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$$a) \frac{d}{du} (u^5) \cdot \frac{d}{dy} (u) = y' = 5u^4 \cdot 2$$

$$y' = 5(2x+1)^4 \cdot 2$$

$$b) \frac{d}{du} (u^9) \cdot \frac{d}{dx} (y-3x) = y' = 9u^8 \cdot (-3)$$

$$y' = 9(4-3x)^8 \cdot (-3)$$

$$c) \frac{d}{du} (u^{-7}) \cdot \frac{d}{dx} \left(7 - \frac{x}{7}\right) = y' = 7u^{-8} \cdot \left(-\frac{1}{7}\right)$$

$$y' = 7\left(7 - \frac{x}{7}\right)^{-8} \cdot \left(-\frac{1}{7}\right)$$

$$d) \frac{d}{du} (u^{-10}) \cdot \frac{d}{dx} \left(\frac{x}{2} - 1\right) = y' = -10u^{-11} \cdot \frac{1}{2}$$

$$y' = -10 \cdot \left(\frac{x}{2} - 1\right)^{-11} \cdot \frac{1}{2}$$

$$e) \frac{d}{du} (u^4) \cdot \frac{d}{dx} \left(\frac{x^2}{8} + x - \frac{1}{x}\right) = (4u)^3 \cdot \left(\frac{1}{4}x + 1 - \frac{1}{x^2}\right) =$$

$$4\left(\frac{x^2}{8} + x - \frac{1}{x}\right)^3 \cdot \left(\frac{1}{4}x + 1 - \frac{1}{x^2}\right)$$

$$f) \frac{d}{du} (\sqrt{u}) \cdot \frac{d}{dx} (3x^2 - 4x + 6) = \frac{1}{2\sqrt{u}} \cdot (3 \cdot 2x - 4)$$

$$= \frac{1}{2\sqrt{3x^2 - 4x + 6}} \cdot (3 \cdot 2x - 4)$$

$$g) \frac{d}{du} (\sec(u)) \cdot \frac{d}{dx} (tg(x)) = tg(u) \cdot \sec(u) \cdot \sec^2 x$$

$$= tg(tg(x)) \cdot \sec(tg(x)) \cdot \sec^2 x$$

$$h) \frac{d}{du} (\cotg(u)) \cdot \frac{d}{dx} \left(\pi - \frac{1}{x} \right) = -\operatorname{cosec}^2 u \cdot \frac{1}{x^2} \\ = -\operatorname{cosec}^2 \left(\pi - \frac{1}{x} \right) \cdot \frac{1}{x^2}$$

$$i) \frac{d}{du} (u^3) \cdot \frac{d}{dx} \operatorname{sen}(x) = 3u^2 \cdot \cos(x) \\ = 3 \operatorname{sen}(x)^2 \cdot \cos(x)$$

$$j) 5 \cdot \frac{d}{du} (u^{-4}) \cdot \frac{d}{dx} (\cos(x)) = 5 \cdot -4u^{-5} \cdot (-\operatorname{sen}(x)) \\ = 5 \cdot (-4 \cos(x))^{-5} \cdot (-\operatorname{sen}(x))$$

$$k) \frac{d}{du} (e^u) \cdot \frac{d}{dx} (-5x) = e^u \cdot -5 = e^{-5x} \cdot (-5)$$

$$l) \frac{d}{du} (e^u) \cdot \frac{d}{dx} \left(\frac{2x}{3} \right) = e^u \cdot \frac{2}{3} = e^{\frac{2x}{3}} \cdot \frac{2}{3}$$

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$$a) \frac{d}{du} (6u-9) \cdot \frac{d}{dx} \left(\left(\frac{1}{2} \right) \cdot x^4 \right) = 6 \cdot 2x^3$$

$$b) \frac{d}{du} (2u^3) \cdot \frac{d}{dx} (8x-1) = 6u^2 \cdot 8 = 6 \cdot (8x-1)^2 \cdot 8$$

$$c) \frac{d}{du} (\operatorname{sen}(u)) \cdot \frac{d}{dx} (3x+1) = \cos(u) \cdot 3 = \cos(3x+1) \cdot 3$$

$$d) \frac{d}{du} (\cos(u)) \cdot \frac{d}{dx} \left(-\frac{x}{3} \right) = -\operatorname{sen}(u) \cdot \left(-\frac{1}{3} \right) = -\operatorname{sen} \left(-\frac{x}{3} \right) \cdot \left(-\frac{1}{3} \right)$$

$$e) \frac{d}{du} (\cos(u)) \cdot \frac{d}{dx} (\sin(x)) = -\sin(x) \cos(x) \\ -\sin(\sin(x)) \cdot \cos(x)$$

12-

$$a) \frac{d}{dx} 2 \cdot f(x) = \frac{1}{3}$$

$$d) \frac{d}{dx} \cdot \frac{f(x)}{g(x)} = \frac{\frac{1}{3} \cdot 2 - 8 \cdot -3}{2^2}$$

$$b) \frac{d}{dx} f(x) + g(x) = 2\pi + 5$$

$$e) \frac{d}{dx} f(g(x)) = \frac{1}{3} \left(\frac{2}{1} \right) \cdot (-3)$$

$$c) \frac{d}{dx} f(x) \cdot g(x) = 2\pi \cdot -4 + 3 \cdot 5 \\ = 2\pi \cdot -4 + 15$$

$$f) \frac{d}{du} (v_u) \cdot \frac{d}{dx} (f(x)) = \frac{1}{2v_x} \cdot \frac{1}{3}$$

$$g) \frac{d}{du} \left(\frac{1}{u} \right) \cdot \frac{d}{dx} (g^2(x)) = -\frac{1}{u^2} \cdot 5^2 = \frac{-1}{g^2(x)} \cdot 5^2$$

$$h) \frac{d}{du} (v_u) \cdot \frac{d}{dx} (f^2(x) + g^2(x)) = \frac{1}{2v_g} - \frac{7}{3} \cdot 2 - 3$$