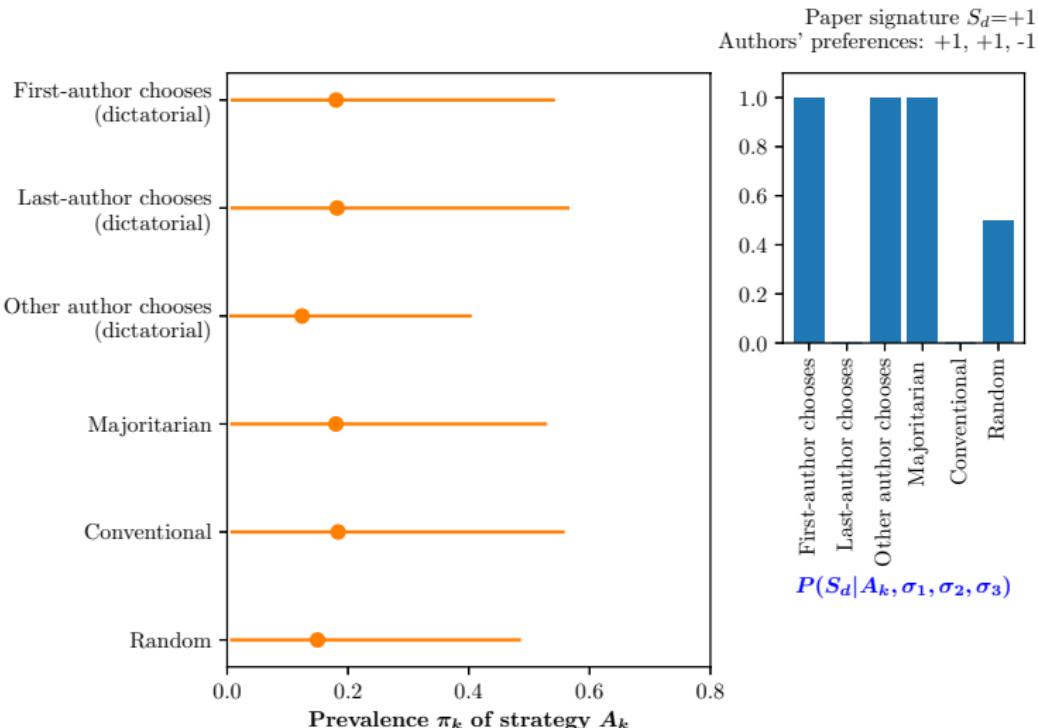
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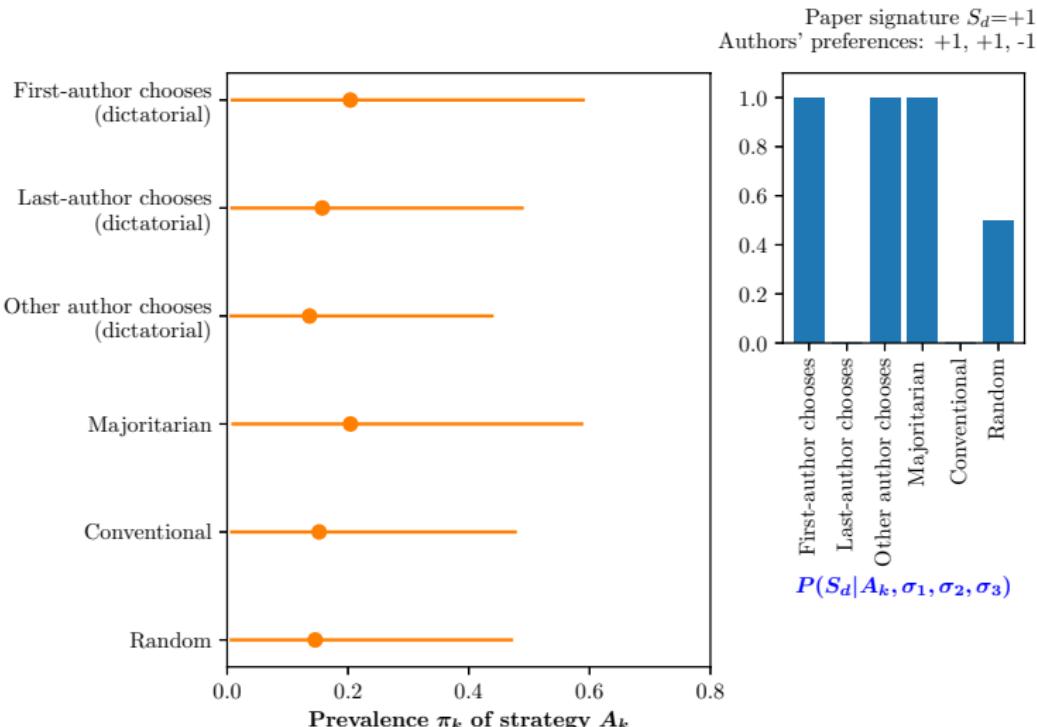
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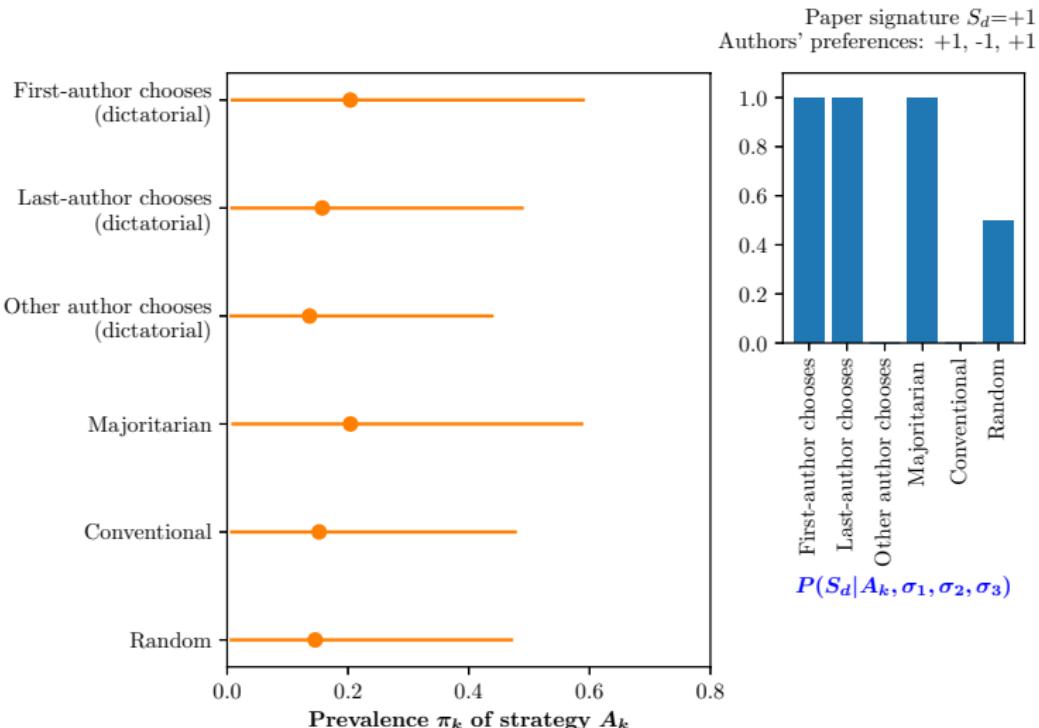
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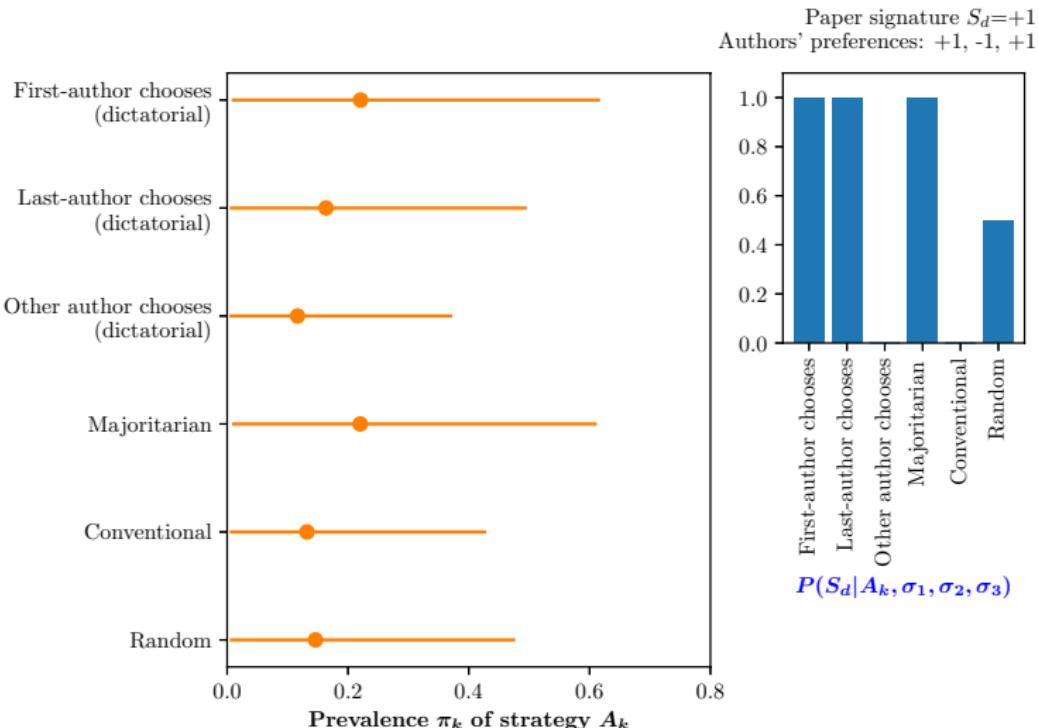
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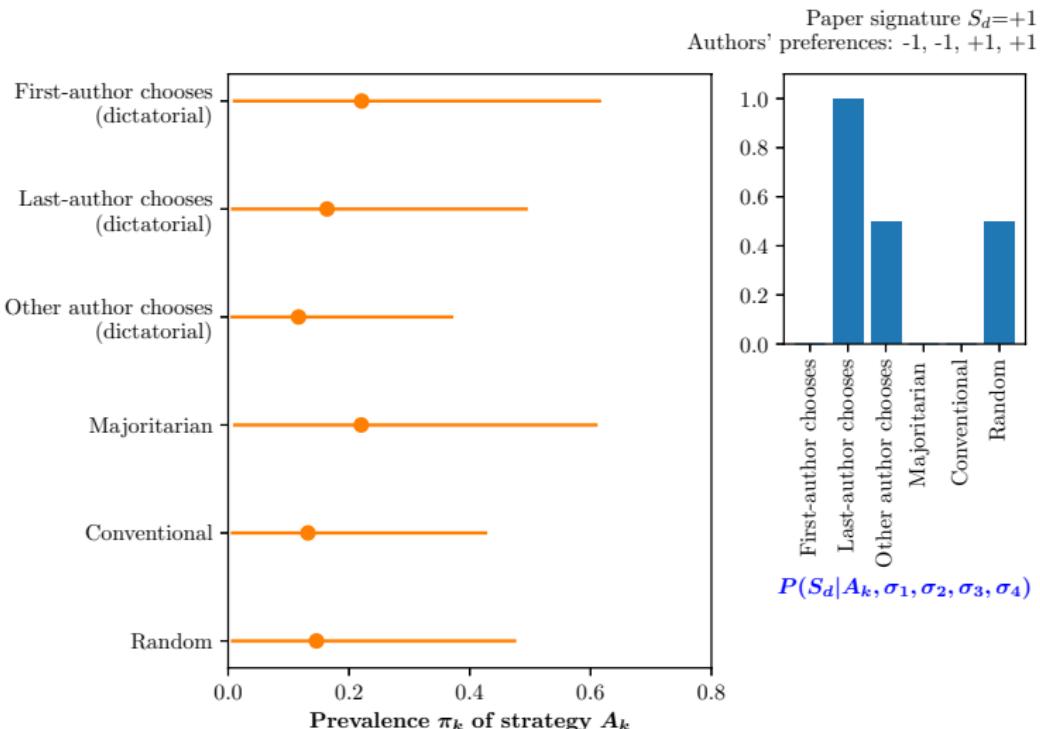
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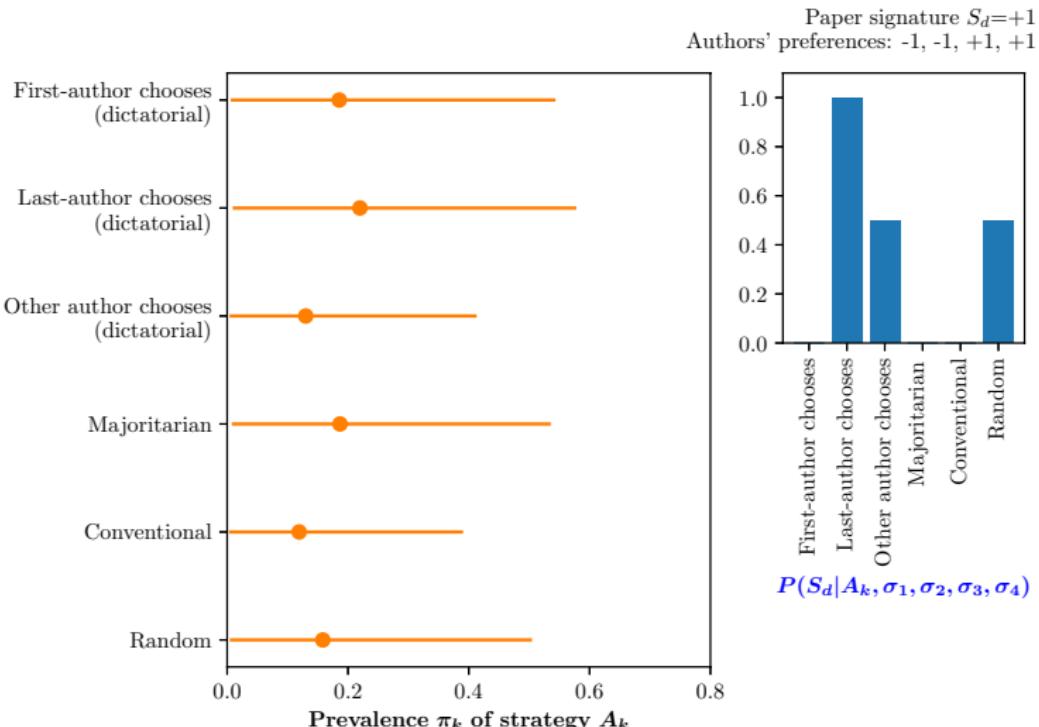
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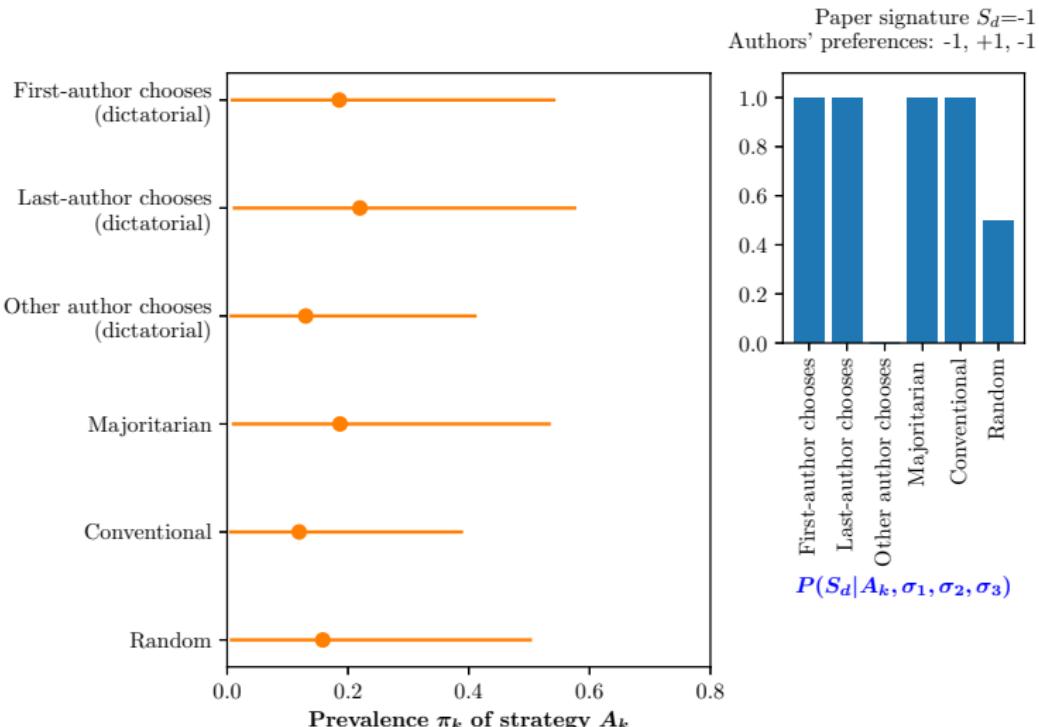
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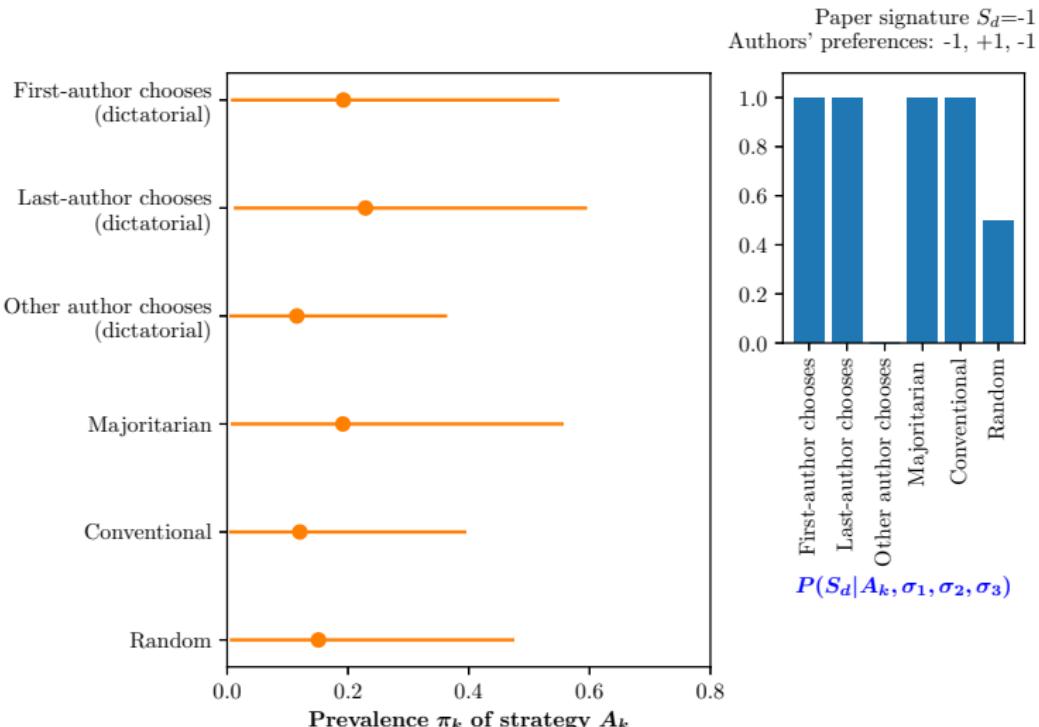
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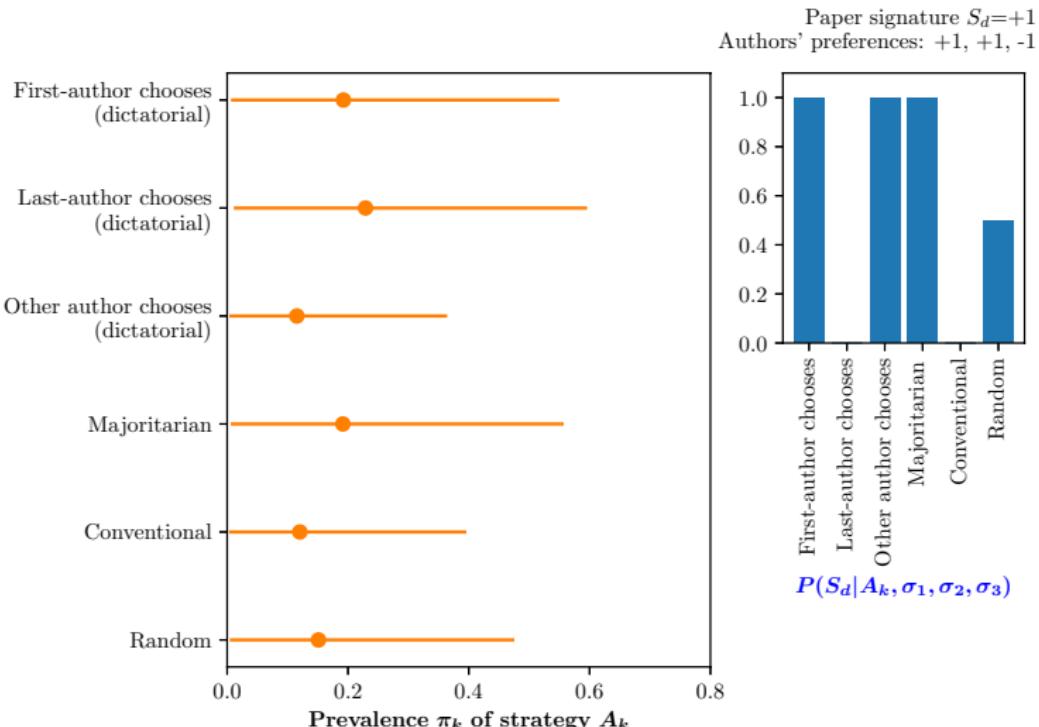
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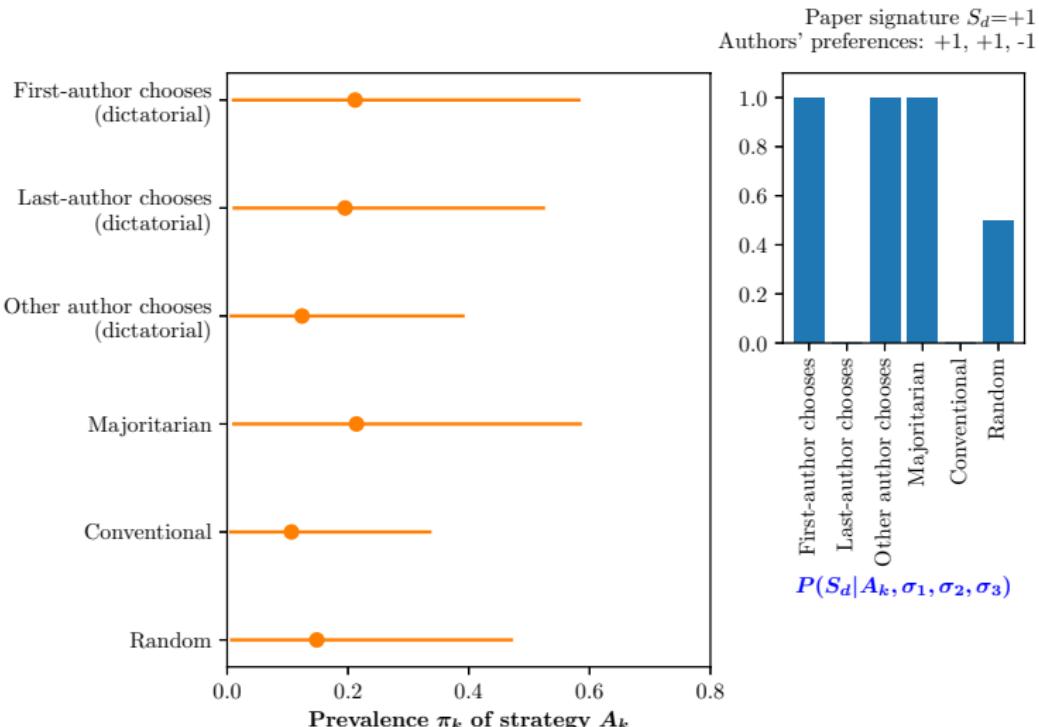
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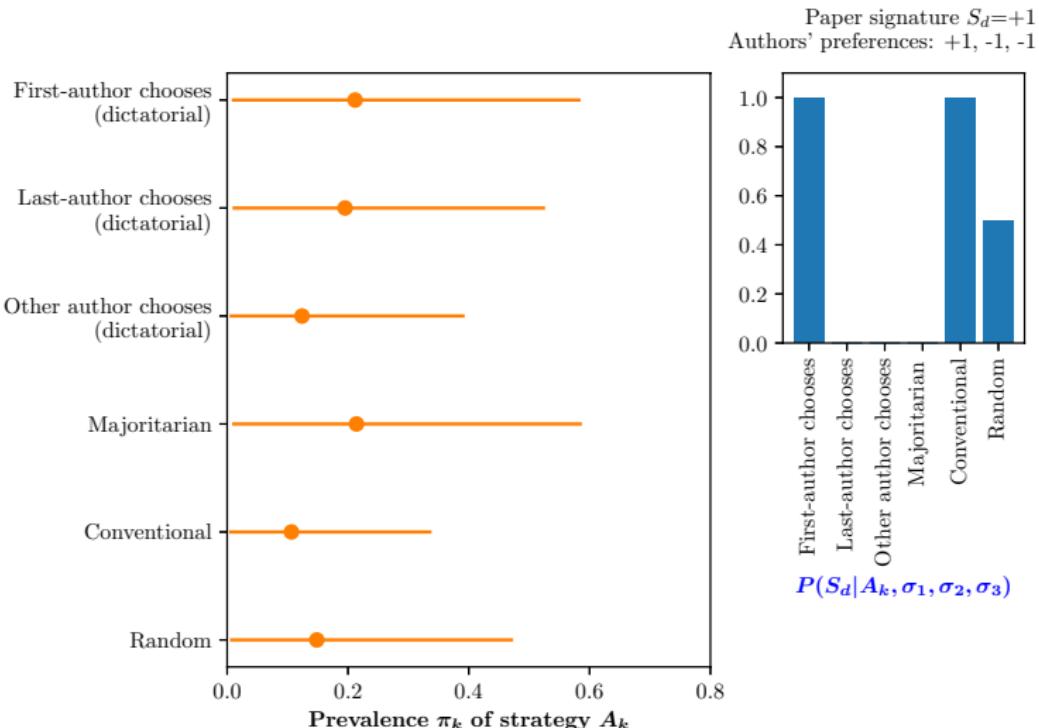
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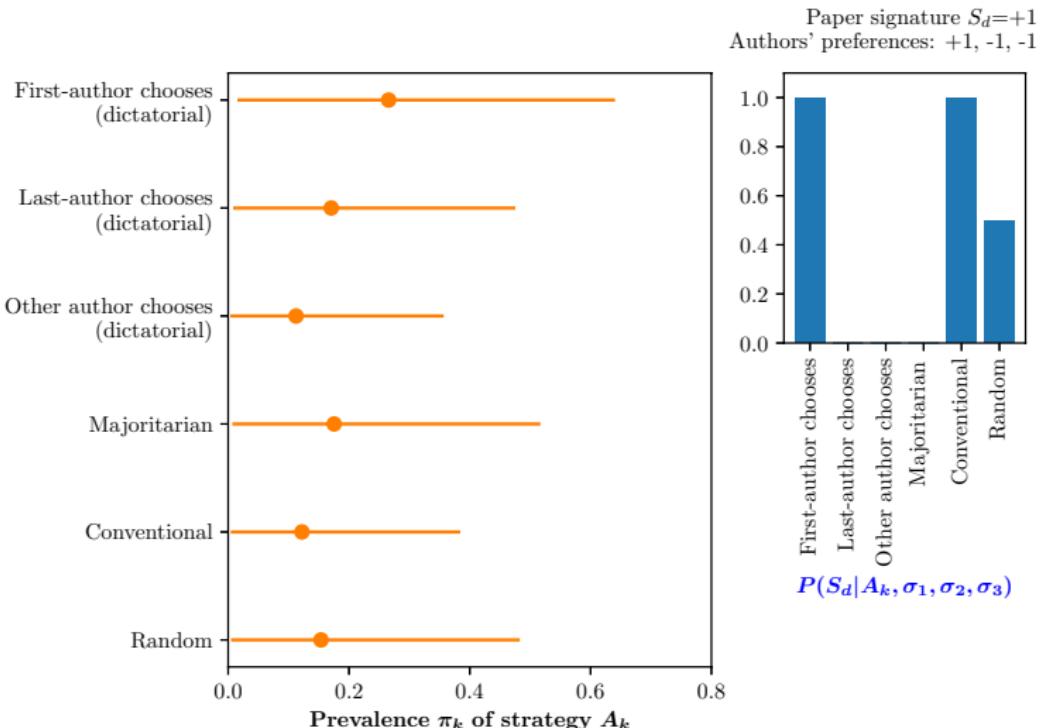
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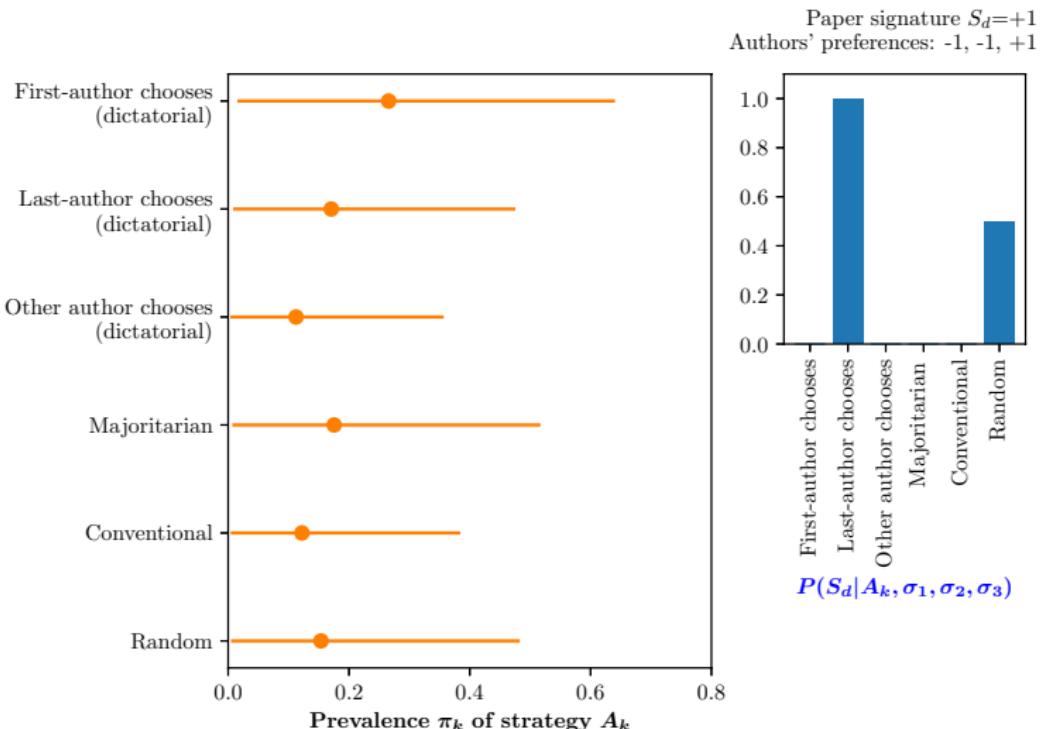
