

Análise de Sistemas de Potência

Aula 01: Introdução ao SEP

Prof. Lucas Melo

Universidade Federal do Ceará

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Sumário

Apresentação

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**Lucas S. Melo, Dr.
Prof. Adjunto**

**Departamento de Engenharia Elétrica - UFC
Grupo de Redes Elétricas Inteligentes - GREI**



lucassmelo@dee.ufc.br



<https://lucassm.pro>

Áreas de Interesse na Pesquisa

- ▶ Recursos Energéticos Distribuídos - Modelagem, Simulação e Controle;
- ▶ Aplicação de Co-simulação em sistemas elétricos de potência;
- ▶ Aplicação de técnicas de otimização em sistemas elétricos de potência
- ▶ Automação/Proteção de Sistemas de Distribuição (IEC 61850);
- ▶ Sistemas de energia transativos.

Apresentação: GREI



Professores pesquisadores:

- ▶ Profa. Ruth Leão (UFC)
- ▶ Prof. Raimundo Furtado (UFC)
- ▶ Profa. Raquel Gregory (UFC)
- ▶ Prof. Lucas Melo (UFC)

Apresentação: GREI

Pesquisas desenvolvidas com projetos e artigos publicados nas áreas de:

- ▶ Automação da distribuição;
- ▶ Microrredes;
- ▶ Medição inteligente;
- ▶ Geração distribuída;
- ▶ Gestão de ativos;
- ▶ Armazenamento de energia; e
- ▶ Resposta à demanda;
- ▶ Entre outros.

Apresentação: GREI

Projetos atuais:

- ▶ CNPq: Co-simulação de Sistemas de Controle Transativos na Rede de Distribuição de Energia Elétrica;
- ▶ Funcap: Automação da Rede Elétrica;
- ▶ Funcap: Hidrogênio Verde.

Mais Informações

Página web com informações sobre as atividades do GREI



<https://www.grei-ufc.github.io>

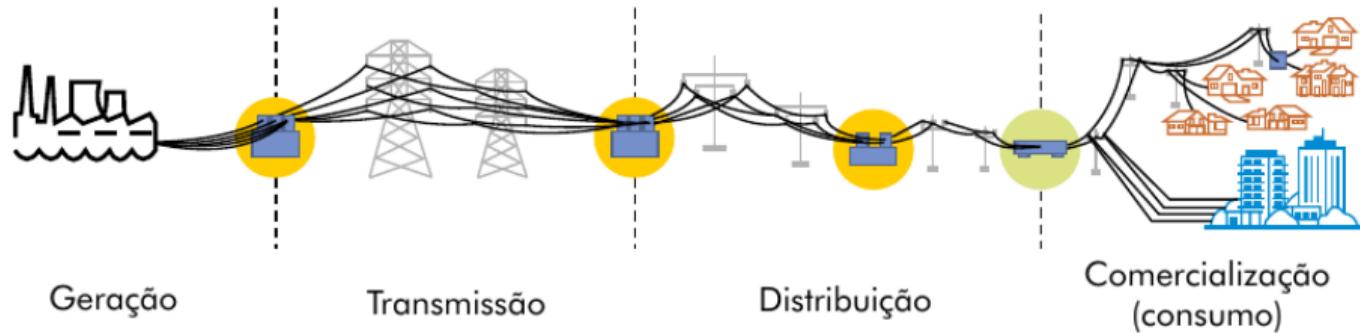
Apresentação: ASP

Página web com todas as informações sobre a disciplina de ASP



<https://www.lucassm.pro/teaching/ASP>

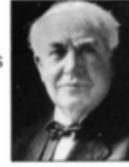
O Sistema Elétrico de Potência



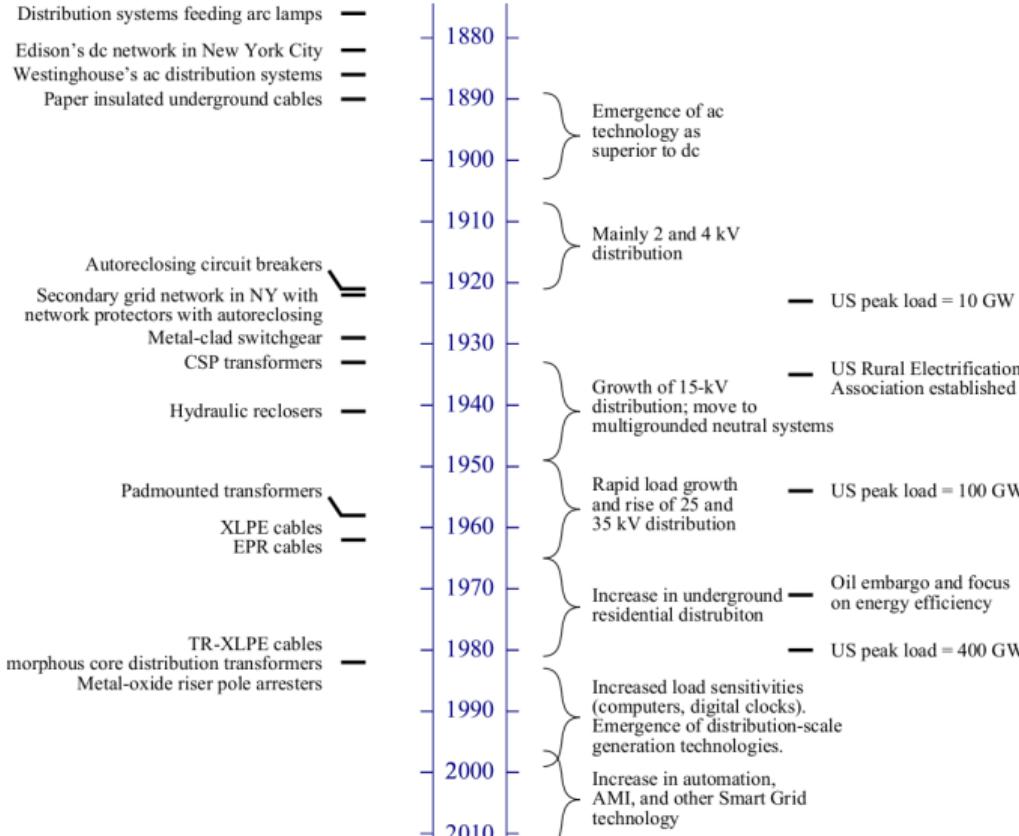
Histórico do SEP

- ▶ Telegraphic Lines (First Economic exploration of electricity): First trans-oceanic cable in (1858) 1866;
- ▶ DC systems;
- ▶ AC systems;
- ▶ Three-Phase Lines;
- ▶ Power Plants and Transmission Lines.

