

Imitation Learning & Behavioral Cloning

Lucas Janson

**CS/Stat 184(0): Introduction to Reinforcement Learning
Fall 2024**

Today

- Feedback from last lecture
- Recap
- Imitation Learning problem statement
- Behavioral Cloning
- DAgger

Feedback from feedback forms

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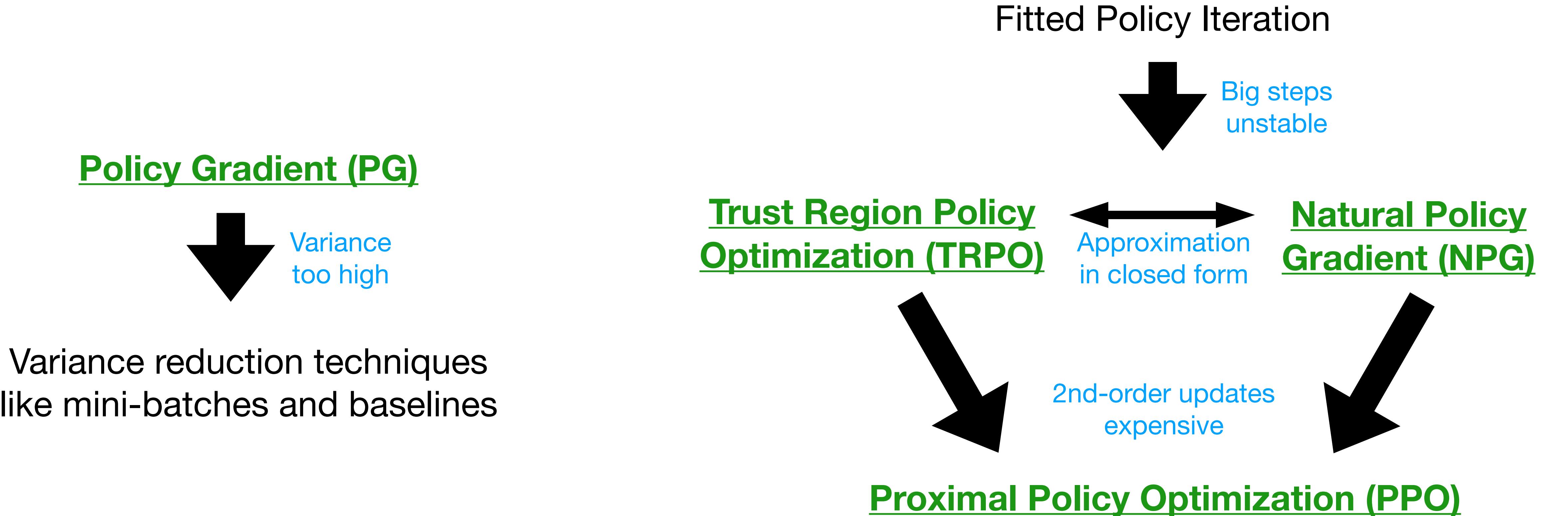
1. Thank you to everyone who filled out the forms!

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All Policy Gradient Algorithms in One Slide

Parameterize policy and optimize directly while sampling from MDP



PPO gets 2nd-order optimization benefits over PG and 1st-order computation benefits over TRPO/NPG

“Lack of Exploration” leads to Optimization and Statistical Challenges



- Suppose $H \approx \text{poly}(|S|)$ & $\mu(s_0) = 1$ (i.e. we start at s_0).
- A randomly initialized policy π^0 has prob. $O(1/3^{|S|})$ of hitting the goal state in a trajectory.
- Thus a sample-based approach, with $\mu(s_0) = 1$, require $O(3^{|S|})$ trajectories.
 - Holds for (sample based) Fitted DP
 - Holds for (sample based) PG/TRPO/NPG/PPO
- Basically, for these approaches, there is no hope of learning the optimal policy if $\mu(s_0) = 1$.

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Why not do one trajectory that always moves right?

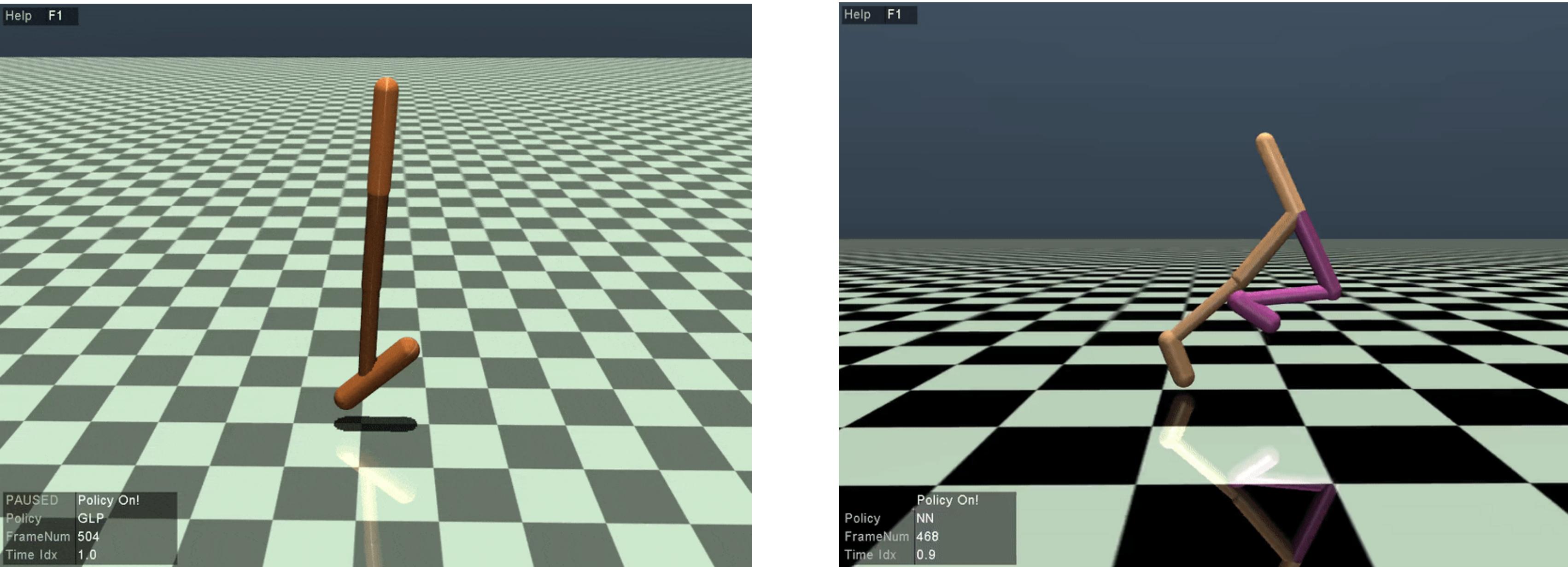
Let's examine the role of μ



Thrun '92

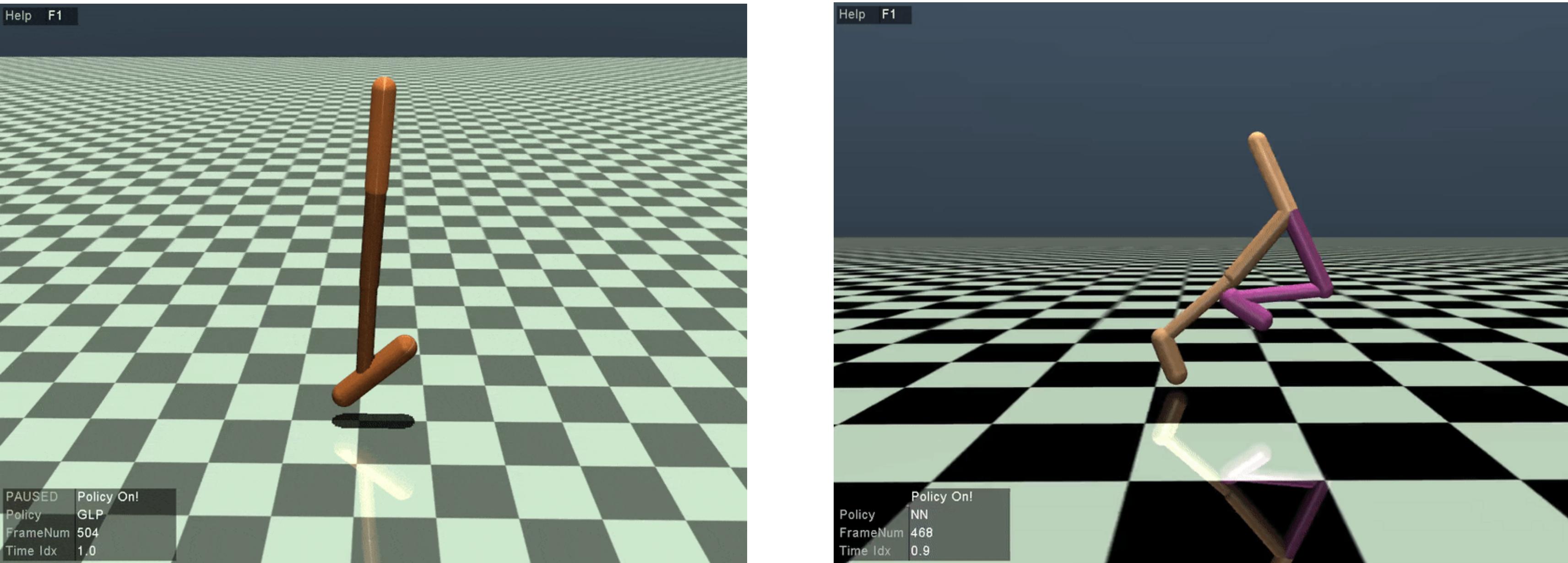
- Suppose that somehow the distribution μ had better coverage.
 - e.g, if μ was uniform overall states in our toy problem, then all approaches we covered would work (with mild assumptions)
 - Theory: TRPO/NPG/PPO have better guarantees than fitted DP methods (assuming some “coverage”)
- Strategies without coverage:
 - If we have a simulator, sometimes we can design μ to have better coverage.
 - this is helpful for robustness as well.
 - Imitation learning (next time).
 - An expert gives us samples from a “good” μ .
 - Explicit exploration:
 - UCB-VI: we'll merge two good ideas!
 - Encourage exploration in PG methods.
 - Try with reward shaping

Aside: Brittle policies if we train starting from only from one configuration!



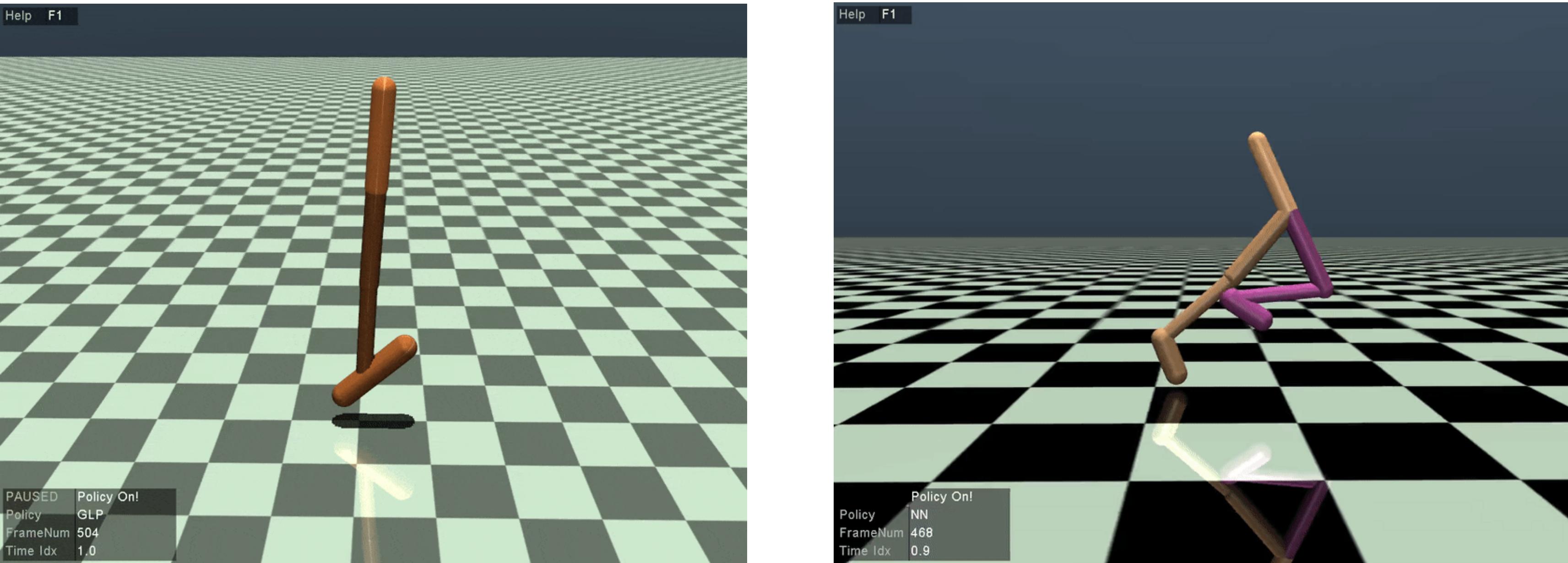
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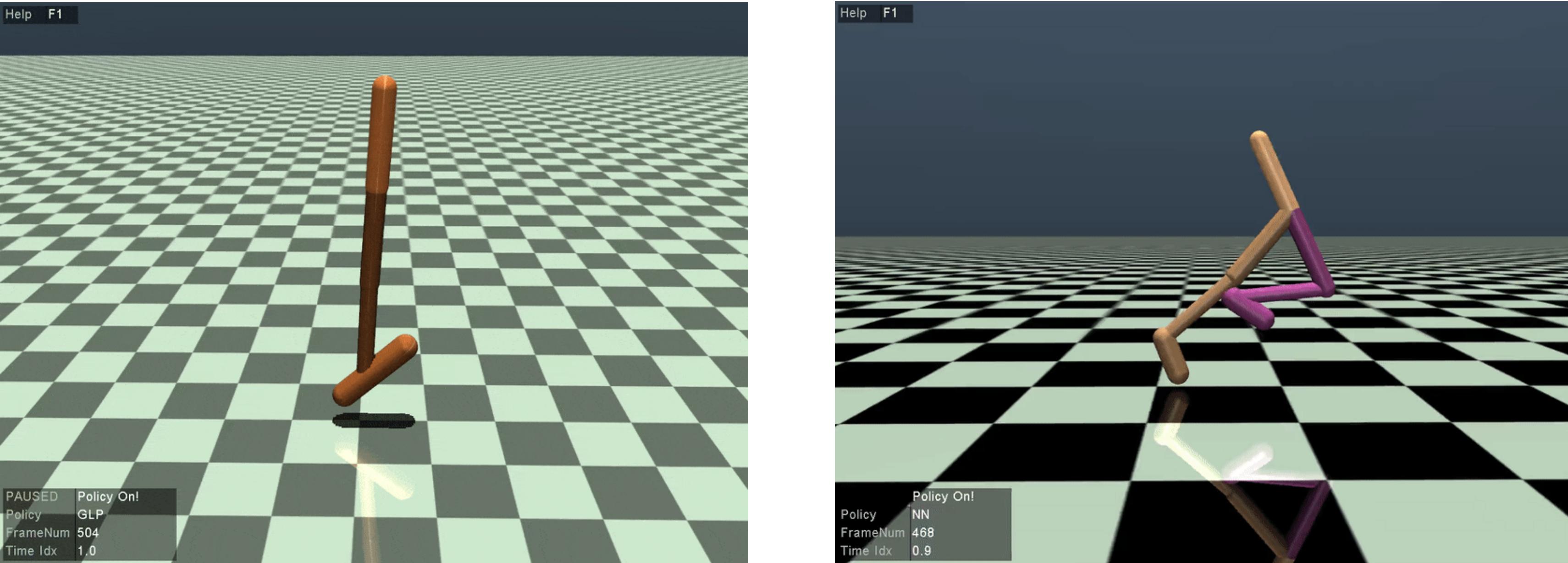
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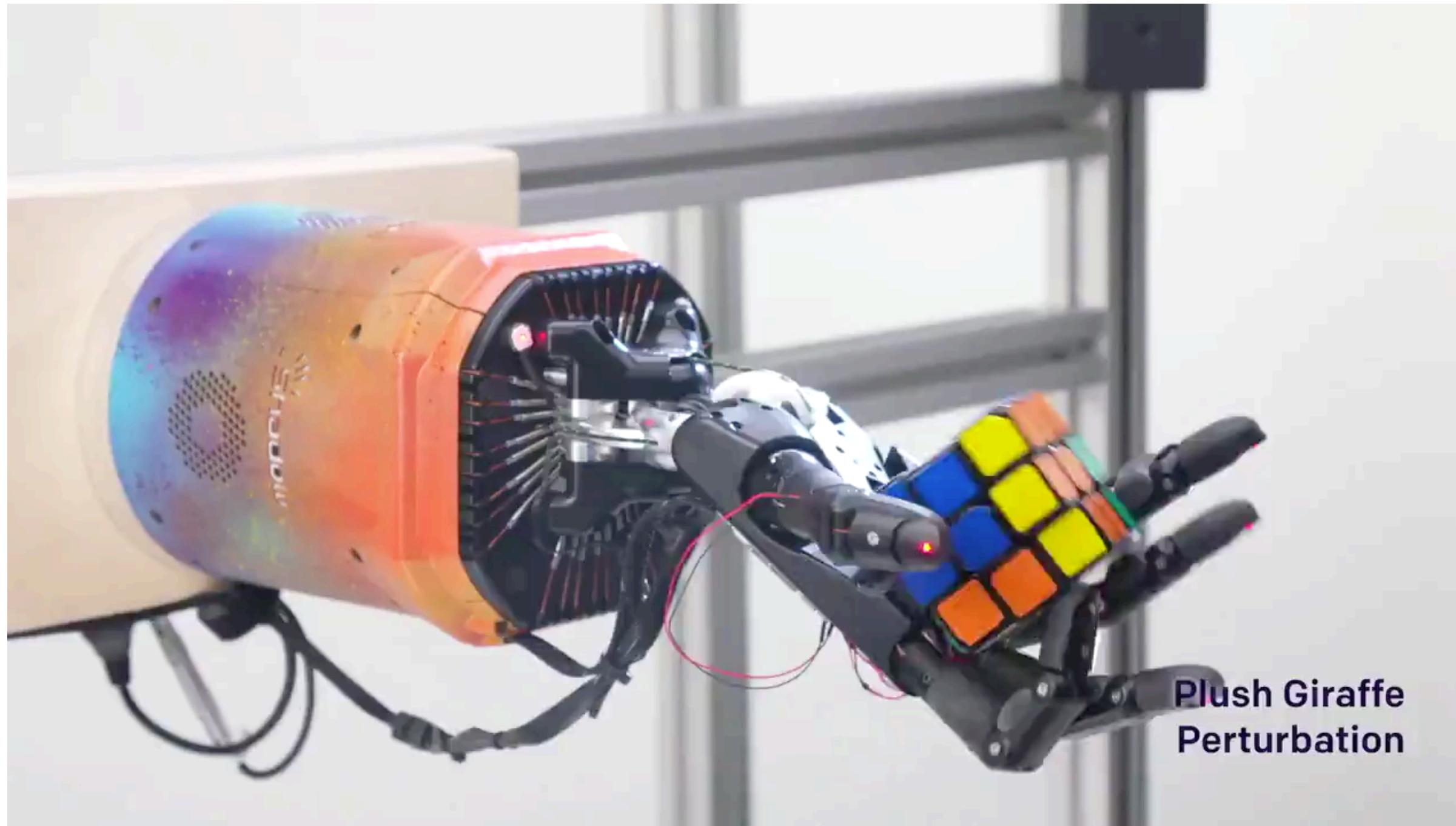
- [Rajeswaran, Lowrey, Todorov, K. 2017]: showed policies optimized for a single starting configuration s_0 are not robust!
- How to fix this?
 - Training from different starting configurations sampled from $s_0 \sim \mu$ fixes this:

$$\max_{\theta} \mathbb{E}_{s_0 \sim \mu}[V^\theta(s_0)]$$

Even if starting position concentrated at just one point—good for robustness!