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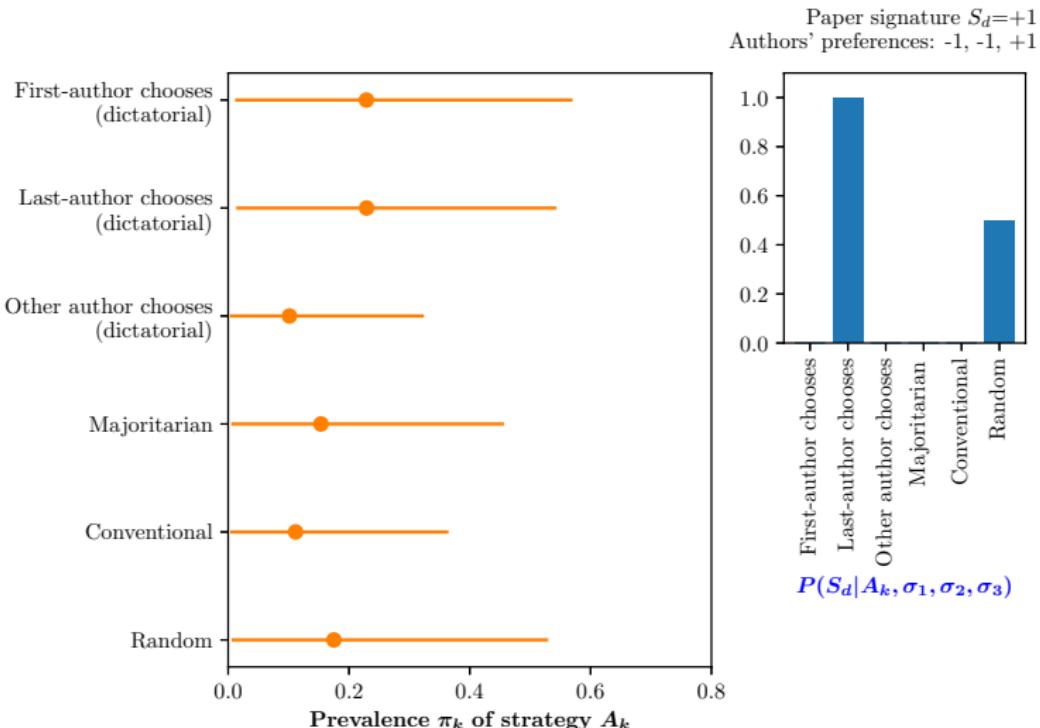
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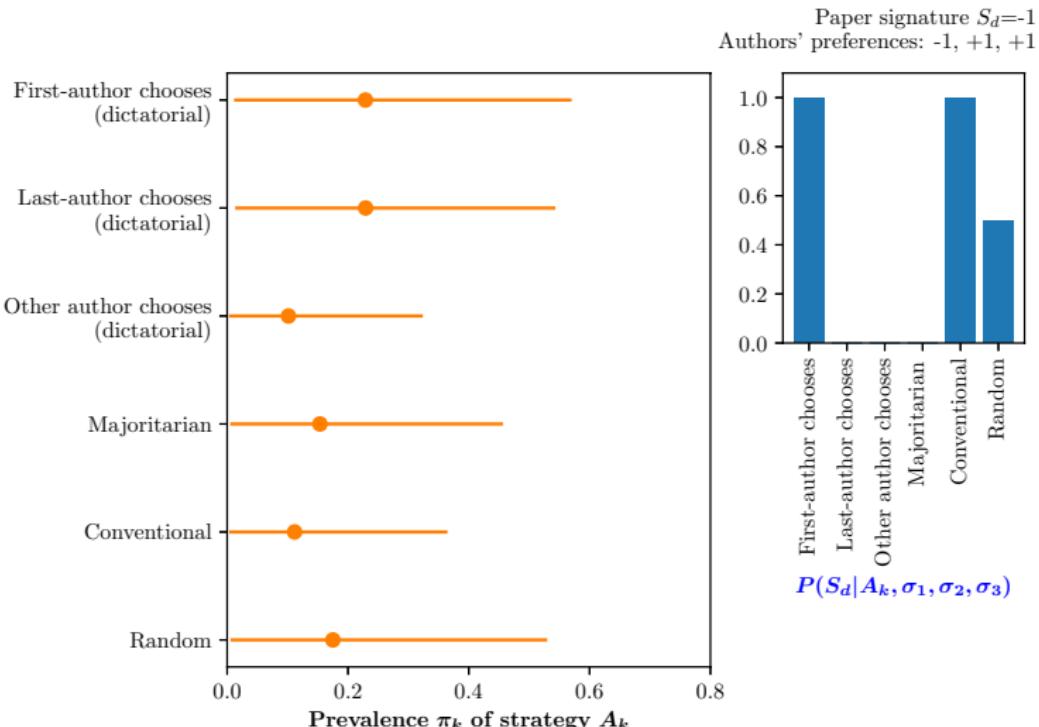
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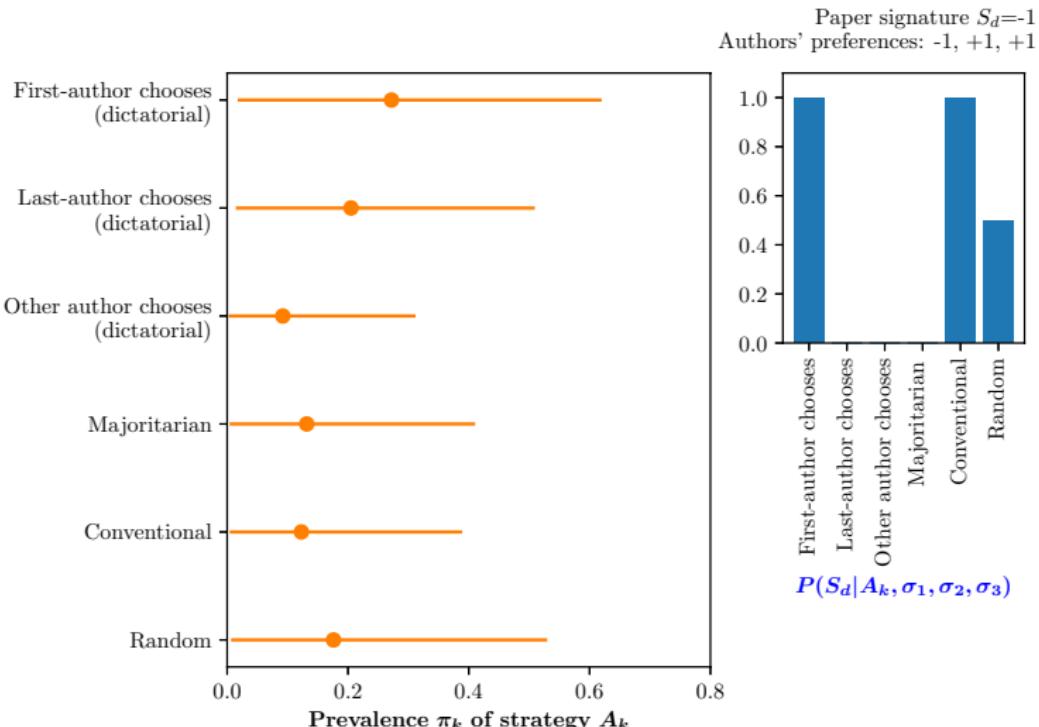
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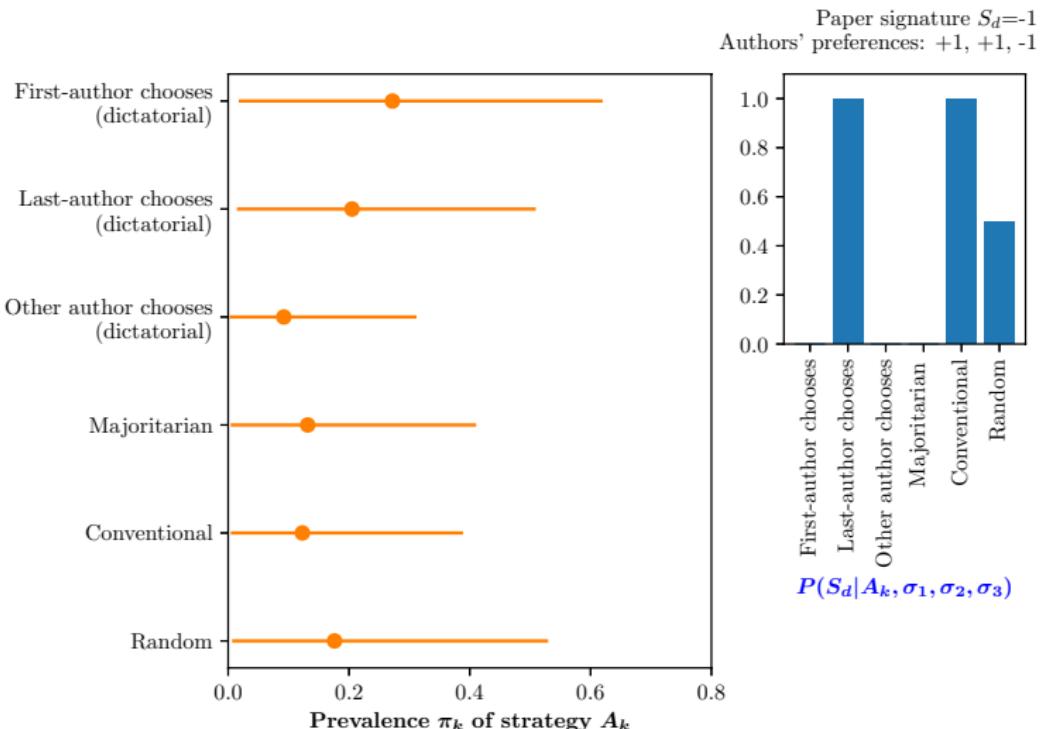
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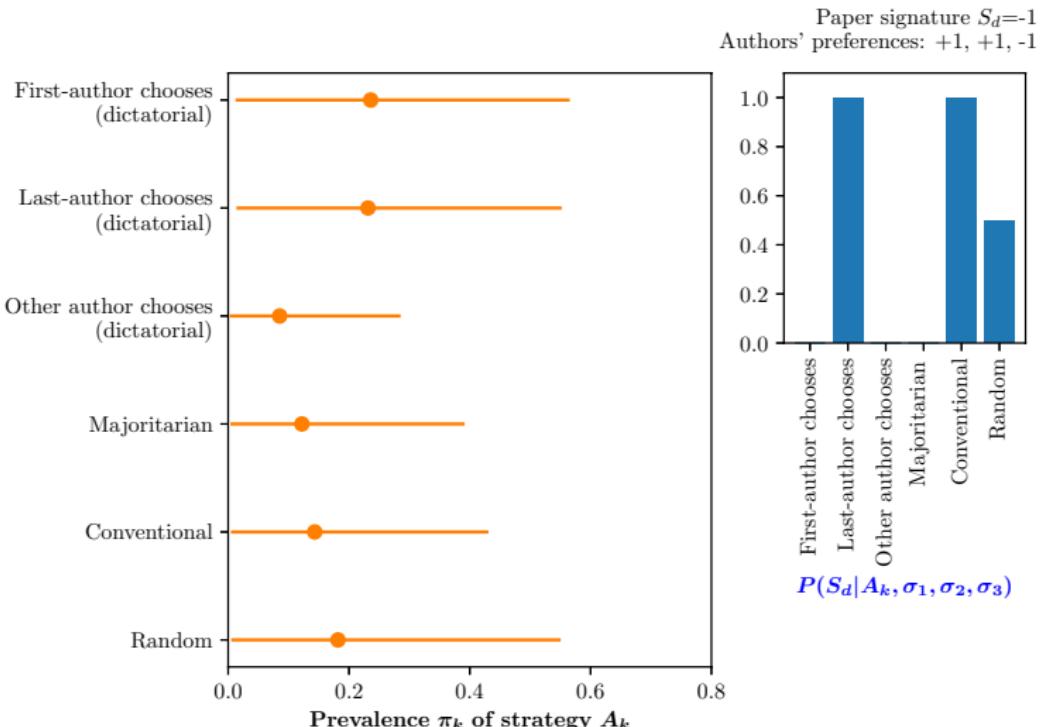
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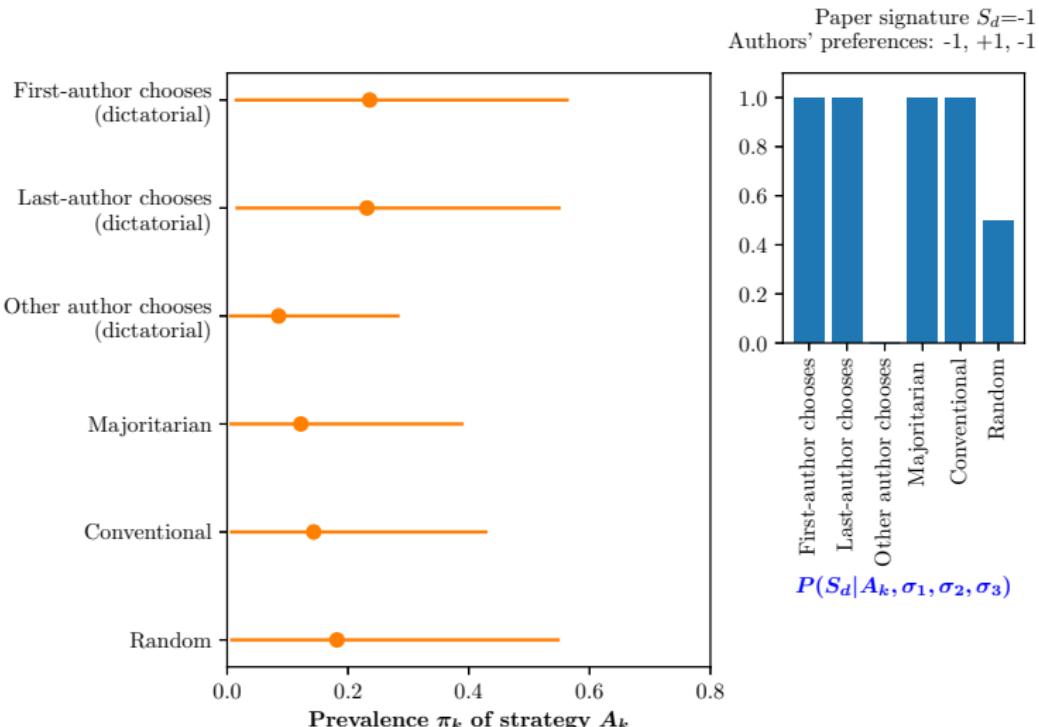
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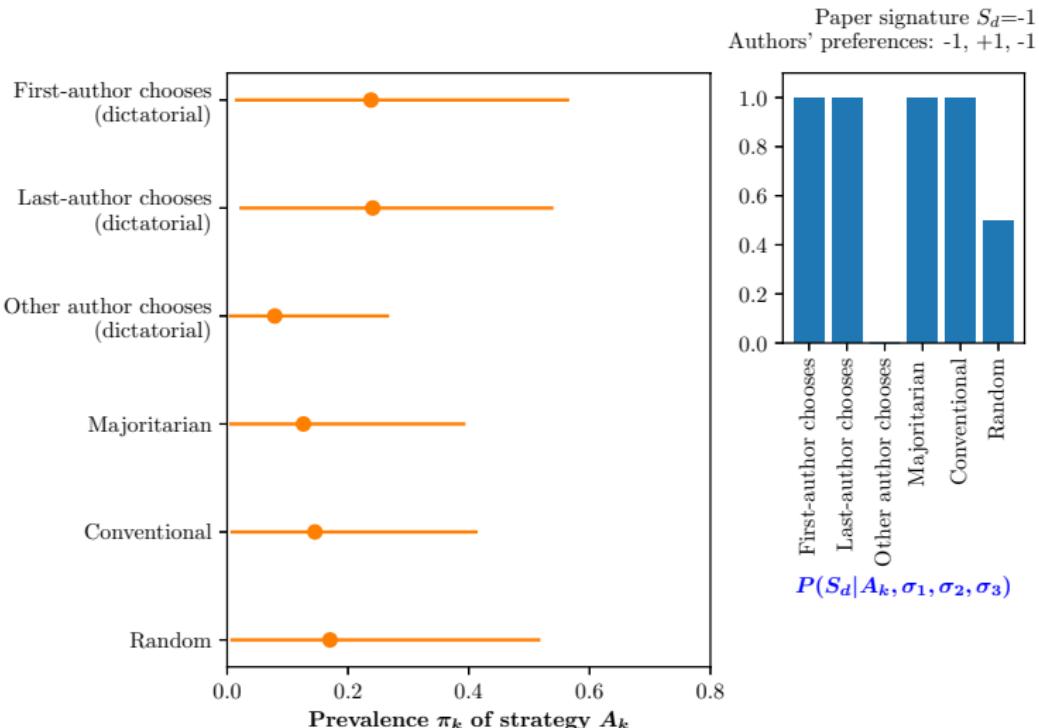
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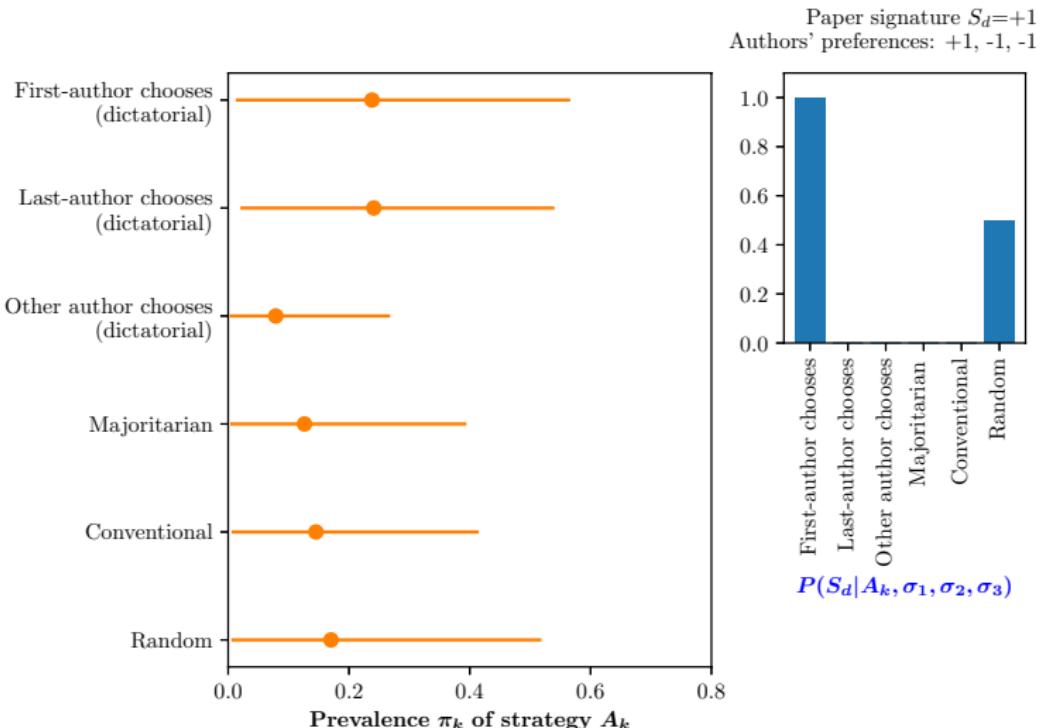
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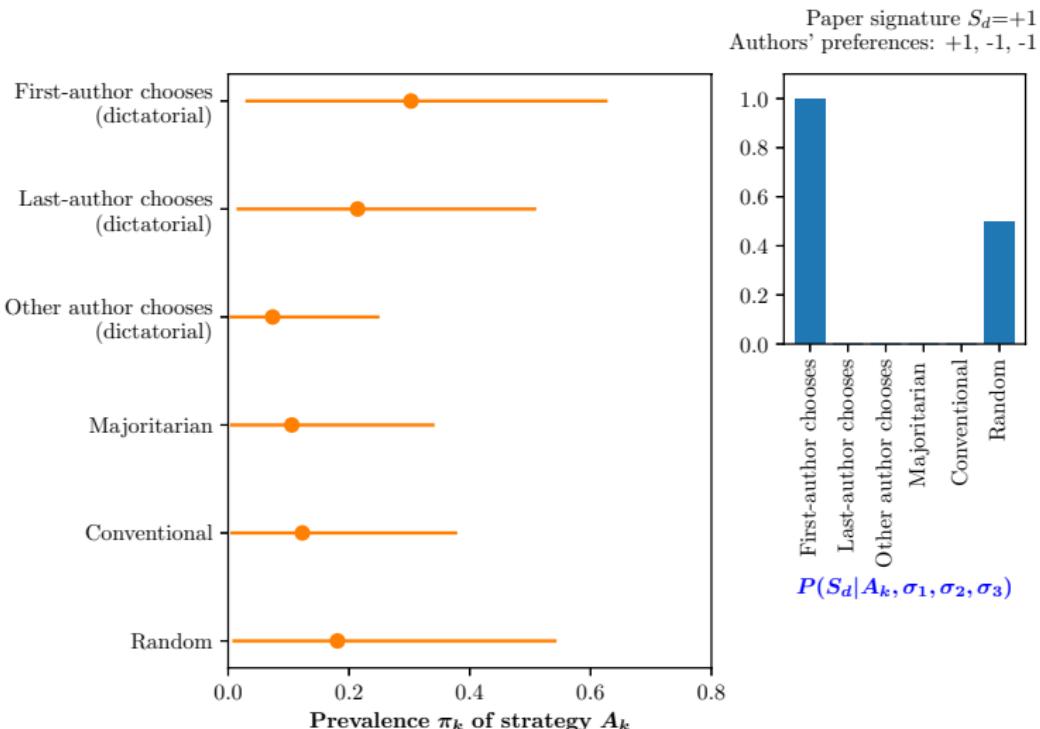
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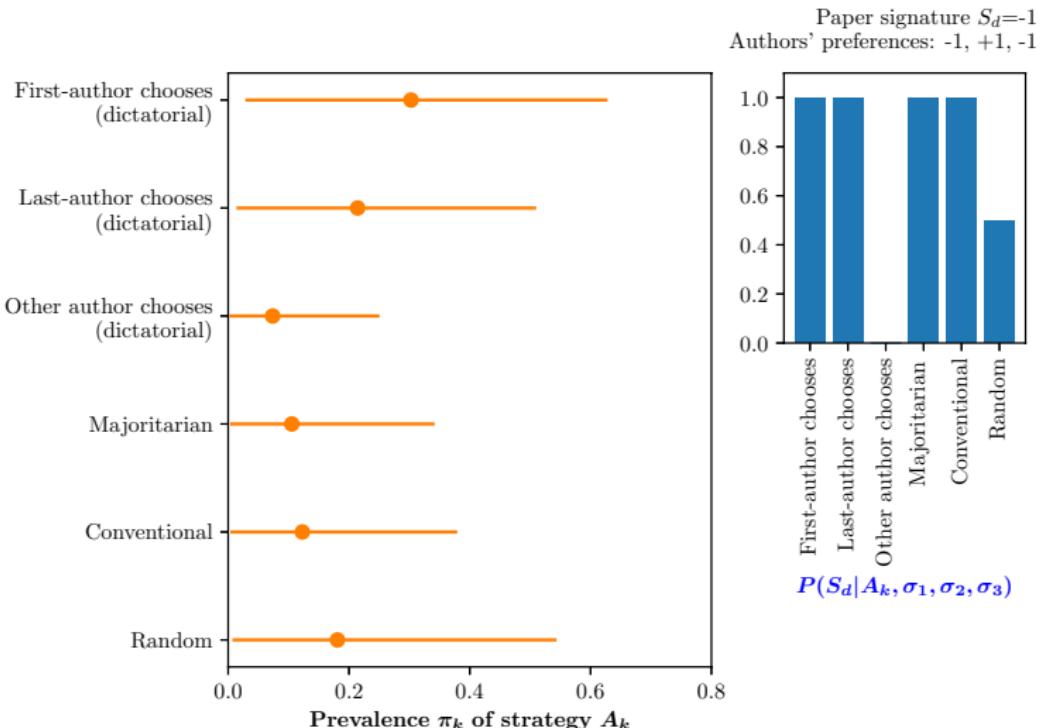
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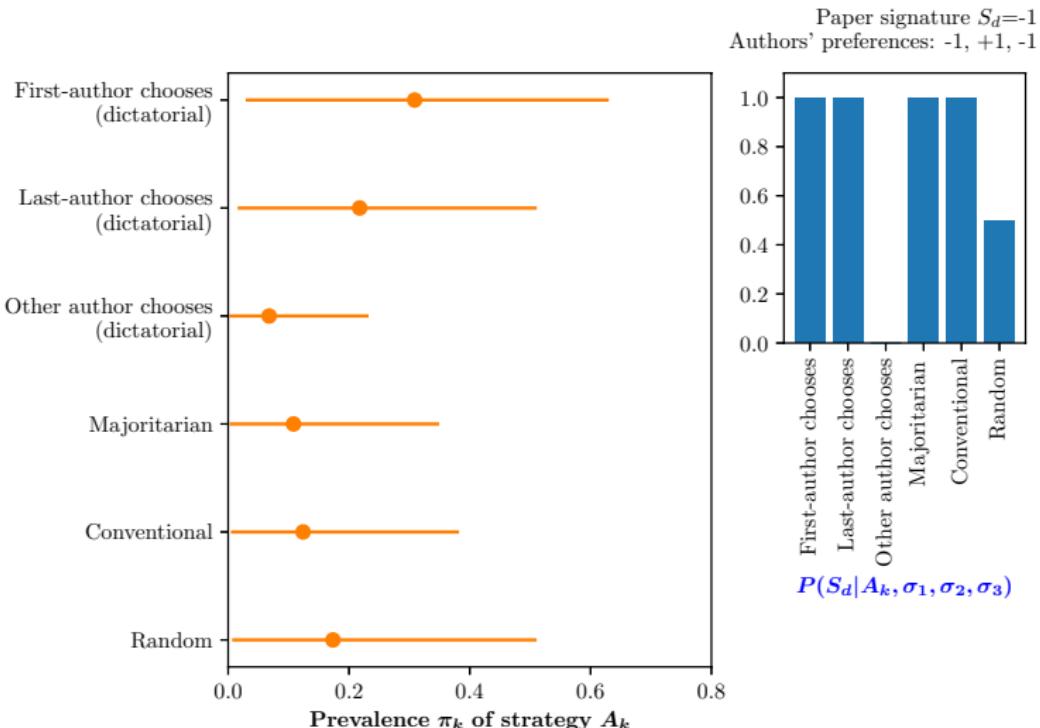
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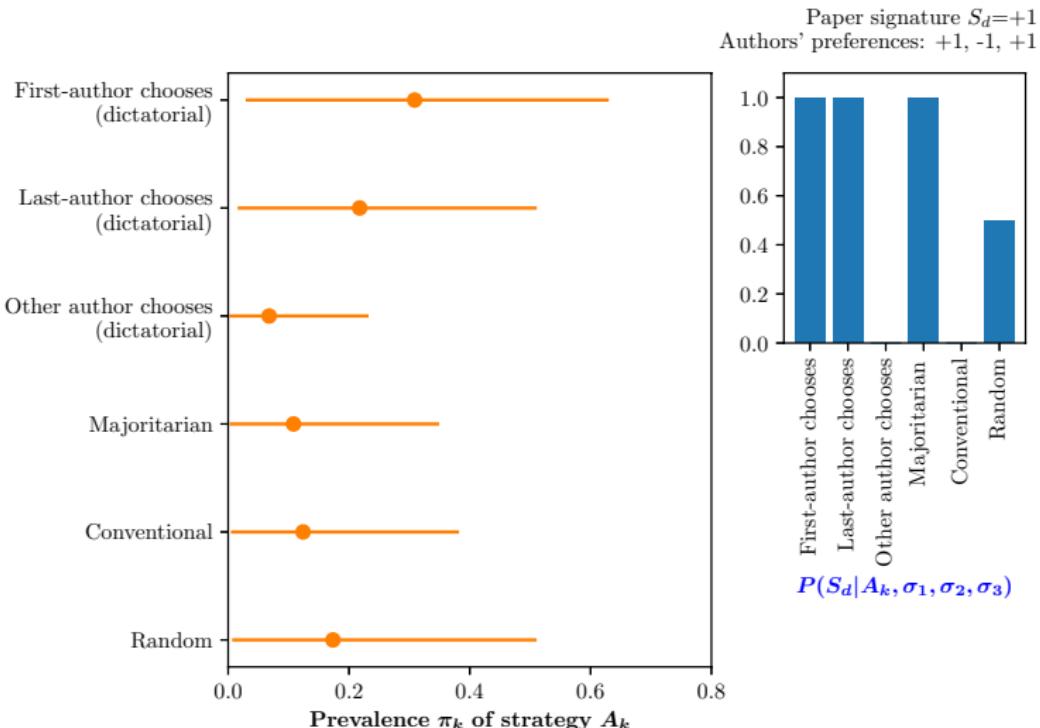
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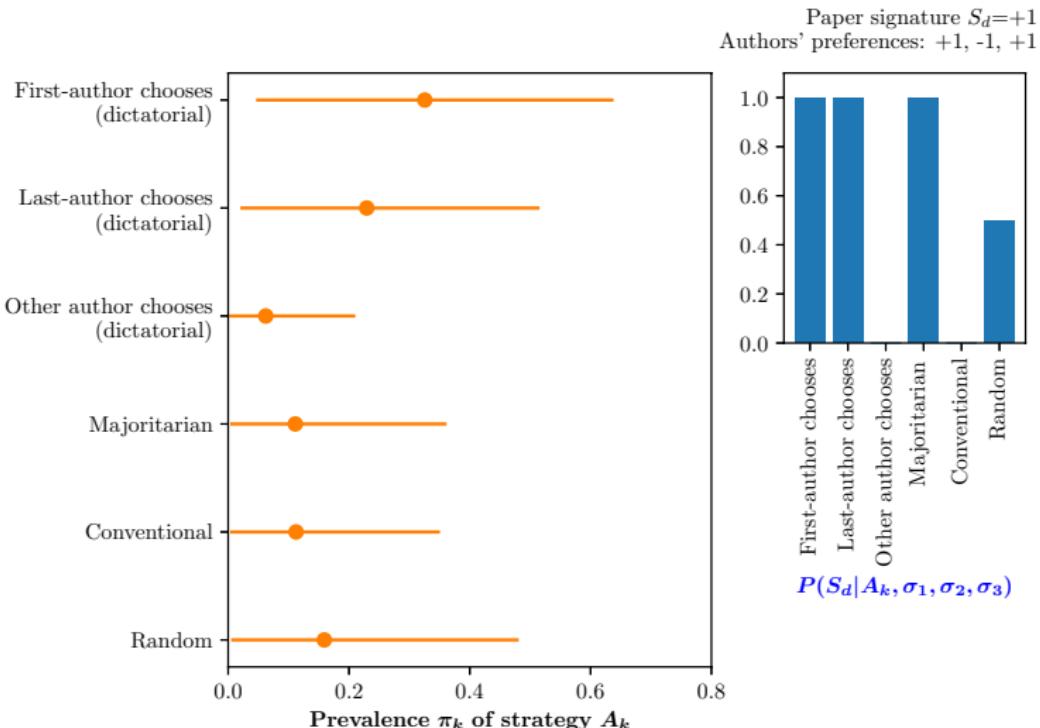
