## Learning Multi-Step Predictive State Representations

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# Predictive State Representations (PSR)

#### Goals:

- Make predictions in partially observable environments
- 2 Learn a representation of hidden states

#### Advantages over HMMs

- Globally optimal predictions
- Smaller representations of state

#### Why Multi-Step PSRs?

- Leverage structure of underlying environment
- Oirectly apply transitions which occur at longer time-scales

# PSR: The single observation case

- PSR defined by:  $\langle \alpha_0, \{A_\sigma\}, \alpha_\infty \rangle$  where  $\alpha_0$  is an initial weighting on states (1xn)  $A_\sigma$  is a transition matrix (nxn)  $\alpha_\infty$  is a normalizer (nx1) n: number of latent states
- ② PSRs compute probabilities of observations  $f(\sigma^k) = \alpha_0 \cdot A_{\sigma}^k \cdot \alpha_{\infty}$

### Spectral Learning of PSRs

Step 1: Represent Data as a Hankel Matrix

Step 2: Singular Value Decomposition

Step 3: Pick Model Size

Step 4: Linear Algebra

Result:  $\langle \alpha_0, \{A_\sigma\}, \alpha_\infty \rangle$ 

## Adding multi-step operators: The Base System

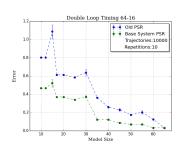
• Learn  $\{A_{\sigma}, A_{\sigma^2}, A_{\sigma^4}, A_{\sigma^8}, ... A_{\sigma^{2N}}\}$  as extra transition operators Operators learned separately so  $A_{\sigma} \cdot A_{\sigma} \neq A_{\sigma^2}$ 

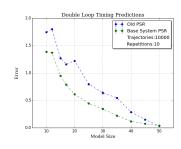
Why might this help? Reduce build up of error Faster computations

# Base System Performance for Loops

64-16 Loop Lengths

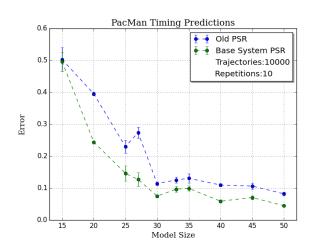
47-27 Loop Lengths





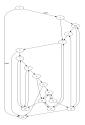


## Pacman-like Labyrinth





(a) Pacman

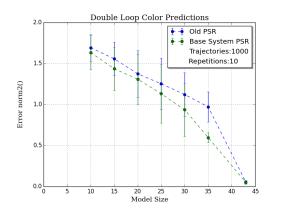


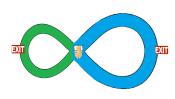
(b) Graph

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#### Wall Color Predictions

We paint the first loop green and the second loop blue





# In general, which operators to learn?

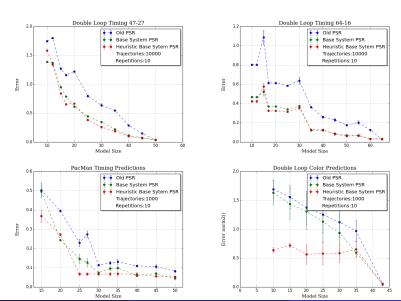
- Observations:  $\{a^{30}b^{15}, a^{60}, b^{15}\}$ Desired operators:  $A_{a^{30}b^{15}}, A_{a^{60}}, A_{a^{30}}, A_{b^{15}}, A_a, A_b$
- Sub-string properties: long, frequent, diverse Structured environments should be easier
- Trade-off between number of operators and learning time Iterative greedy heuristic works well
   Could also try an entropy based approach

#### How should we execute queries

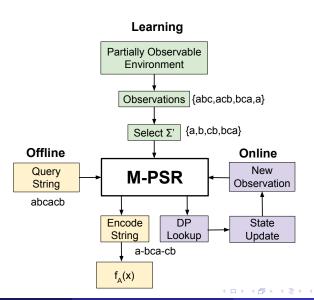
Minimize number of matrices
 Represent transitions as compactly as possible

- ② Query string: "abcacb", Operators =  $\{A_{ab}, A_{bca}, A_{cb}, A_a, A_b\}$ Desired partition: "a—bca—cb" Computation:  $f(abcacb) = \alpha_0 \cdot A_a \cdot A_{bca} \cdot A_{cb} \cdot \alpha_{\infty}$
- Solution: dynamic programming
   State update for online applications

#### Performance of Heuristics



#### The Big Picture



# Questions?