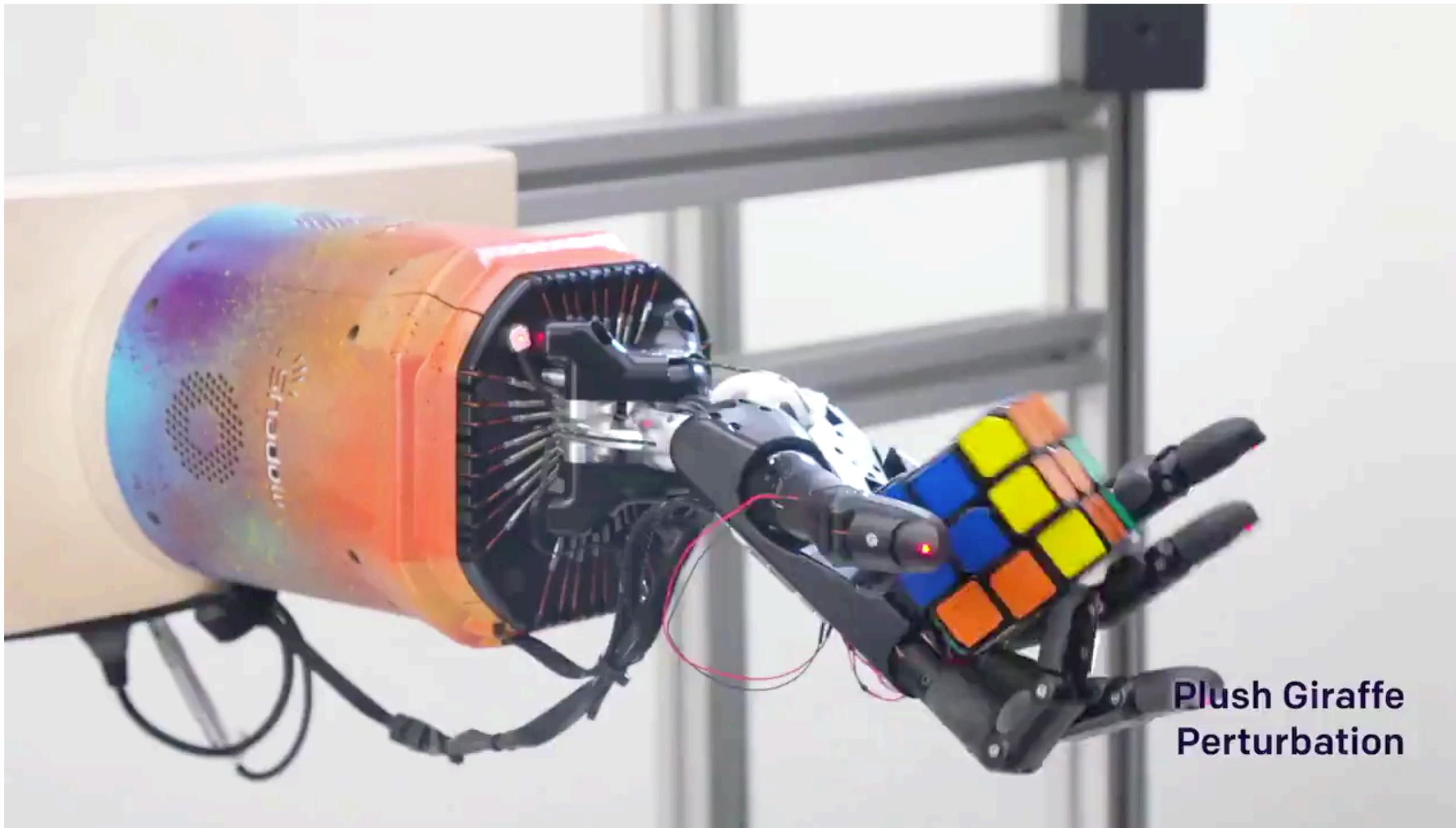
OpenAI: progress on dexterous hand manipulation

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Plush Giraffe
Perturbation

OpenAI: progress on dexterous hand manipulation



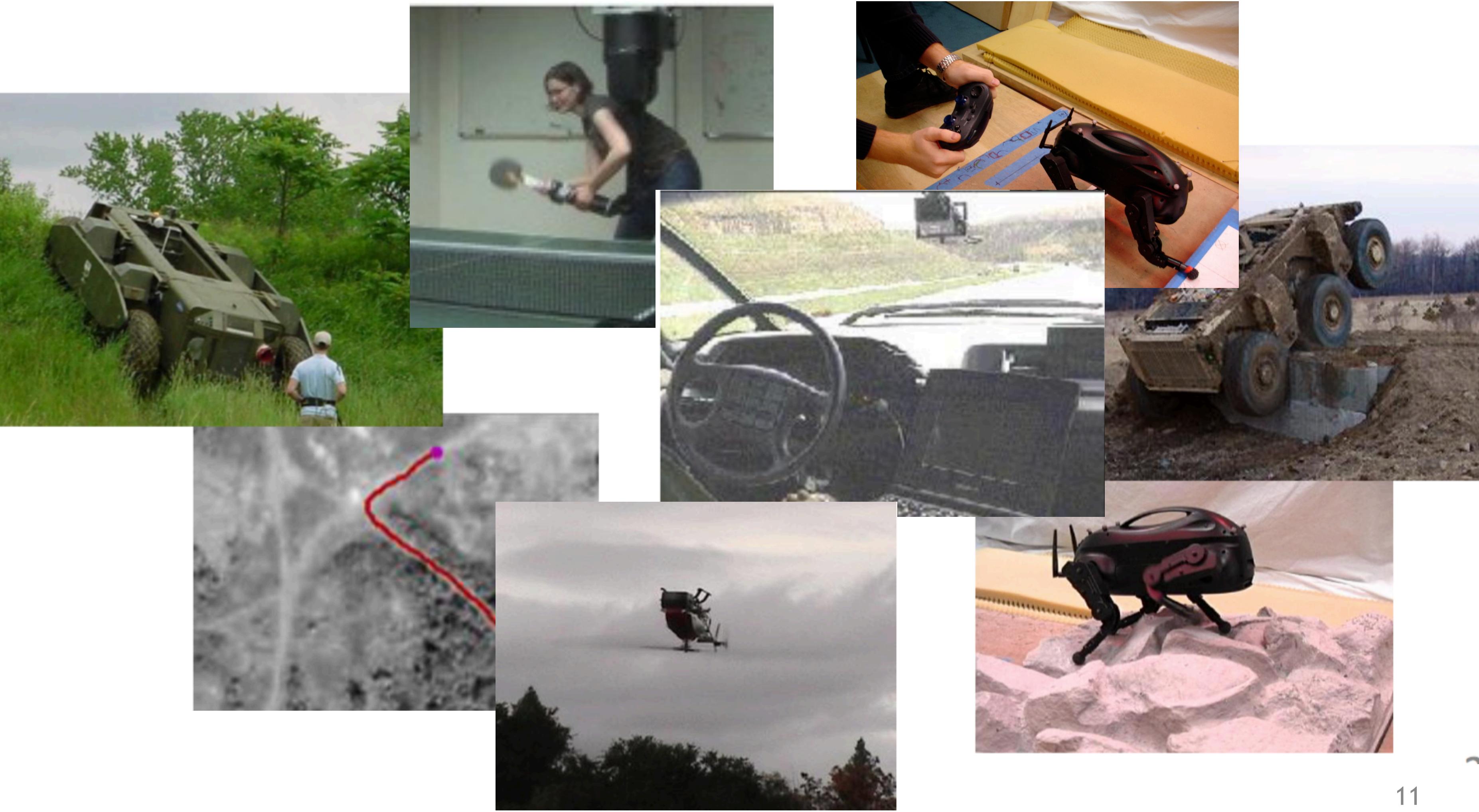
Trained with “domain randomization”

Basically, the measure $s_0 \sim \mu$ was diverse.

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Imitation Learning



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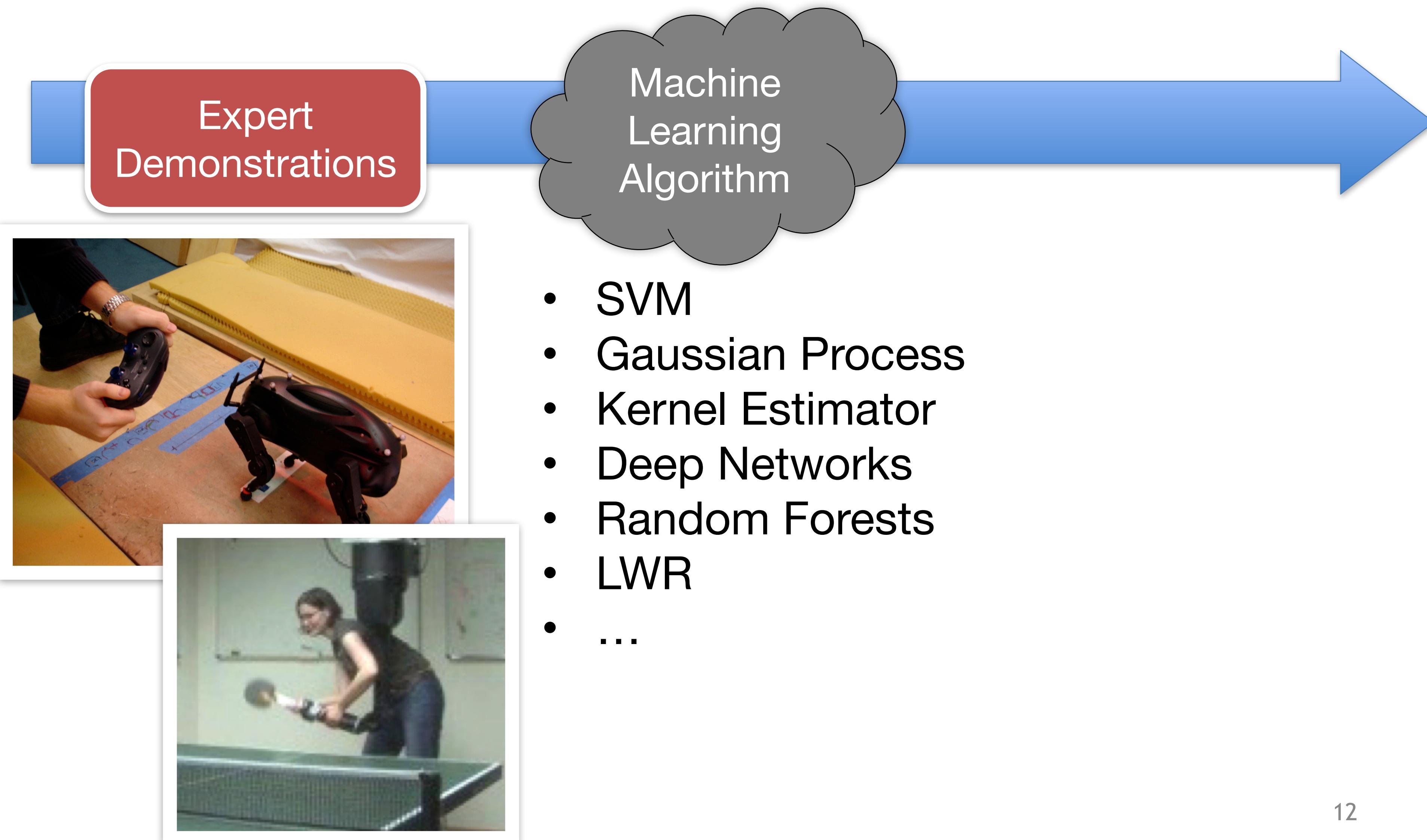


Imitation Learning

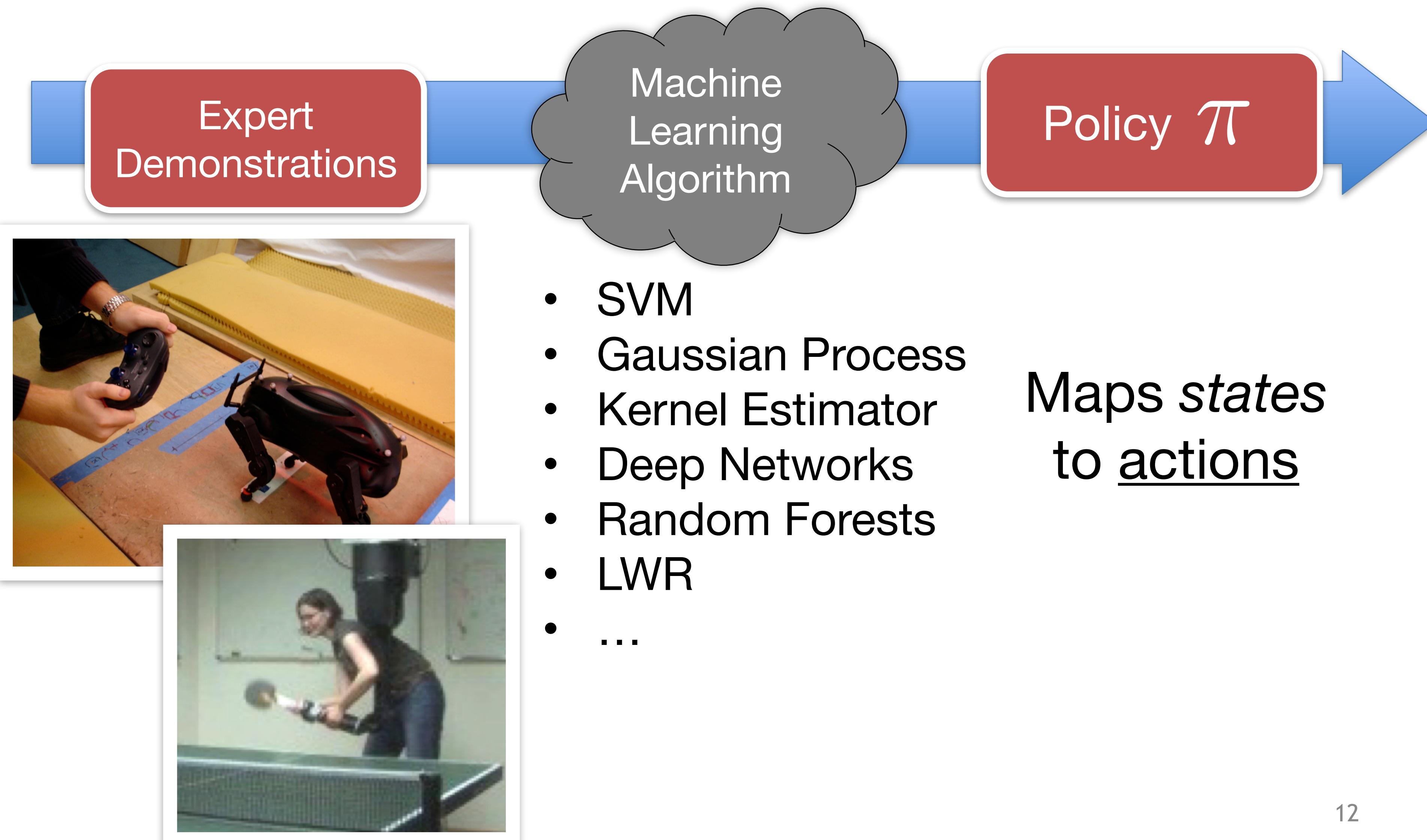
Expert
Demonstrations



Imitation Learning



Imitation Learning



Learning to Drive by Imitation

[Pomerleau89, Saxena05, Ross11a]

Input:



Camera Image

Output:



