

1. The *Stokes number*, St , used in particle-dynamics studies, is a dimensionless combination of *five* variables: acceleration of gravity g , viscosity μ , density ρ , particle velocity U , and particle diameter D . (a) If St is proportional to μ and inversely proportional to g , find its form. (b) Show that St is actually the quotient of two more traditional dimensionless groups.
2. A pendulum has an oscillation period T which is assumed to depend upon its length L , bob mass m , angle of swing θ , and the acceleration of gravity. A pendulum 1 m long, with a bob mass of 200g, is tested on earth and found to have a period of 2.04s when swinging at 20° . (a) What is its period when it swings at 45° ? A similarly constructed pendulum, with $L = 30$ cm and $m = 100$ g, is to swing on the moon ($g = 1.62$ m/s²) at $\theta = 20^\circ$. (b) What will be its period?
3. Use dimensional analysis to determine the energy E released in an intense point blast if the blastwave propagation distance D into an undisturbed atmosphere of density ρ is known as a function of time t following the energy release.



4. To good approximation, the thermal conductivity k of a gas depends only on the density ρ , mean free path l , gas constant R , and absolute temperature T . For air at 20°C and 1 atm, $k \approx 0.026$ W/(m \cdot K) and $l \approx 6.5\text{E}-8$ m. Use this information to determine k for hydrogen at 20°C and 1 atm if $l \approx 1.2\text{E}-7$ m.
5. A student needs to measure the drag on a prototype of characteristic length d_p moving at velocity U_p in air at sea-level conditions. He constructs a model of characteristic length d_m , such that the ratio $d_p/d_m = a$ factor f . He then measures the model drag under dynamically similar conditions, in sea-level air. The student claims that the drag force on the prototype will be identical to that of the model. Is this claim correct? Explain.