Twisted escaped radial (TER) configuration calculations

Lucas Myers

February 14, 2024

1 Frank free energy

Parameters α and β are defined so that the director $\hat{\mathbf{n}}$ is given by:

$$\hat{\mathbf{n}} = \cos \alpha \sin \beta \,\hat{\mathbf{r}} + \sin \alpha \sin \beta \,\hat{\boldsymbol{\varphi}} + \cos \beta \,\hat{\mathbf{z}} \tag{1}$$

Then the corresponding Frank free energy is given by:

$$F = \frac{1}{2r^2} \left[K_1 \left(-r\sin\left(\alpha\right)\sin\left(\beta\right)\alpha_r + r\cos\left(\alpha\right)\cos\left(\beta\right)\beta_r + \sin\left(\beta\right)\cos\left(\alpha\right) \right)^2 + \frac{K_2}{16} \left(-r\sin\left(\alpha - 2\beta\right)\alpha_r + r\sin\left(\alpha + 2\beta\right)\alpha_r + 4r\sin\left(\alpha\right)\beta_r + \cos\left(\alpha - 2\beta\right) - \cos\left(\alpha + 2\beta\right) \right)^2 + K_3\sin^2\left(\beta\right) \left(-r^2\sin^2\left(\alpha\right)\sin^2\left(\beta\right)\left(\alpha_r\right)^2 - r^2\sin^2\left(\alpha\right)\left(\beta_r\right)^2 + r^2\sin^2\left(\beta\right)\left(\alpha_r\right)^2 + r^2\sin^2\left(\beta\right)\sin^2\left(\beta\right)\cos\left(\alpha\right)\alpha_r + \sin^2\left(\alpha\right)\sin^2\left(\beta\right) \right) \right]$$

$$\left. + r^2\left(\beta_r\right)^2 + 2r\sin\left(\alpha\right)\sin^2\left(\beta\right)\cos\left(\alpha\right)\alpha_r + \sin^2\left(\alpha\right)\sin^2\left(\beta\right) \right) \right]$$

$$(2)$$