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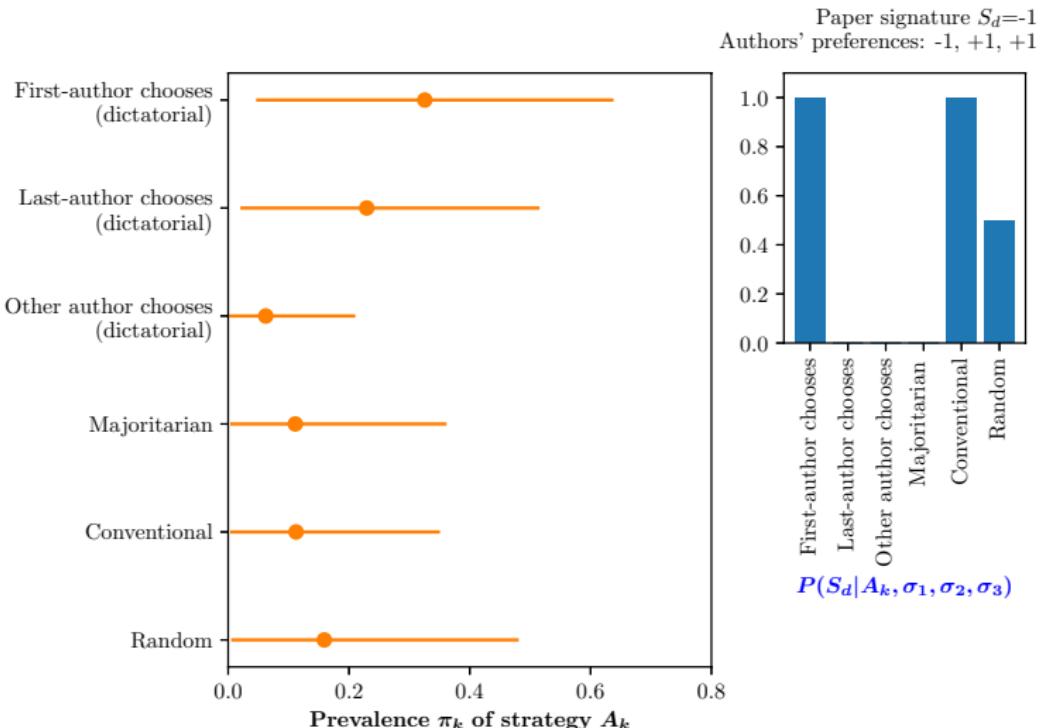
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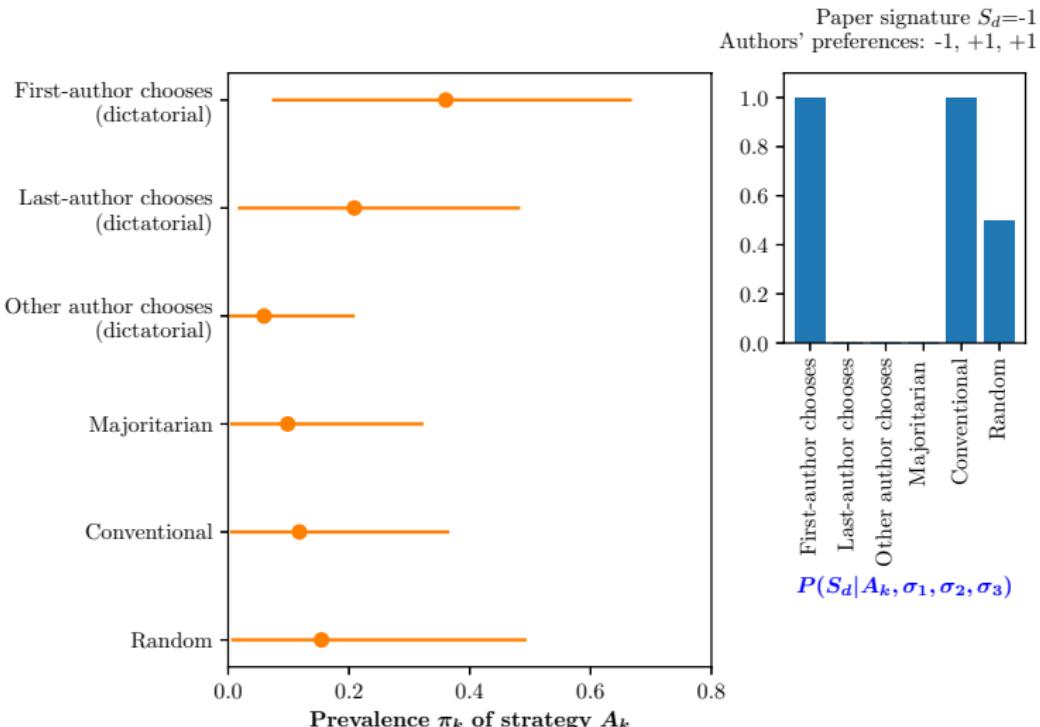
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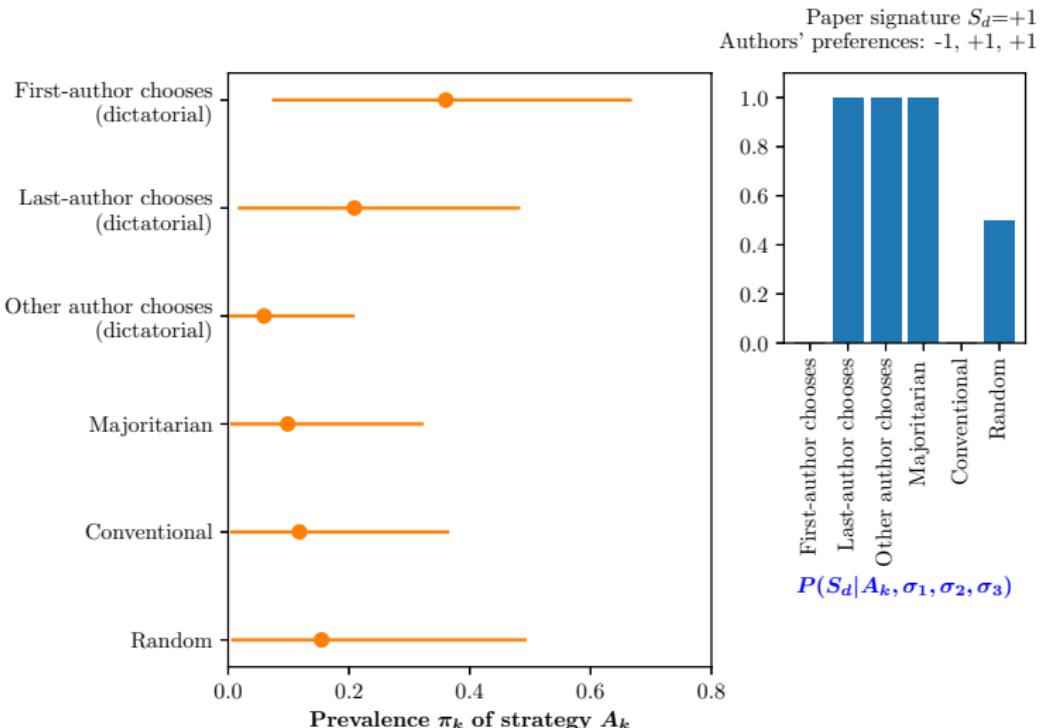
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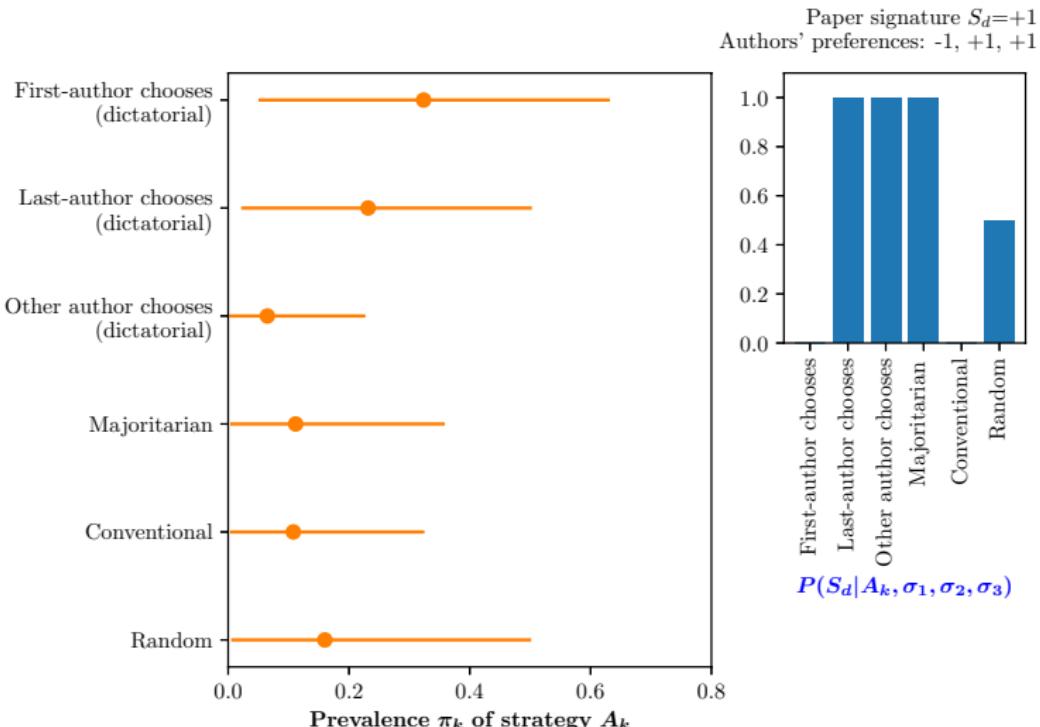
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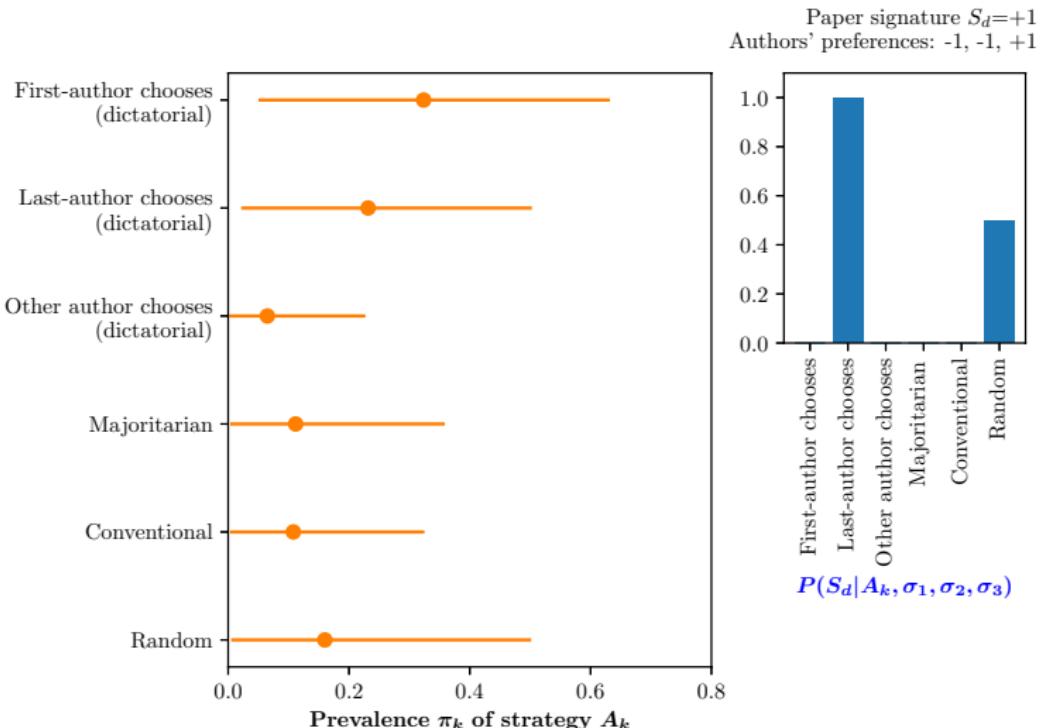
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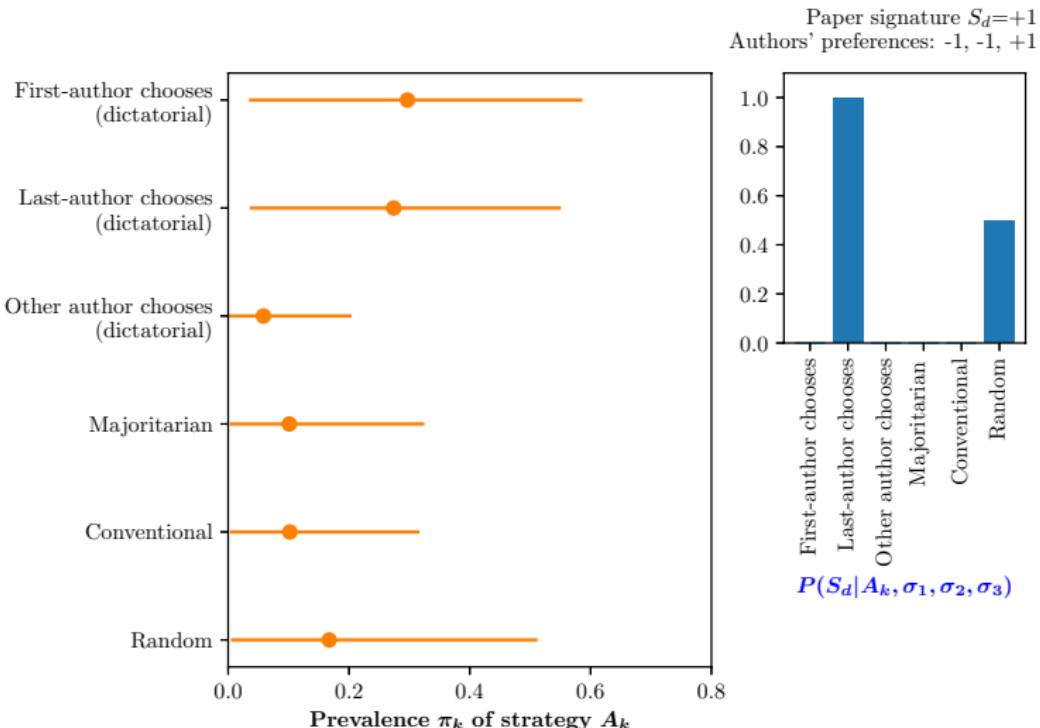
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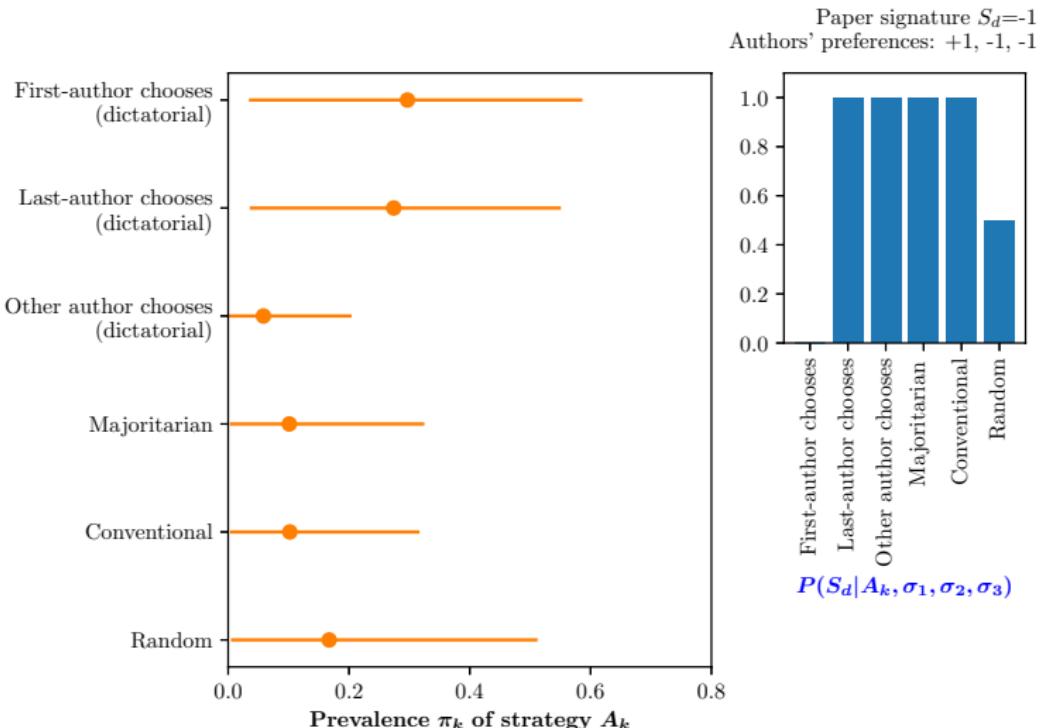
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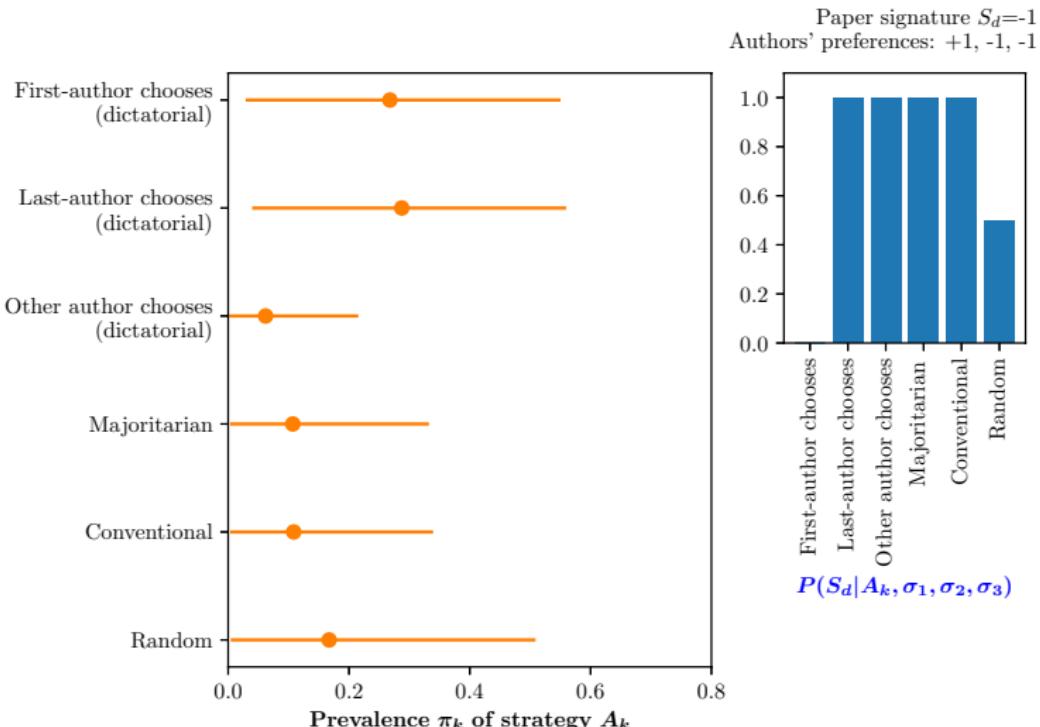
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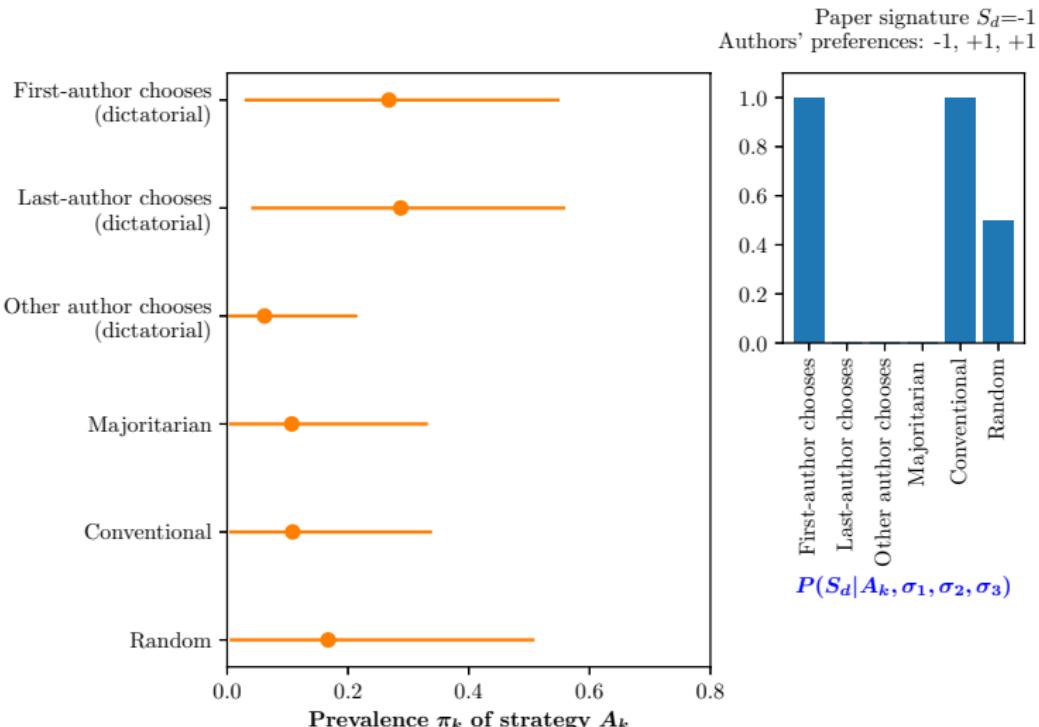
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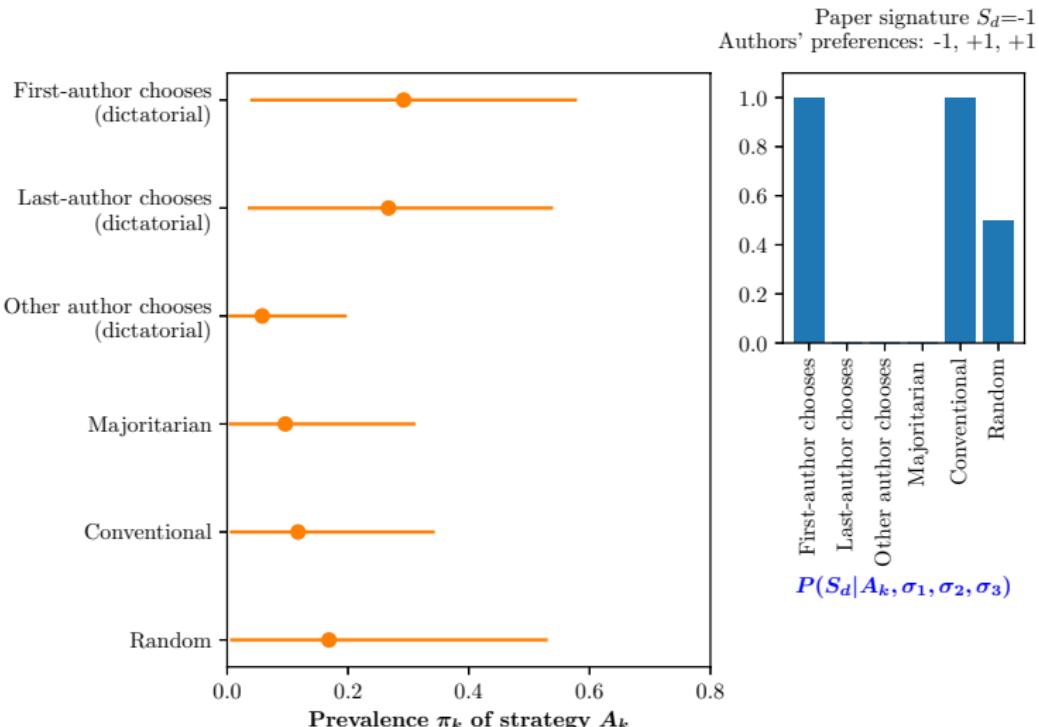
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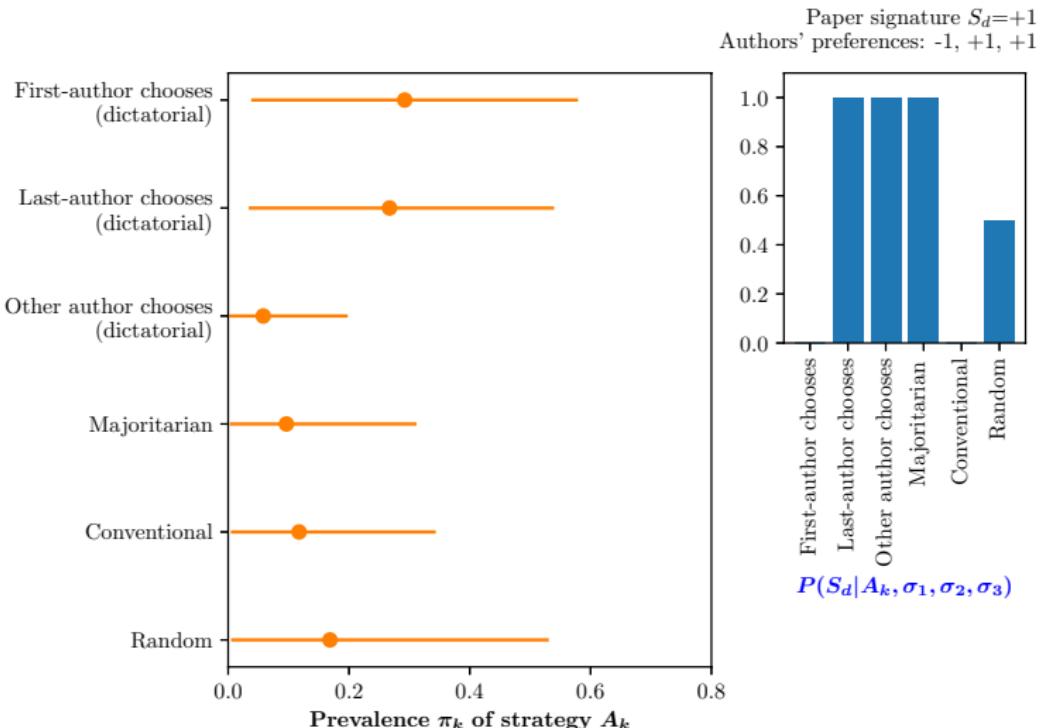
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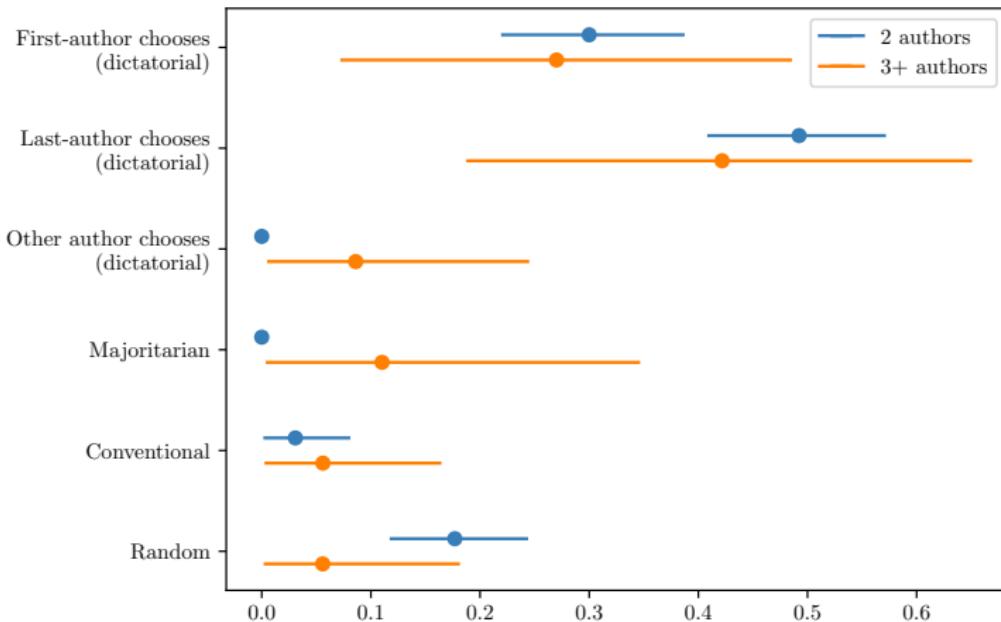


