

One patch, with and without effect of microbes on pollinators

This creates phase plane and time series plots for one-plant model with and without feedbacks between microbes and pollinators, and with low and high yeast dispersal rates (keeping bacterial dispersal rates constant).

Load package and set working directory:

```
In[ ]:= Needs["EcoEvo`"];  
SetDirectory[NotebookDirectory[]];  
SetDirectory[ParentDirectory[] <> "_figures/_raw-nb"];
```

Define model in EcoEvo:

```
In[ ]:= SetModel[{Pop[Y] → {Equation ⇒ dy disp[B, h, S0, L0] Y (1 - Y - B) - m Y,  
    Range ⇒ Interval[{0, 1}], Color → RGBColor["#FFCC33"]},  
    Pop[B] → {Equation ⇒ (db0 + db disp[B, h, S0, L0]) B (1 - Y - B) - m B,  
    Range ⇒ Interval[{0, 1}], Color → RGBColor["#333399"]},  
    Parameters ⇒ {dy ≥ 0, db0 ≥ 0, db ≥ 0, h ≥ 0, L0 ≥ 0, m ≥ 0, S0 ≥ 0}}];  
disp[B_, h_, S0_, L0_] := Module[{P},  
    P = S0^h / (S0^h + B^h);  
    P / (L0 + P)  
];
```

Create functions used throughout and define unchanging parameter values:

```

In[ ]:= Pvec[S0_, h_, L0_, t_, simBFun_] = disp[simBFun[t], h, S0, L0];
timeseriesPlot[maxt_?NumericQ, hiStart_?NumericQ, loStart_?NumericQ] :=
Module[{sim1, sim2, simp1, simp2, p1, p2, pp1, pp2},
  sim1 = EcoSim[{Y → hiStart, B → loStart}, maxt];
  sim2 = EcoSim[{Y → loStart, B → hiStart}, maxt];
  simp1 = PlotDynamics[sim1, AxesLabel → None];
  simp2 = PlotDynamics[sim2, AxesLabel → None];
  p1 = Plot[Pvec[S0, h, L0, t, sim1[[2]][[2]]],
    {t, 0, maxt}, PlotStyle → Directive[Thick, Gray, Dashed],
    AspectRatio → 0.85, PlotRange → {Automatic, {0, 1}}];
  p2 = Plot[Pvec[S0, h, L0, t, sim2[[2]][[2]]],
    {t, 0, maxt}, PlotStyle → Directive[Thick, Gray, Dashed],
    AspectRatio → 0.85, PlotRange → {Automatic, {0, 1}}];
  pp1 = Show[p1, simp1, PlotRange → {Automatic, {0, 1}}, AxesOrigin → {0, 0}];
  pp2 = Show[p2, simp2, PlotRange → {Automatic, {0, 1}}, AxesOrigin → {0, 0}];
  GraphicsRow[{pp1, pp2}, ImageSize → Medium]
];

db = 0.4;
db0 = 0.3;
m = 0.1;
S0 = 0.4;