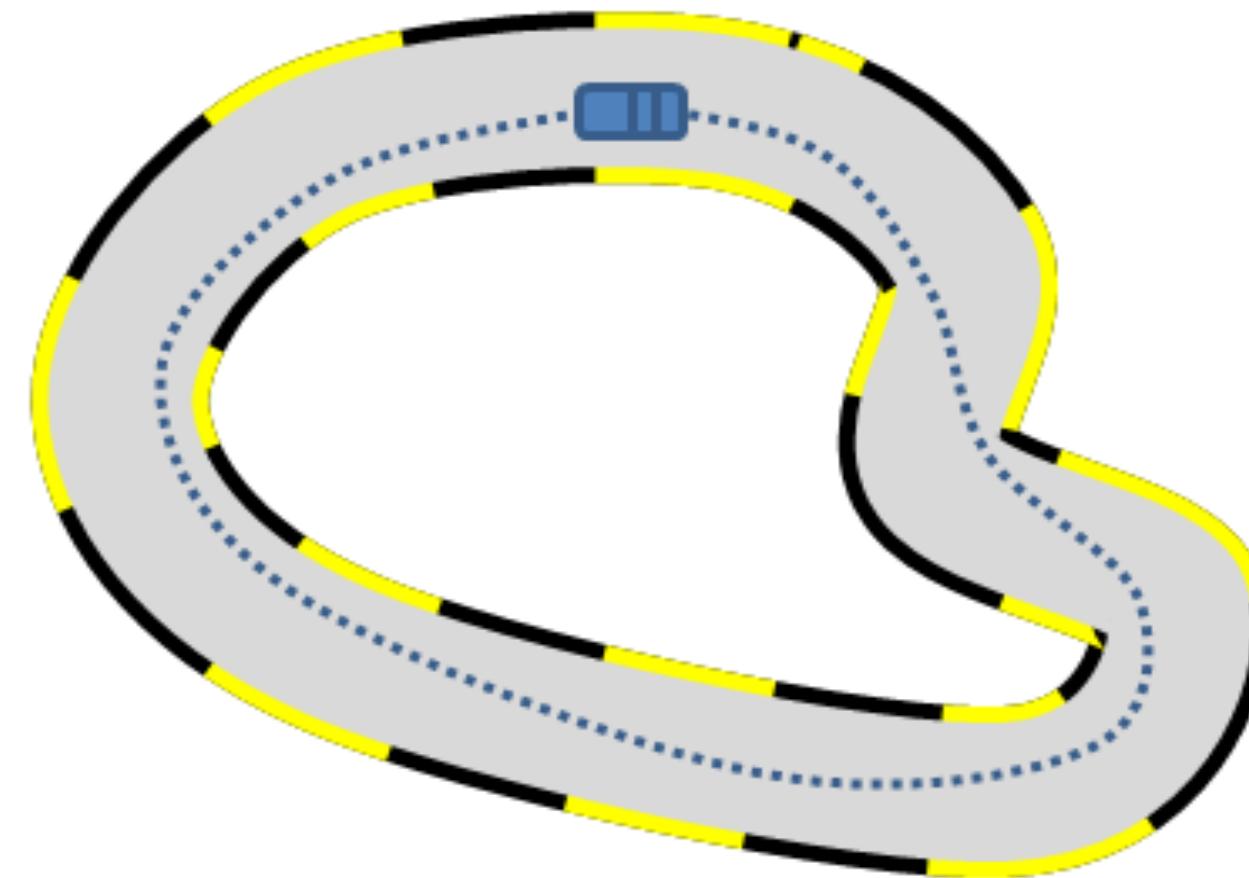
Steering Angle
in $[-1, 1]$

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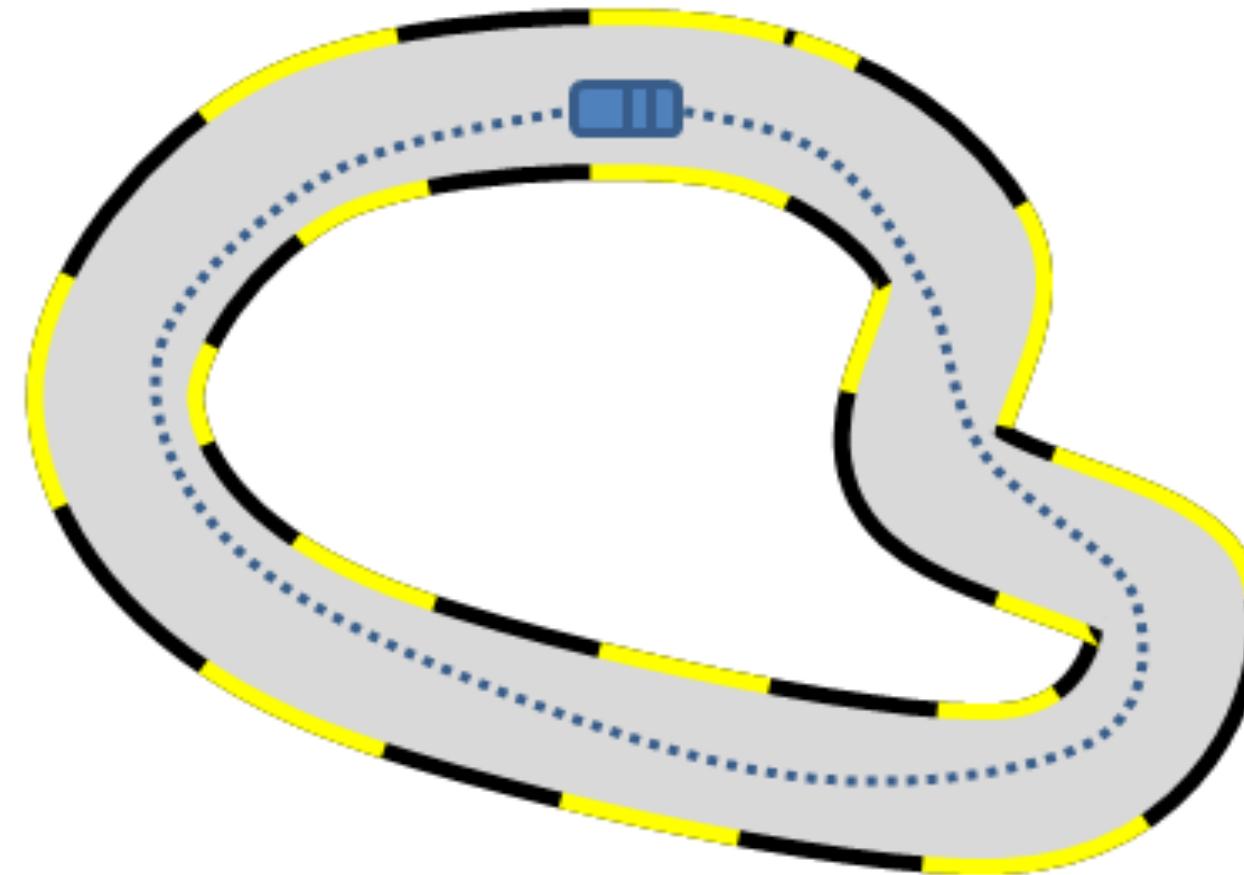
Supervised Learning Approach: Behavior Cloning

Expert Trajectories

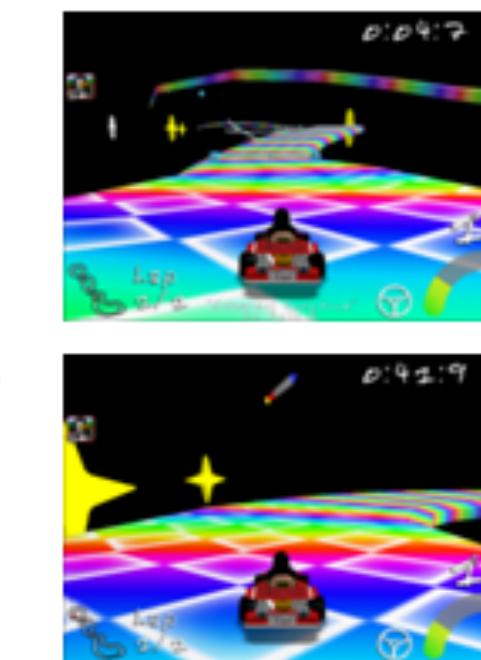


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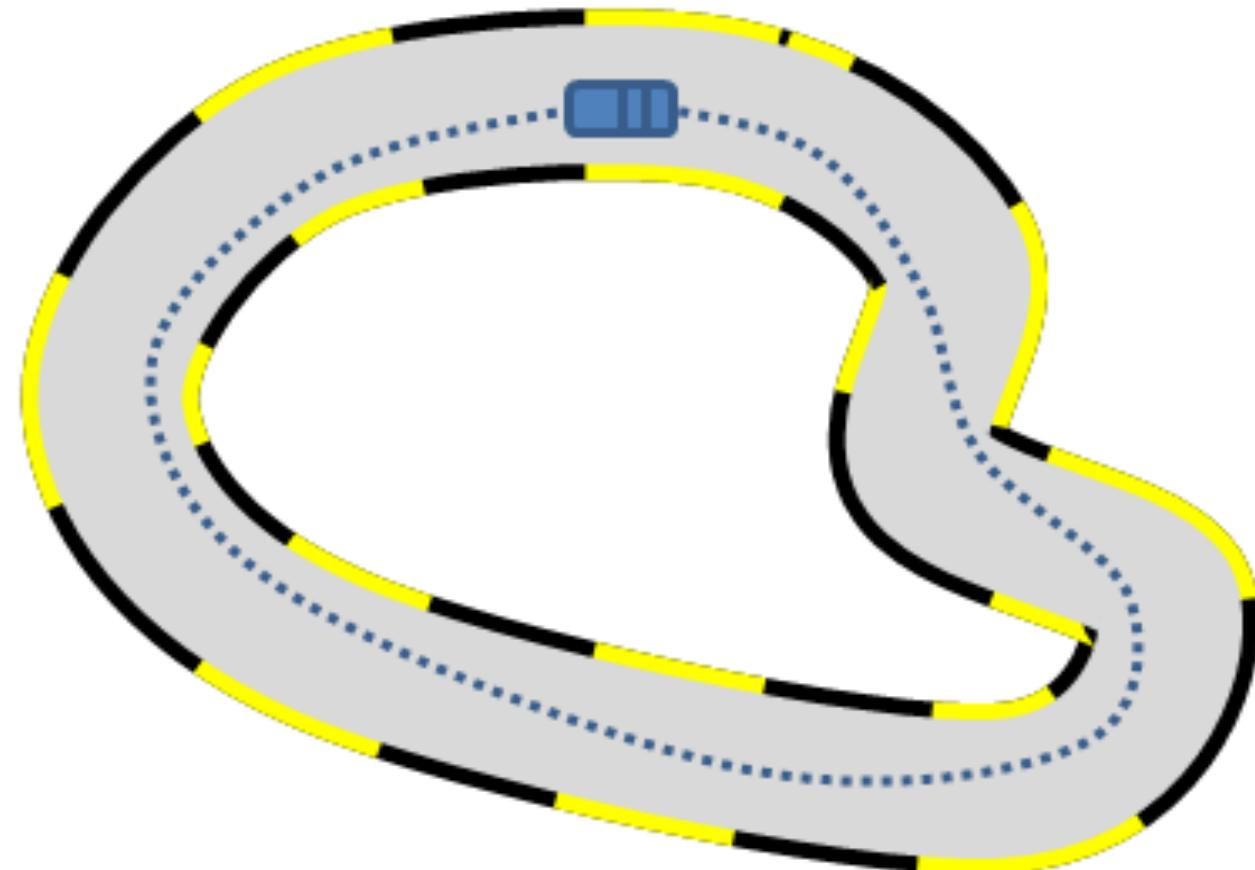
Dataset



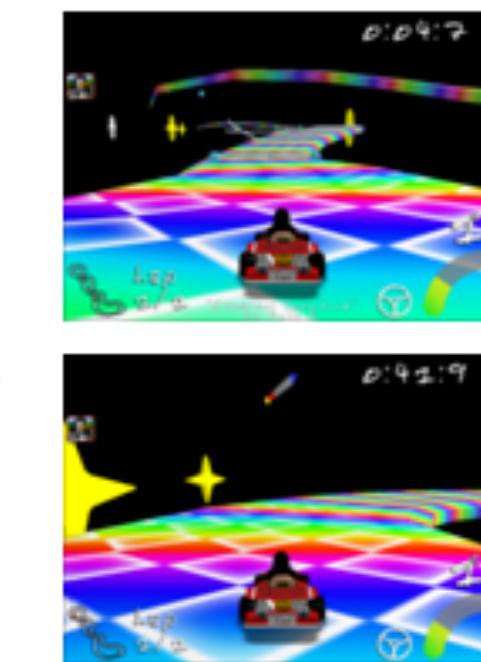
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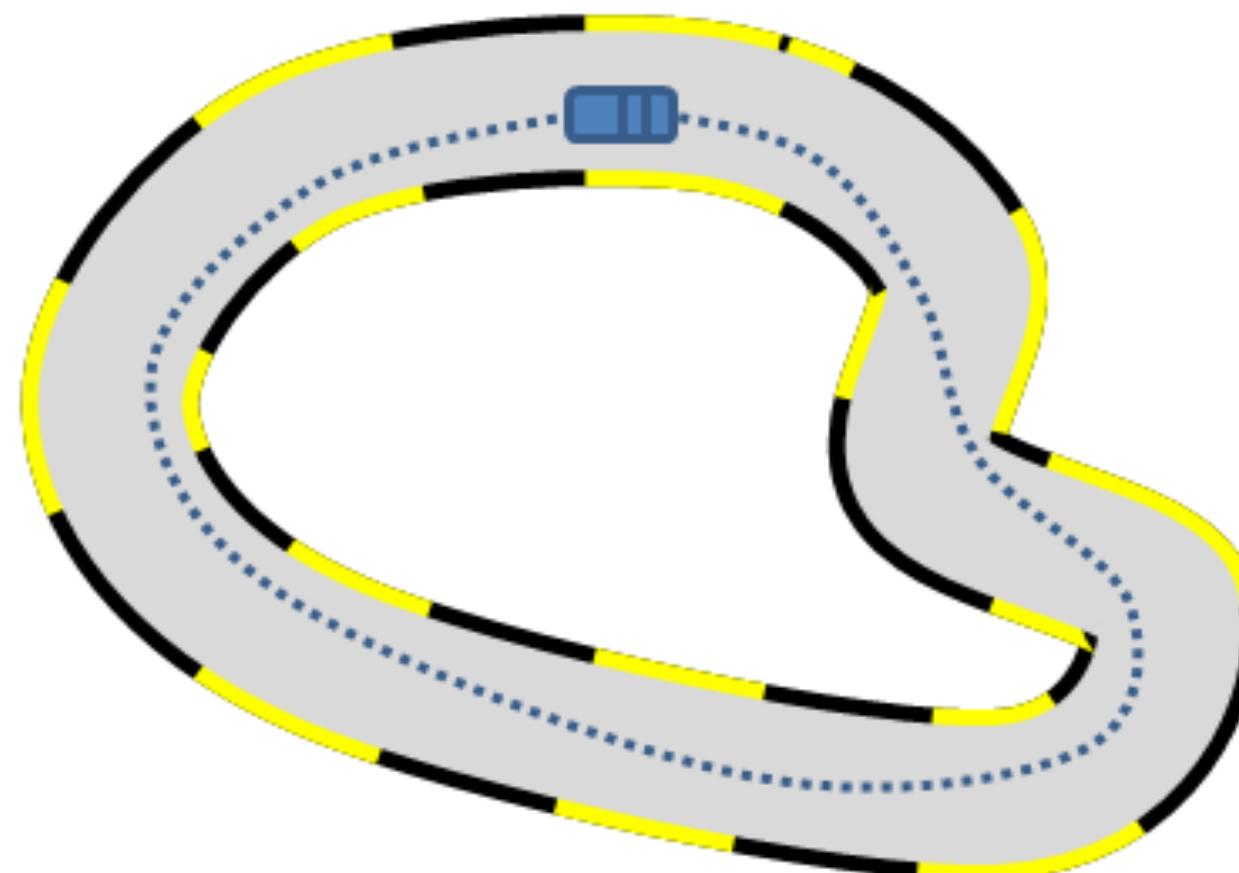


$X : Y$

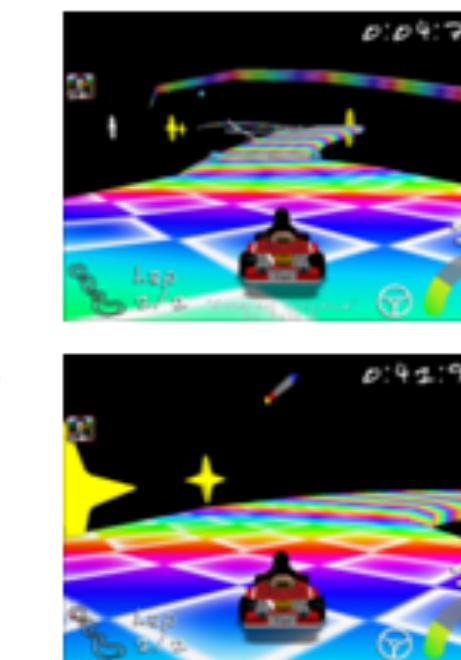
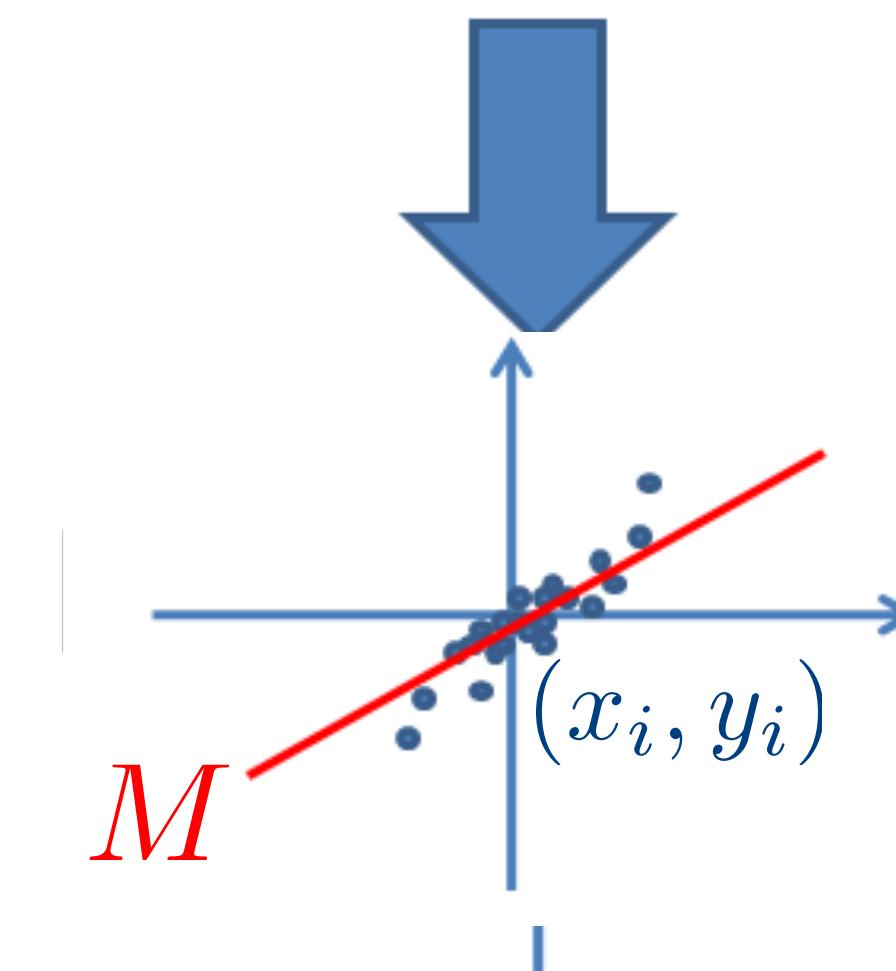