Histórico do SEP

	Waterwheel-driven dc generator installed in Appleton, Wisconsin	1882	Thomas A. Edison opens Pearl St. Station, NYC	
	Frank J. Sprague produces dc motor for Edison systems	1882	First transmission lines installed in Germany (2400 V dc, 59 km)	
	Nikola Tesla presents paper on two-phase ac induction and synchronous motors	1884	William Stanley develops commercially practical transformer	
		1885/6		
		1888		
		1889	First single-phase ac transmission line in United States, in Oregon: Oregon City to Portland (4 kV, 21 km)	
	First three-phase ac transmission line in Germany (12 kV, 179 km)	1891		
		1893	First three-phase ac transmission line in United States, in California (2.3 kV, 12 km)	

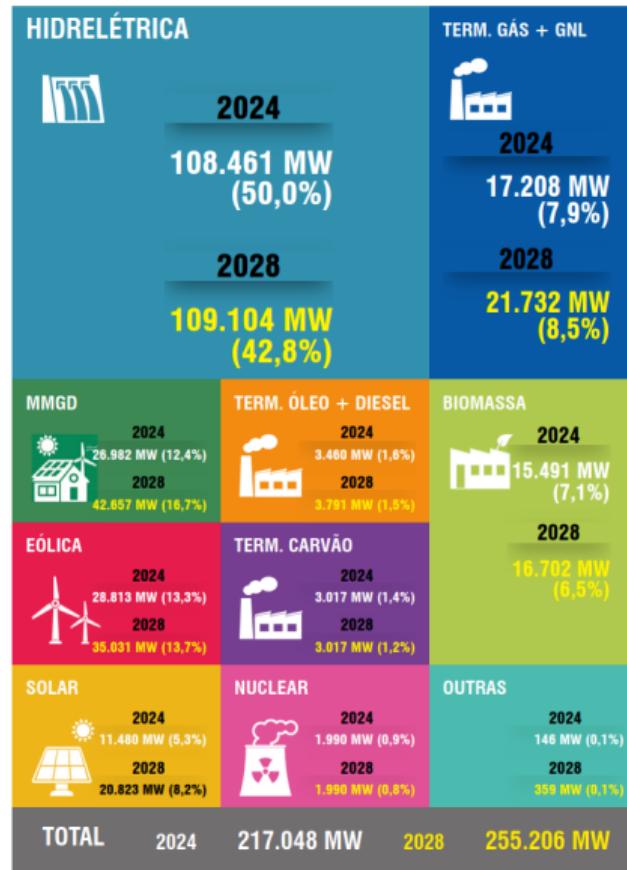
Histórico do SEP



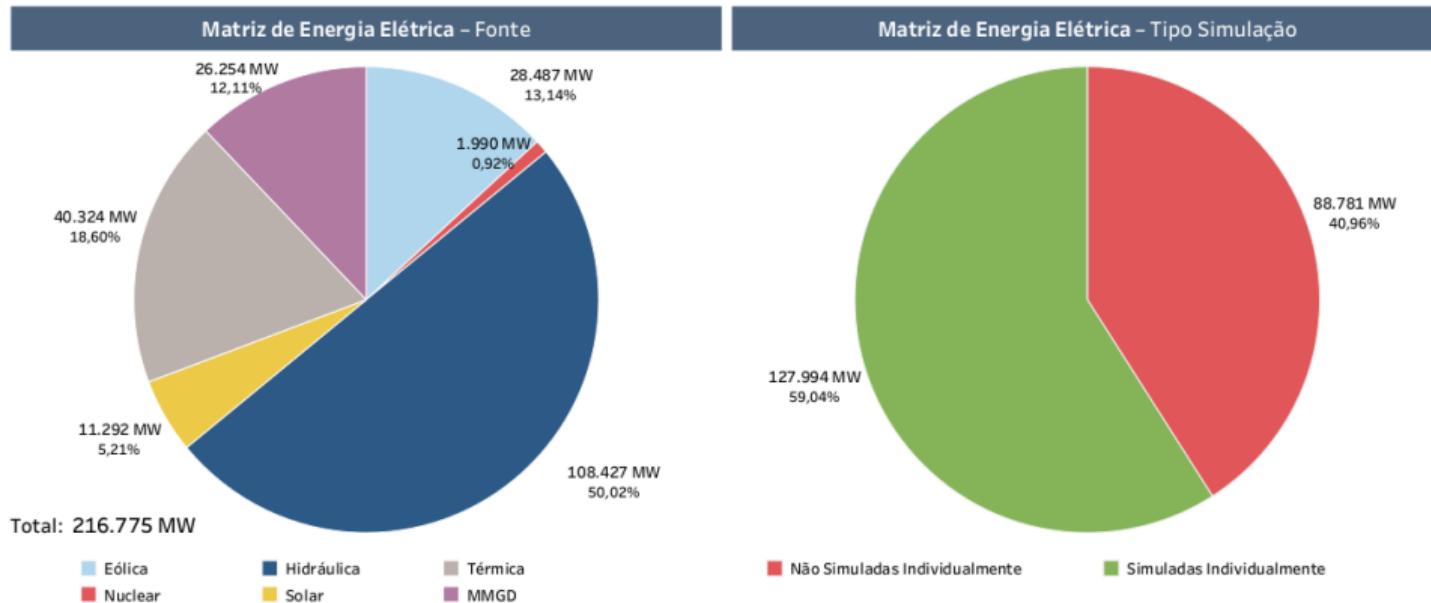
Generation

- ▶ Water Powered (Hydro) Turbine Plants;
- ▶ Steam Powered Turbine Plants: Coal, Nuclear, Gas;
- ▶ Renewable Energy: include conventional hydroelectric, geothermal, wood, wood waste, all municipal waste, landfill gas, other biomass, solar, and wind power.

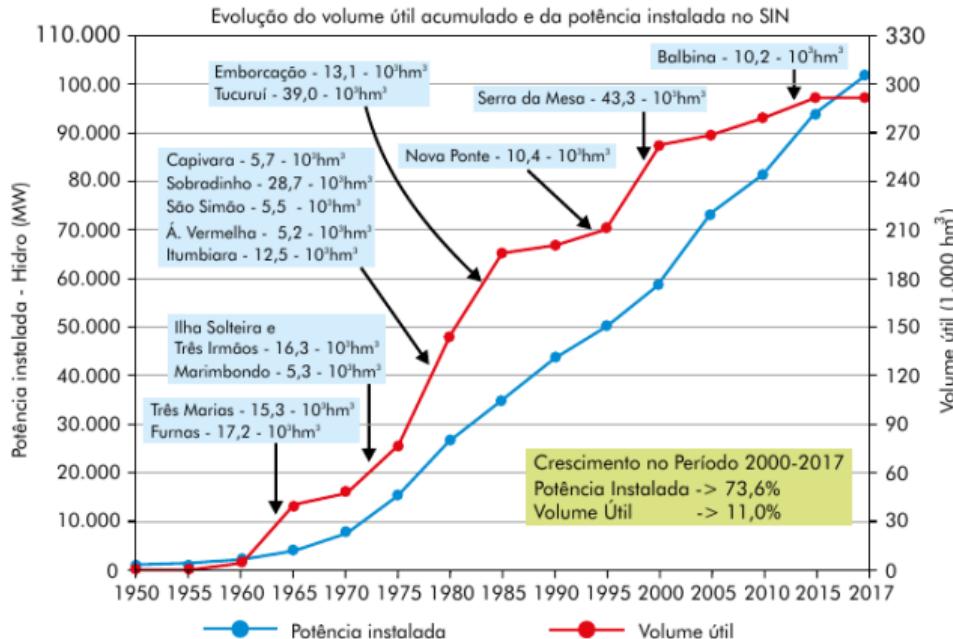
Evolução da Capacidade Instalada no SIN - Fevereiro 2024 / Dezembro 2028