```

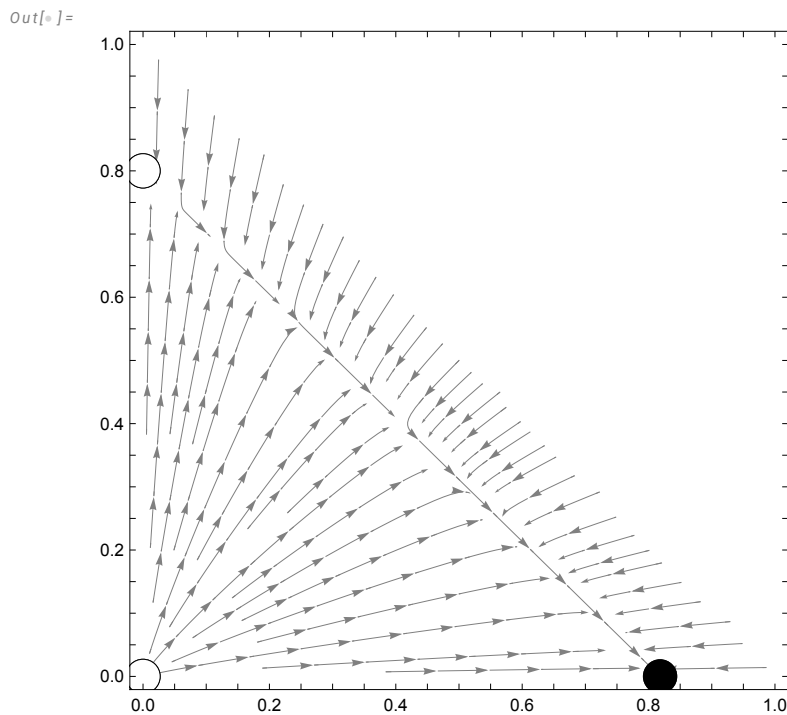
Phase planes and time series plots

No feedbacks, high yeast dispersal

```

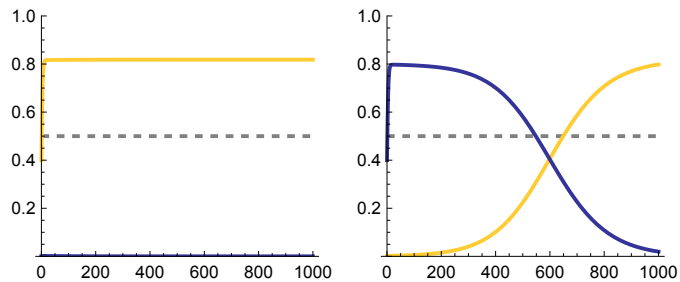
In[ ]:= Clear[h, dy, L0];
h = 0.0; dy = 1.1; L0 = 0.5;
p = PlotEcoPhasePlane[ {Y, 0, 1}, {B, 0, 1},
  IsoclineStyle -> {Opacity[0], Opacity[0]},
  RuleListPlotOpts -> {StableMarker ->
    {Graphics[{Black, Disk[{0, 0}]}], ImageSize -> 20, AlignmentPoint -> {0, 0}}},
    UnstableMarker -> {Graphics[{EdgeForm[{Black}], FaceForm[White], Disk[{0, 0}]}],
      ImageSize -> 20, AlignmentPoint -> {0, 0}}},
  FrameLabel -> None,
  RegionFunction -> Function[{Y, B}, 0 ≤ Y + B ≤ 1]]
Export[File["1patch-h0-dy1.1-phase.pdf"], p];
Clear[p];

```



```
In[ ]:= Clear[h, dy, L0];  
h = 0.0; dy = 1.1; L0 = 0.5;  
combinedPlot = timeseriesPlot[1000, 0.4, 0.001]  
Export[File["1patch-h0-dy1.1-timeseries.pdf"], combinedPlot];  
Clear[combinedPlot];
```