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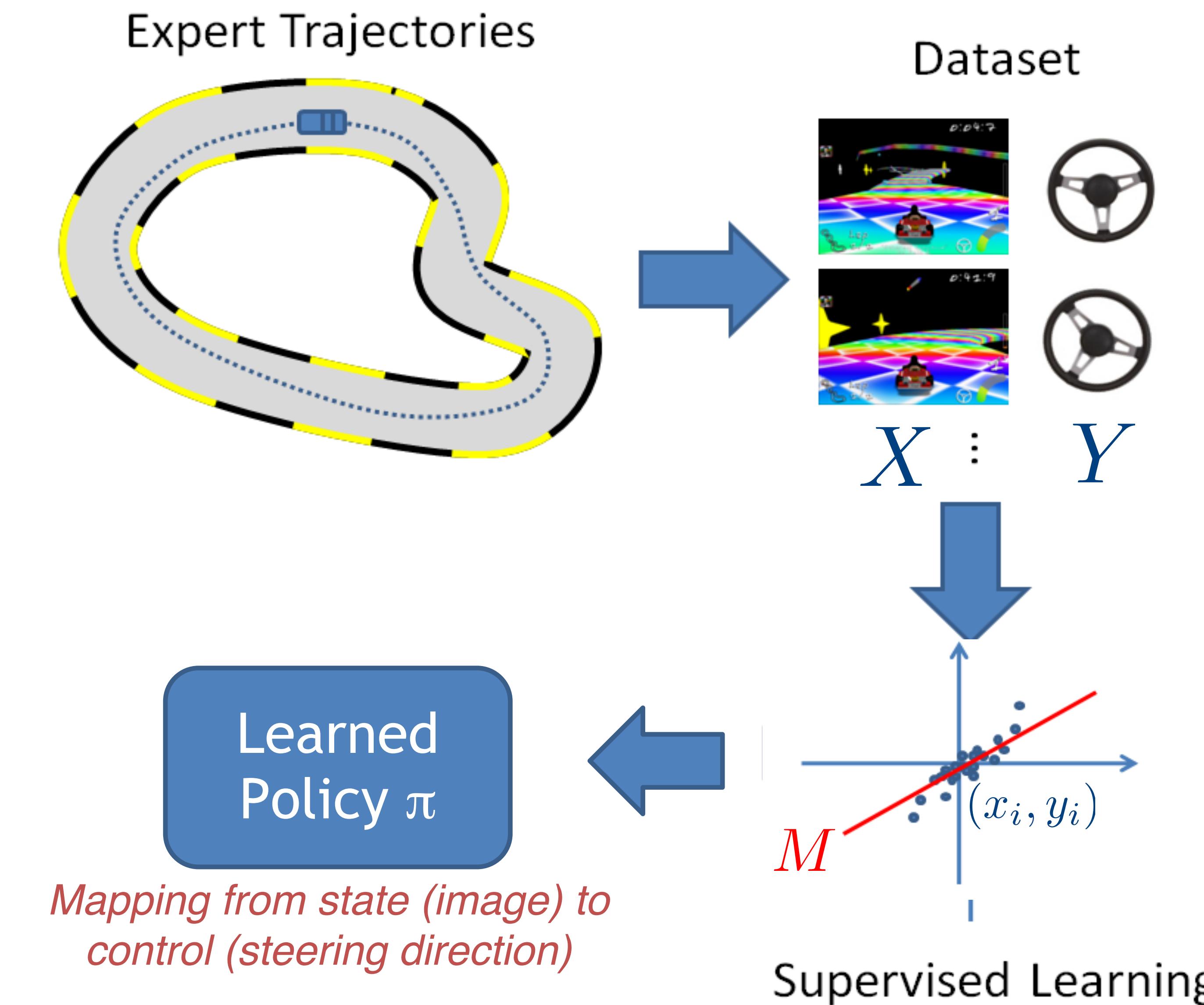
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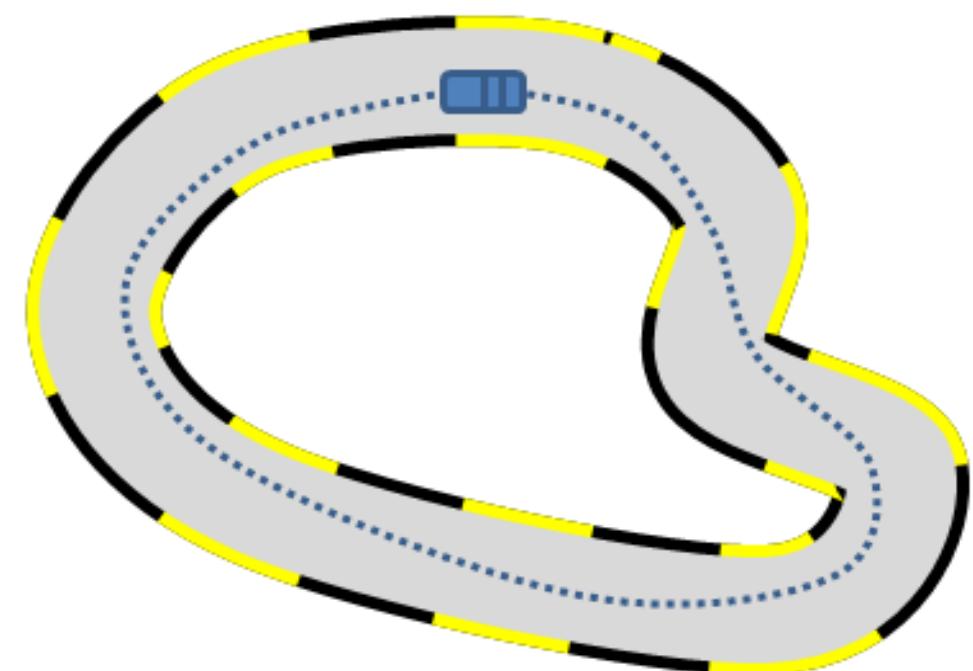
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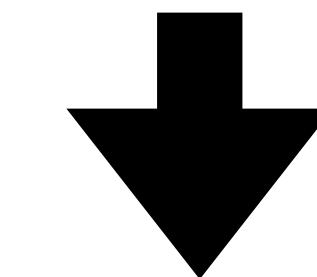


Let's formalize the offline IL Setting and the Behavior Cloning algorithm

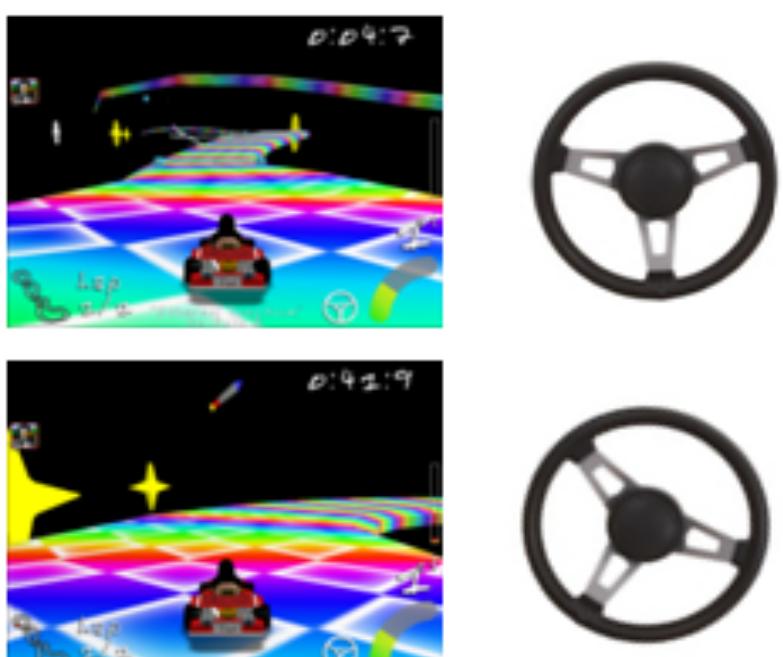
Expert Trajectories



Finite horizon MDP \mathcal{M}

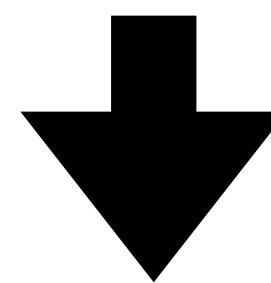
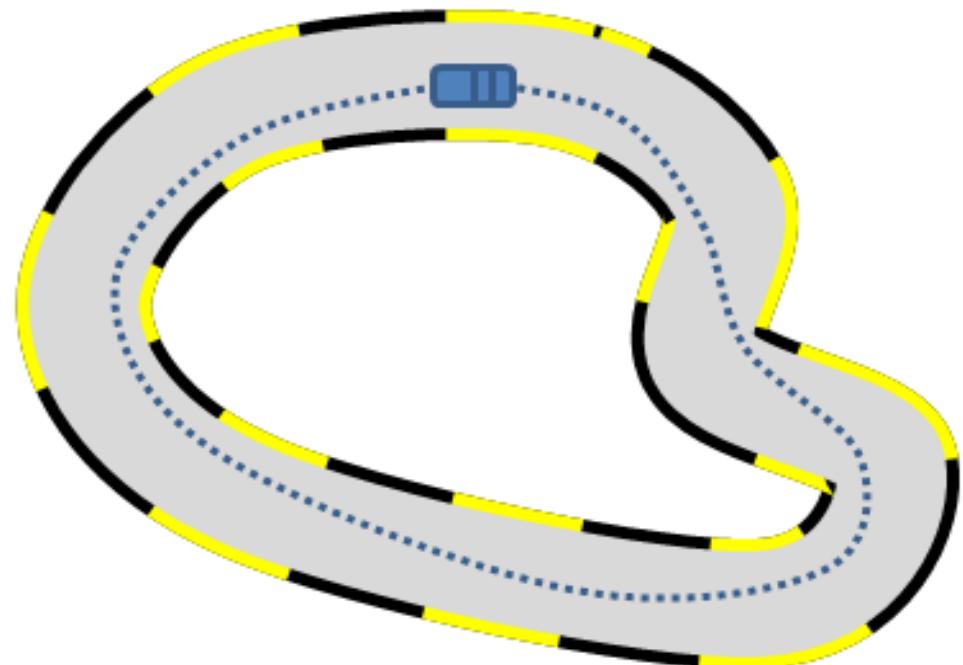


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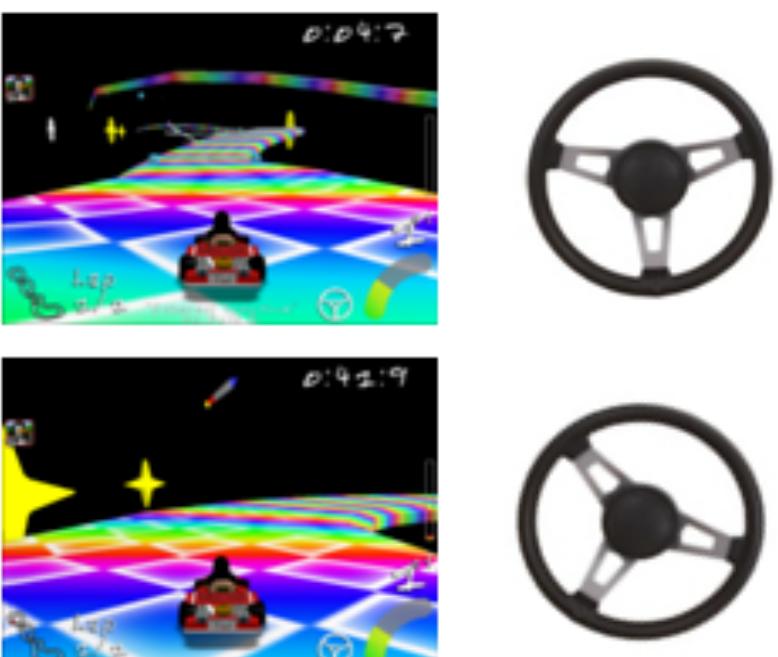


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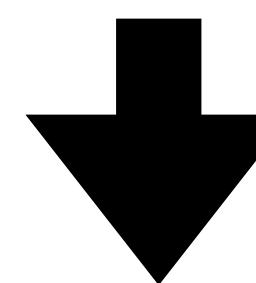
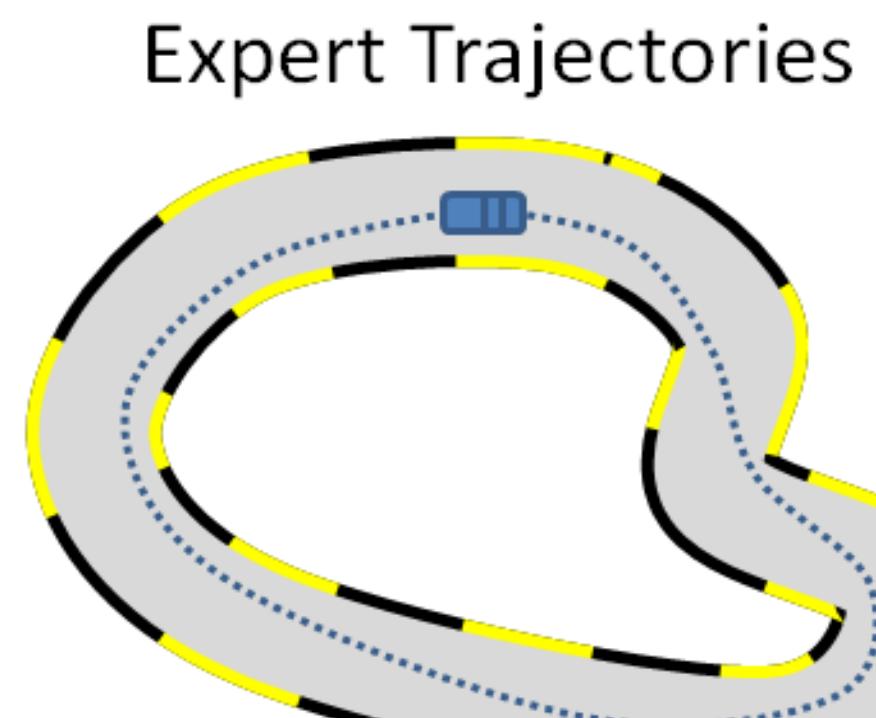


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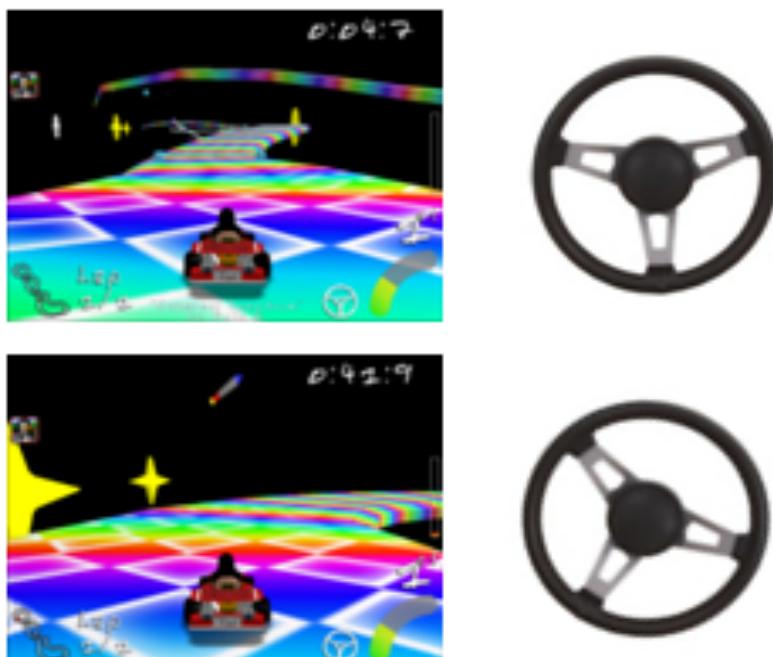
Finite horizon MDP \mathcal{M}

Ground truth reward $r(s, a) \in [0, 1]$ is unknown;
Assume the expert has a good policy π^* (not necessarily opt)

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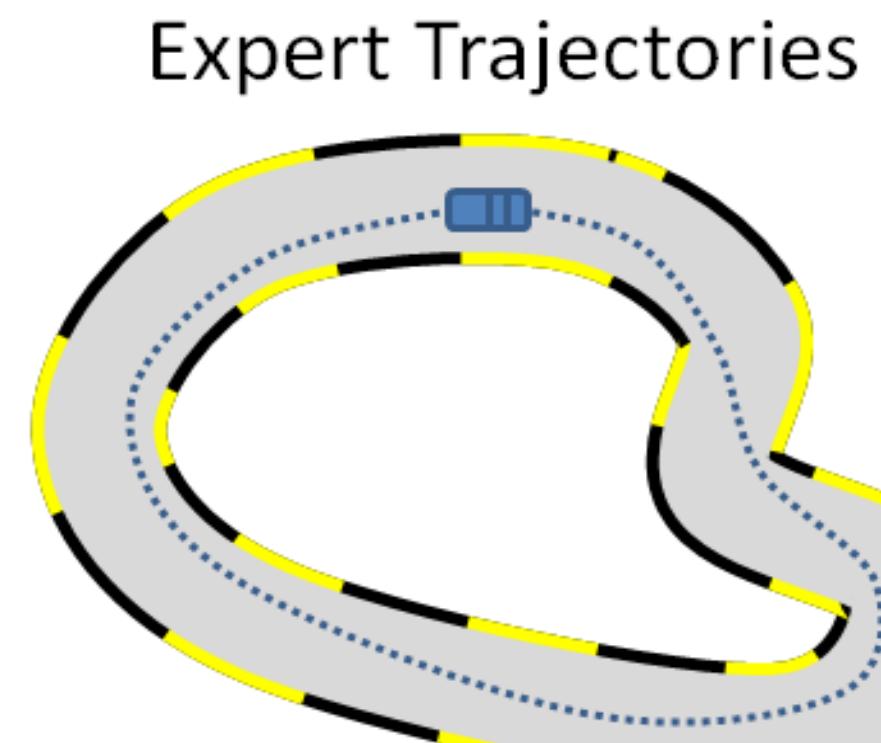
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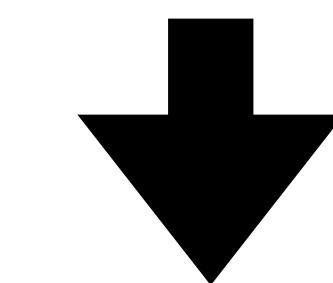
We have a dataset of M trajectories: $\mathcal{D} = \{\tau_1, \dots, \tau_M\}$,
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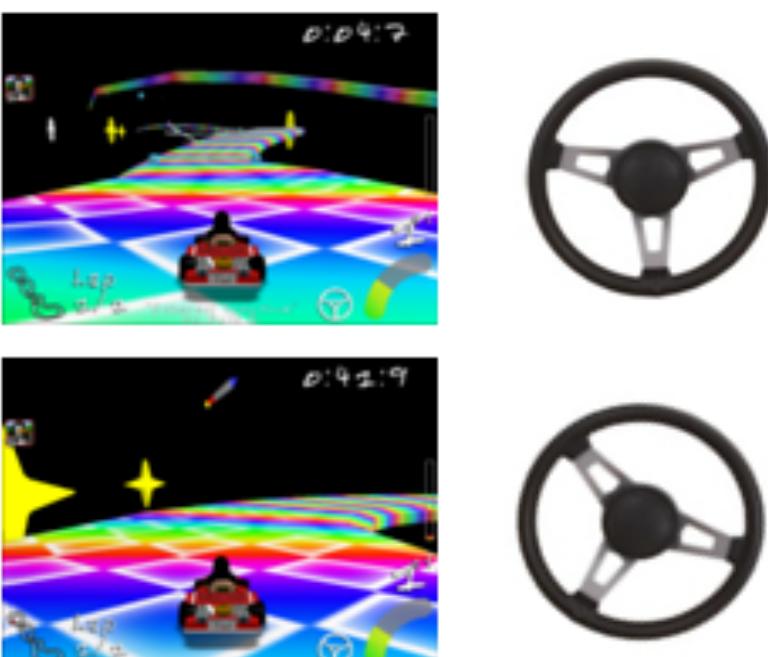


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Goal: learn a policy from \mathcal{D} that is as good as the expert π^*

:

Let's formalize the Behavior Cloning (BC) algorithm

BC Algorithm input: a restricted policy class $\Pi = \{\pi : S \mapsto \Delta(A)\}$

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3. square loss (i.e., regression for continuous action): $\ell(\pi, s, a) = \|\pi(s) - a\|_2^2$

Theorem: IL is (almost) as easy as SL

$$\hat{\pi} = \arg \min_{\pi \in \Pi} \sum_{i=1}^M \sum_{h=0}^{H-1} \ell(\pi, s_h^i, a_h^i)$$

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Theorem [BC Performance]:

suppose we assume supervised learning succeeds, with ϵ classification error:

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then we have:

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The quadratic amplification is annoying

Proof:

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By the PDL

$$|V^{\pi^\star}(s) - V^{\hat{\pi}}(s)| = \left| \mathbb{E}_{\tau \sim \rho_{\pi^\star}} \left[\sum_{h=0}^{H-1} A_h^{\hat{\pi}}(s_h, a_h) \right] \right|$$

