

Spectral learning for structured partially observable environments

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1 A Spectral Algorithm for PSRs

2 The Base System

Predictive state representations (PSRs) are for computing a probability distribution over observations in a dynamical system [Littman et al.]

Also known as Weighted Automata (motivation dependent)

PSRs compute a function on finite strings of observations sequences $f(\text{abaab} \dots)$.

Defined by three parameters: $\langle \alpha, A_x, \beta \rangle$

α : Weighting on states E.g $\alpha = [0.5, 0.5]$

A_x : Transition operator for symbol x

$$A_x = \begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 3 & 4 & 5 & 6 & 7 \end{bmatrix}$$

β : Normalizer on states E.g

$$M = \begin{bmatrix} 1 & 2 \end{bmatrix}$$

$$f(\text{abaaba}) = \alpha * A_a * A_b * A_a * A_a * A_b * \beta$$

Bullet Points

- HMMs are an example of PSRs
- $A_x = O_x * T_x$
- O_x being an observation matrix
- T_x being a transition matrix
- So why bother the general framework of PSRs?

A Learning Algorithm

- Turns out that with spectral can learn PSRs from data, but learning HMMs cannot be done.
- $\langle \alpha, A_x, \beta \rangle$ v.s $\langle \alpha * M^{-1}, M * A_x * M^{-1}, M * \beta \rangle$
- $A_x = O_x * T_x$
- O_x being an observation matrix
- T_x being a transition matrix
- So why bother the general framework of PSRs?

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Block 1

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Heading

- 1 Statement
- 2 Explanation
- 3 Example

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Table

Treatments	Response 1	Response 2
Treatment 1	0.0003262	0.562
Treatment 2	0.0015681	0.910
Treatment 3	0.0009271	0.296

Table : Table caption

Theorem

Theorem (Mass–energy equivalence)

$$E = mc^2$$

Example (Theorem Slide Code)

```
\begin{frame}  
\frametitle{Theorem}  
\begin{theorem}[Mass--energy equivalence]  
$E = mc^2$  
\end{theorem}  
\end{frame}
```

Figure

Uncomment the code on this slide to include your own image from the same directory as the template .TeX file.

An example of the `\cite` command to cite within the presentation:

This statement requires citation [Smith, 2012].



John Smith (2012)

Title of the publication

Journal Name 12(3), 45 – 678.

The End