Out[]=

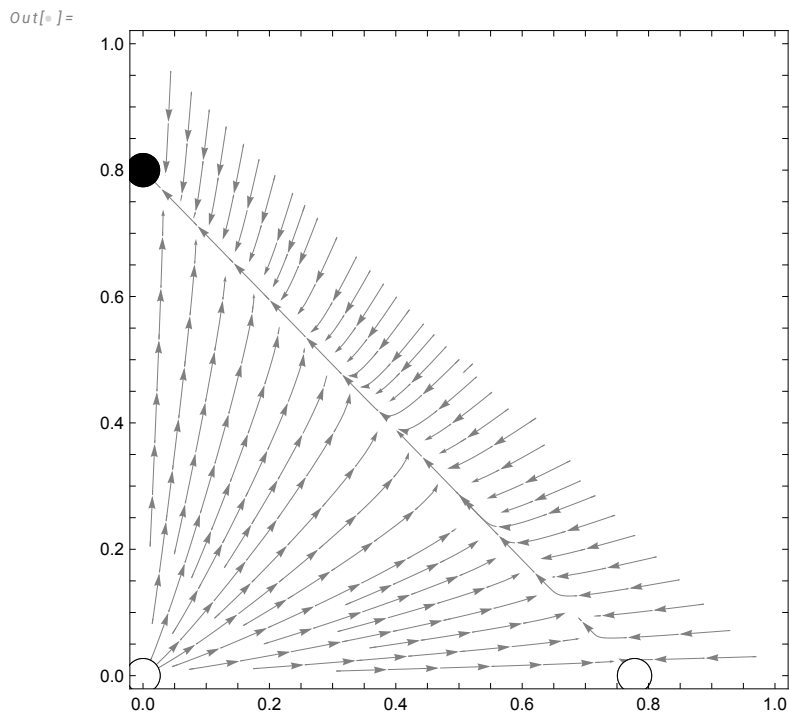


No feedbacks, low yeast dispersal

```

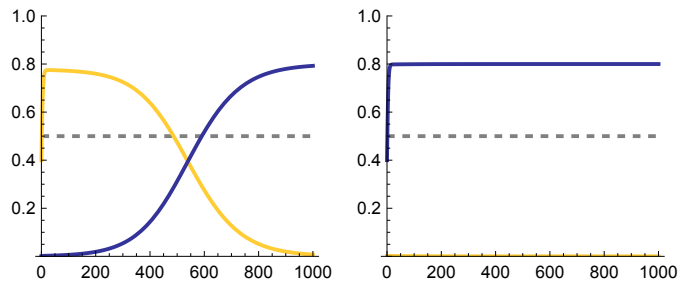
In[ ]:= Clear[h, dy, L0];
h = 0.0; dy = 0.9; L0 = 0.5;
p = PlotEcoPhasePlane[ {Y, 0, 1}, {B, 0, 1},
  IsoclineStyle → {Opacity[0], Opacity[0]},
  RuleListPlotOpts → {StableMarker →
    {Graphics[{Black, Disk[{0, 0}]}], ImageSize → 20, AlignmentPoint → {0, 0}}},
    UnstableMarker → {Graphics[{EdgeForm[{Black}], FaceForm[White], Disk[{0, 0}]}],
      ImageSize → 20, AlignmentPoint → {0, 0}}},
  FrameLabel → None,
  RegionFunction → Function[{Y, B}, 0 ≤ Y + B ≤ 1]]
Export[File["1patch-h0-dy0.9-phase.pdf"], p];
Clear[p];

```



```
In[ ]:= Clear[h, dy, L0];  
h = 0.0; dy = 0.9; L0 = 0.5;  
combinedPlot = timeseriesPlot[1000, 0.4, 0.001]  
Export[File["1patch-h0-dy0.9-timeseries.pdf"], combinedPlot];  
Clear[combinedPlot];
```

Out[]=

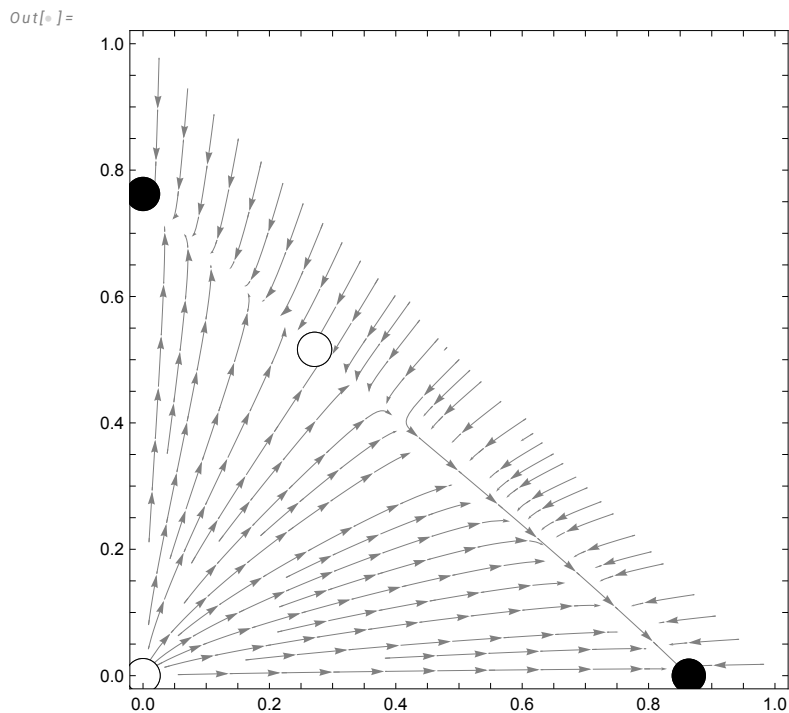


With feedbacks, high yeast dispersal

```

In[ ]:= Clear[h, dy, L0];
h = 2.0; dy = 1.1; L0 = 0.5;
p = PlotEcoPhasePlane[ {Y, 0, 1}, {B, 0, 1},
  IsoclineStyle → {Opacity[0], Opacity[0]},
  RuleListPlotOpts → {StableMarker →
    {Graphics[{Black, Disk[{0, 0}]}], ImageSize → 20, AlignmentPoint → {0, 0}}},
    UnstableMarker → {Graphics[{EdgeForm[{Black}], FaceForm[White], Disk[{0, 0}]}],
      ImageSize → 20, AlignmentPoint → {0, 0}}},
  FrameLabel → None,
  RegionFunction → Function[{Y, B}, 0 ≤ Y + B ≤ 1]]
Export[File["1patch-h2-dy1.1-phase.pdf"], p];
Clear[p];