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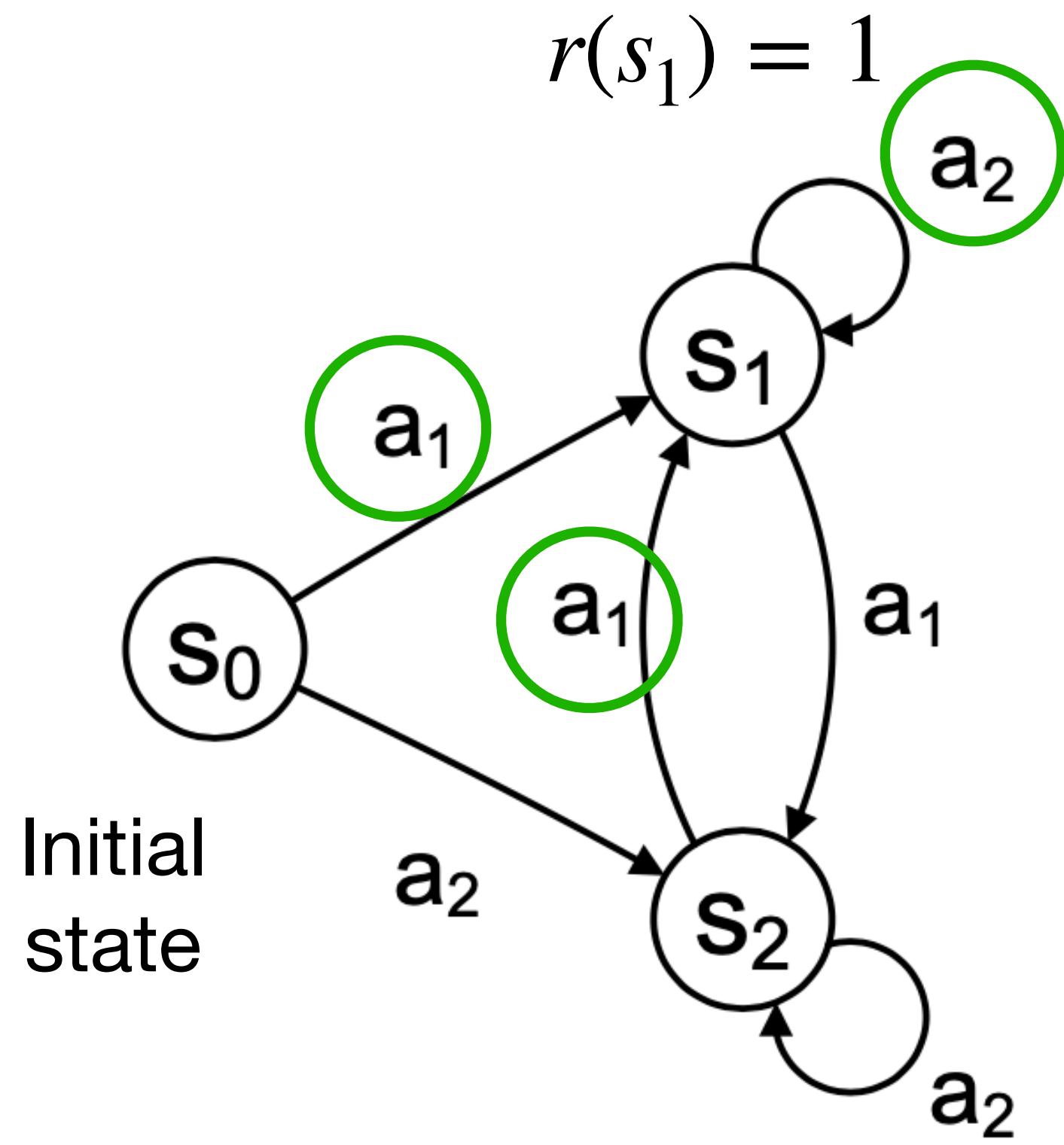
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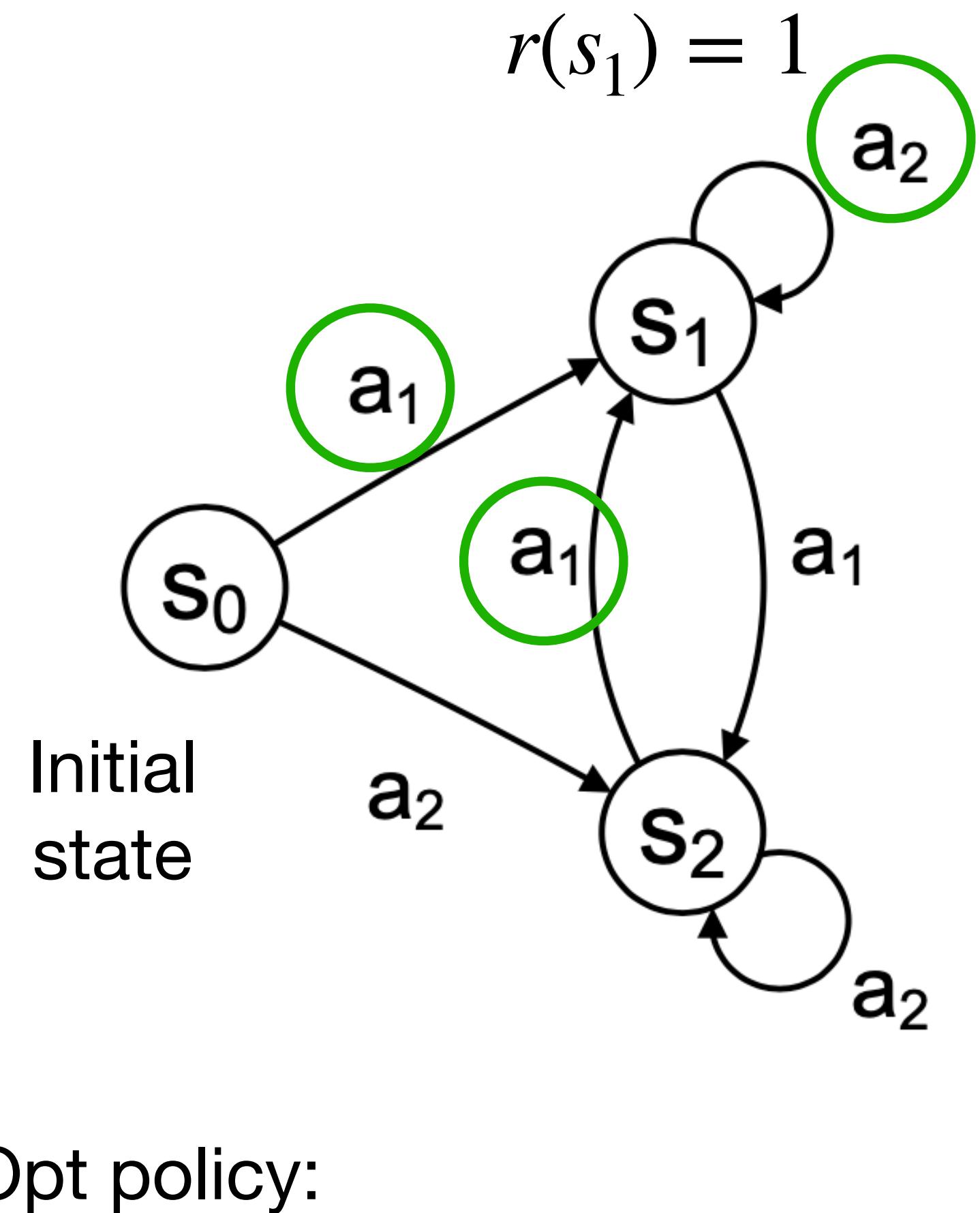
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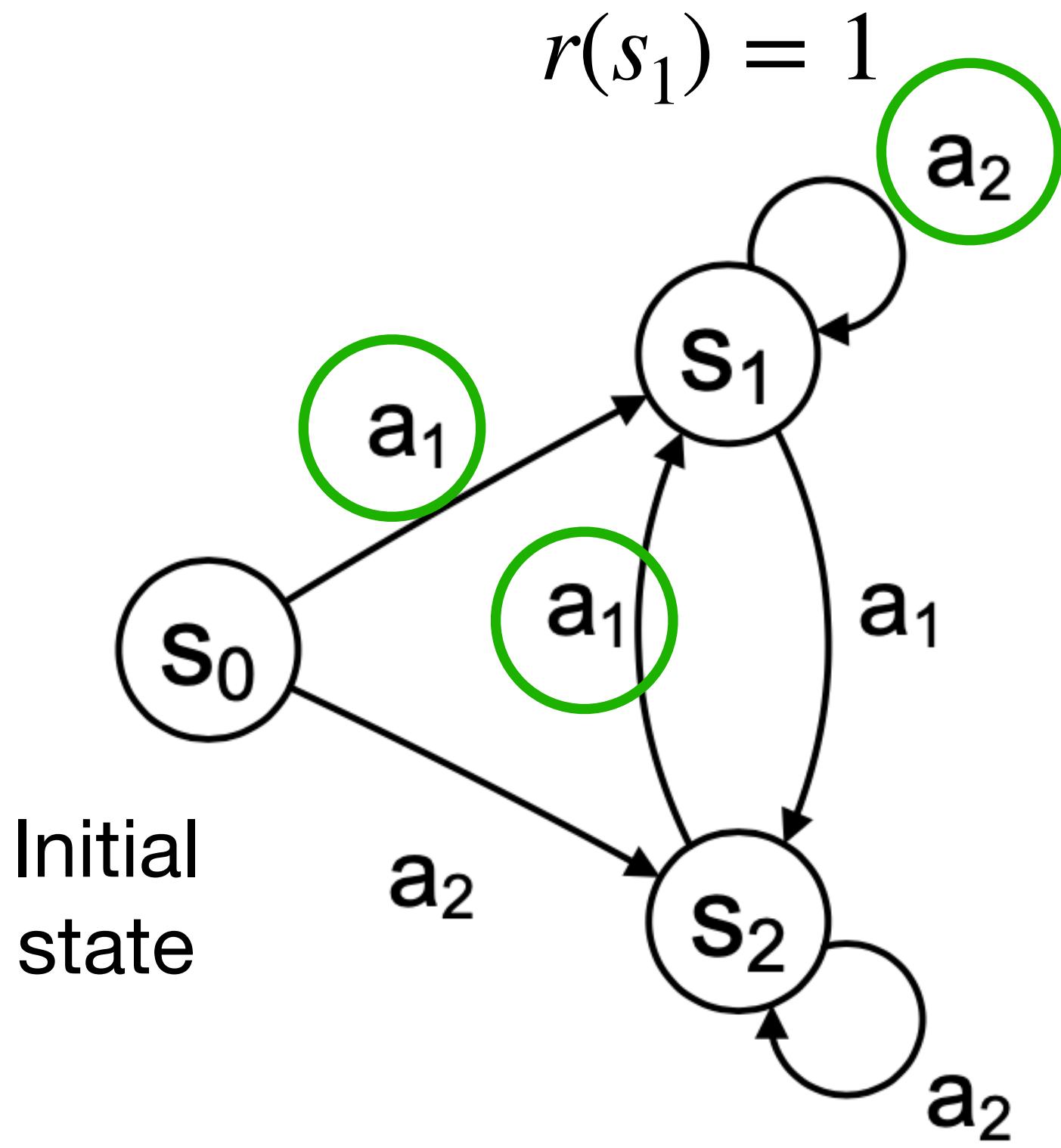
Distribution Shift Example (H^2 factor is tight)



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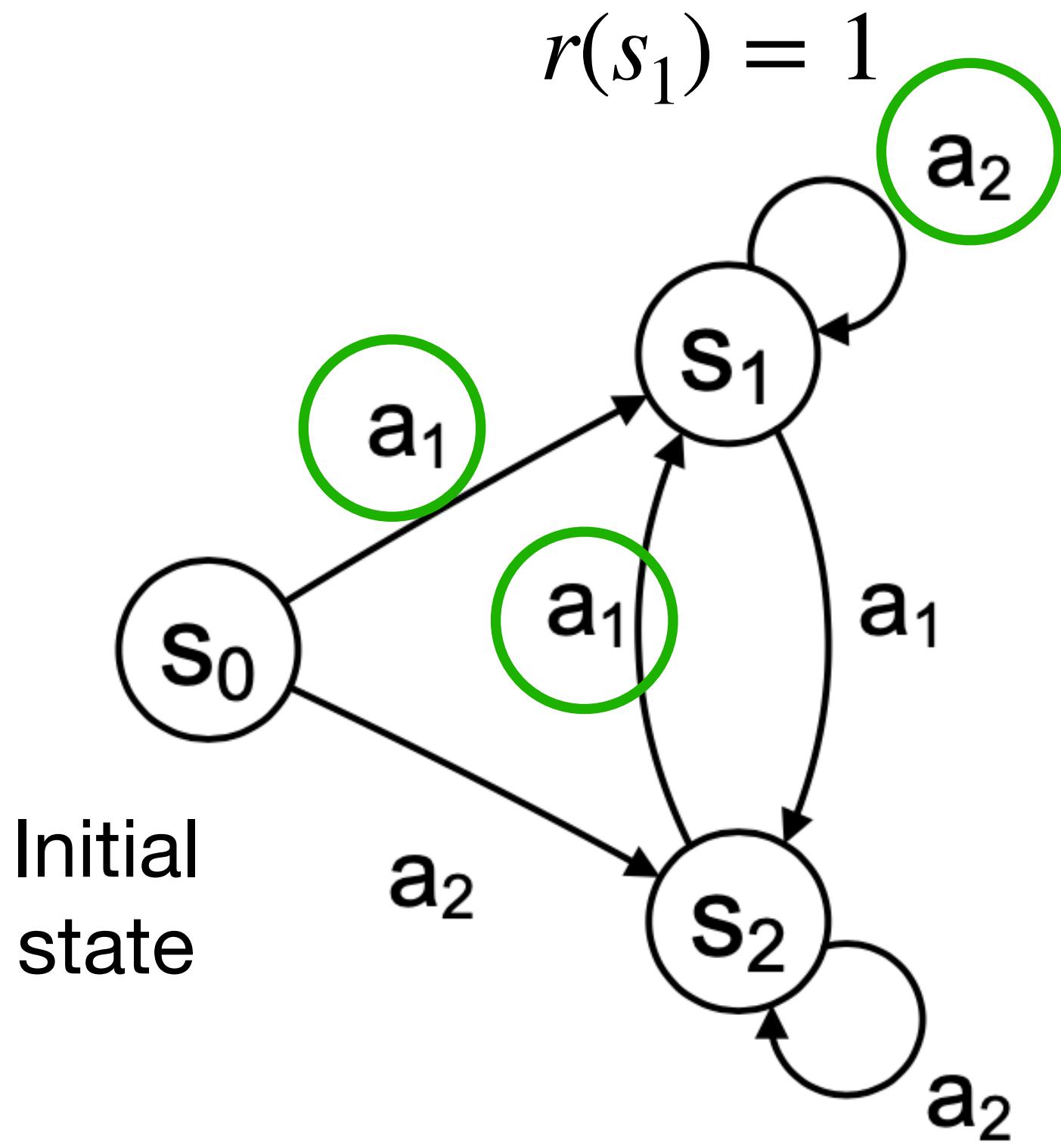
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Under ρ_{π^\star} , trajectory is s_0, s_1, s_1, \dots

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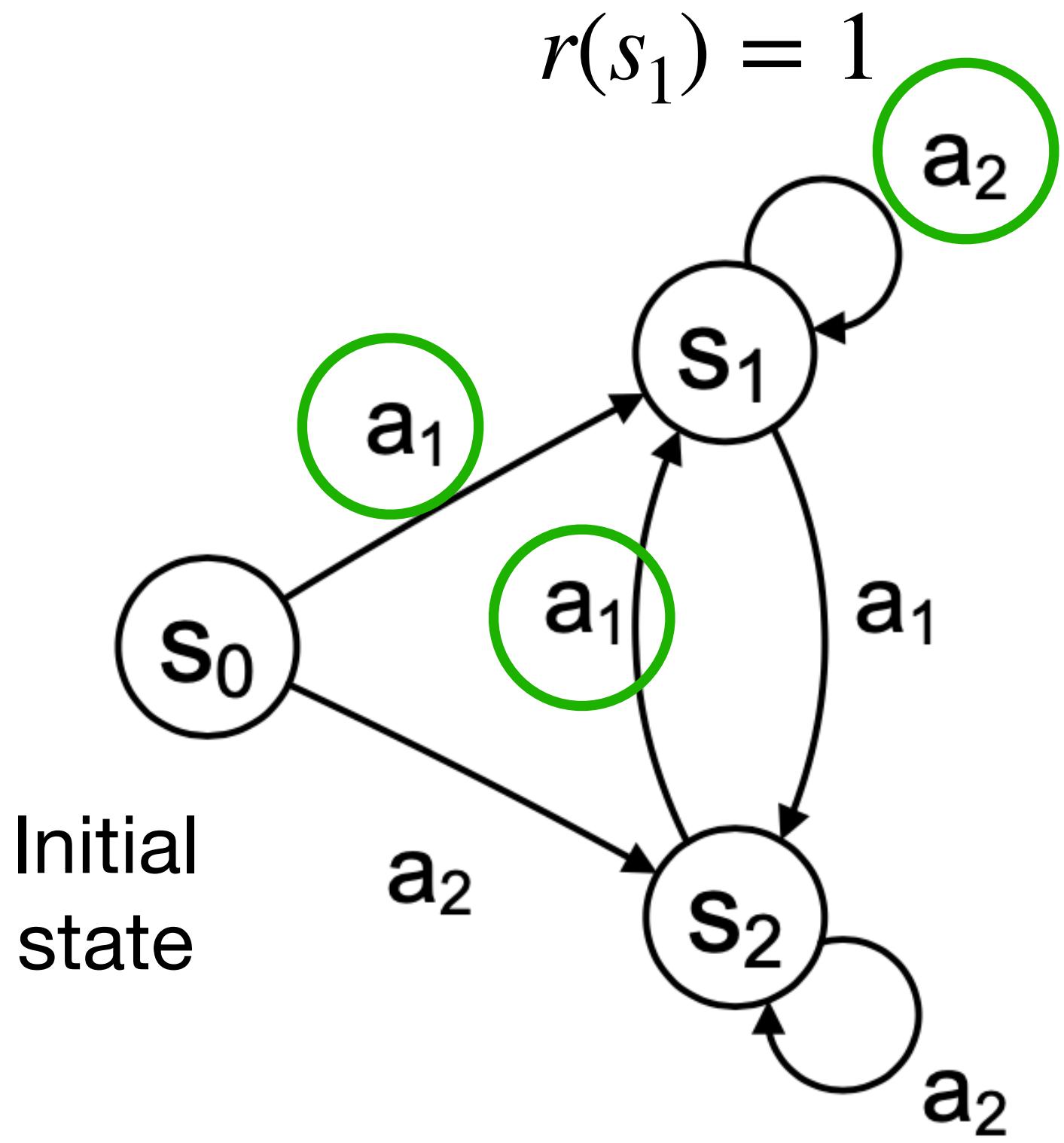