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# Prevalence of each preference-aggregation strategy

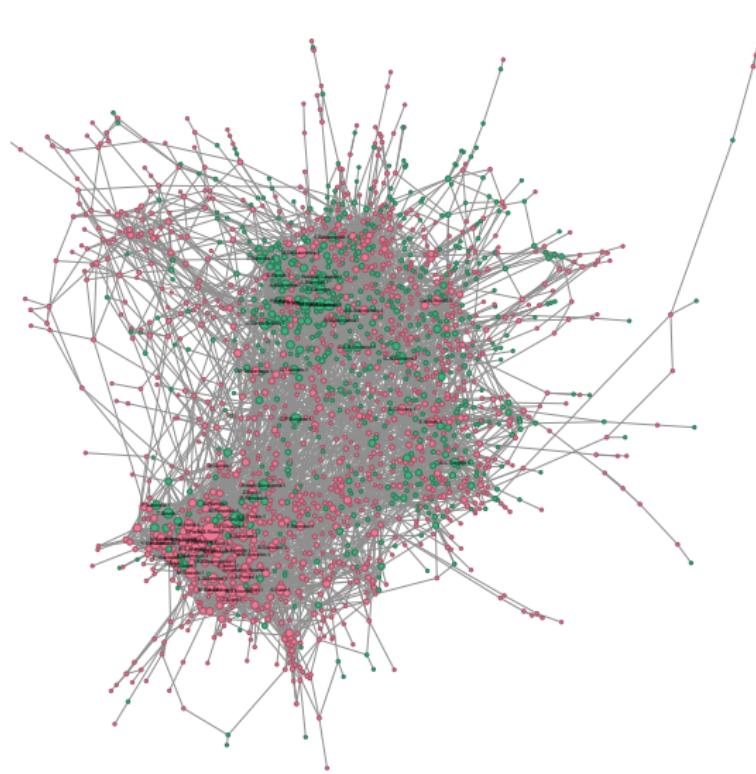


## 1 Inverse problems for philosophers and agent-based modelers

## 2 A case-study of conventions: the metric signature in particle physics

- How do physicists choose which convention to use in their own papers?
- How do scientists resolve conflicting preferences in collaborations?
- How do physicists' preferences get formed?

# Authors' preferences



Observed outcome: the preference of each author,

$$O_{\text{obs}} = (\sigma_1, \dots, \sigma_n), \sigma \in \{-1, +1\}$$

( $n = 2277$  authors)

# How do physicists' preferences get formed?

- Let's assume three models of the formation of physicists' preference towards the convention:
  - A “**strategic agent**” model ( $M_1$ ) assuming that individuals navigate three costs (coordination costs, inconsistency costs, and maladaptation costs) depending on their collaborators' preferences and the research areas in which they publish.
  - A **global cultural transmission model** ( $M_2$ ), in which physicists settle once and for all for a specific convention with a certain probability that depends on their primary research area (textbooks?)
  - A **local cultural transmission model** ( $M_3$ ), in which physicists copy the preference of their first collaborator.
- Which of these is more plausible given the observed patterns of preferences?