Generation



Generation



Generation

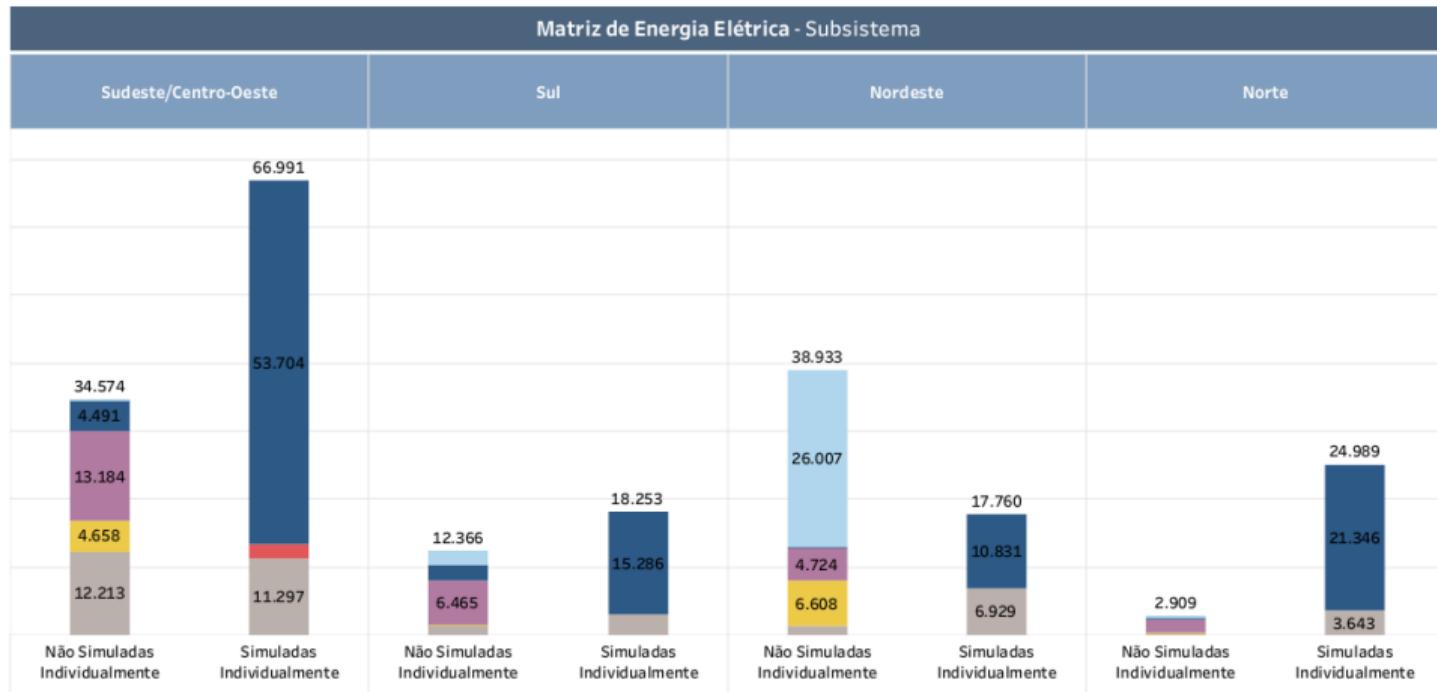
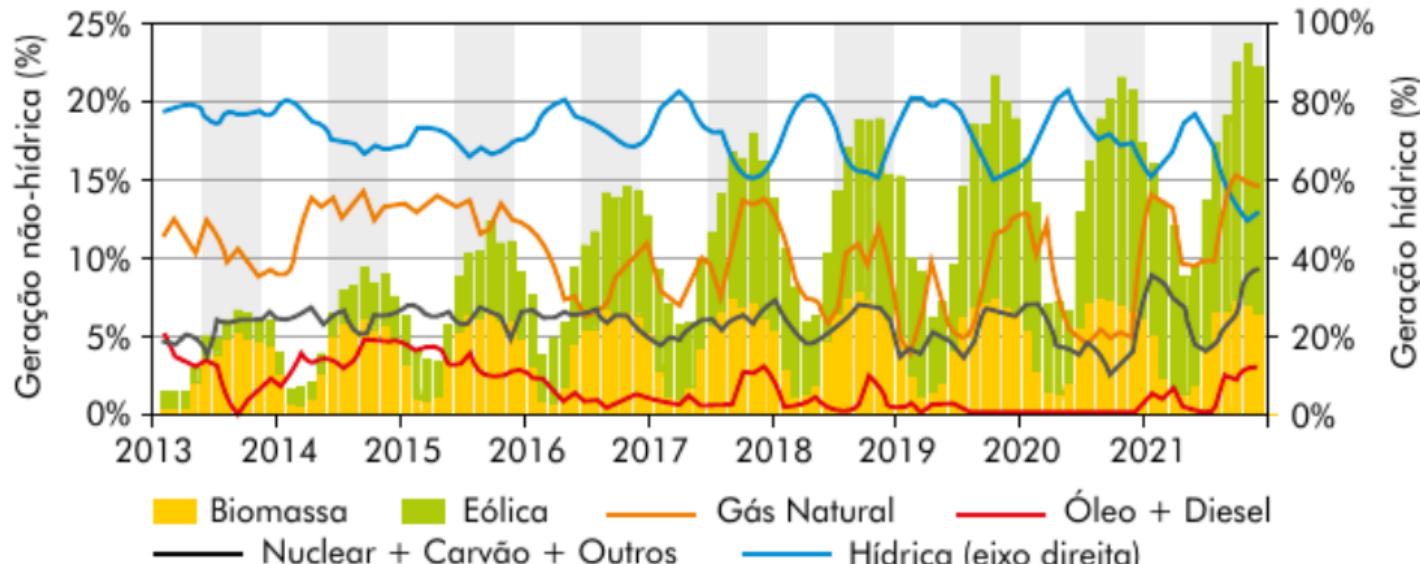
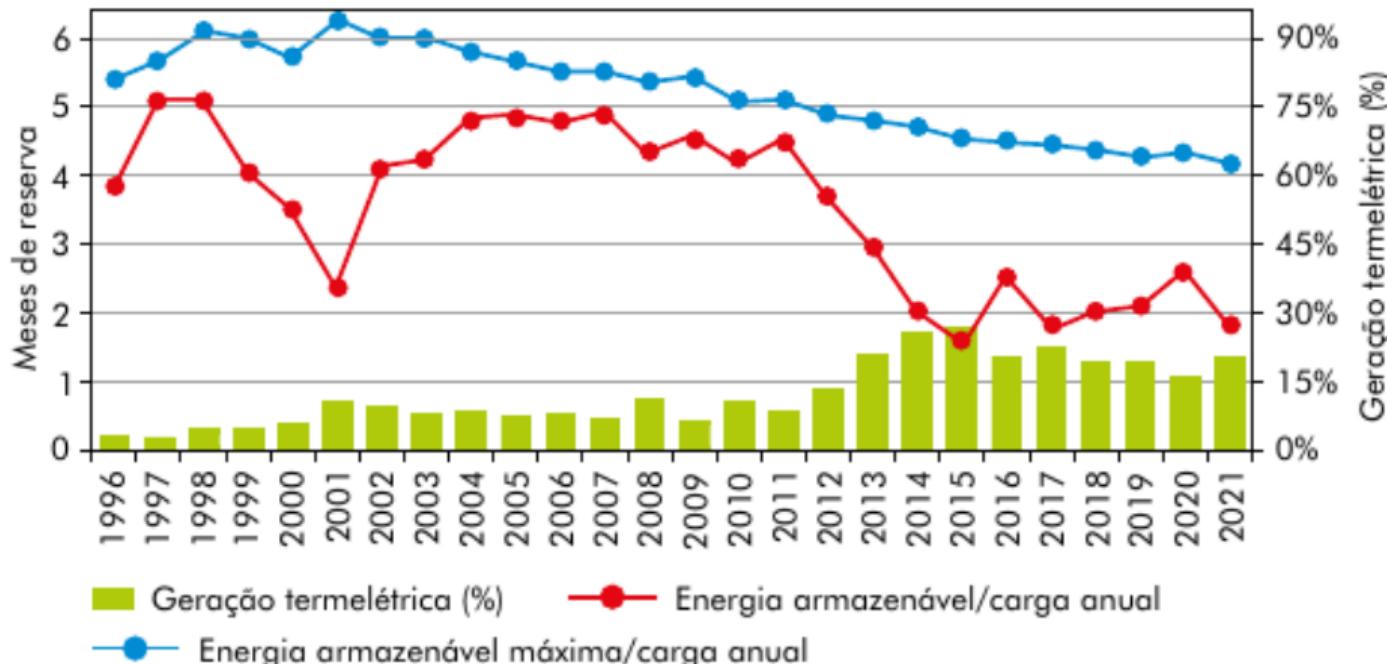