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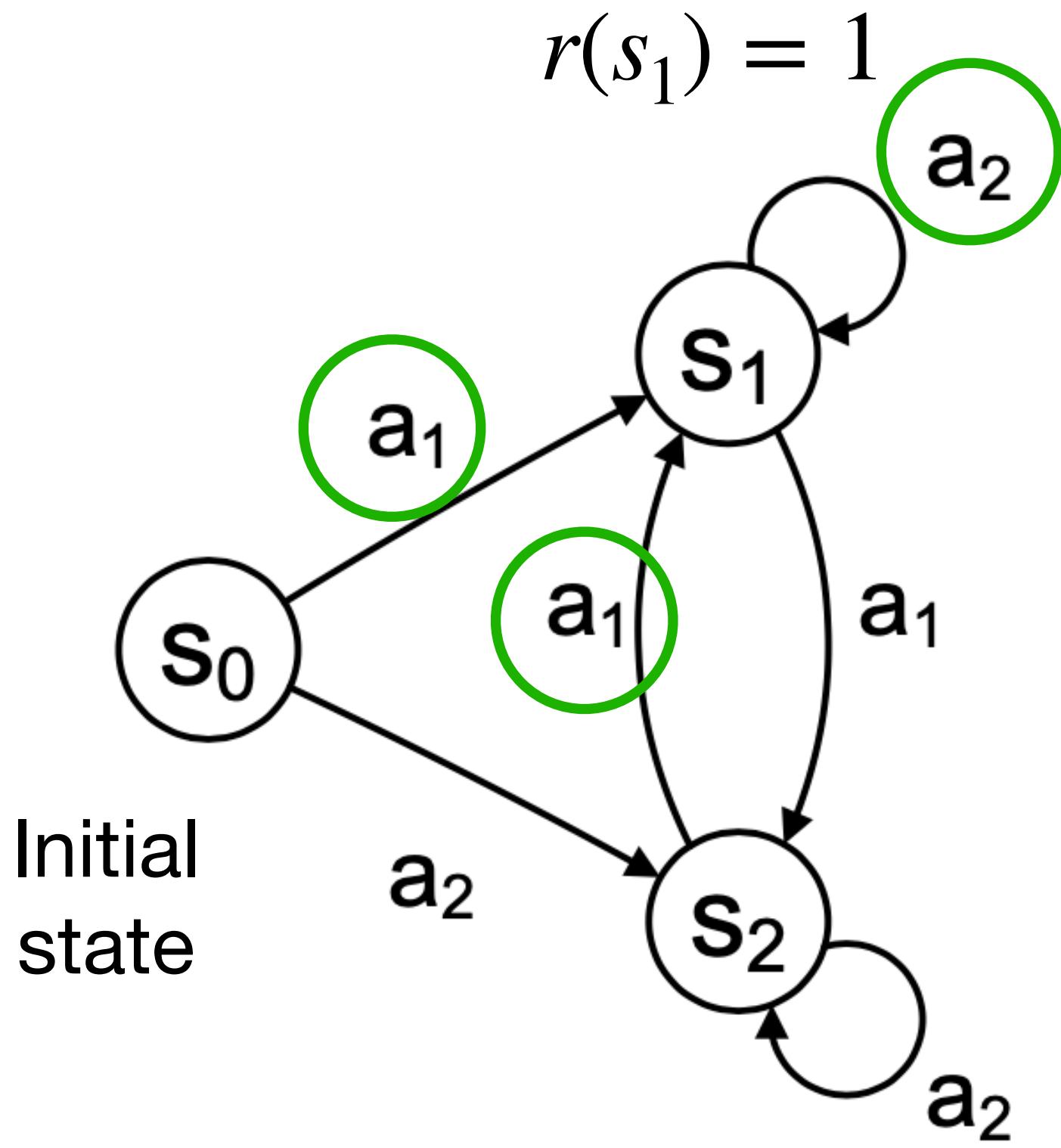
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$$\rho_{\pi^\star}(s_h = s_2) = 0$$

$$V_0^{\pi^\star}(s_0) = H - 1$$

Distribution Shift Example (H^2 factor is tight)



Assume SL returns the policy $\hat{\pi}$:

$$\hat{\pi}(s_0) = \begin{cases} a_1 & \text{w/ prob } 1 - H\epsilon \\ a_2 & \text{w/ prob } H\epsilon \end{cases}, \quad \hat{\pi}(s_1) = a_2, \hat{\pi}(s_2) = a_2$$

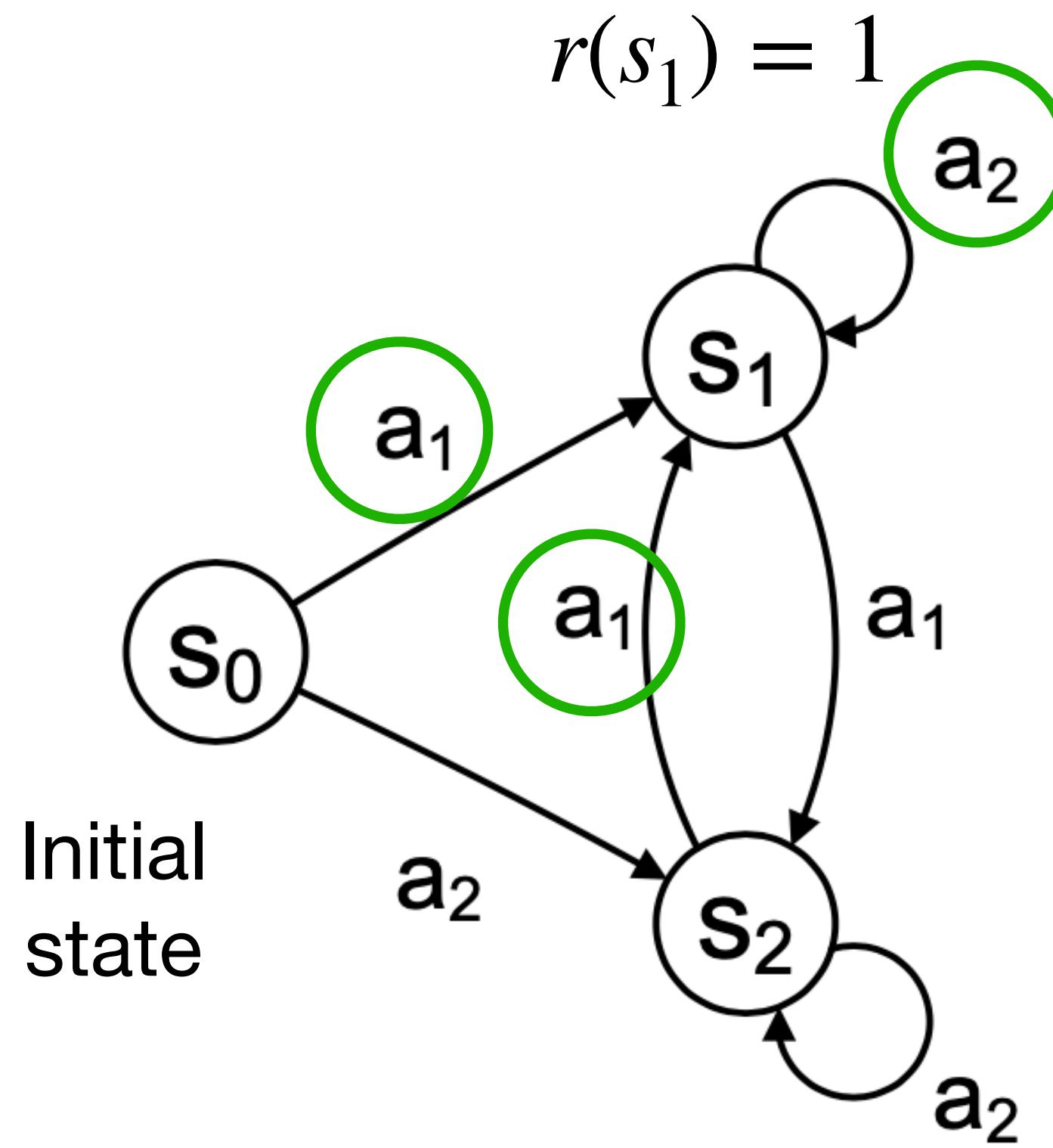
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Distribution Shift Example (H^2 factor is tight)



Assume SL returns the policy $\hat{\pi}$:

$$\hat{\pi}(s_0) = \begin{cases} a_1 & \text{w/ prob } 1 - H\epsilon \\ a_2 & \text{w/ prob } H\epsilon \end{cases}, \quad \hat{\pi}(s_1) = a_2, \hat{\pi}(s_2) = a_2$$

This policy has good supervised learning error:

$$\mathbb{E}_{\tau \sim \rho_{\pi^\star}} \left[\frac{1}{H} \sum_{h=0}^{H-1} \mathbf{1} [\hat{\pi}(s_h) \neq \pi^\star(s_h)] \right] = \epsilon$$

note: while $\hat{\pi}(s_2) \neq \pi^\star(s_2)$, state s_2 is never visited under π^\star

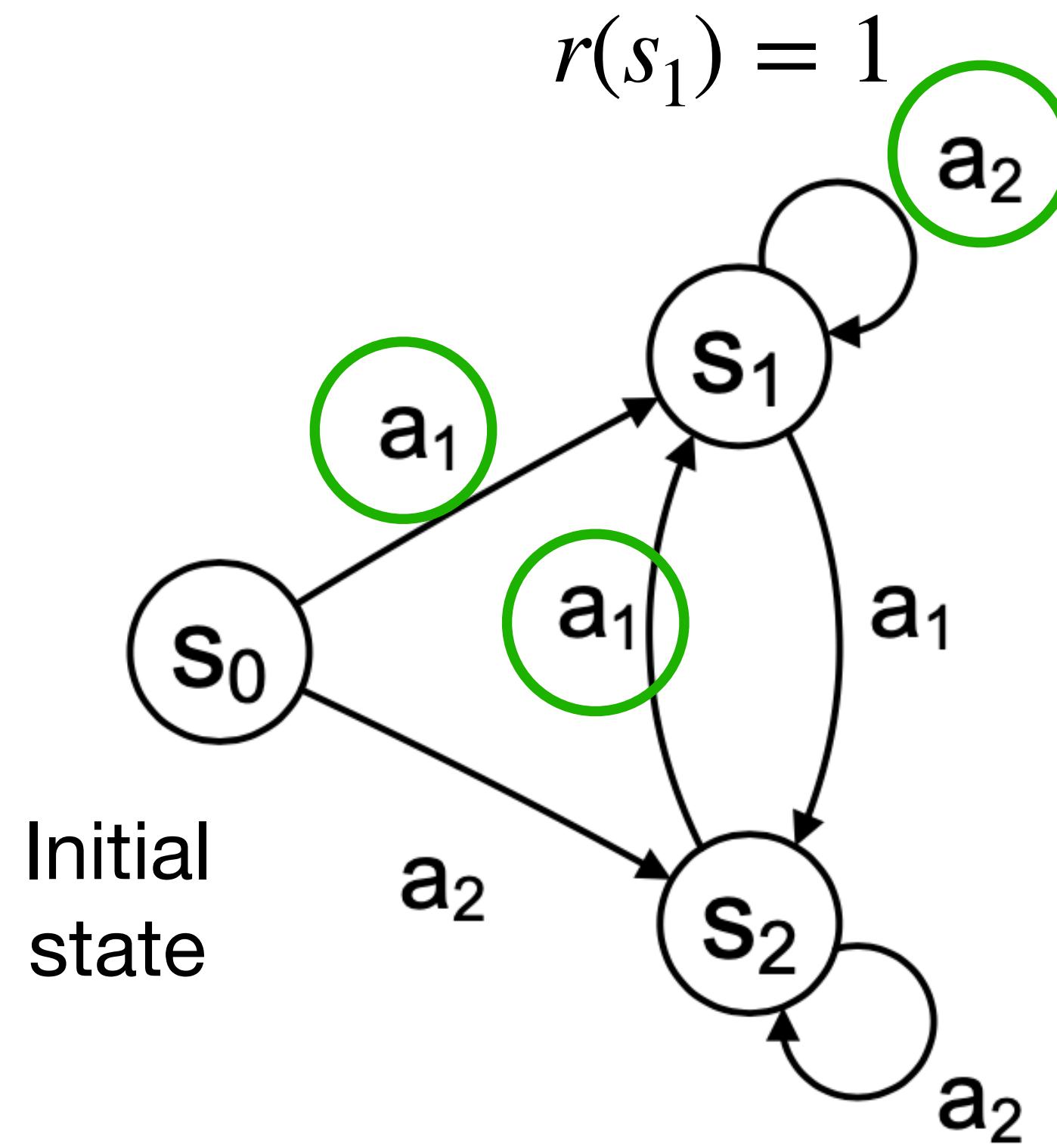
Opt policy:

Under ρ_{π^\star} , trajectory is s_0, s_1, s_1, \dots

$$\rho_{\pi^\star}(s_h = s_2) = 0$$

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Distribution Shift Example (H^2 factor is tight)



Opt policy:

Under ρ_{π^*} , trajectory is s_0, s_1, s_1, \dots

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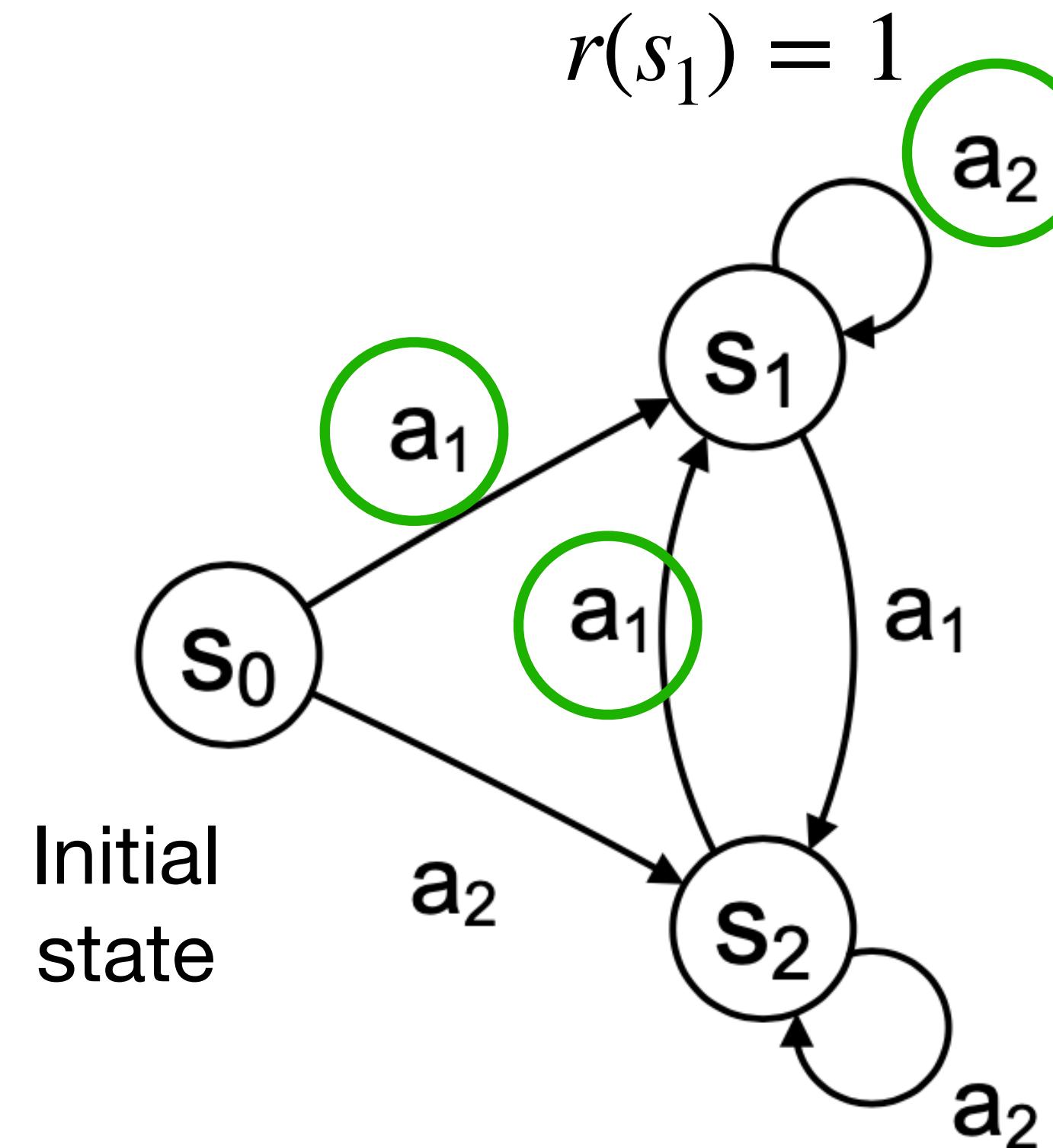
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We have quadratic degradation (in H):

$$V_0^{\hat{\pi}}(s_0) = (1 - H\epsilon) \cdot V_0^{\pi^*}(s_0) + H\epsilon \cdot 0 = V_0^{\pi^*}(s_0) - \epsilon H(H - 1)$$

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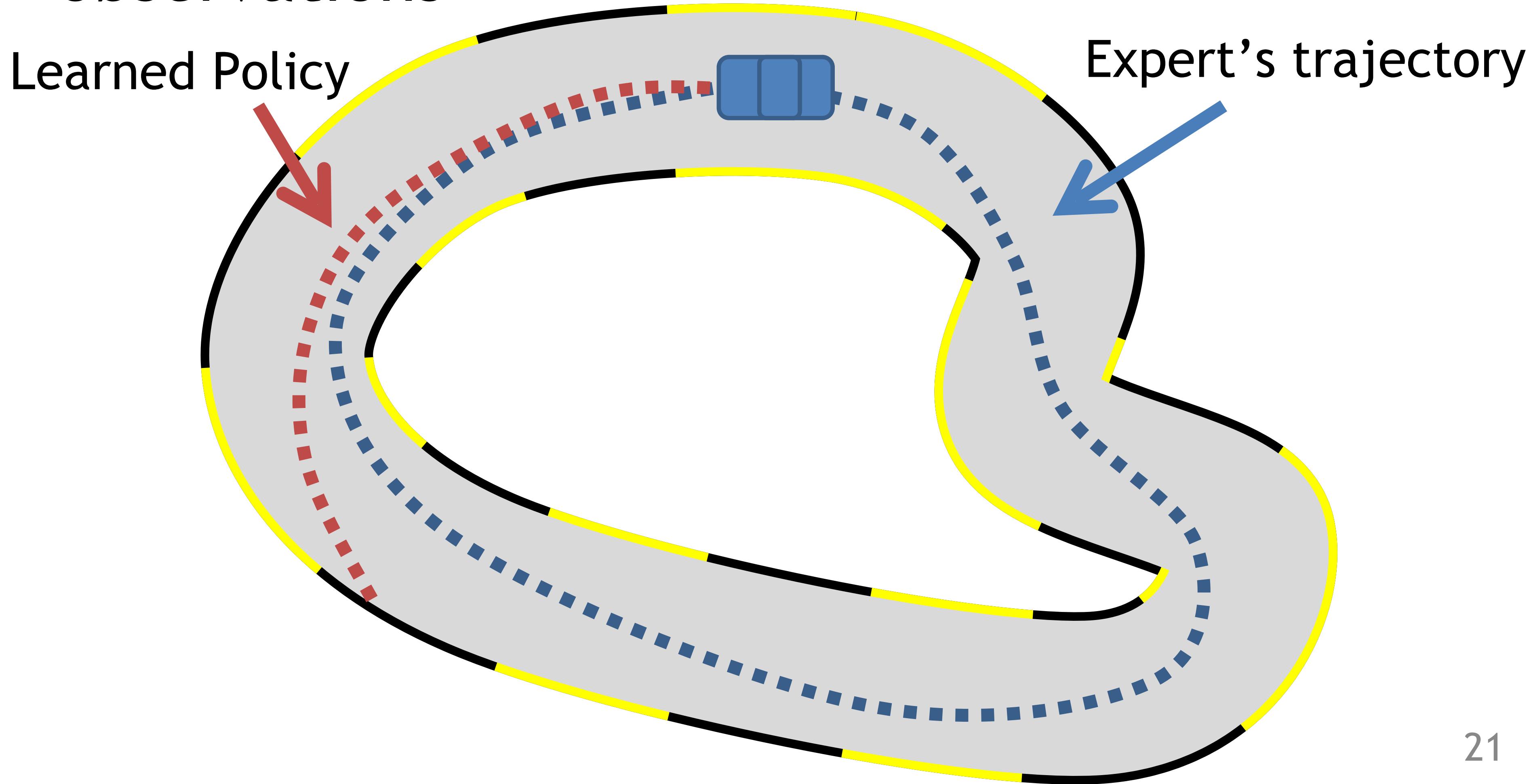
We have **quadratic degradation** (in H):

$$V_0^{\hat{\pi}}(s_0) = (1 - H\epsilon) \cdot V_0^{\pi^*}(s_0) + H\epsilon \cdot 0 = V_0^{\pi^*}(s_0) - \epsilon H(H - 1)$$

Intuition: once we make a mistake at s_0 , we end up in s_2 which is not in the training data!