## Example: the strategic agent model ( $M_1$ )

The model  $M_1$  has multiple unknown parameters:

- $c_s$ : the cost of switching from one convention to another
- $c_c$ : the cost of disagreeing with co-authors
- $c_r$  the cost of using a suboptimal convention in a given research area

The **outcome**  $O_{\text{sim}}$  is the joint value of each author's preference:

$$O_{\text{sim}} = (\sigma_1, \dots, \sigma_n) \text{ where } \sigma_i = \pm 1$$

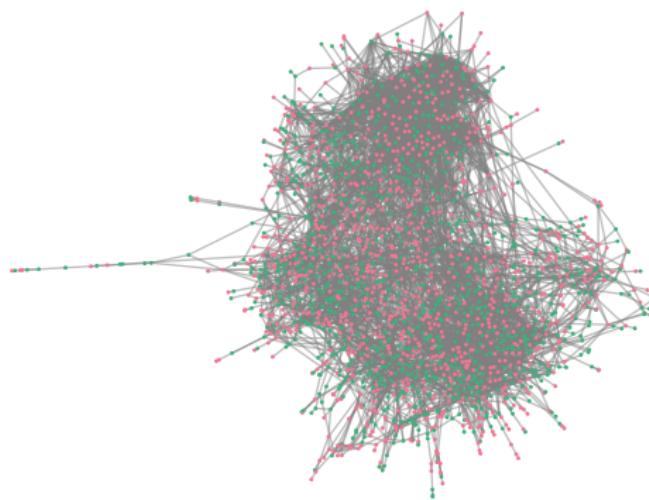
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# Simulation-based inference

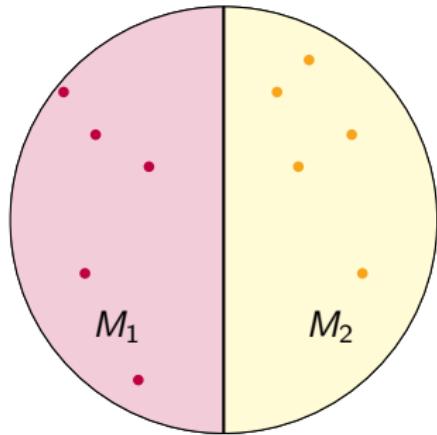
$$P(M_1|O) = \overbrace{P(O|M_1)}^{\text{Posterior}} \frac{P(M_1)}{P(O)} \quad (4)$$

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$$P(M_1|O) = \overbrace{P(O|M_1)}^{\text{Unknown in ABMs!}} \frac{P(M_1)}{P(O)} \quad (4)$$

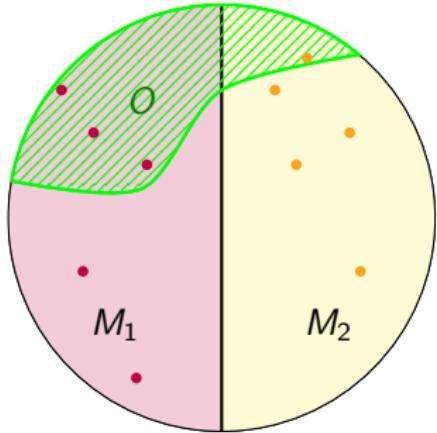
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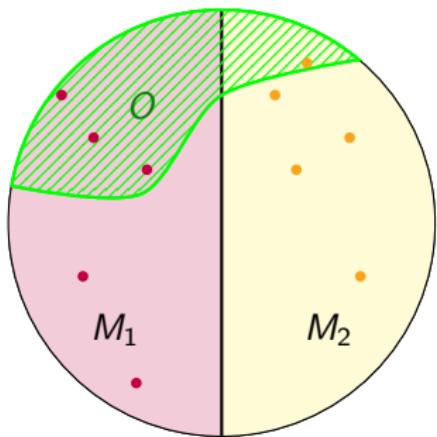
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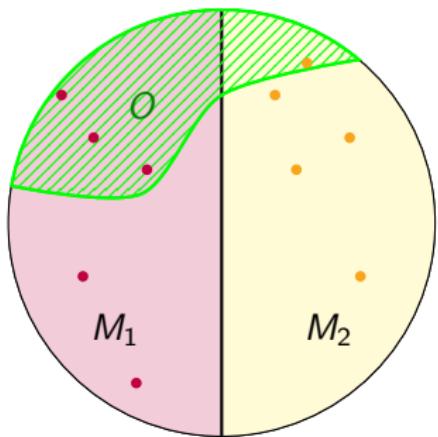
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$$P(O|M_1) = \frac{\text{[Area of green hatched region]}}{\text{[Area of M1 section]}} \simeq \frac{3}{5}$$

# Simulation-based inference

$$P(M_1|O) = \overbrace{P(O|M_1)}^{\text{Unknown in ABMs!}} \frac{P(M_1)}{P(O)} \quad (4)$$



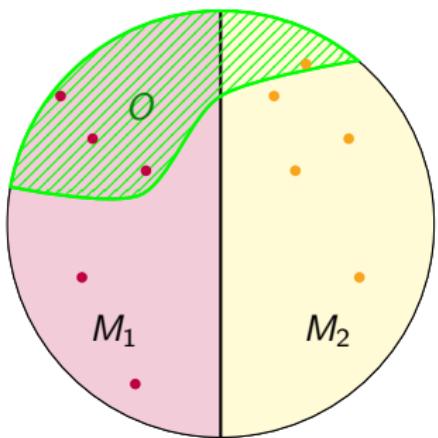
$$P(O|M_1) = \frac{\text{Shaded Area}}{\text{Total Area}} \simeq \frac{3}{5}$$

$$P(O|M_2) = \frac{\text{Shaded Area}}{\text{Total Area}} \simeq \frac{1}{5}$$

# Simulation-based inference

Unknown  
in ABMs!

$$P(M_1|O) = \overbrace{P(O|M_1)}^{\text{Unknown in ABMs!}} \frac{P(M_1)}{P(O)} \quad (4)$$



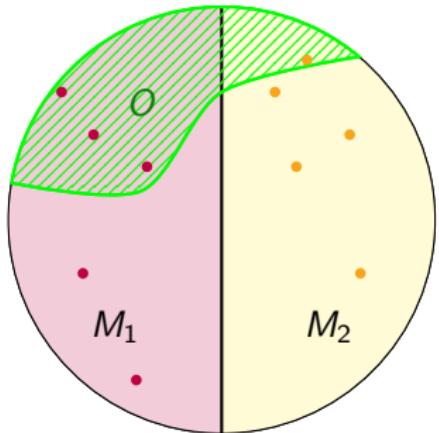
$$P(O|M_1) = \frac{\text{[Area of overlapping region]}}{\text{[Area of M1]}} \approx \frac{3}{5}$$

$$P(O|M_2) = \frac{\text{[Area of overlapping region]}}{\text{[Area of M2]}} \approx \frac{1}{5}$$

$$P(M_1|O) = P(O|M_1) \frac{P(M_1)}{P(O)} = \frac{\text{[Area of overlapping region]}}{\text{[Area of M1]}} \times \frac{\text{[Area of M1]}}{\text{[Area of overlapping region]}} = 1$$

# Simulation-based inference

$$P(M_1|O) = \overbrace{P(O|M_1)}^{\text{Unknown in ABMs!}} \frac{P(M_1)}{P(O)} \quad (4)$$



$$P(O|M_1) = \frac{\text{[Intersection of } O \text{ and } M_1]}{\text{Total area of } M_1} \simeq \frac{3}{5}$$

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$$P(M_2|O) = P(O|M_2) \frac{P(M_2)}{P(O)} = \frac{\text{[Intersection of } O \text{ and } M_2]}{\text{Total area of } M_2} \times \frac{\text{Total area of } M_2}{\text{Total area of } M_1 + \text{Total area of } M_2} = \frac{\text{[Intersection of } O \text{ and } M_2]}{\text{Total area of } M_1 + \text{Total area of } M_2}$$

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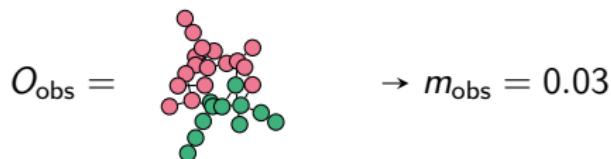
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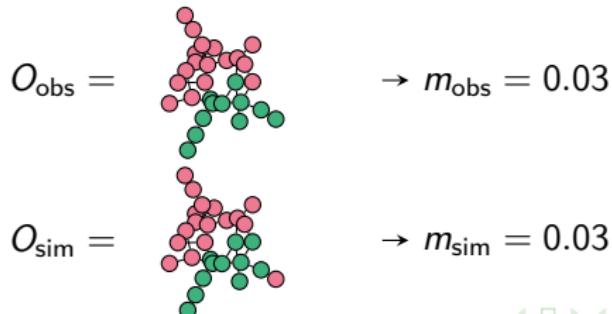
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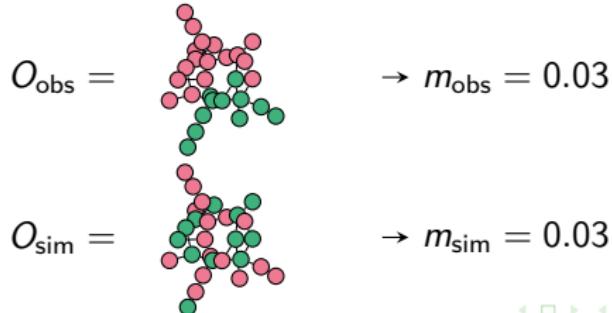
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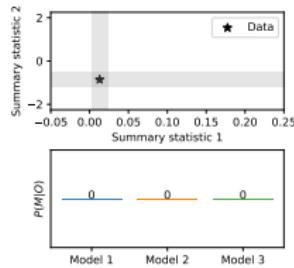
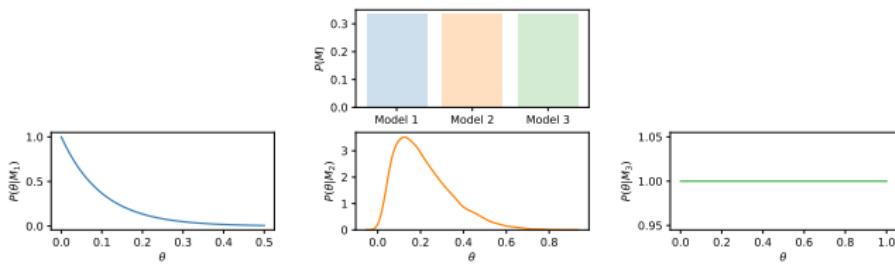


# Summary statistics in simulation-based inference

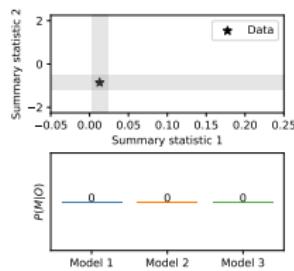
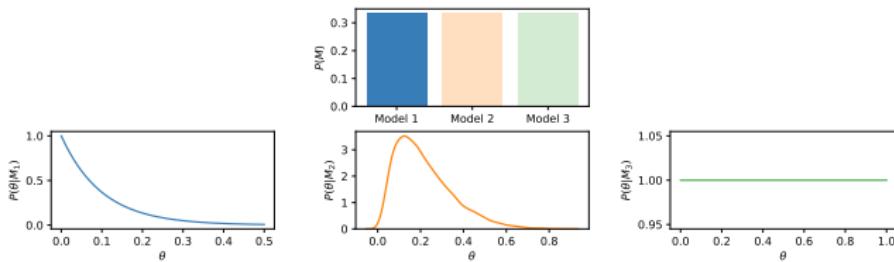
There are two main approaches for choosing adequate summary statistics:

- ① Hand-picking interpretable summary statistics based on our own intuitions.
- ② Using sophisticated methods to learn statistically optimal (but potentially un-interpretable) summary statistics. Optimal summary statistics reduce our posterior uncertainty given a fixed amount of data.

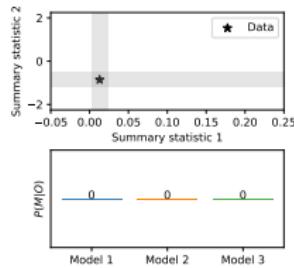
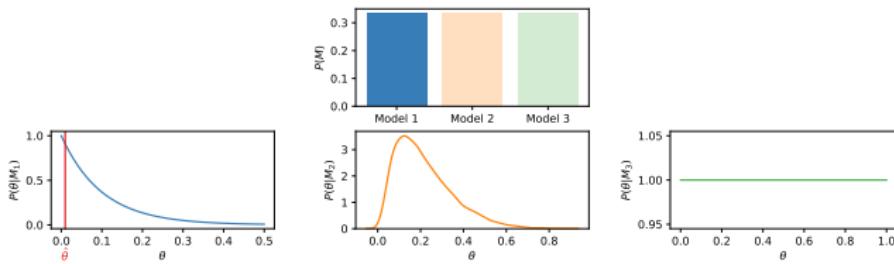
# Simulation-based inference with summary statistics