Figura 3.4 Geração média mensal por fonte no SIN (%)



Fonte: FGV a partir de dados da CCEE

Figura 3.5 Perda da capacidade relativa de armazenamento dos reservatórios do SIN



Nota: A energia armazenada considera o nível dos reservatórios registrado no fim do período úmido (abril). A carga de 2021 considera a segunda revisão quadrimestral da carga (69.940 MWmed).

Generation

Sistema de Informações de Geração da ANEEL - SIGA



Standard Frequency

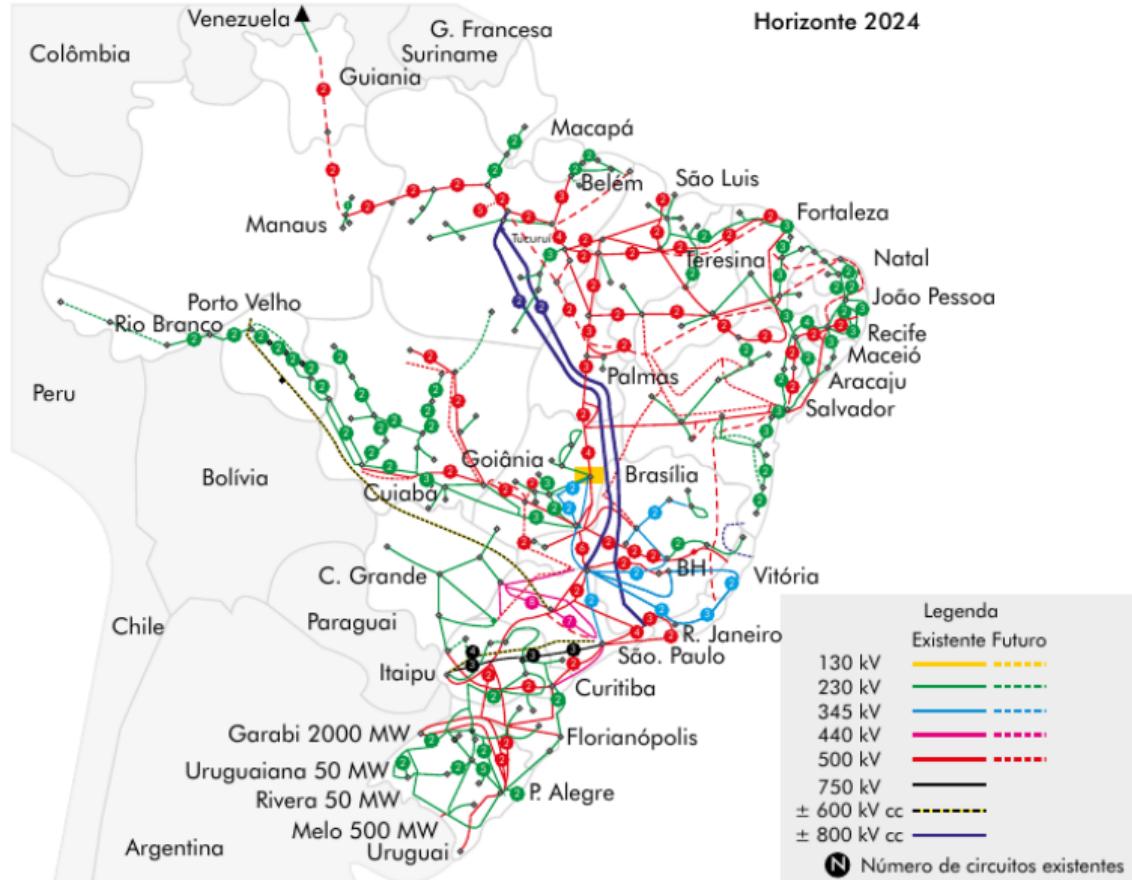
- ▶ The early ac systems operated at various frequencies including 25, 50, 60, and 133 Hz.
- ▶ In 1891, it was proposed that 60 Hz be the standard frequency in the United States.
- ▶ Today, the two standard frequencies for generation, transmission, and distribution of electric power in the world are:
- ▶ 60 Hz (in the United States, Canada, Mexico, and Brazil) and
- ▶ 50 Hz (in Europe, the former Soviet republics, China, South America, except Brazil, and India).
- ▶ In Japan, the western part of the country, including Kyoto, uses 60 Hz, while the eastern part, including Tokyo, uses 50 Hz.

Growth of the System: Generation, Transmision and Load

Análise de Alguns dados do SIN

Pico de carga do SIN: No dia 10 de março de 2022, foi registrado o recorde histórico de carga média diária do Sistema Interligado Nacional (SIN): 80.458 MW-méd.