What could go wrong?

- Predictions affect future inputs/observations



Expert Demos







Features

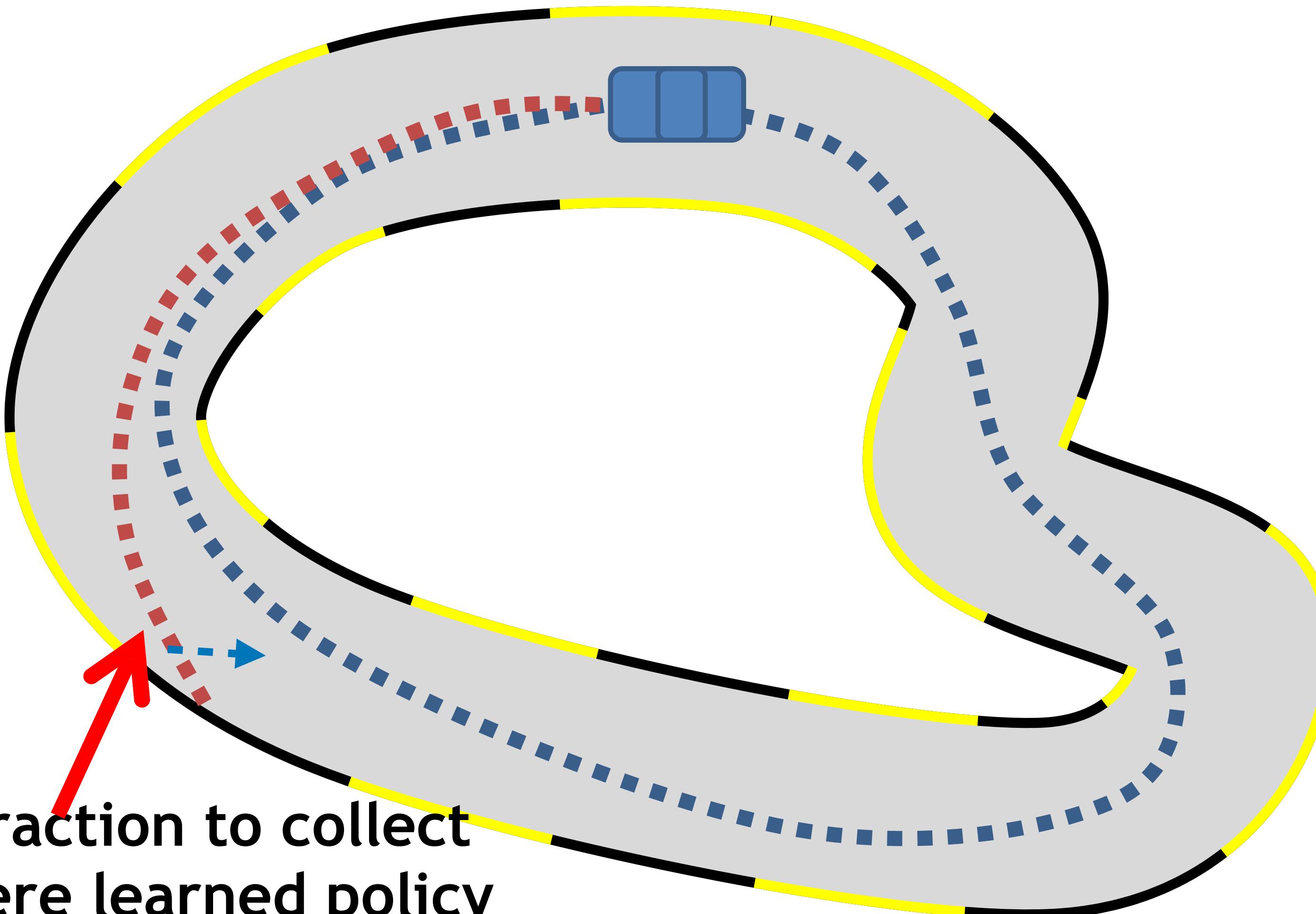


Features

Today

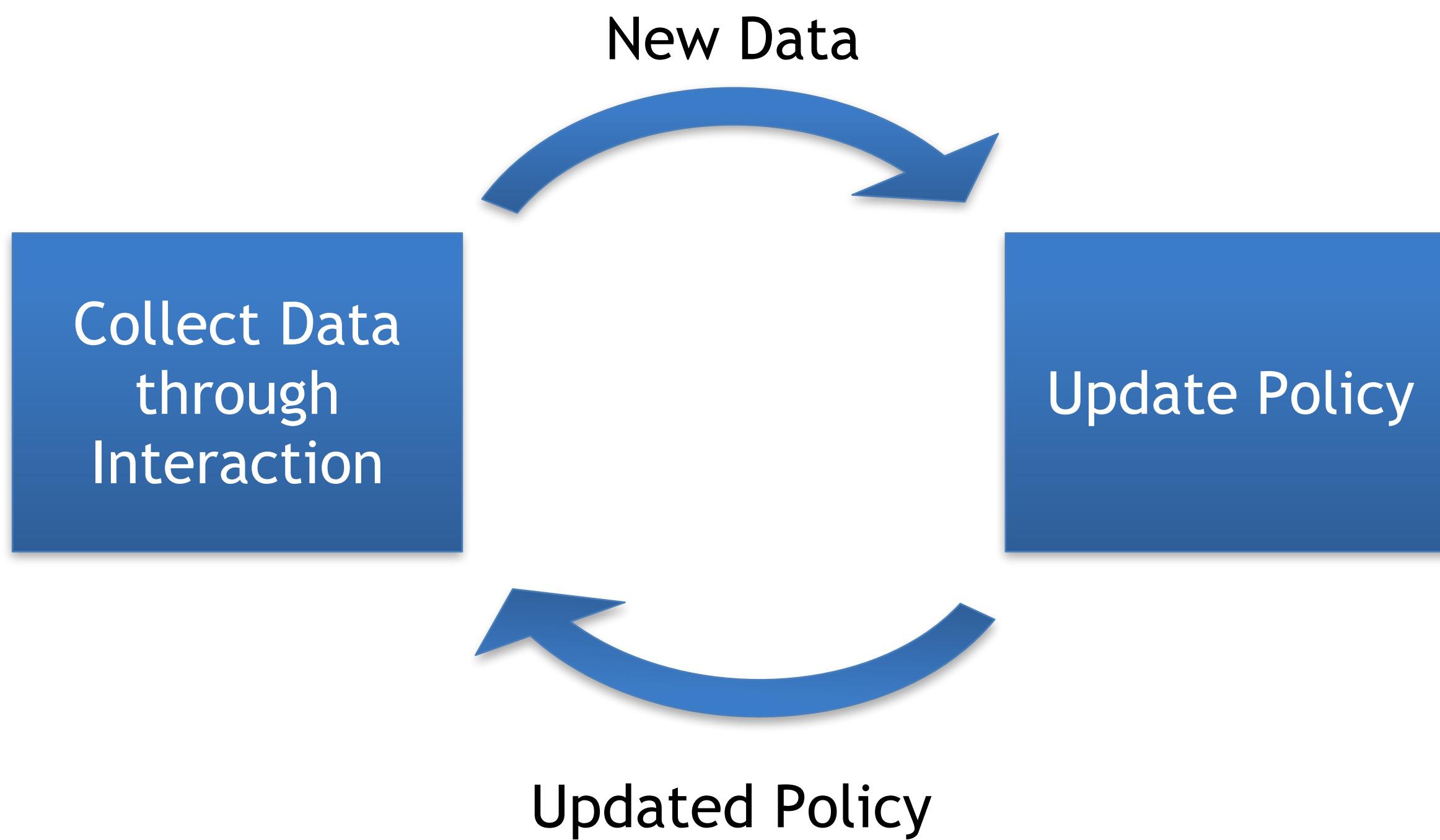
- ✓ • Feedback from last lecture
- ✓ • Recap
- ✓ • Imitation Learning problem statement
- ✓ • Behavioral Cloning
- DAgger

Intuitive solution: Interaction



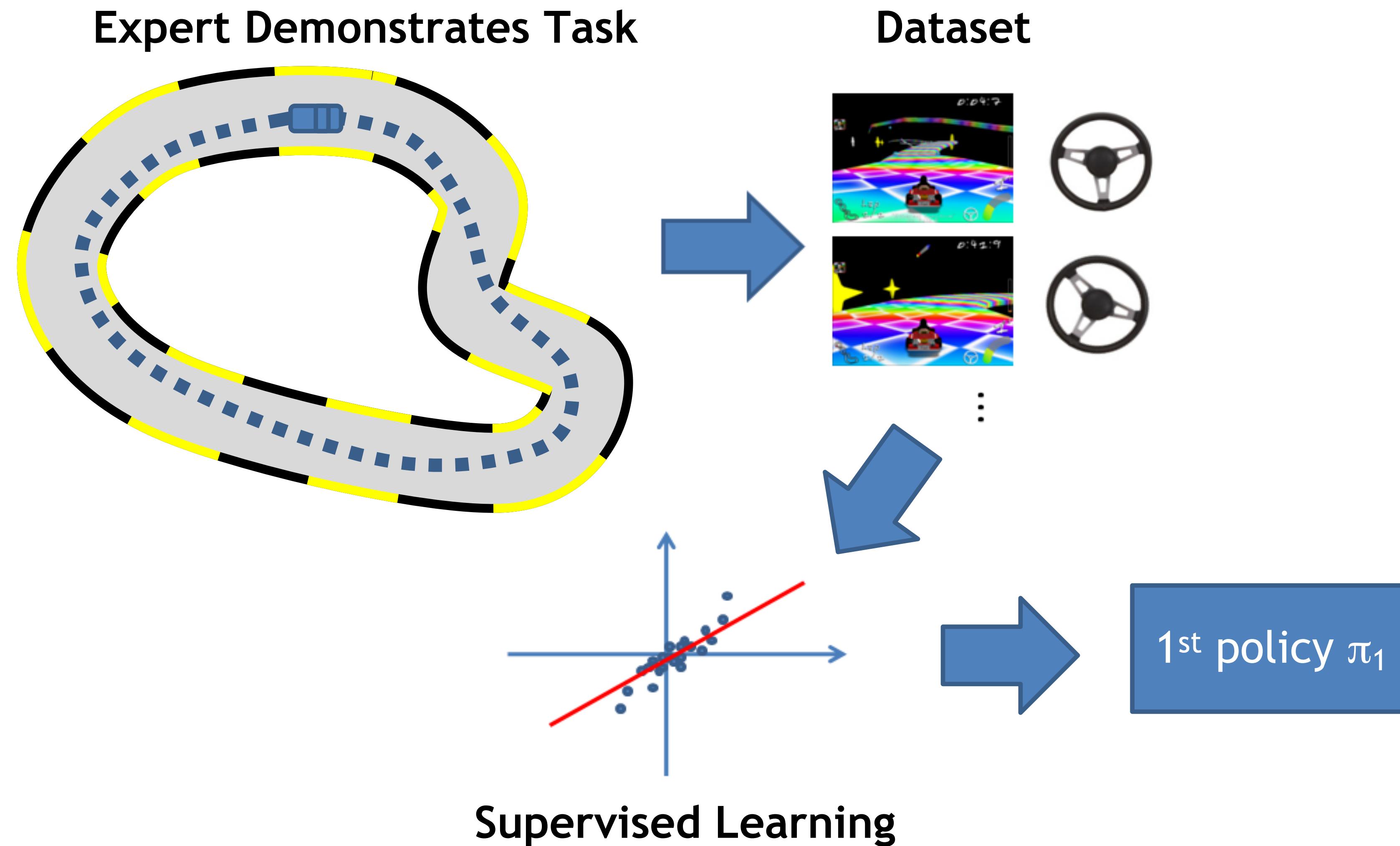
Use interaction to collect
data where learned policy
goes

