

$$f) H(z) = (1 - C, z^{-N}) \frac{b_0 + b_1 z^{-1} + b_2 z^{-2}}{\frac{1}{a_0} - a_1 z^{-1} - a_2 z^{-2}}; \quad \begin{matrix} a_0 = 1 & b_0 = R & R = \frac{-D}{D+2} \\ a_1 = -R & b_1 = 1 \\ a_2 = 0 & b_2 = 0 & D \in [-0,5; +0,5] \\ C = 0 \end{matrix}$$

$$\hookrightarrow H(z) = \frac{R + z^{-1}}{1 + R z^{-1}} \Rightarrow H(e^{-j\Omega}) = \frac{R - 1 + 1 + e^{-j\Omega}}{1 + e^{-j\Omega} + (R-1)e^{-j\Omega}} = \frac{e^{j\Omega/2} + e^{-j\Omega/2} + (R-1)e^{j\Omega/2}}{e^{j\Omega/2} + e^{-j\Omega/2} + (R-1)e^{j\Omega/2}} =$$

$$H(e^{j\Omega}) = \frac{2\cos(\Omega/2) + (R-1)\cos(\Omega/2) + j(R-1)\sin(\Omega/2)}{2\cos(\Omega/2) + (R-1)\cos(\Omega/2) - j(R-1)\sin(\Omega/2)} =$$

$$= \frac{(R+1)\cos(\Omega/2) + j(R-1)\sin(\Omega/2)}{(R+1)\cos(\Omega/2) - j(R-1)\sin(\Omega/2)}$$

$$\hookrightarrow |H(\Omega)|^2 = \frac{(R+1)^2 \cos^2(\Omega/2) + (R-1)^2 \sin^2(\Omega/2)}{(R+1)^2 \cos^2(\Omega/2) + (R-1)^2 \sin^2(\Omega/2)} = 1 \Rightarrow |H(\Omega)| = 1$$

$$\underline{\varphi(\Omega)} = \arctg\left[\frac{R-1}{R+1} \tan(\Omega/2)\right] + \arctg\left[-\frac{R-1}{R+1} \tan(\Omega/2)\right] = \underline{2\arctg\left[\frac{R-1}{R+1} \tan(\Omega/2)\right]}$$

$$-\frac{d\varphi(\Omega)}{d\Omega} = \tau_c(\Omega) = -\cancel{1} \frac{1}{1 + \frac{(R-1)^2}{(R+1)^2} \tan^2(\Omega/2)} \cdot \left(\frac{R-1}{R+1}\right) \frac{1}{\cancel{1} \cos^2(\Omega/2)} =$$

$$= \frac{1-R}{1+R} \frac{1}{\cos^2(\Omega/2) + \left(\frac{1-R}{1+R}\right)^2 \sin^2(\Omega/2)}; \quad R = \frac{-D}{D+2} \Rightarrow \frac{1-R}{1+R} = \frac{1 + \frac{D}{D+2}}{1 - \frac{D}{D+2}} =$$

$$= \frac{2D+2}{2} = D+1$$

$$\Rightarrow \underline{\tau_c(\Omega)} = \frac{1}{\frac{1}{D+1} \cos^2(\Omega/2) + (D+1) \sin^2(\Omega/2)}$$

$$\hookrightarrow \Omega = 0 \rightarrow \underline{\tau_c(\Omega=0) = D+1}$$

MARGEN 5% RESPECTO DE $\tau_c(\Omega=0) = D+1$

$$0,95 < \frac{\tau_c(\Omega)}{\tau_c(0)} < 1,05$$

$$0,95 < \frac{1}{\frac{1}{D+1} \cos^2(\Omega/2) + (D+1) \sin^2(\Omega/2)} < 1,05$$

$$0,95 < \frac{1}{\cos^2(\Omega/2) + (D+1)^2 \sin^2(\Omega/2)} < 1,05$$

$$\frac{20}{19} > \cos^2(\Omega/2) + (D^2+2D) \sin^2(\Omega/2) + \sin^2(\Omega/2) < \frac{20}{21}$$

$$\frac{20}{19} > 1 + (D^2+2D) \sin^2(\Omega/2) > \frac{20}{21}$$

$$\rightarrow \frac{1}{19} > (D^2+2D) \sin^2(\Omega/2) > -\frac{1}{21}$$

$$\hookrightarrow \sin^2(\Omega/2) \geq 0$$

$$\hookrightarrow (D^2+2D) \begin{cases} > 0 & \text{si } D > 0 \\ < 0 & \text{si } D < 0 \\ = 0 & \text{si } D = 0 \end{cases}$$

$$\hookrightarrow \underline{D \geq 0} \Rightarrow \Omega < 2 \arccos \left[\sqrt{\frac{1}{19(D^2+2D)}} \right]$$

$$\hookrightarrow \underline{D < 0} \Rightarrow \Omega > 2 \arccos \left[\sqrt{\frac{1}{-21(D^2+2D)}} \right]$$