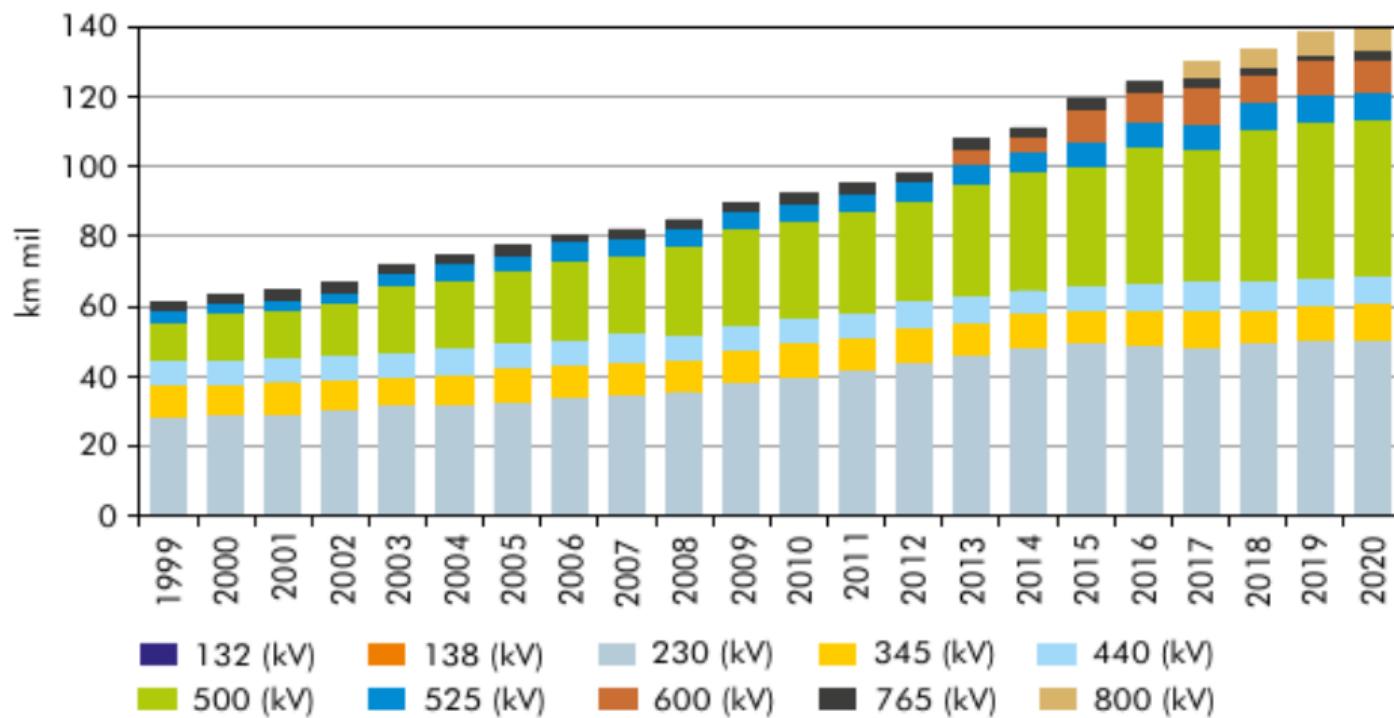
Nesse mesmo dia, a demanda máxima horária do SIN alcançou 88.617 MW, maior valor registrado desde o dia 1º de fevereiro de 2019.



EXTENSÃO DA REDE BÁSICA DE TRANSMISSÃO

230 kV	2022 67.137 km	2027 75.115 km
345 kV	2022 10.491 km	2027 11.406 km
440 kV	2022 6.934 km	2027 7.027 km
500/525 kV	2022 70.044 km	2027 97.039 km
600 kV	2022 12.816 km	2027 12.816 km
750 kV	2022 2.683 km	2027 2.683 km
800 kV	2022 9.204 km	2027 10.671 km
TOTAL	179.311 km	216.759 km

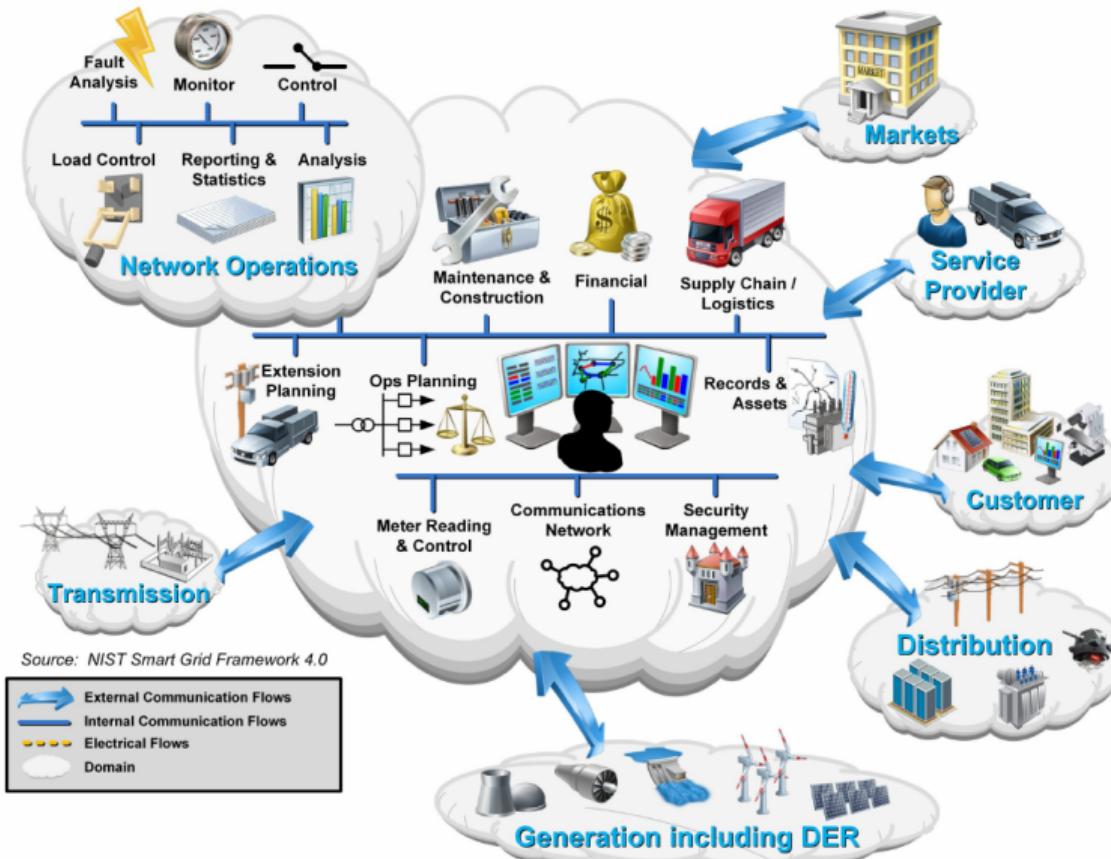
Figura 3.2 Evolução da extensão das linhas de transmissão do SIN, por nível de tensão



