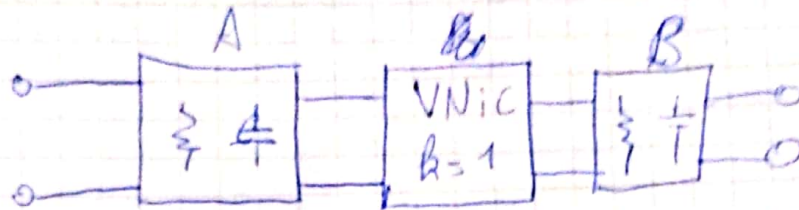


Sintetizar de funciões activas

Tarefas manual 11



$$\begin{pmatrix} V_1 \\ I_1 \end{pmatrix} = \begin{pmatrix} A & B \\ C & D \end{pmatrix} \begin{pmatrix} V_2 \\ -I_2 \end{pmatrix} \rightarrow \begin{pmatrix} -k^{-1} & 0 \\ 0 & -1 \end{pmatrix} \rightarrow T \text{ de VNic}$$

$$T_X = \begin{pmatrix} A_A & B_A \\ C_A & D_A \end{pmatrix} \begin{pmatrix} -k & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} A_B & B_B \\ C_B & D_B \end{pmatrix}$$

$$\frac{V_2}{I_1} \Big|_{I_2=0} = \frac{1}{C_X} \quad \text{OK}$$

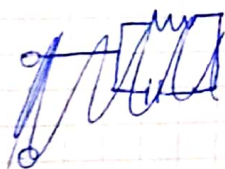
$$T_X = \begin{pmatrix} -k^{-1} A_A & B_A \\ -k^{-1} C_A & D_A \end{pmatrix} \begin{pmatrix} A_B & B_B \\ C_B & D_B \end{pmatrix} \rightarrow C_X = -k^{-1} A_A B_B + D_A C_B$$

$$C_X = k^{-1} \frac{Z_{22A}}{Z_{21A}} \cdot \frac{1}{Z_{21B}} - \frac{1}{Z_{21A}} \cdot \frac{Z_{11B}}{Z_{21B}}$$

$$\frac{1}{C_X} = \frac{Z_{21A} Z_{21B}}{k^{-1} Z_{22A} - Z_{11B}}$$

$$\frac{V_2}{I_1} \Big|_{I_2=0} = \frac{k Z_{21A} Z_{21B}}{Z_{22A} - k Z_{11B}}$$

b)



$$H(s) = \frac{1}{(s+1)(s^2+s+1)} = \frac{N(s)}{D(s)}$$

$$Q(s) = s(s+\frac{1}{2})(s+2) \rightarrow \text{arbitrario } (G_N(s) = G_N(D))$$

$$\frac{D(s)}{Q(s)} = K_0 + \frac{K_1}{s} + \frac{K_2}{s+\frac{1}{2}} + \frac{K_3}{s+2} = \frac{(s+1)(s^2+s+1)}{s(s+\frac{1}{2})(s+2)}$$

$$K_0 = \lim_{s \rightarrow \infty} = 1$$

$$K_1 = \lim_{s \rightarrow 0} s \frac{D(s)}{Q(s)} = 1$$

$$K_2 = \lim_{s \rightarrow -\frac{1}{2}} (s+\frac{1}{2}) \frac{D(s)}{Q(s)} = -\frac{1}{2}$$

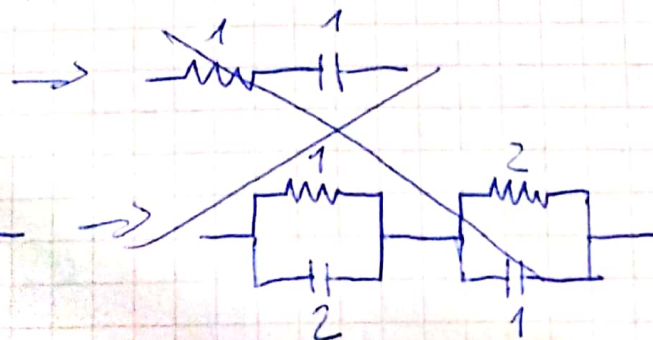
$$K_3 = \lim_{s \rightarrow -2} (s+2) \frac{D(s)}{Q(s)} = -1$$

} Z_{22A}

} Z_{11B} (porque con (-))

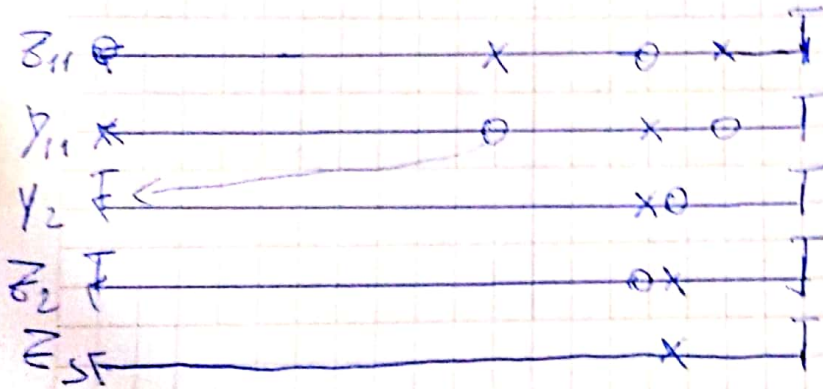
$$Z_{22A} = 1 + \frac{1}{s}$$

$$Z_{11B} = \frac{\frac{1/2}{s+\frac{1}{2}}}{1} + \frac{1}{s+2} = \frac{1}{2s+1}$$



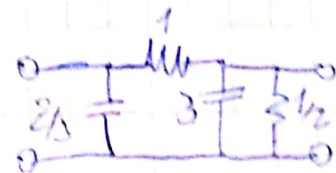
$$Z_{11B} = \frac{1,5(s+1)}{(s+2)(s+\frac{1}{2})} = \frac{1,5s+1,5}{s^2+s\frac{5}{2}+1}$$

$$Z_{21B} = \frac{K}{(s+\frac{1}{2})(s+2)}$$



$$\frac{s^2 + s\frac{5}{2} + 1}{1,5s + 1,5} \cdot \frac{1,5s + 1,5}{\frac{2,5}{3}} \rightarrow C \frac{1}{3}$$

$$\frac{3/2s + 1}{1/2} \cdot \frac{1/2}{3s} \rightarrow \frac{1}{3s} \rightarrow \frac{1}{s} \rightarrow \frac{1}{0,5}$$



$$Z_{22A} = 1 + \frac{1}{s}$$

$$Z_{21A} = \frac{1}{s}$$