```

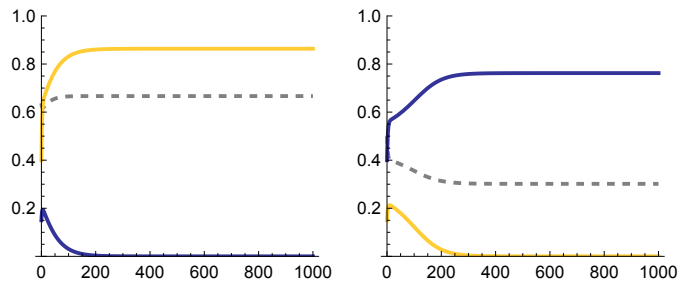


```

In[ ]:= Clear[h, dy, L0];
h = 2.0; dy = 1.1; L0 = 0.5;
combinedPlot = timeseriesPlot[1000, 0.4, 0.15]
Export[File["1patch-h2-dy1.1-timeseries.pdf"], combinedPlot];
Clear[combinedPlot];

```

Out[]=

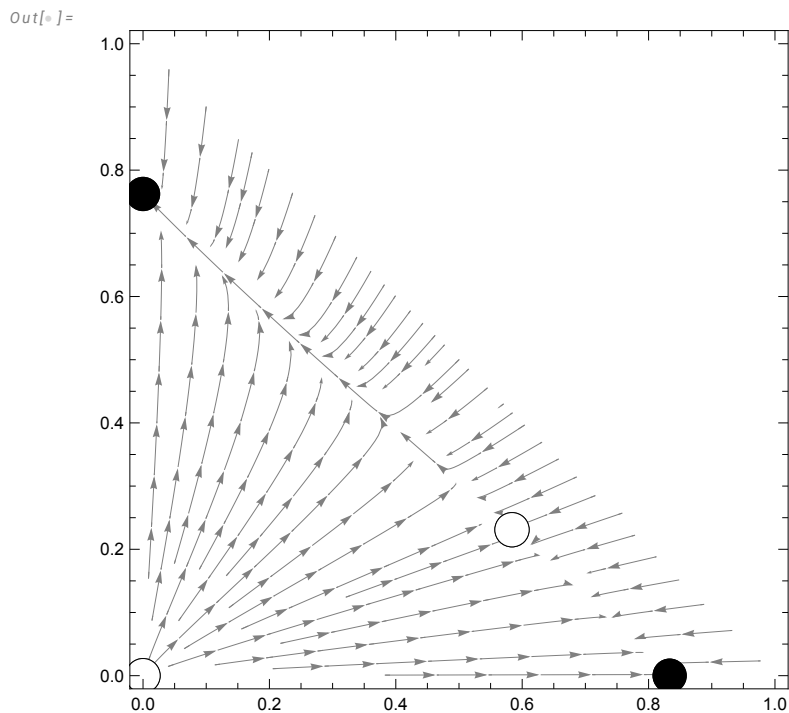


With feedbacks, low yeast dispersal

```

In[ ]:= Clear[h, dy, L0];
h = 2.0; dy = 0.9; L0 = 0.5;
p = PlotEcoPhasePlane[ {Y, 0, 1}, {B, 0, 1},
  IsoclineStyle → {Opacity[0], Opacity[0]},
  RuleListPlotOpts → {StableMarker →
    {Graphics[{Black, Disk[{0, 0}]}], ImageSize → 20, AlignmentPoint → {0, 0}}},
    UnstableMarker → {Graphics[{EdgeForm[{Black}], FaceForm[White], Disk[{0, 0}]}],
      ImageSize → 20, AlignmentPoint → {0, 0}}},
  FrameLabel → None,
  RegionFunction → Function[{Y, B}, 0 ≤ Y + B ≤ 1]]
Export[File["1patch-h2-dy0.9-phase.pdf"], p];
Clear[p];

```



```

In[ ]:= Clear[h, dy, L0];
h = 2.0; dy = 0.9; L0 = 0.5;
combinedPlot = timeseriesPlot[1000, 0.4, 0.15]
Export[File["1patch-h2-dy0.9-timeseries.pdf"], combinedPlot];
Clear[combinedPlot];

```

Out[]=