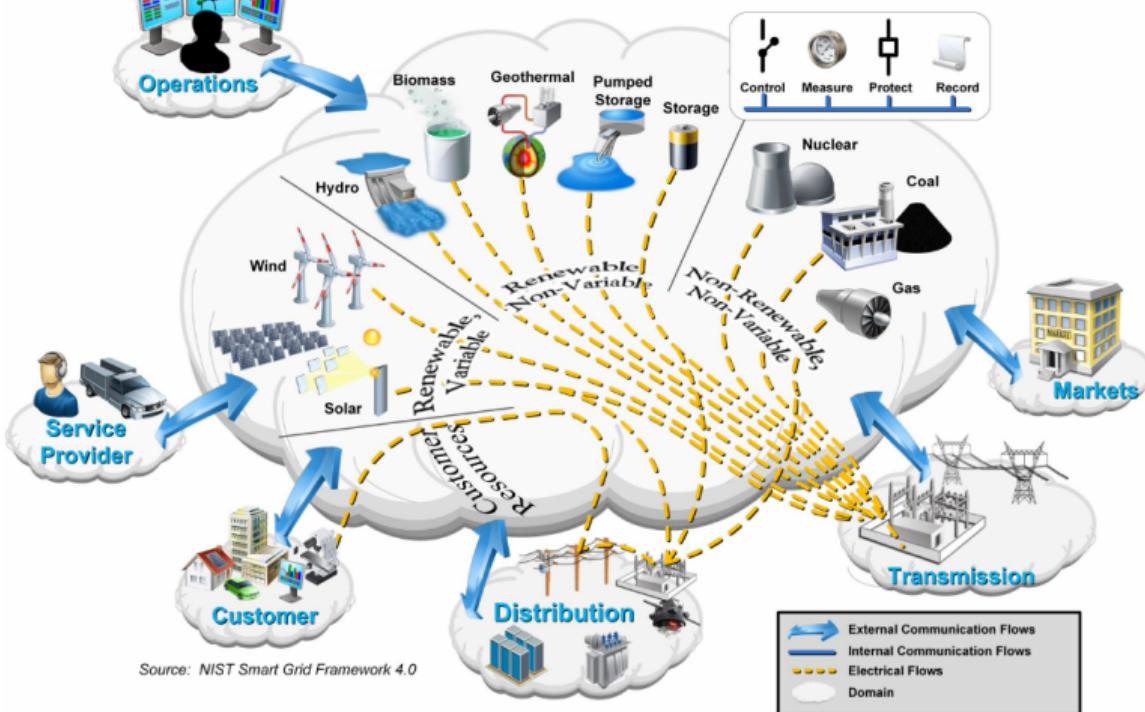
Present And Future Trends

- ▶ In Generation;
- ▶ In Transmission;
- ▶ In Distribution;
- ▶ The Smart Grids Concept;
- ▶ The Electricity Markets and the Energy Sector Liberalization.

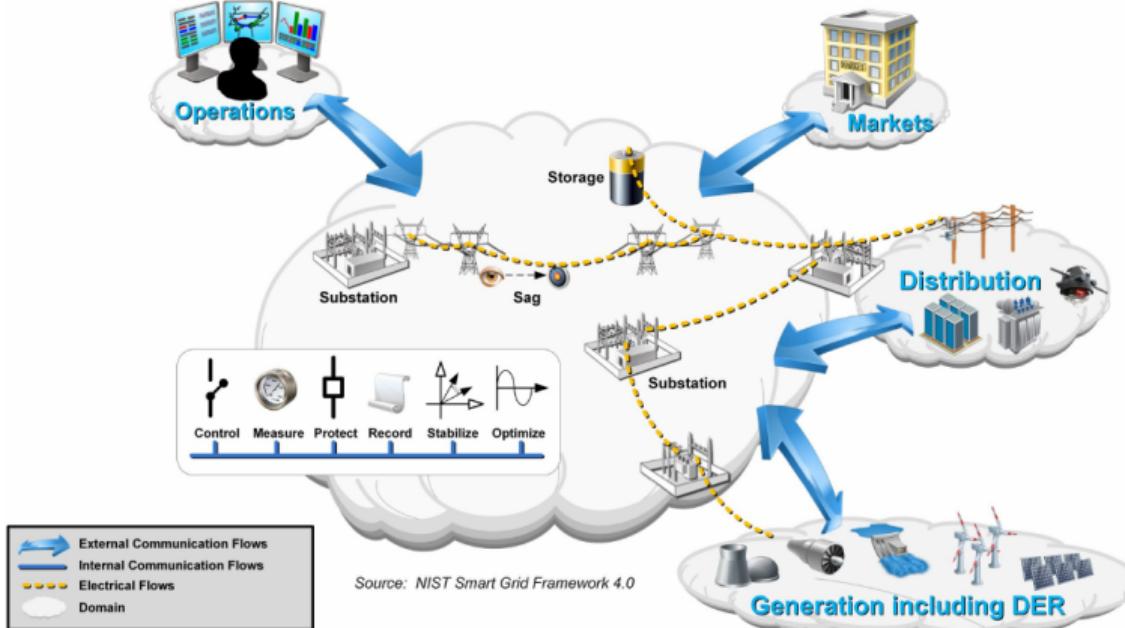
Operations



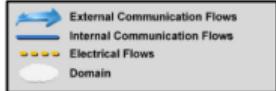
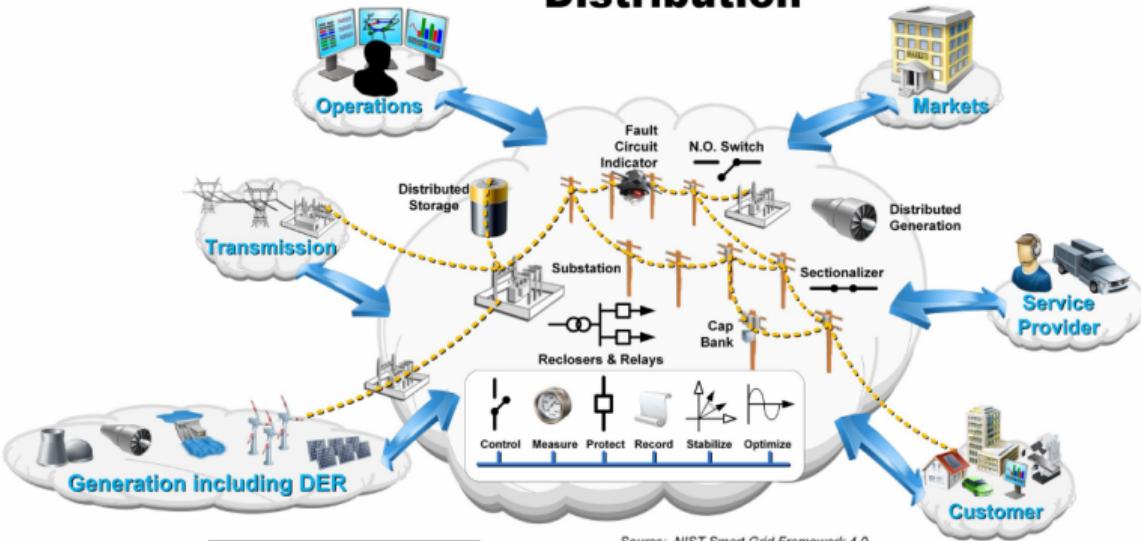
Generation Including DER



Transmission



Distribution



Computer in Power Systems

- ▶ Power Flow analysis;
- ▶ Short Circuit analysis;
- ▶ Stability analysis;
- ▶ Transient analysis.

Power Flow Analisys

Using Y_{bus} , the nodal equations for a power system network are written as:

$$\mathbf{I} = Y_{\text{bus}} \mathbf{V}$$

Where:

\mathbf{I} is the N vector of source currents injected into each bus; and

\mathbf{V} is the N vector of bus voltages.