General Idea: Iterative Interactive Approach



DAgger: Dataset Aggregation

0th iteration

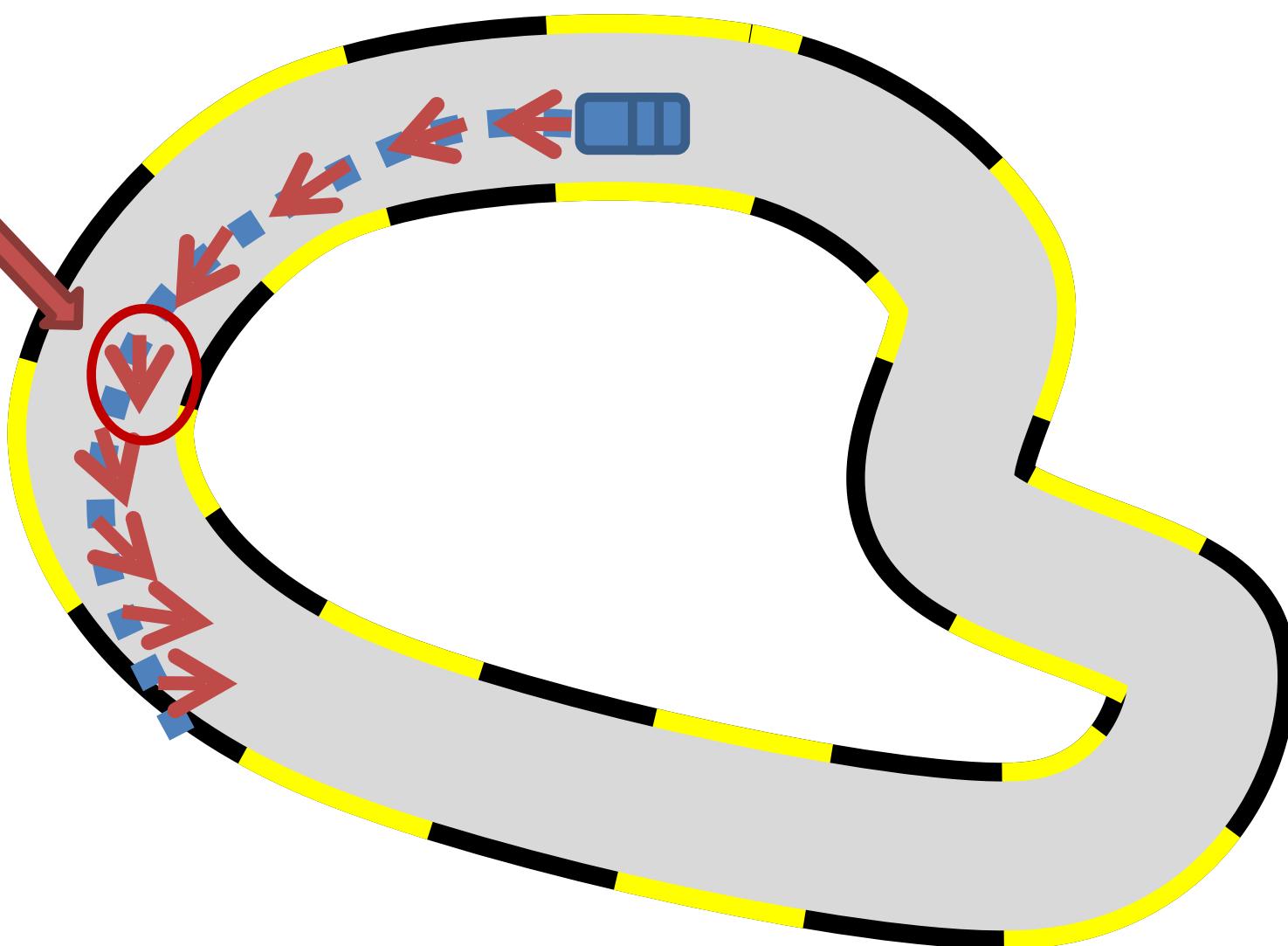


DAgger: Dataset Aggregation

1st iteration

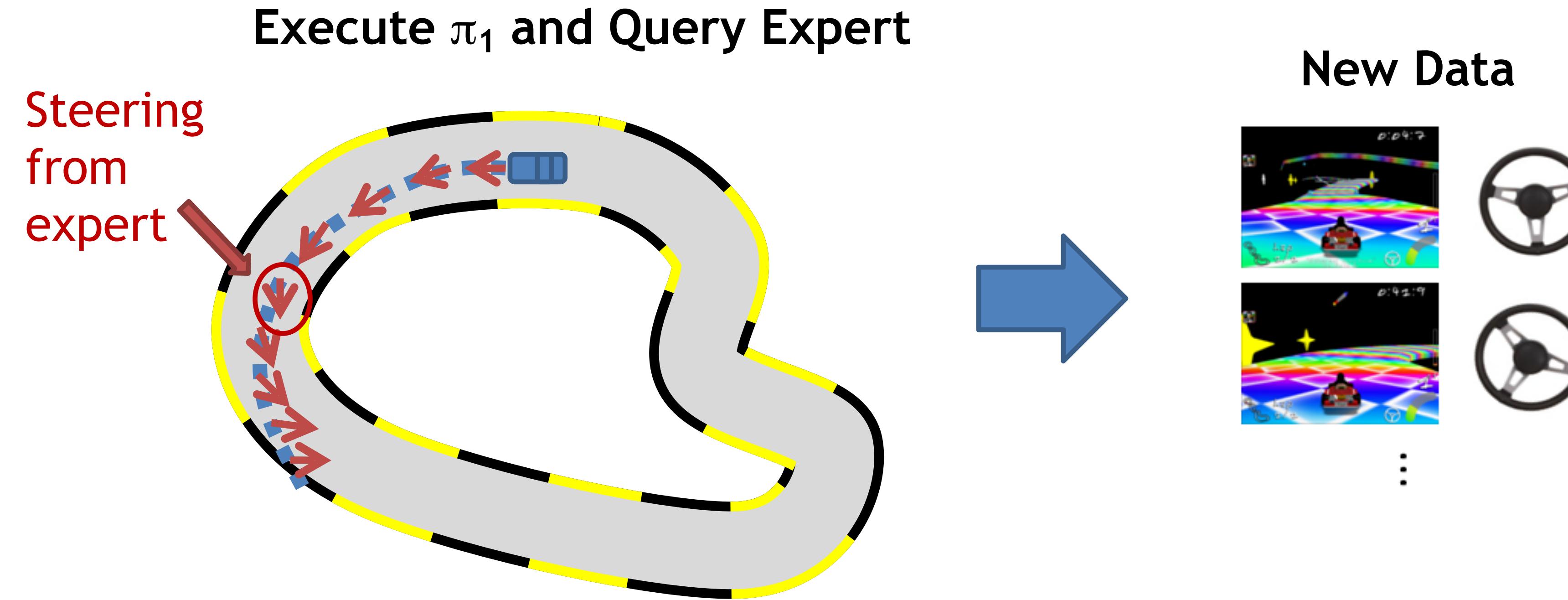
Execute π_1 and Query Expert

Steering
from
expert



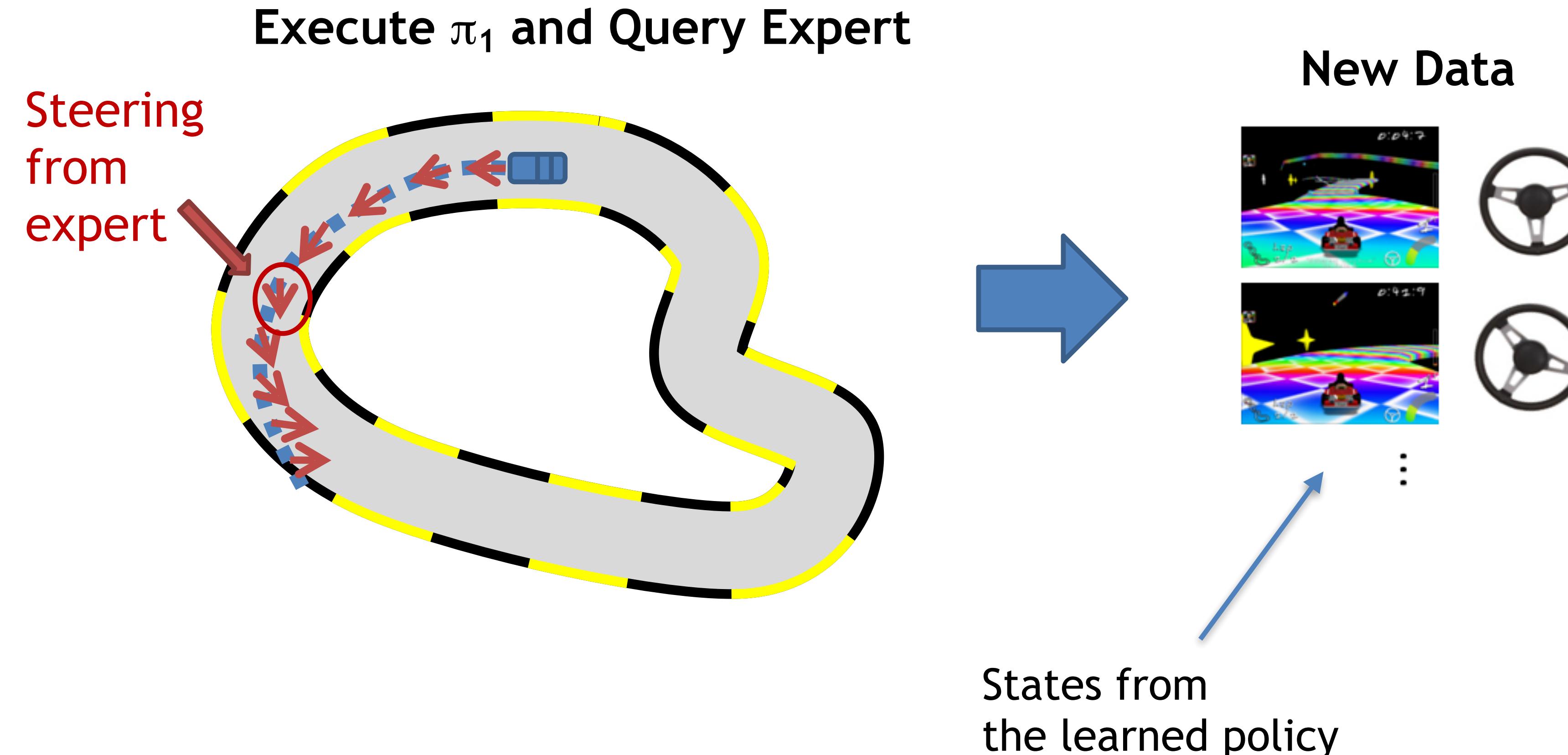
DAgger: Dataset Aggregation

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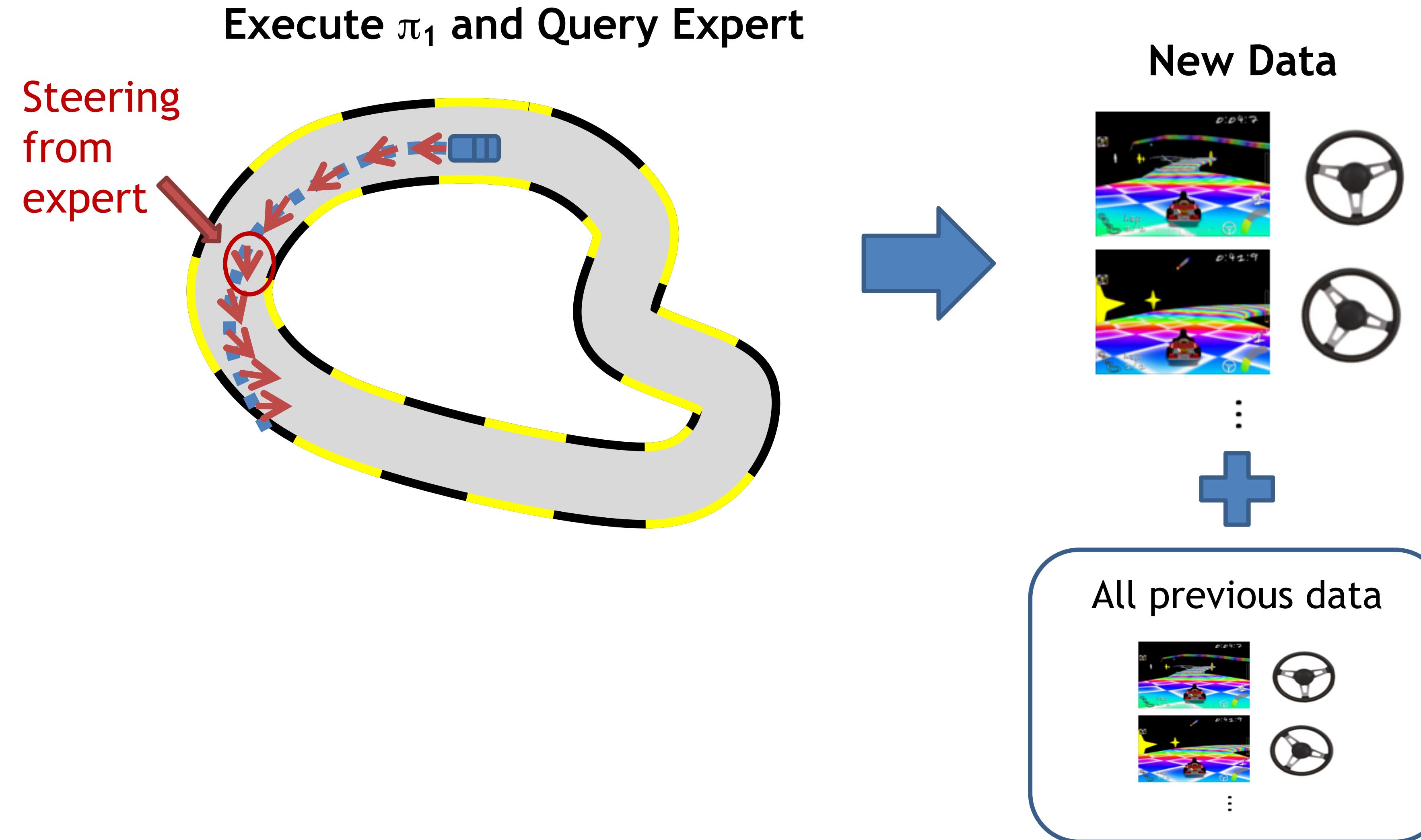
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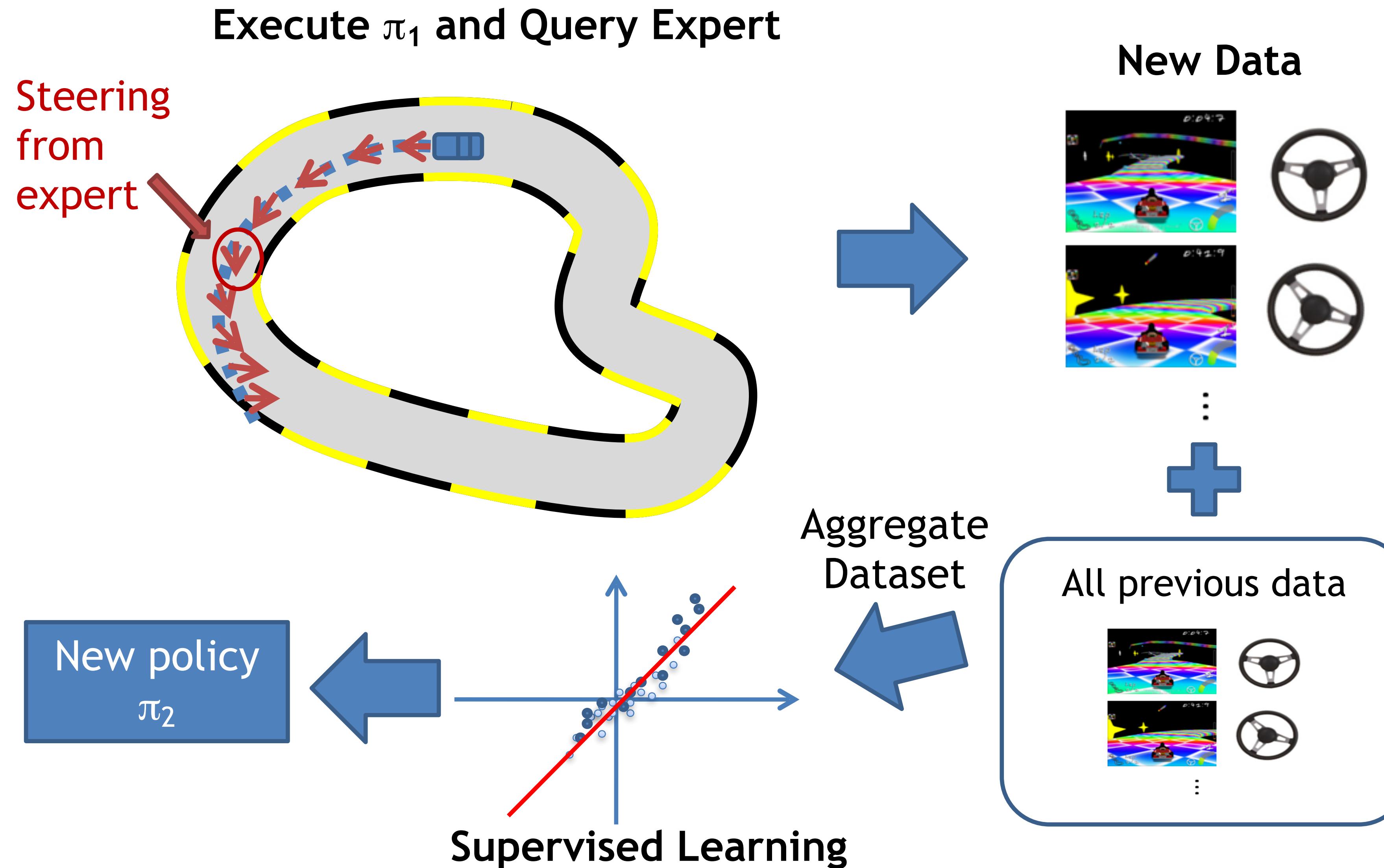
DAgger: Dataset Aggregation

1st iteration



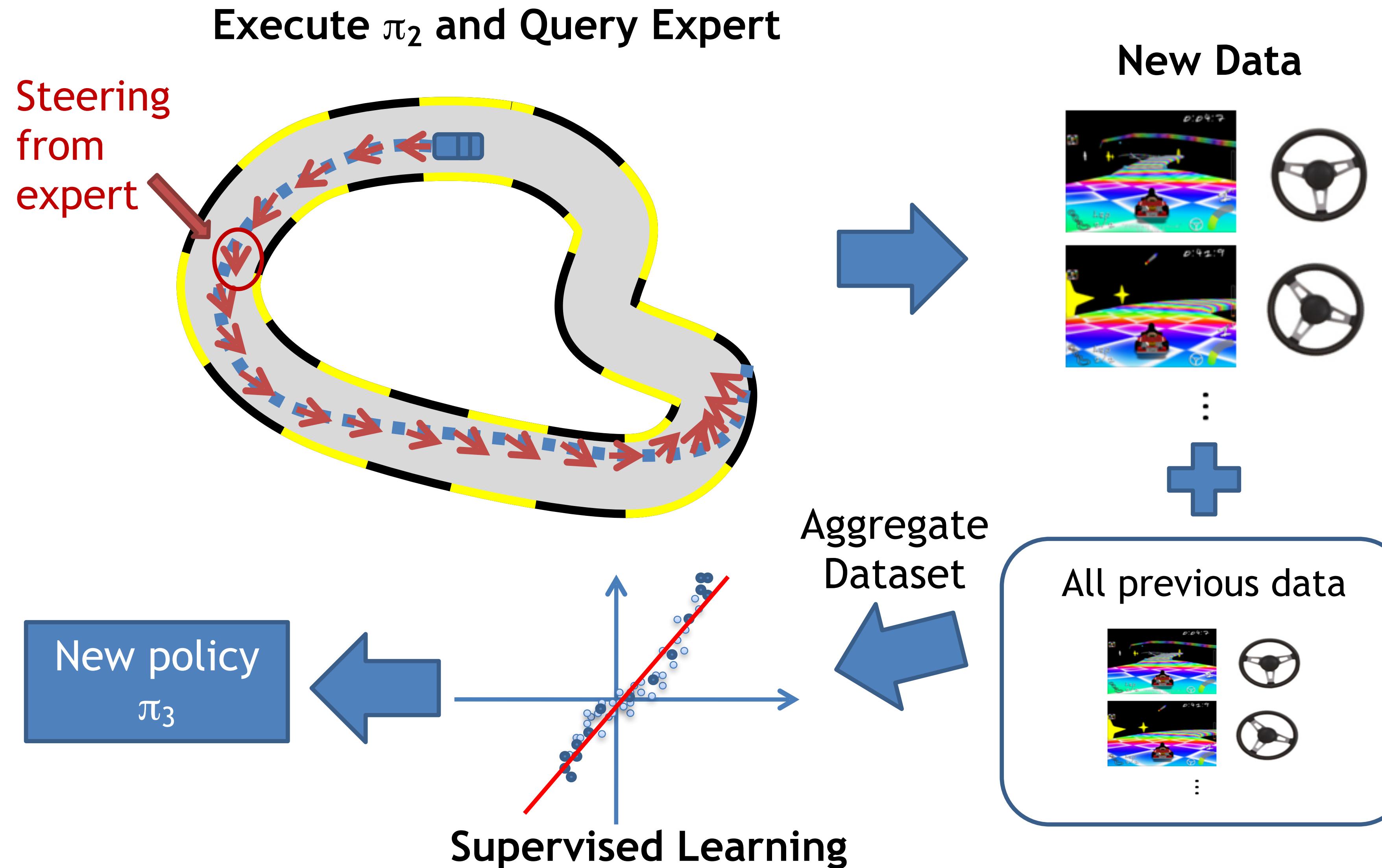
DAgger: Dataset Aggregation

1st iteration



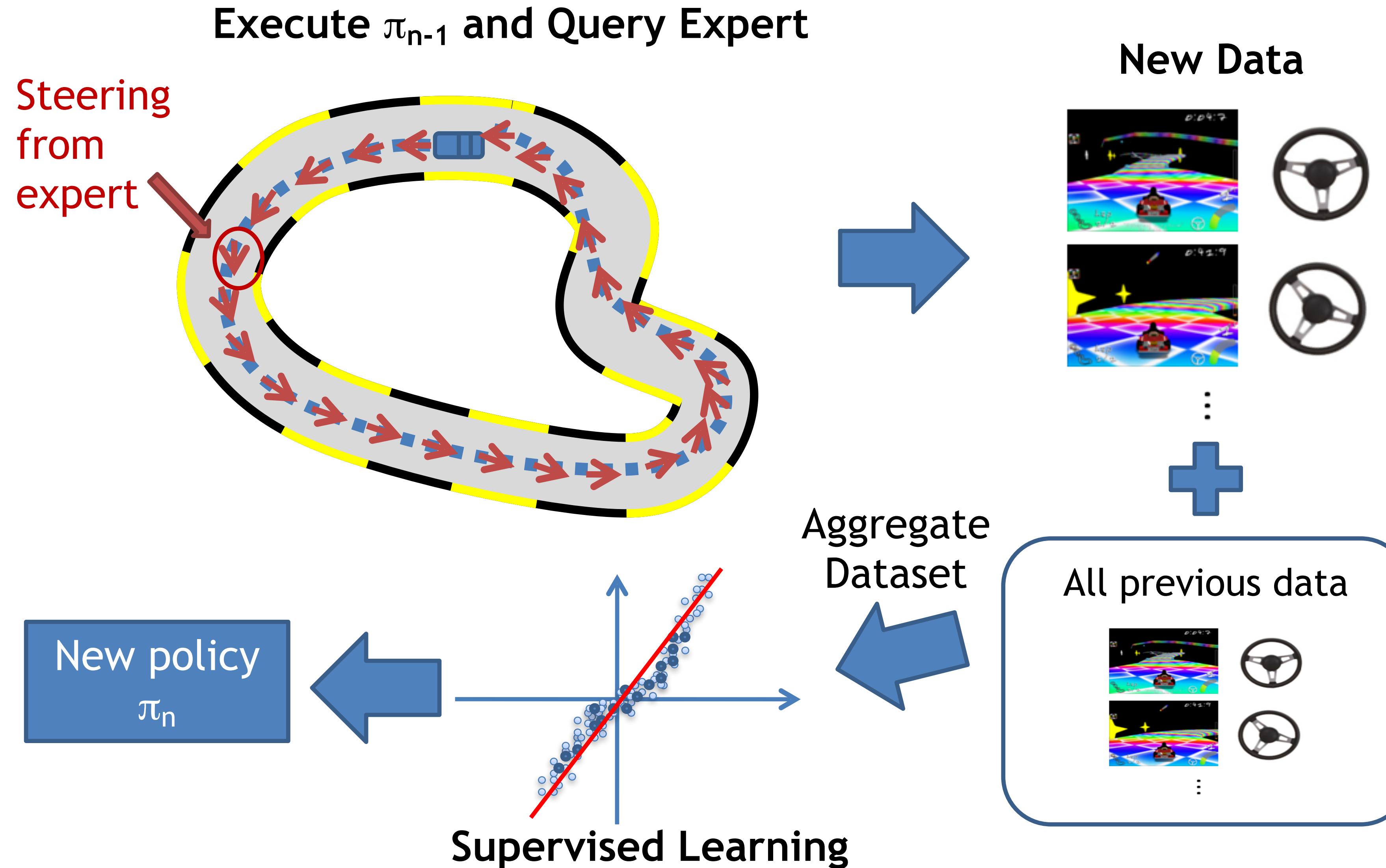
DAgger: Dataset Aggregation

2nd iteration



DAgger: Dataset Aggregation

n^{th} iteration



The DAgger algorithm

Initialize π^0 , and dataset $\mathcal{D} = \emptyset$

For $t = 0 \rightarrow T - 1$:

|

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where for all trajectories $s_h \sim \rho_{\pi^t}$, $a_h = \pi^\star(s_h)$

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In practice, the DAgger algorithm requires less human labeled data than BC.

[Informal Theorem] Under more assumptions + assuming ϵ SL error is achievable, the DAgger algorithm has error: $|V^{\pi^\star} - V^{\hat{\pi}}| \leq H\epsilon$

Success!



Success!



Today

- ✓ • Feedback from last lecture
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- ✓ • DAgger

Summary:

1. IL can help a lot to explore the space
2. BC pretty good but brittle -> quadratic-in-horizon error
3. Online expert feedback can help with robustness -> linear-in-horizon error

Attendance:

bit.ly/3RcTC9T



Feedback:

bit.ly/3RHtIxy