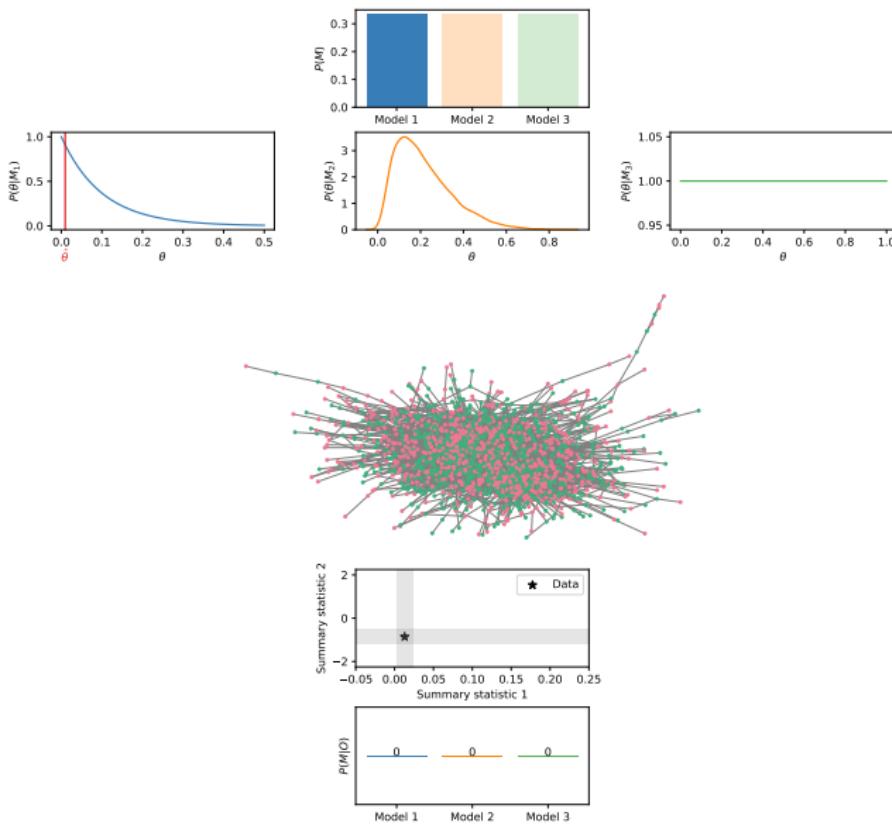
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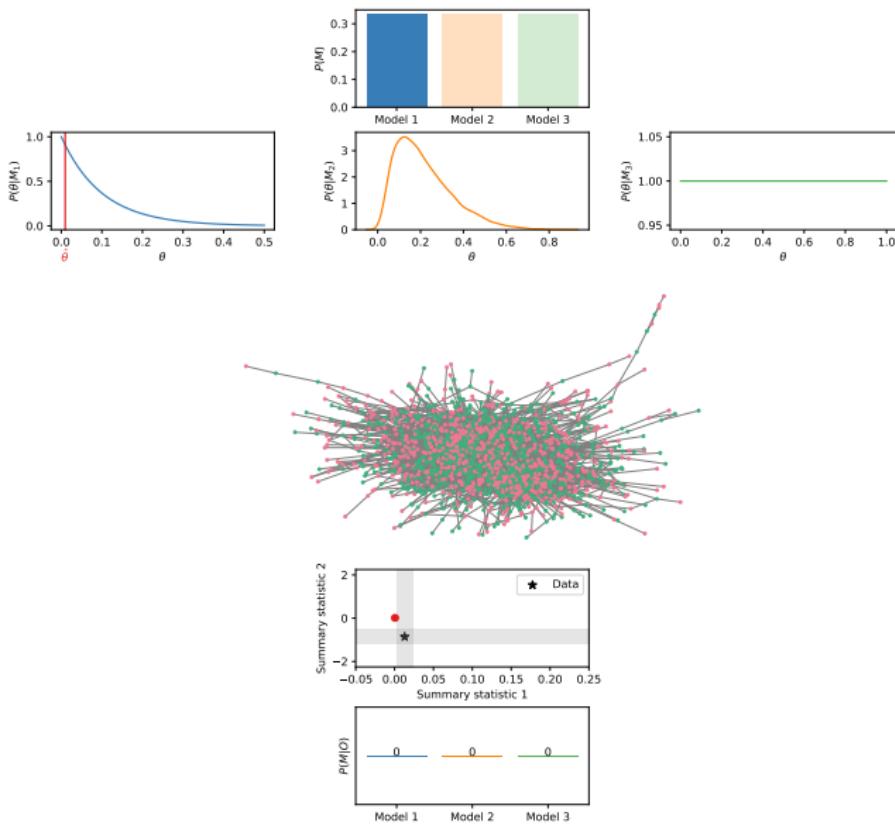
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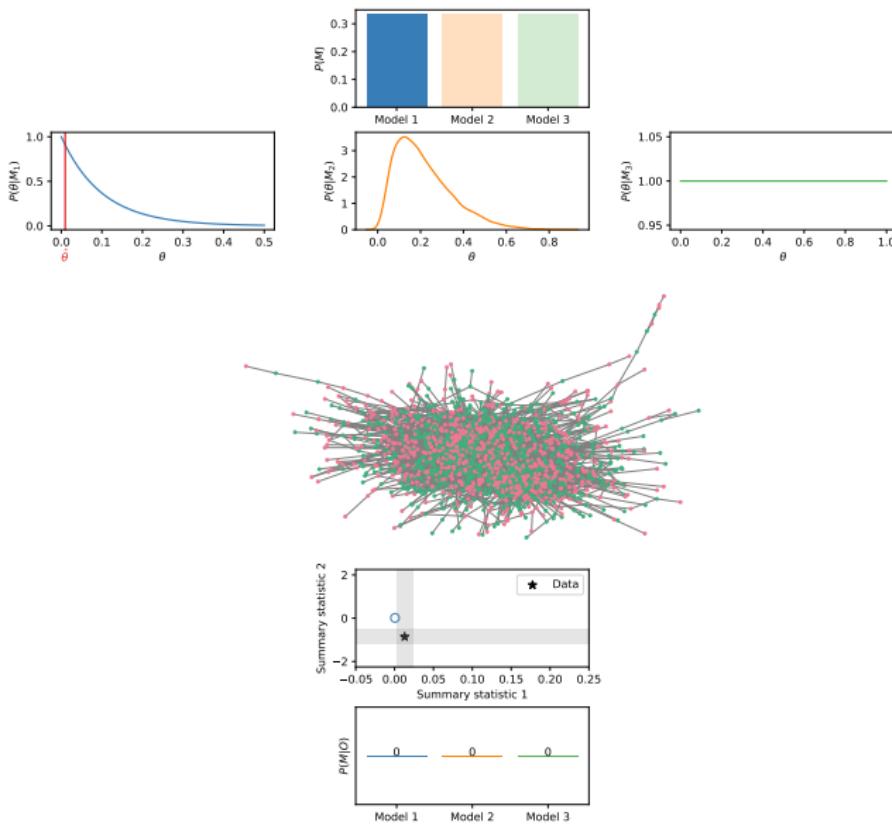
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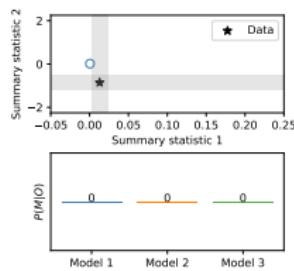
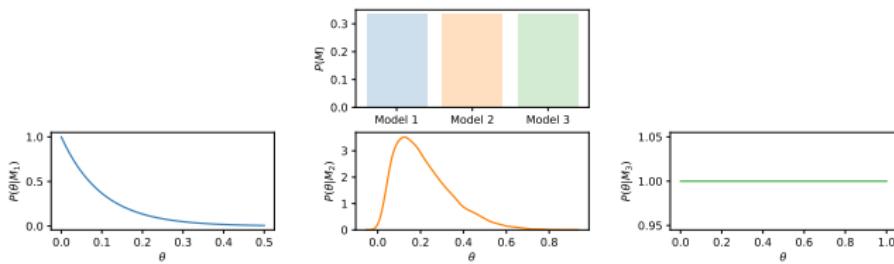
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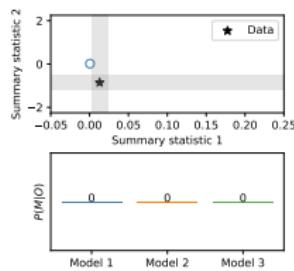
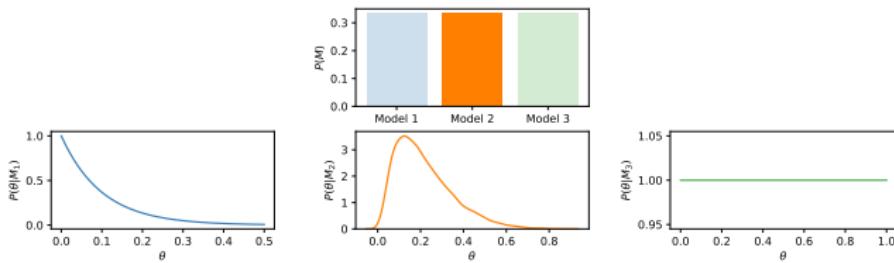
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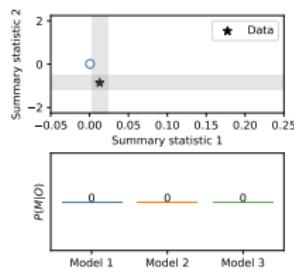
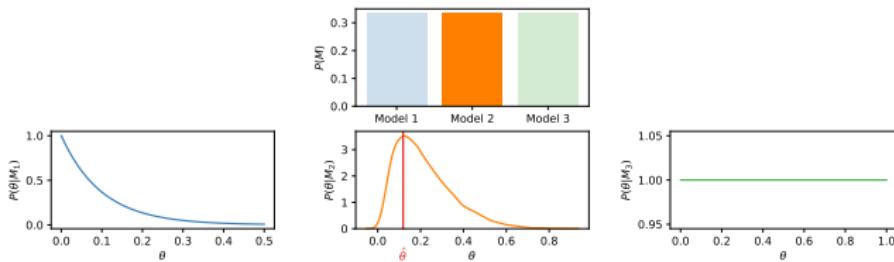
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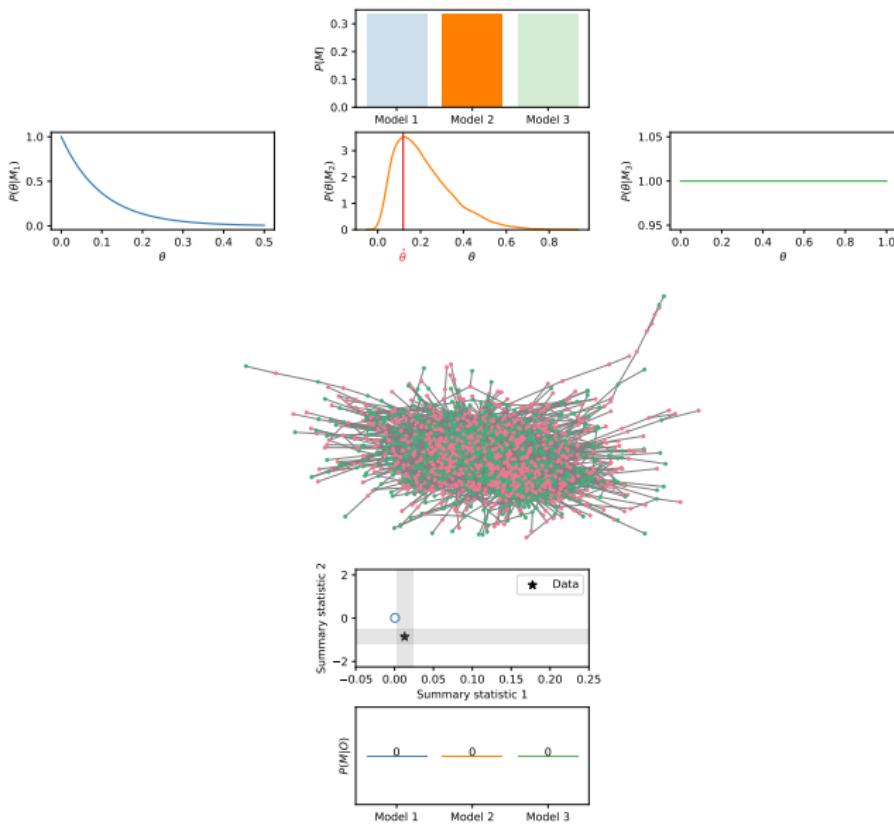
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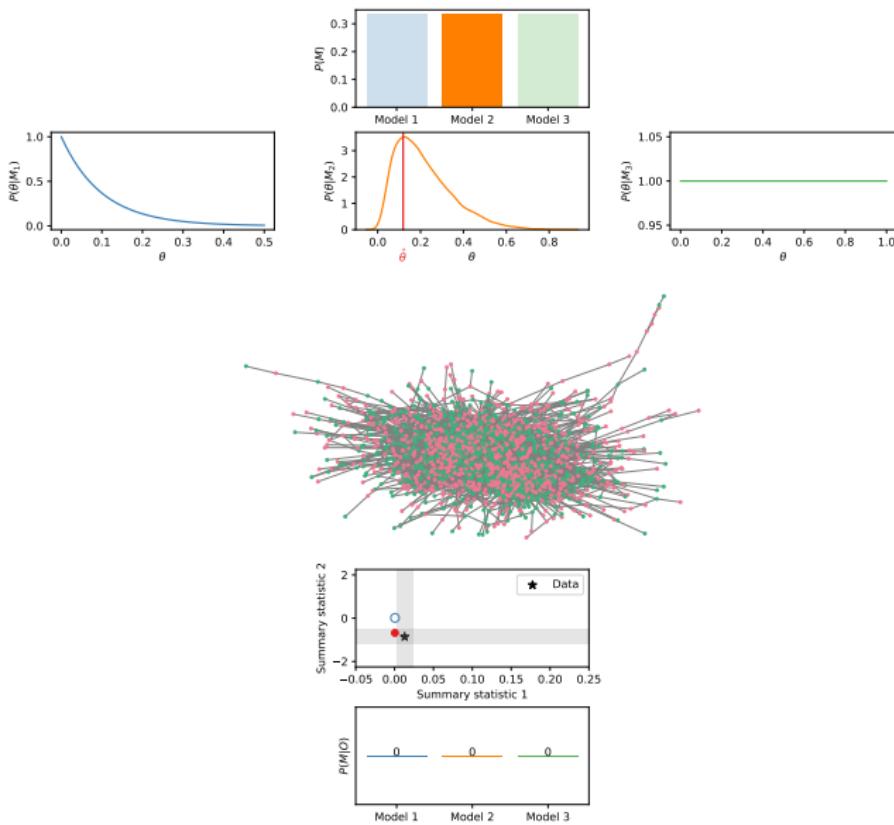
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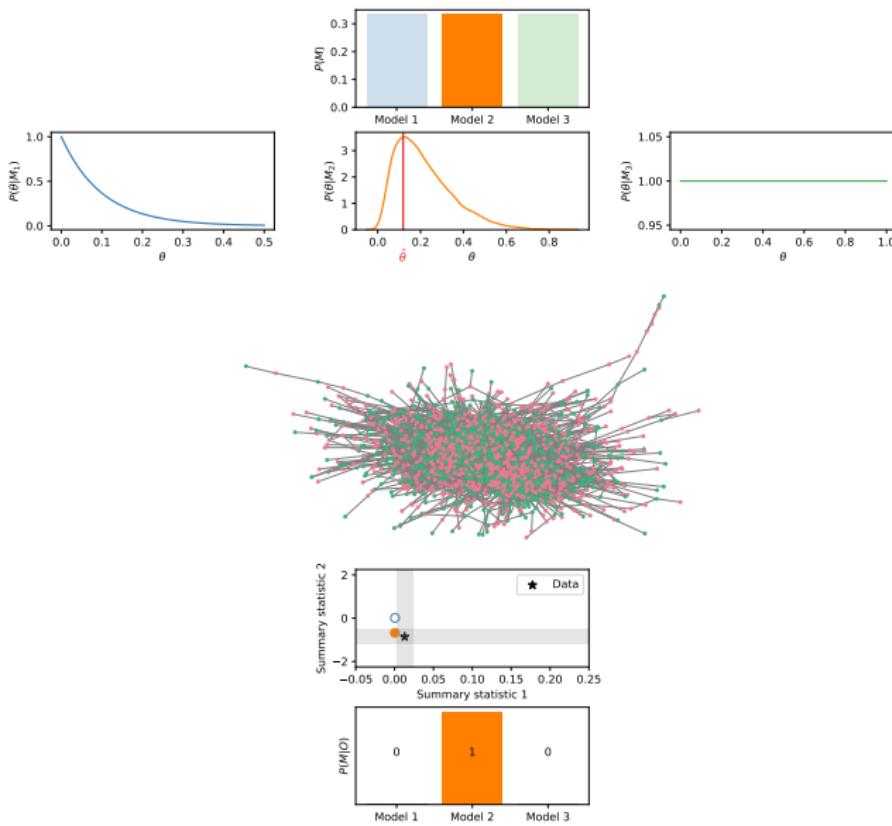
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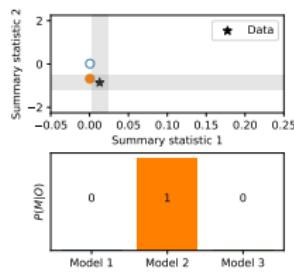
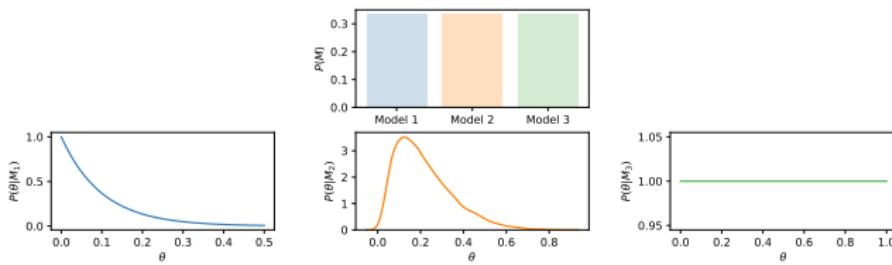
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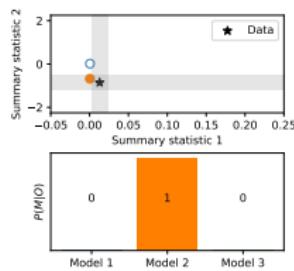
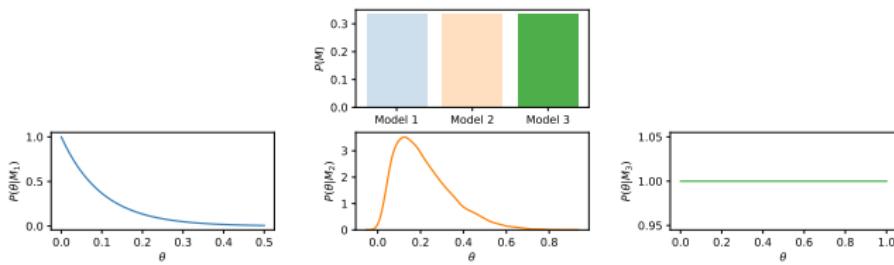
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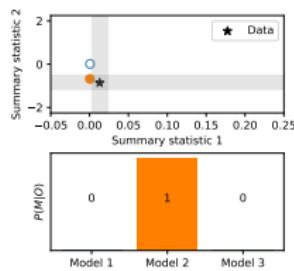
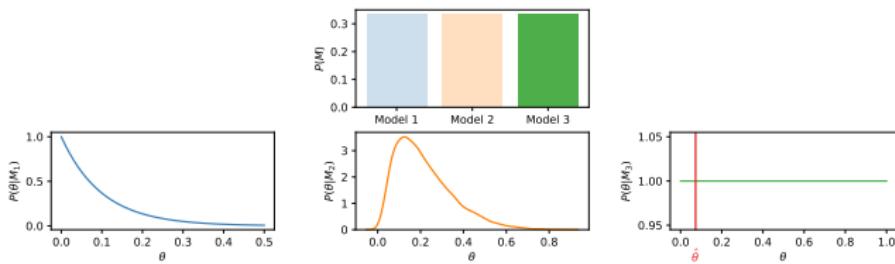
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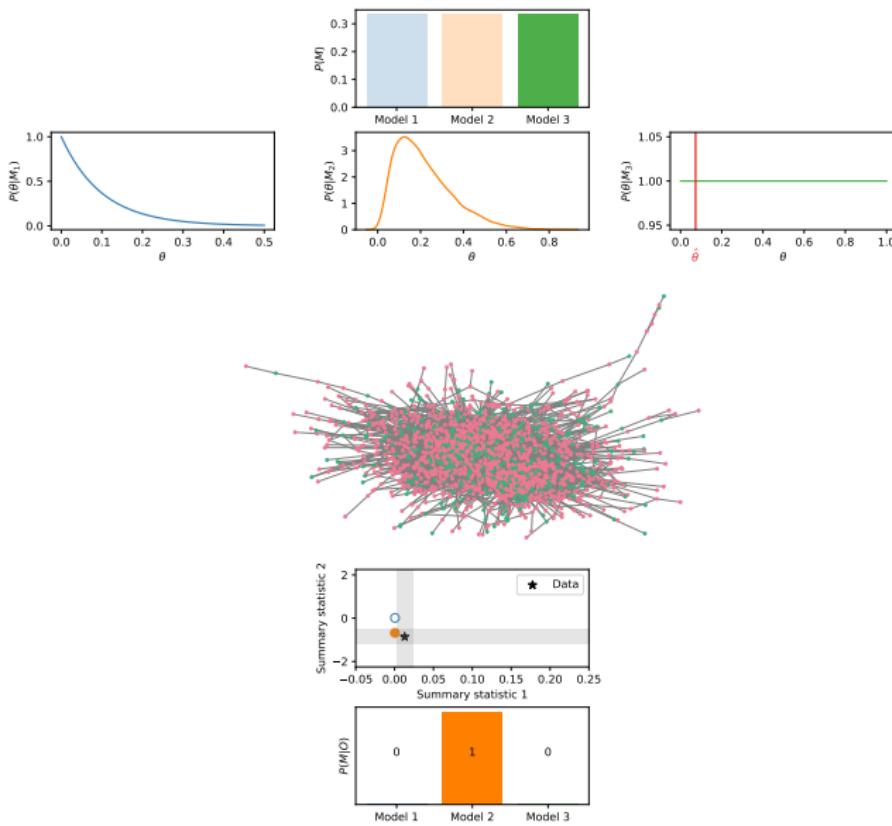
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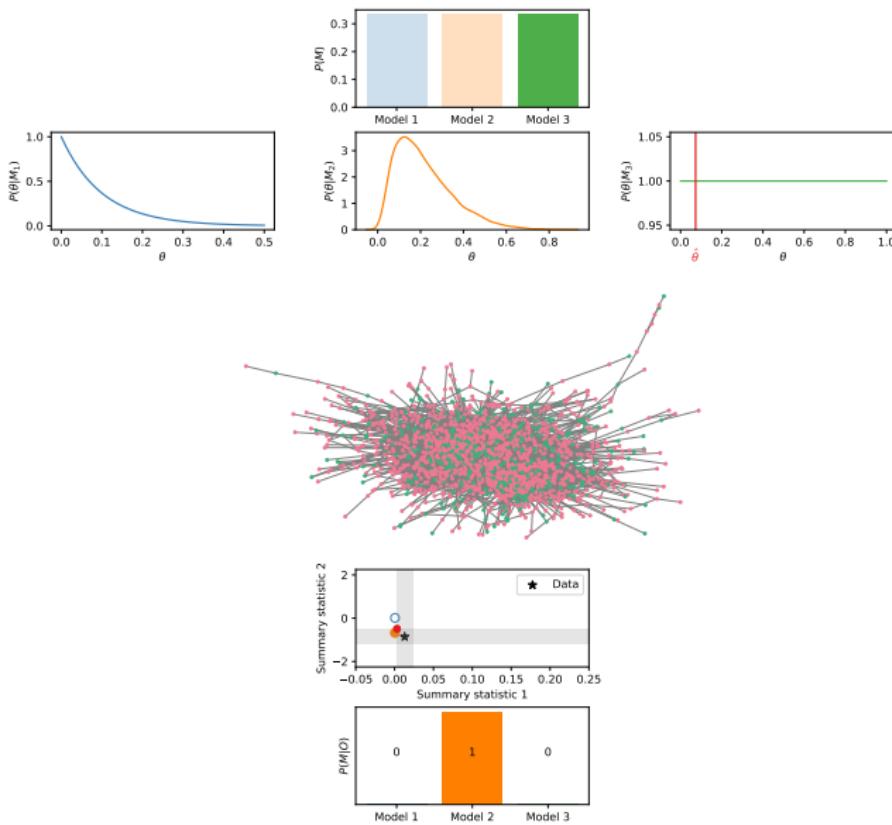
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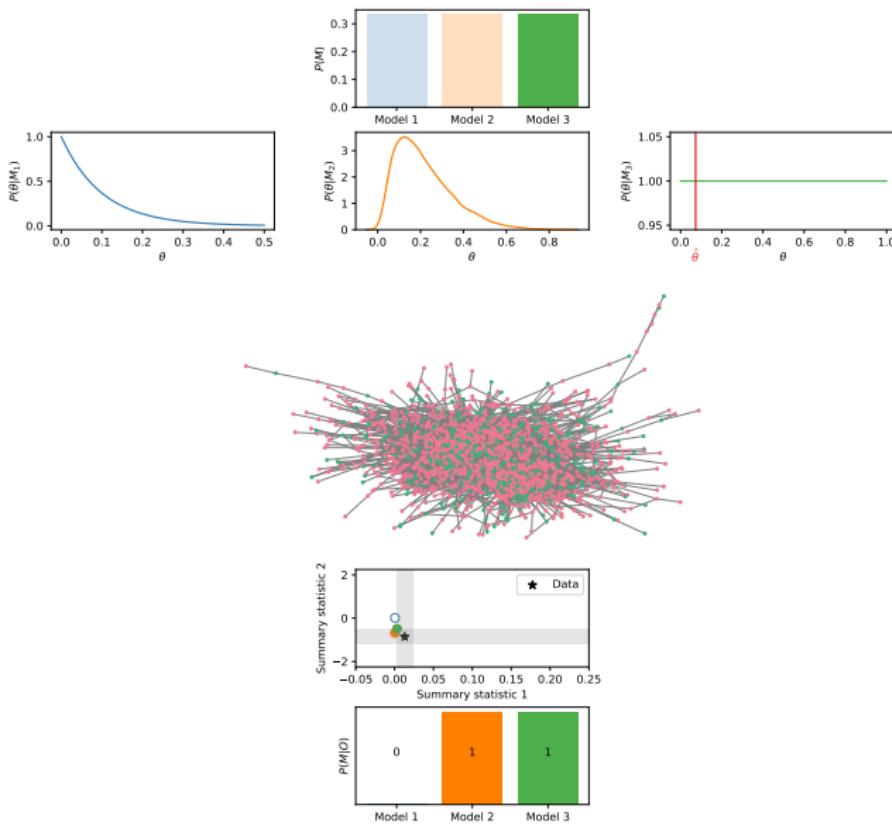
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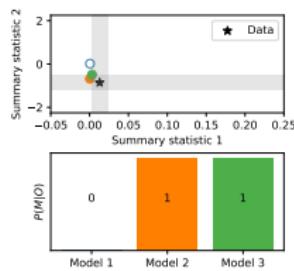
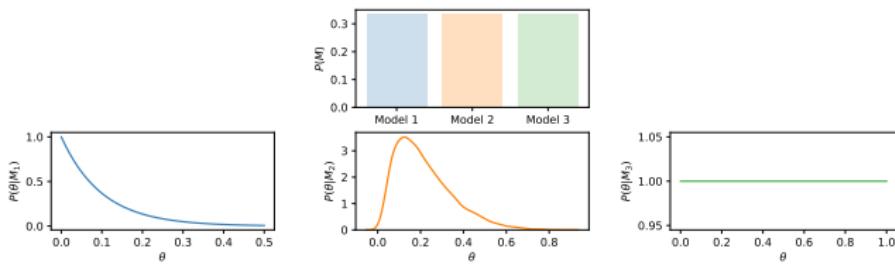
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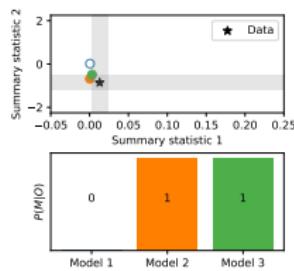
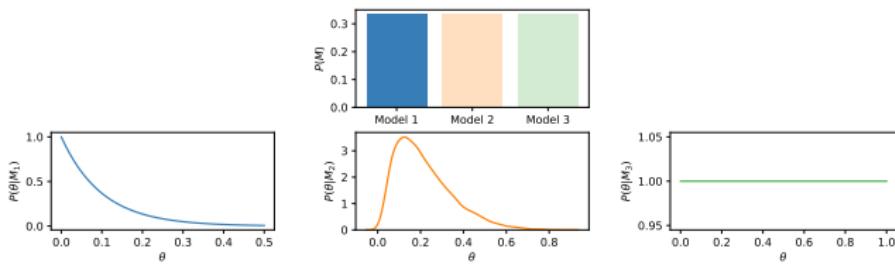
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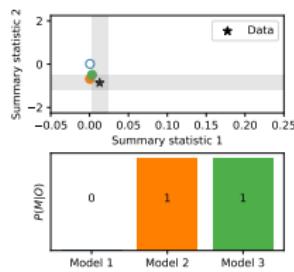
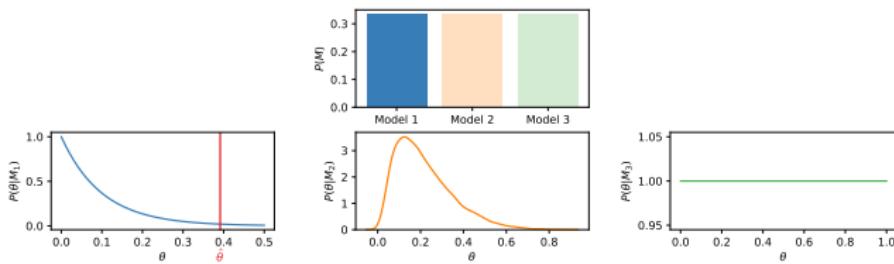
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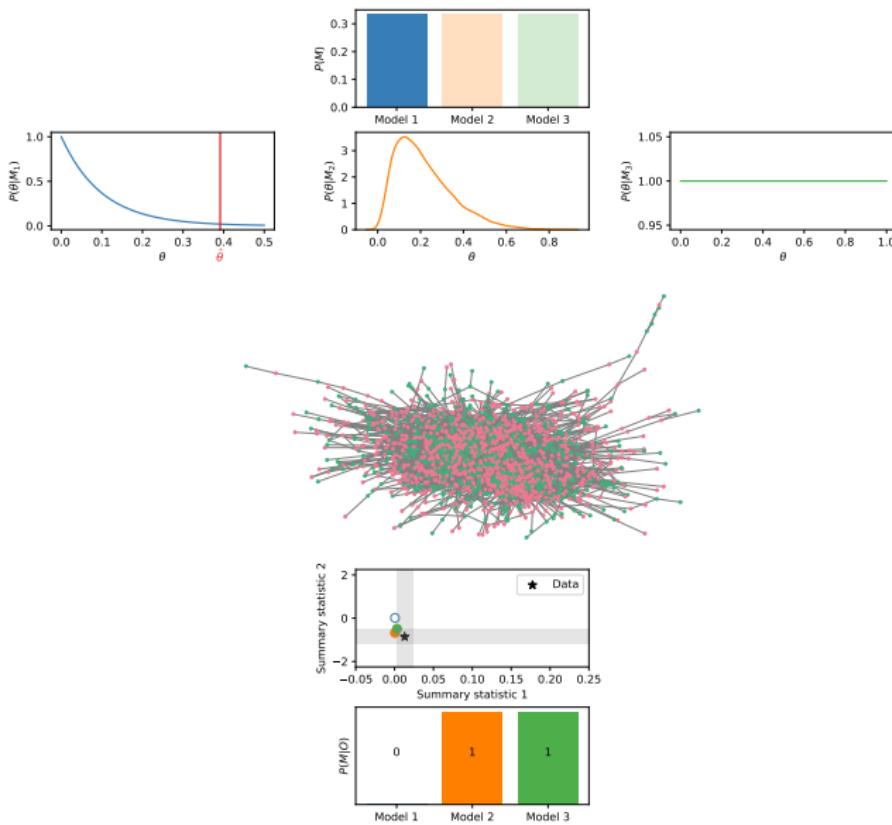
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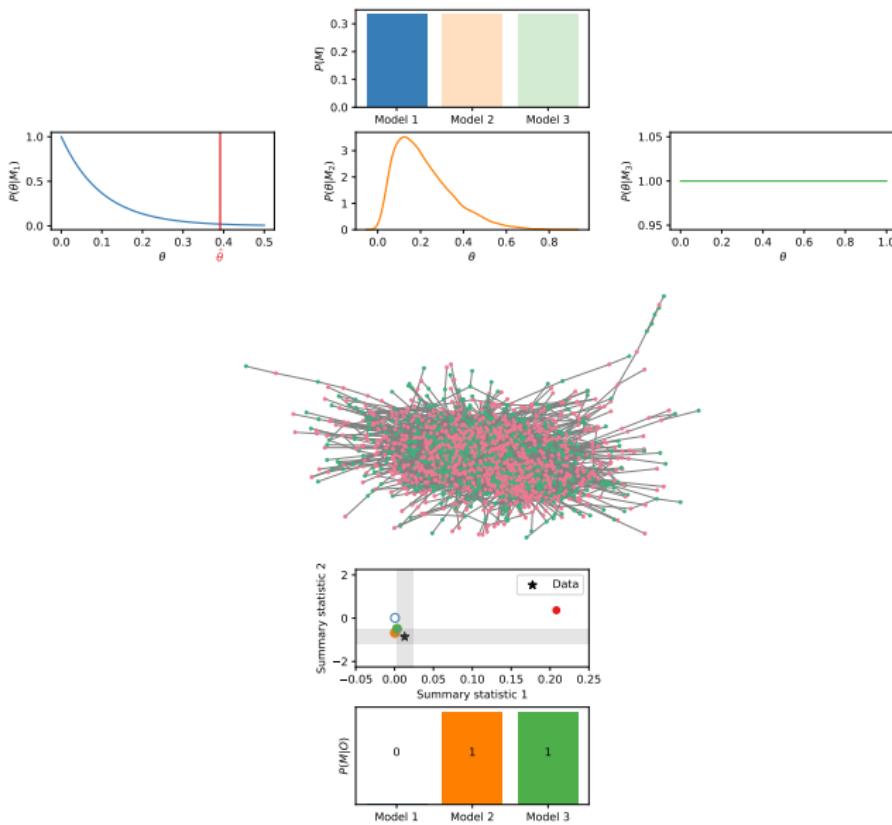
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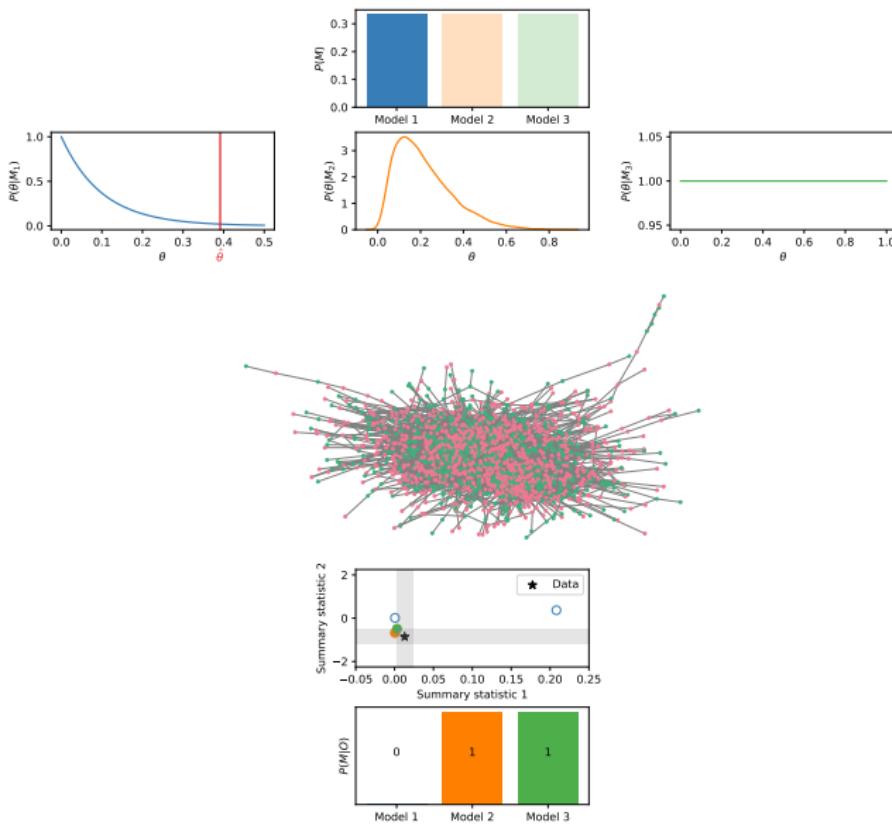
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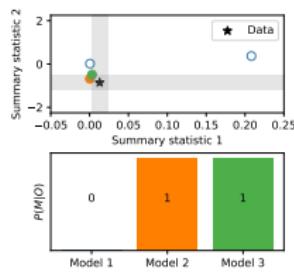
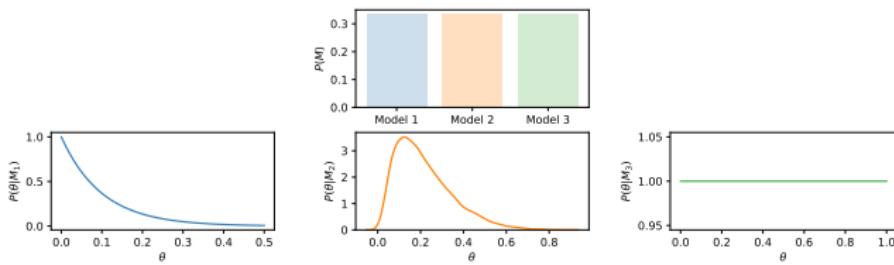
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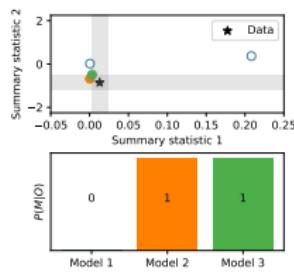
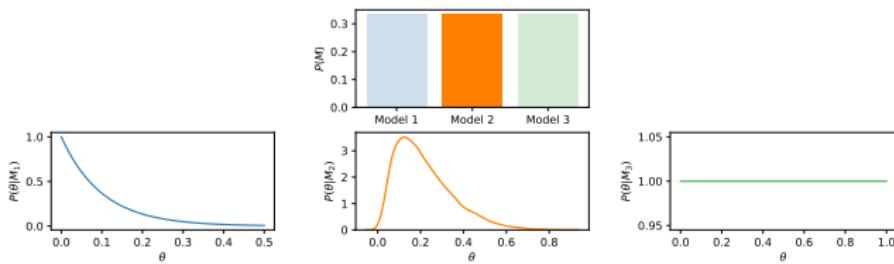
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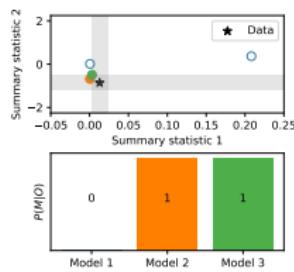
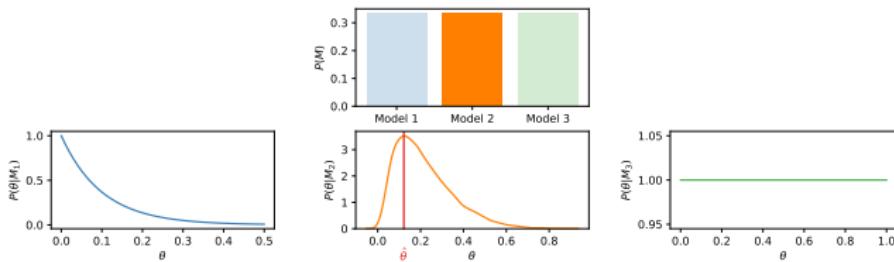
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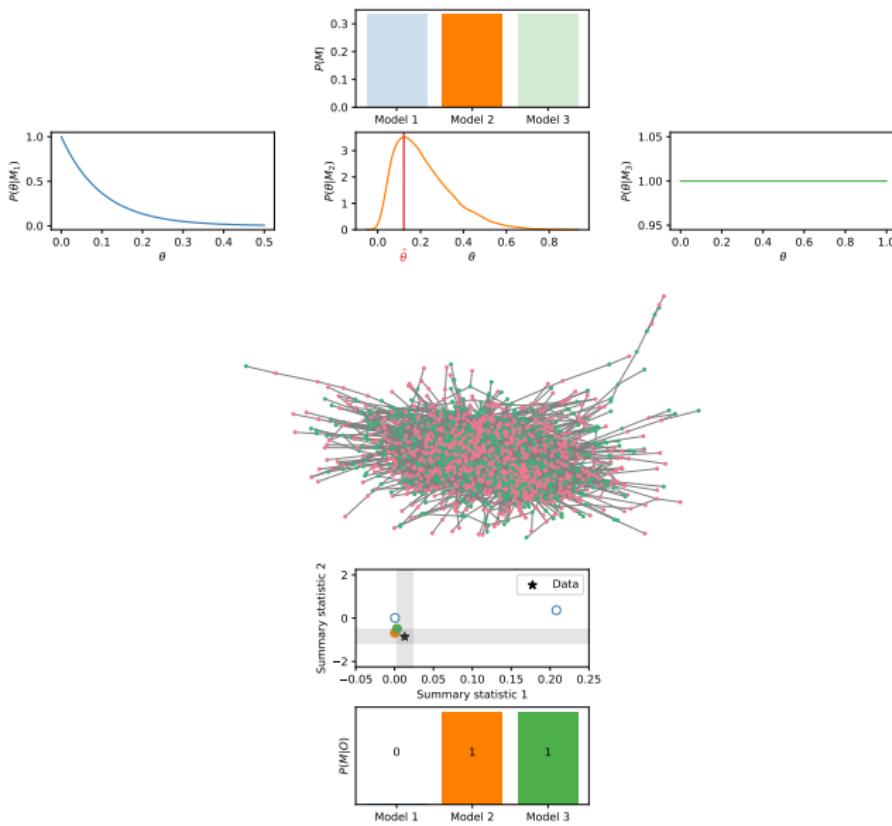
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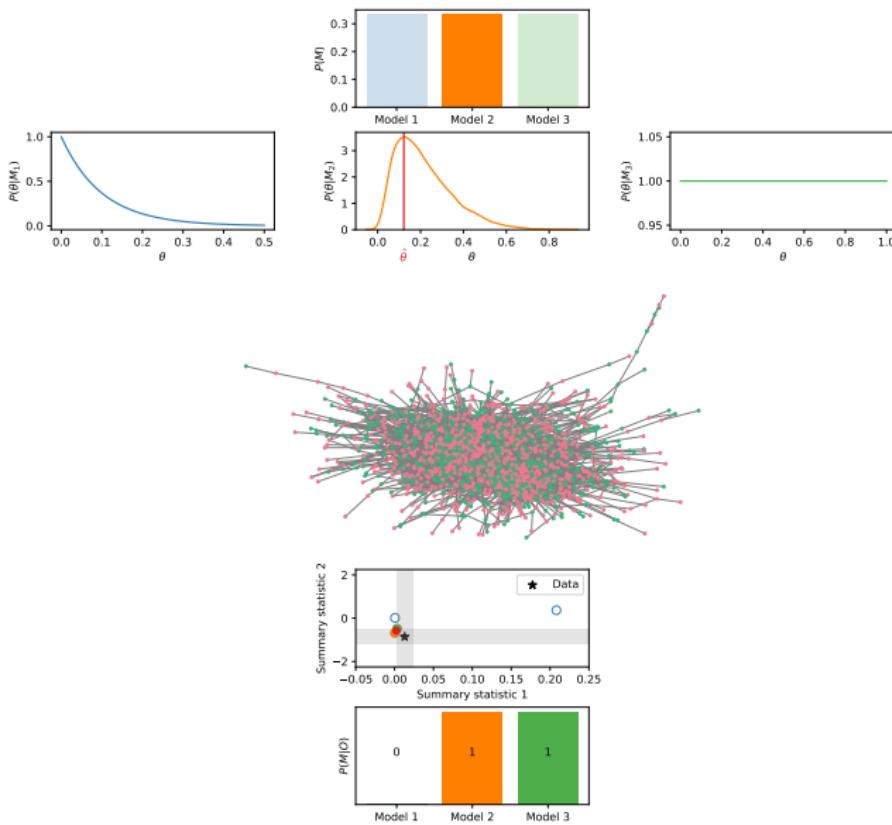
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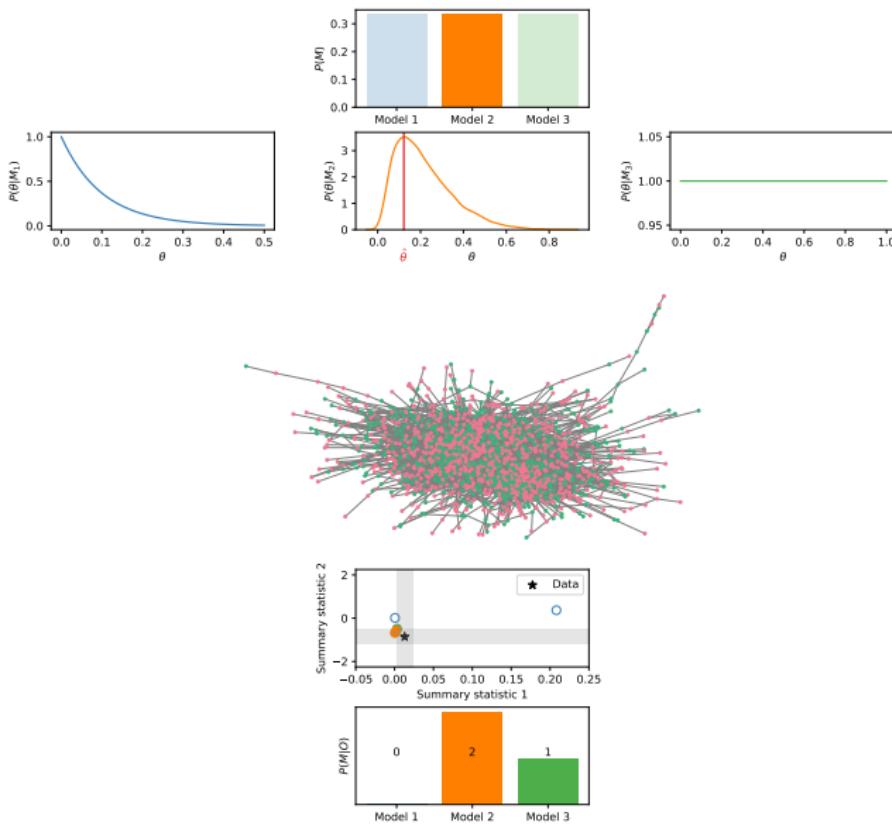
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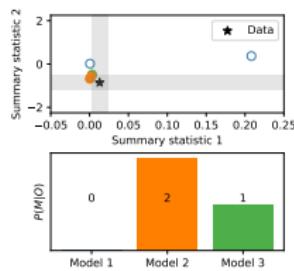
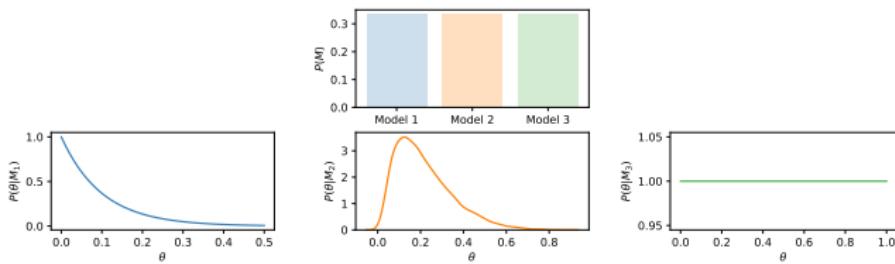
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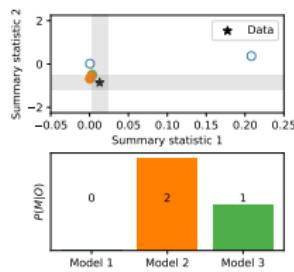
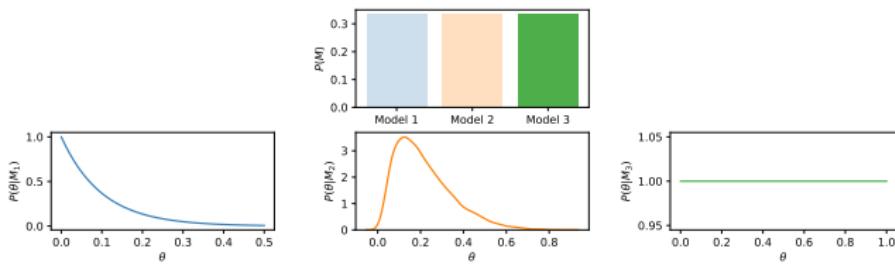
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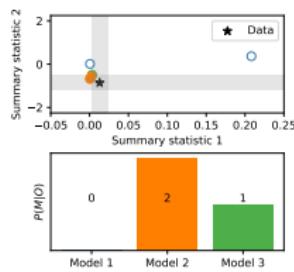
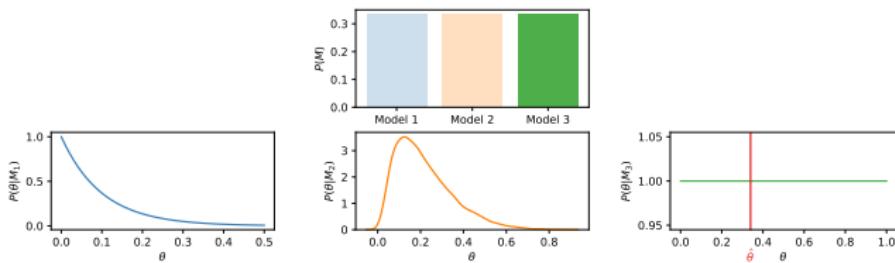
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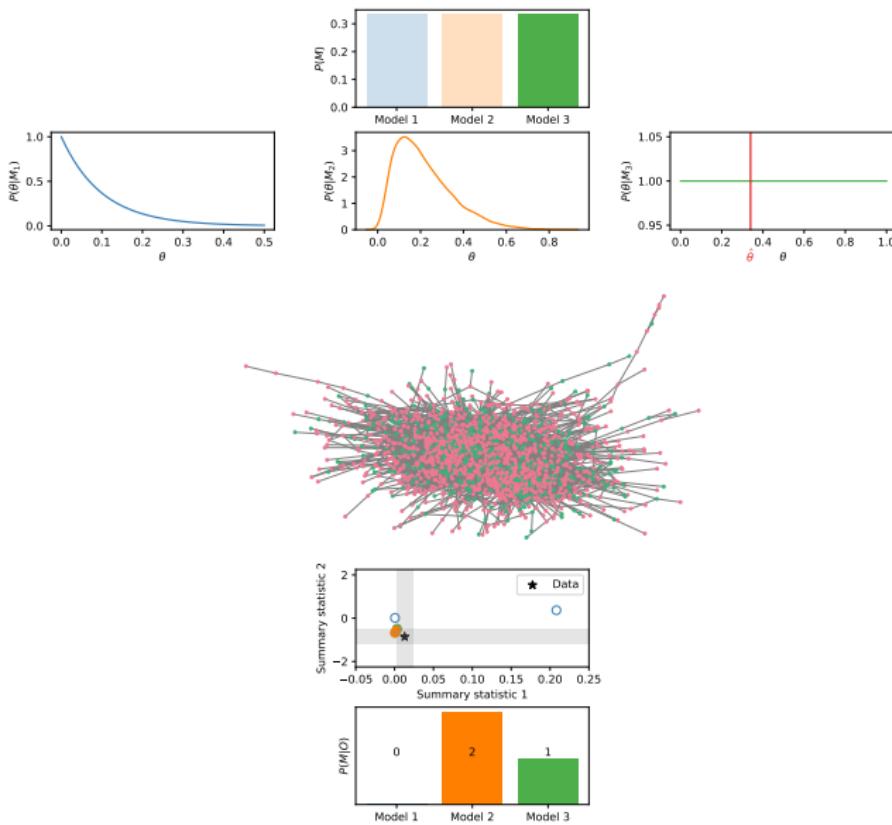
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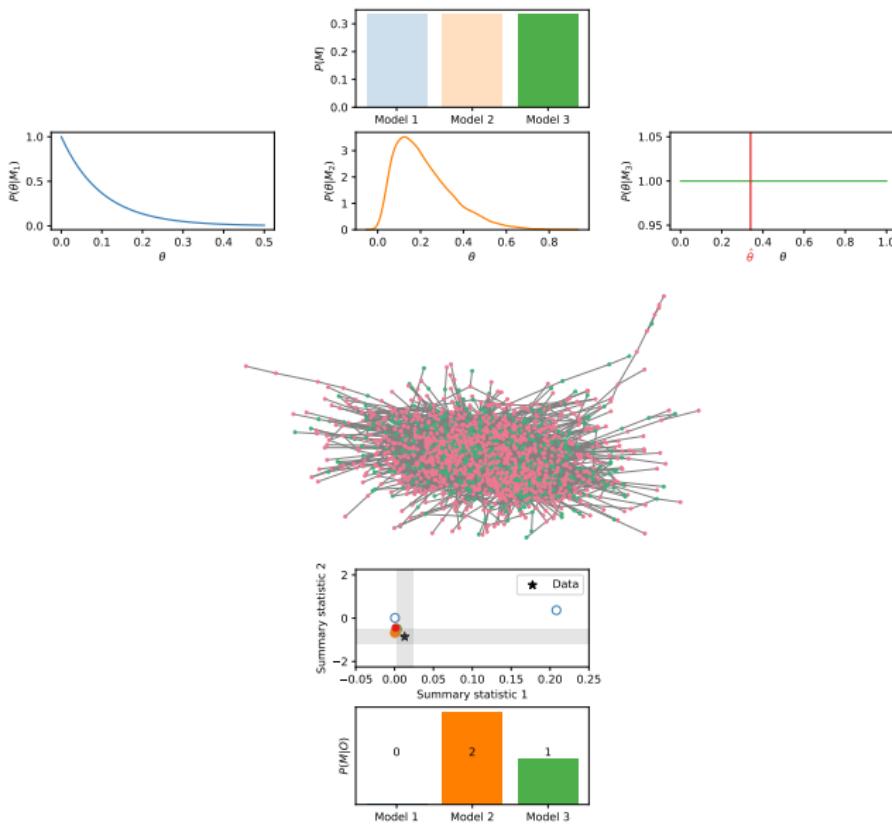
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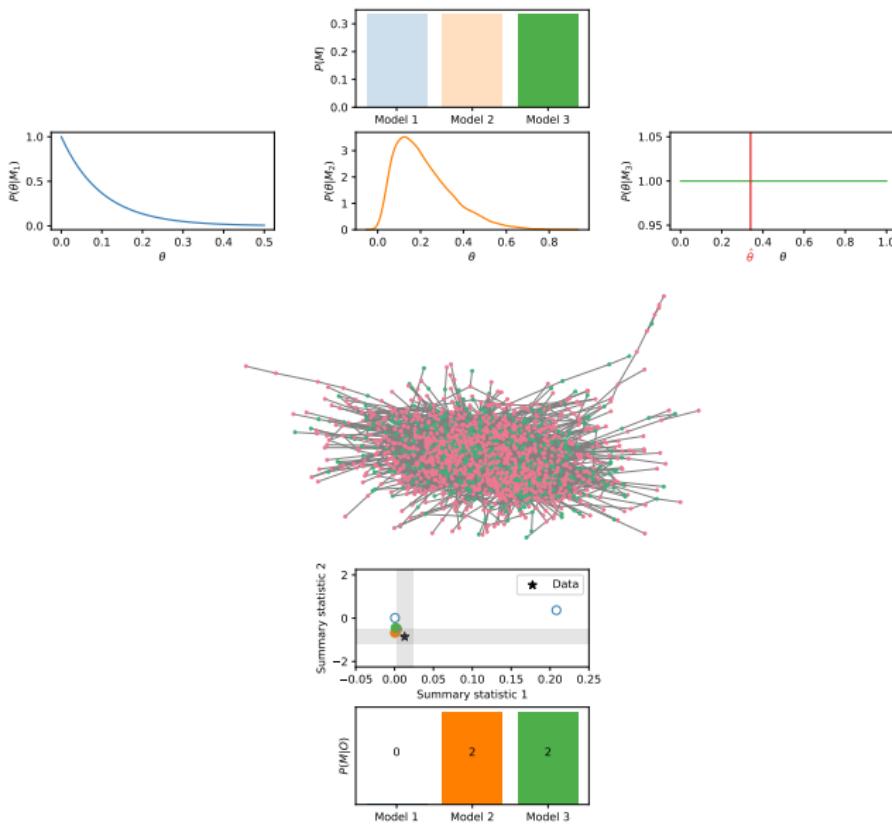
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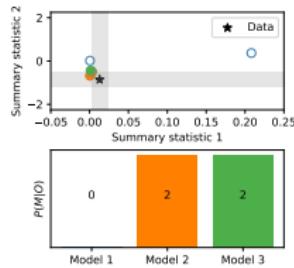
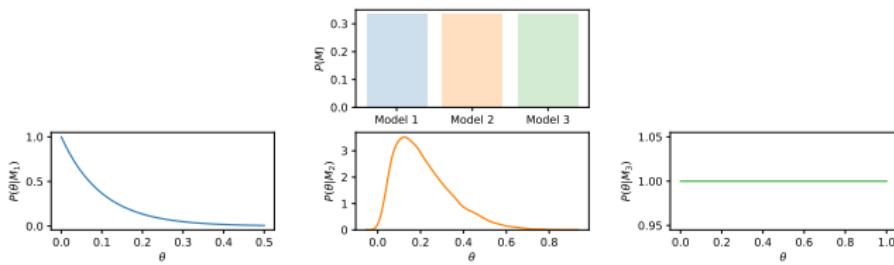
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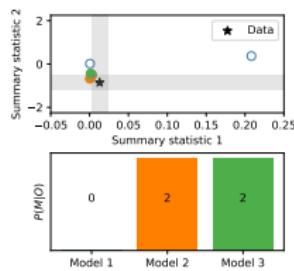
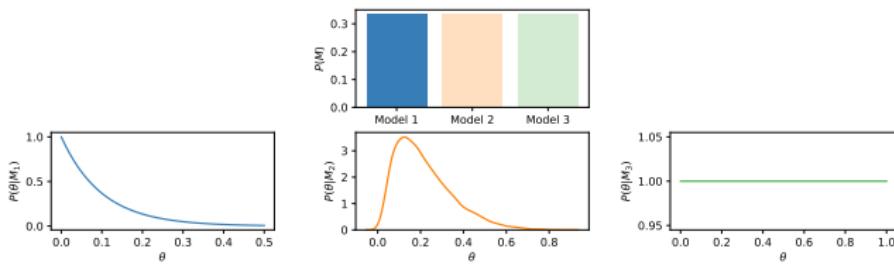
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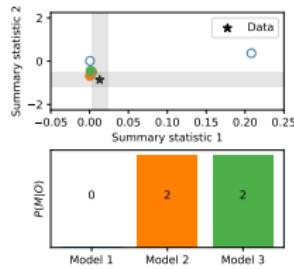
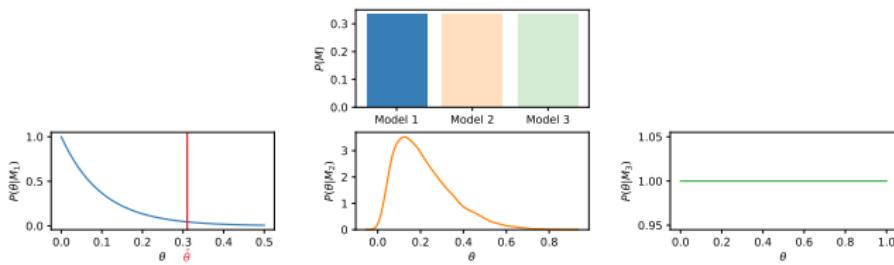
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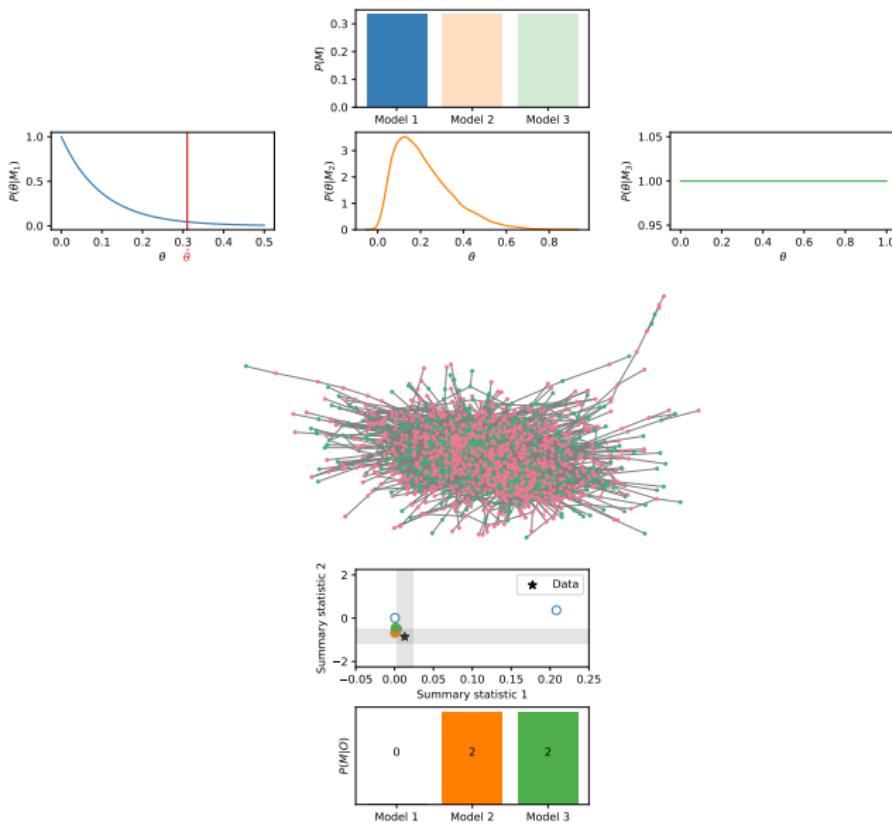
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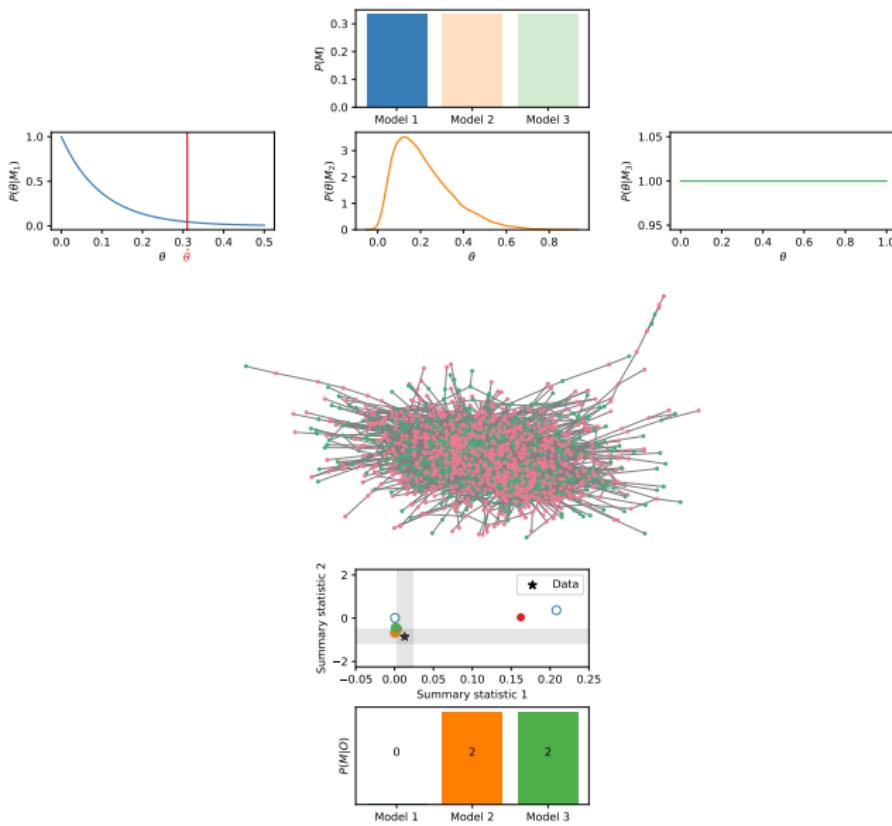
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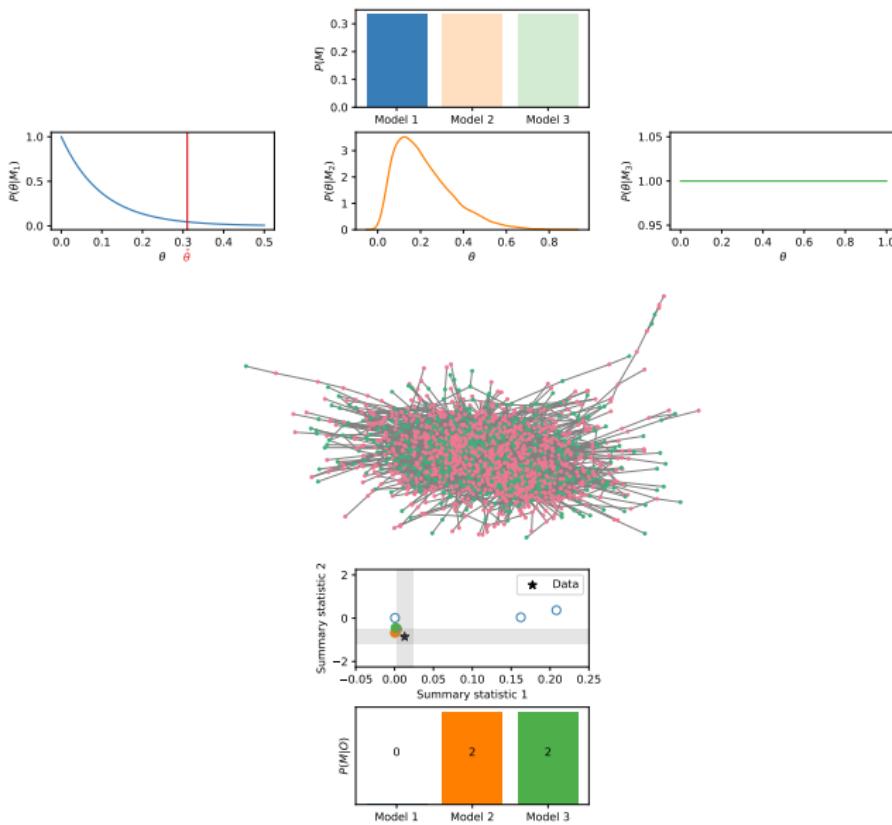
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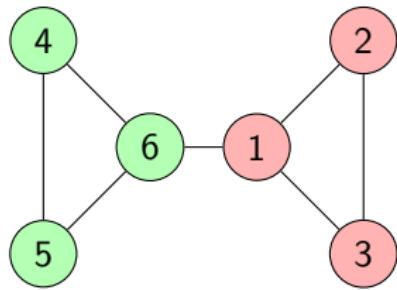
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# Simulation-based inference with summary statistics



# Local versus global mechanisms of coordination

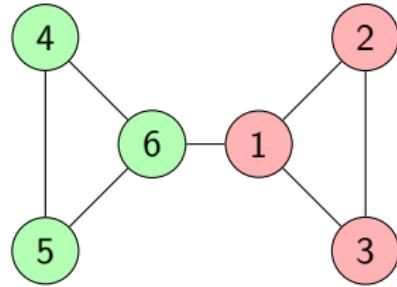


## Local coordination

Strategic alignment,  
imitation of peers...

J

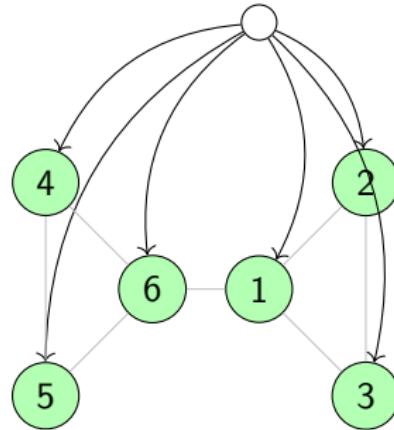
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*J*



## Global coordination

Adaptation to research purposes,  
or shared culture ("disciplinary matrix")

*B*

# The Ising model as an intermediate idealized model

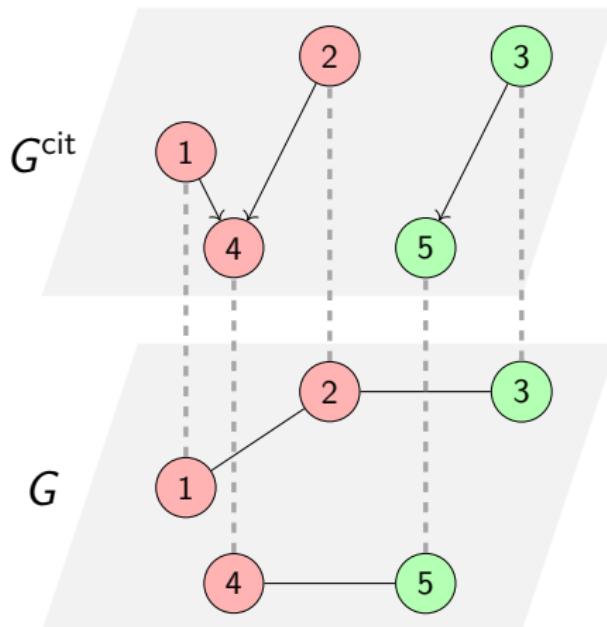
- Atomic magnetic spins in a material can be in two states:  $\uparrow (+1)$  or  $\downarrow (-1)$ .
- Magnetic spins prefer to be aligned to their neighbors ( $\uparrow\uparrow$  or  $\downarrow\downarrow$ )
- Can local interactions between spins at the microscopic level lead to macroscopic alignment?

$$P(\{\sigma_i\}|J, \mathbf{B}) = \frac{1}{Z(J, \mathbf{B})} e^{-H(\{\sigma_i\}, J, \mathbf{B})}, \text{ and } H = - \underbrace{\sum_{i,j} J w_{ij} \sigma_i \sigma_j}_{\text{local pairwise interactions}} - \underbrace{\sum_i B_{C_i} \sigma_i}_{\text{external magnetic field}} \quad (6)$$

<https://mattbierbaum.github.io/isng.js/>

Inverse Ising problem:  $P(J, J^{\text{cit}}, \mathbf{B} | \{\sigma_i\})$

# Local coordination in multi-layered graphs



**Figure: Illustration of local coordination in multilayered social networks.** Nodes can be connected through different kinds of relationships (for instance, authors can be related via collaborations ( $G$ ) or citations ( $G^{\text{cit}}$ )).

# Local versus global coordination

Table: Parameters of the Ising model.

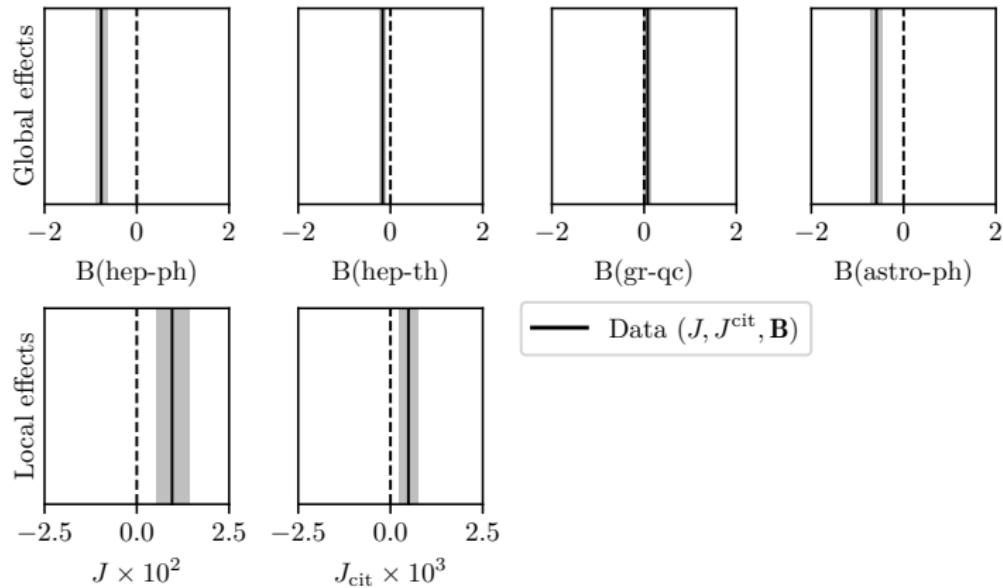
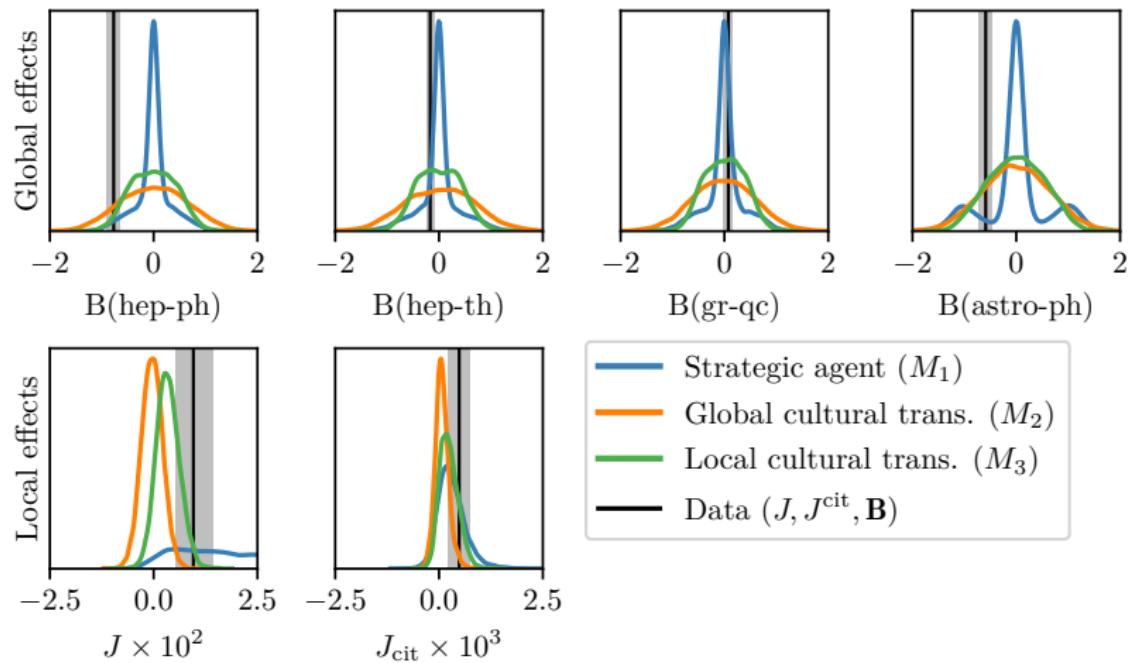


Figure: Ising model fit

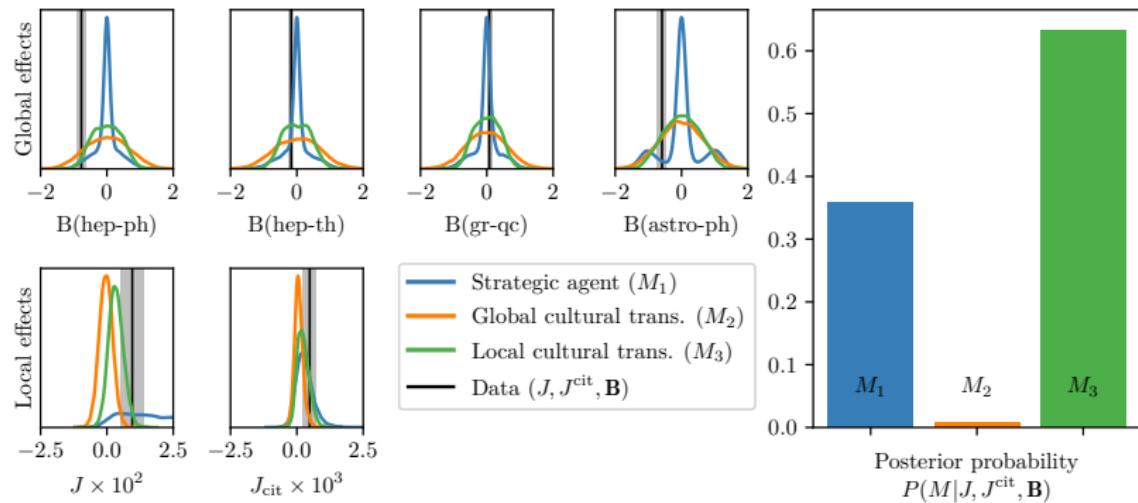
# Local versus global coordination

What values of  $\mathbf{J}$  and  $\mathbf{B}$  do our models predict? In other words, what is the probability  $P(\mathbf{J}, \mathbf{J}^{\text{cit}}, \mathbf{B} | M_i)$  for each model  $M_i$ ?



# Local versus global coordination

Given  $P(J, J^{\text{cit}}, \mathbf{B} | M_i)$ , and the true values of  $\mathbf{J}$  and  $\mathbf{B}$ , what is  $P(M_i | J, J^{\text{cit}}, \mathbf{B})$ ? After a bit of computational trickery – “amortized simulation-based model comparison with neural networks” with BayesFlow –:



# Challenges for model selection

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- Model misspecification: model comparison among highly incorrect models is challenging/meaningless
- Priors on models' parameter matter. A model is disadvantaged if it only is a good fit to the data for improbable parameter values.

# Summary: inverse problems in practice

- ① What **phenomenon**? (Belief-polarization? Discrimination and marginalization? etc.)
- ② What **models**? (“model-space”)
- ③ What **data**?
  - Accessibility (reasonable time/financial cost)
  - Quality (bias? ecological validity?)
  - Quantity (statistical significance)
- ④ What **computational strategies**?
  - **Pre-processing**: e.g. text-classification (natural language processing)?
  - **Inference** (inverse problem): simulation-based inference (with/without neural networks); Hamiltonian Monte-Carlo? Metropolis?

# Thank you! I

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# Amortized simulation-based inference

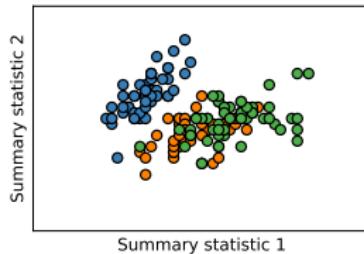
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  - Use amortized inference with neural networks  $\Rightarrow$  train a neuralnet to predict the probability of each model  $M_i$  given one or more observed outcomes. The neuralnet is trained with many simulated training samples  $(M_s, O_s)$  (Radev et al., 2021)

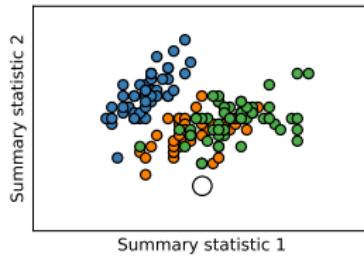
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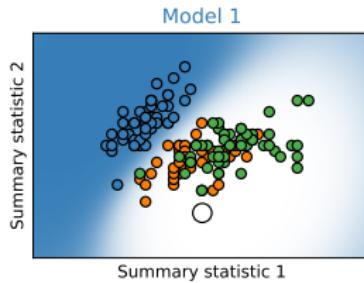
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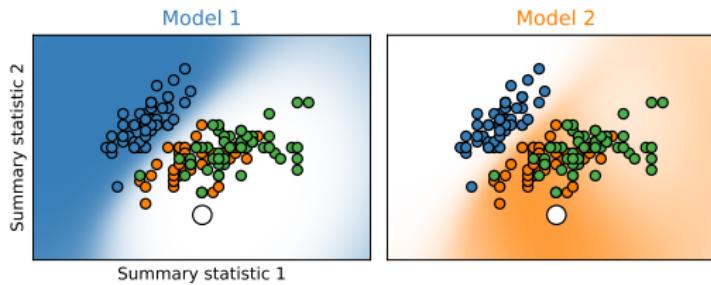
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