Power Flow Analisys

In a more complete forme, the nodal equations for a power system network are written as:

$$\begin{bmatrix} Y_{11} & Y_{12} & Y_{13} & \cdots & Y_{1N} \\ Y_{21} & Y_{22} & Y_{23} & \cdots & Y_{2N} \\ Y_{31} & Y_{32} & Y_{33} & \cdots & Y_{3N} \\ \vdots & \vdots & \vdots & & \vdots \\ Y_{N1} & Y_{N2} & Y_{N3} & \cdots & Y_{NN} \end{bmatrix} \begin{bmatrix} V_{10} \\ V_{20} \\ V_{30} \\ \vdots \\ V_{N0} \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \\ I_3 \\ \vdots \\ I_N \end{bmatrix} \quad (1)$$

Power Flow Analisys

For bus k , the k th equation in this matricial equation is given by:

$$I_k = \sum_{n=1}^N Y_{kn} V_n$$

The complex power delivered to bus k is

$$S_k = P_k + jQ_k = V_k I_k^*$$

Power Flow Analisys

Power flow solutions by Gauss-Seidel are based on nodal equations, with each current source I_k :

$$I_k = \sum_{n=1}^N Y_{kn} V_n$$

Inserted into power equations:

$$I_k = \sum_{n=1}^N Y_{kn} V_n = \frac{P_k - jQ_k}{V_k^*}$$

Power Flow Analisys

This give the closed form of Gauss-Seidel equations are:

$$V_k(i+1) = \frac{1}{Y_{kk}} \left[\frac{P_k - jQ_k}{V_k^*(i)} - \sum_{n=1}^{k-1} Y_{kn} V_n(i+1) - \sum_{n=k+1}^N Y_{kn} V_n(i) \right]$$

Power Flow Analisys

Now, using the current I_k definition and applying in complex power equation delivered to bus k :

$$I_k = \sum_{n=1}^N Y_{kn} V_n$$

$$S_k = P_k + jQ_k = V_k I_k^* = V_k \left[\sum_{n=1}^N Y_{kn} V_n \right]^* \quad k = 1, 2, \dots, N$$

Power Flow Analisys

With the following notation,

$$V_n = V_n e^{j\delta_n}$$

$$Y_{kn} = Y_{kn} e^{j\theta_{kn}} = G_{kn} + jB_{kn} \quad k, n = 1, 2, \dots, N$$

This equation becomes:

$$P_k + jQ_k = V_k \sum_{n=1}^N Y_{kn} V_n e^{j(\delta_k - \delta_n - \theta_{kn})}$$

Power Flow Analisys

Taking the real and imaginary parts of above equation, the *power balance equations* are written as either:

$$P_k = V_k \sum_{n=1}^N Y_{kn} V_n \cos(\delta_k - \delta_n - \theta_{kn})$$

$$Q_k = V_k \sum_{n=1}^N Y_{kn} V_n \sin(\delta_k - \delta_n - \theta_{kn}) \quad k = 1, 2, \dots, N$$

Power Flow Analisys

Or when the Y_{kn} is expressed in rectangular coordinates as:

$$P_k = V_k \sum_{n=1}^N V_n [G_{kn} \cos(\delta_k - \delta_n) + B_{kn} \sin(\delta_k - \delta_n)]$$

$$Q_k = V_k \sum_{n=1}^N V_n [G_{kn} \sin(\delta_k - \delta_n) - B_{kn} \cos(\delta_k - \delta_n)] \quad k = 1, 2, \dots, N$$

Power flow solutions by *Newton-Raphson* are based on these nonlinear power flow equations, in polar or cartesian forms.

Power Flow Analisys

The Jacobian Equation:

$$\mathbf{J} = \left[\begin{array}{ccc|ccc} \frac{\partial P_2}{\partial \delta_2} & \dots & \frac{\partial P_2}{\partial \delta_N} & \frac{\partial P_2}{\partial V_2} & \dots & \frac{\partial P_2}{\partial V_N} \\ \vdots & & & \vdots & & \\ \frac{\partial P_N}{\partial \delta_2} & \dots & \frac{\partial P_N}{\partial \delta_N} & \frac{\partial P_N}{\partial V_2} & \dots & \frac{\partial P_N}{\partial V_N} \\ \frac{\partial Q_2}{\partial \delta_2} & \dots & \frac{\partial Q_2}{\partial \delta_N} & \frac{\partial Q_2}{\partial V_2} & \dots & \frac{\partial Q_2}{\partial V_N} \\ \vdots & & & \vdots & & \\ \frac{\partial Q_N}{\partial \delta_2} & \dots & \frac{\partial Q_N}{\partial \delta_N} & \frac{\partial Q_N}{\partial V_2} & \dots & \frac{\partial Q_N}{\partial V_N} \end{array} \right]$$

Power Flow Equations

Newton Raphson formulation:

$$\left[\begin{array}{c|c} J1(i) & J2(i) \\ \hline J3(i) & J4(i) \end{array} \right] \left[\begin{array}{c} \Delta\delta(i) \\ \DeltaV(i) \end{array} \right] = \left[\begin{array}{c} \DeltaP(i) \\ \DeltaQ(i) \end{array} \right]$$

Whith:

$$x(i+1) = \left[\begin{array}{c} \delta(i+1) \\ V(i+1) \end{array} \right] = \left[\begin{array}{c} \delta(i) \\ V(i) \end{array} \right] + \left[\begin{array}{c} \Delta\delta(i) \\ \DeltaV(i) \end{array} \right]$$

$$\Delta y(i) = \left[\begin{array}{c} \DeltaP(i) \\ \DeltaQ(i) \end{array} \right] = \left[\begin{array}{c} P - P[x(i)] \\ Q - Q[x(i)] \end{array} \right]$$

Short Circuit Analisys

In short-circuit analisys, we have two distinct types of analisys:

- ▶ Symetrical Faults;
- ▶ Assymetrical Faults:

Symetrical faults type:

- ▶ Three Phase;
- ▶ Three Phase to Ground.

Assymetrical faults types:

- ▶ Phase to Ground;
- ▶ Phase to Phase;
- ▶ Phase to Phase to Ground.

Short Circuit Analisys

In short-circuit analisys, the system is modeled by its positive-sequence network, where:

- ▶ Lines and Transformers are represented by series reactances and
- ▶ synchronous machines are represented by constant-voltage sources behind subtransient reactances.

As before, all resistances, shunt admittances, and nonrotating impedance loads, and also for simplicity prefault load currents, are neglected.

Short Circuit Analisys

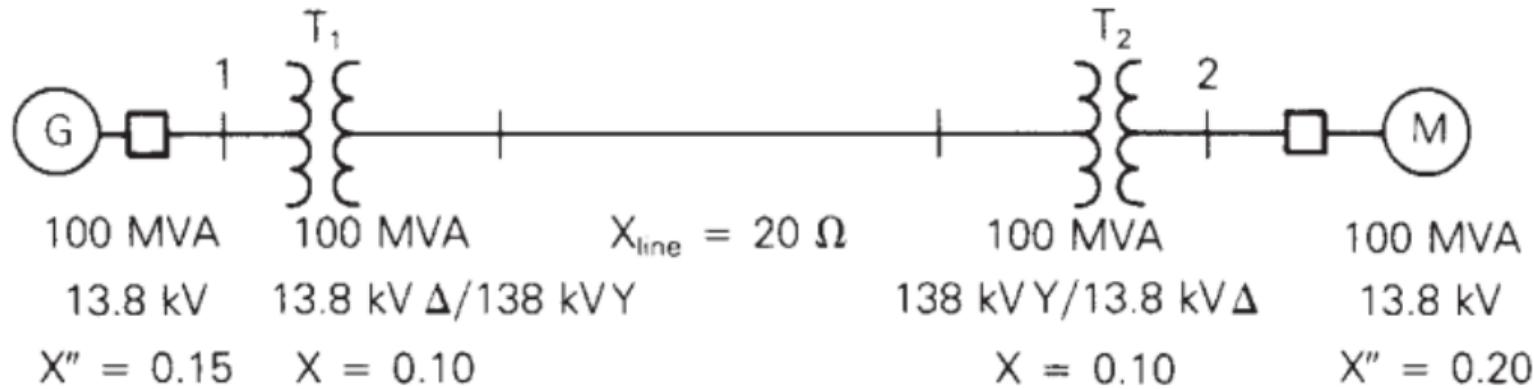
Consider a three-phase short circuit at any bus n . We use the superposition method to analysis this situation:

In the first circuit, all machine-voltage sources are short-circuited, and the only source is due to the prefault voltage at the fault. Writing nodal equations for the first circuit:

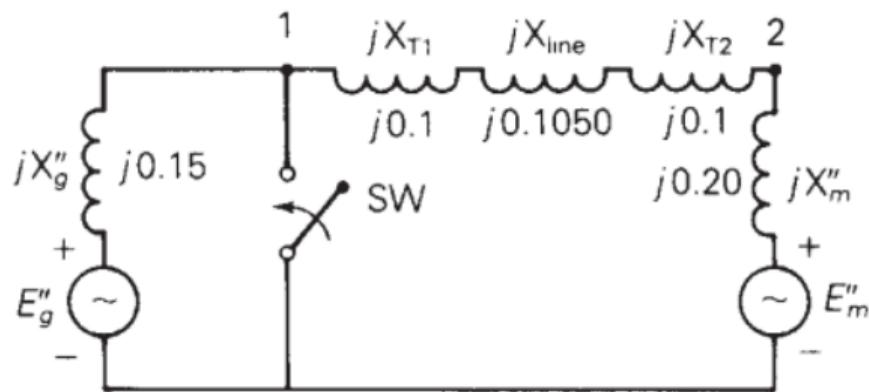
$$Y_{\text{bus}} E^{(1)} = I^{(1)}$$

Where Y_{bus} is the positive-sequence bus admittance matrix, $E^{(1)}$ is the vector of bus voltages, and $I^{(1)}$ is the vector of current sources. The superscript (1) denotes the first circuit.

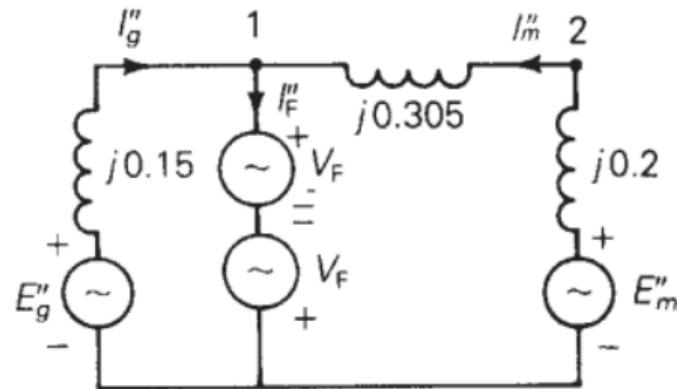
Short Circuit Analisys



Short Circuit Analisys

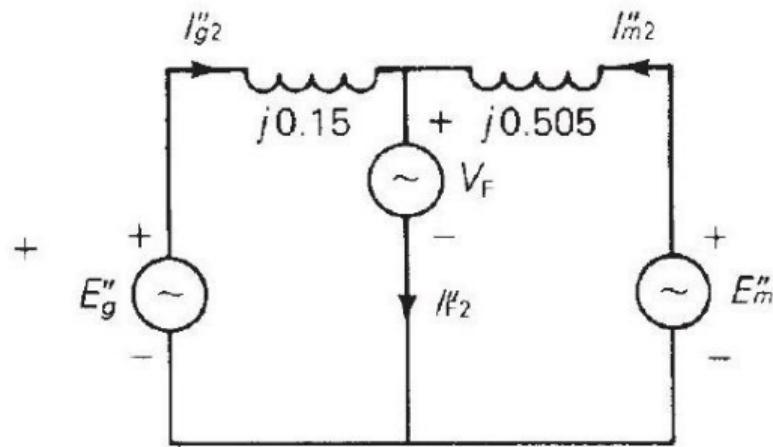
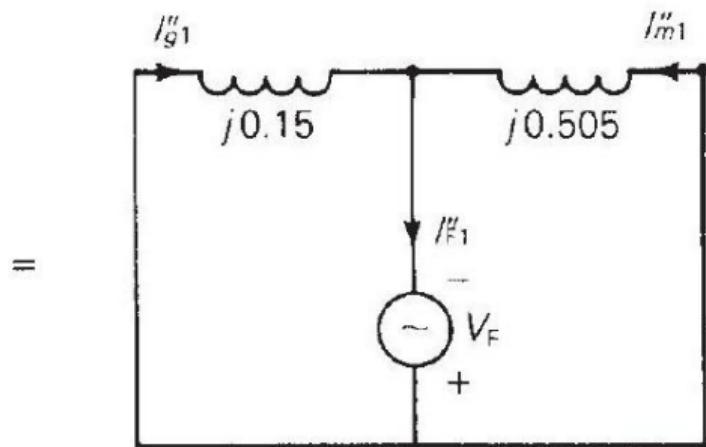


(a) Three-phase short circuit



(b) Short circuit represented by two opposing voltage sources

Short Circuit Analisys



Short Circuit Analisys

Solving:

$$Z_{\text{bus}} I^{(1)} = E^{(1)}$$

Where

$$Z_{\text{bus}} = Y_{\text{bus}}^{-1}$$

Z_{bus} , the inverse of Y_{bus} , is called the positive-sequence bus impedance matrix. Both Z_{bus} and Y_{bus} are symmetric matrices.

Short Circuit Analisys

Since the first circuit contains only one source, located at faulted bus n , the current source vector contains only one nonzero component, $I_n^{(1)} = -I_{Fn}''$.

Also, the voltage at faulted bus n in the first circuit is $E_n^{(1)} = -V_F$:

$$\begin{bmatrix} Z_{11} & Z_{12} & \cdots & Z_{1n} & \cdots & Z_{1N} \\ Z_{21} & Z_{22} & \cdots & Z_{2n} & \cdots & Z_{2N} \\ \vdots & & & & & \\ Z_{n1} & Z_{n2} & \cdots & Z_{nn} & \cdots & Z_{nN} \\ \vdots & & & & & \\ Z_{N1} & Z_{N2} & \cdots & Z_{Nn} & \cdots & Z_{NN} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ \vdots \\ -I_{Fn}'' \\ \vdots \\ 0 \end{bmatrix} = \begin{bmatrix} E_1^{(1)} \\ E_2^{(1)} \\ \vdots \\ -V_F \\ \vdots \\ E_N^{(1)} \end{bmatrix}$$

Short Circuit Analisys

The minus sign associated with the current source in (7.4.4) indicates that the current injected into bus n is the negative of I''_{Fn} , since I''_{Fn} flows away from bus n to the neutral.

In this way, the subtransient fault current is given by:

$$I''_{Fn} = \frac{V_F}{Z_{nn}}$$

Also, the voltage at any bus k in the first circuit is:

$$E_k^{(1)} = Z_{kn} (-I''_{Fn}) = \frac{-Z_{kn}}{Z_{nn}} V_F$$

Short Circuit Analisys

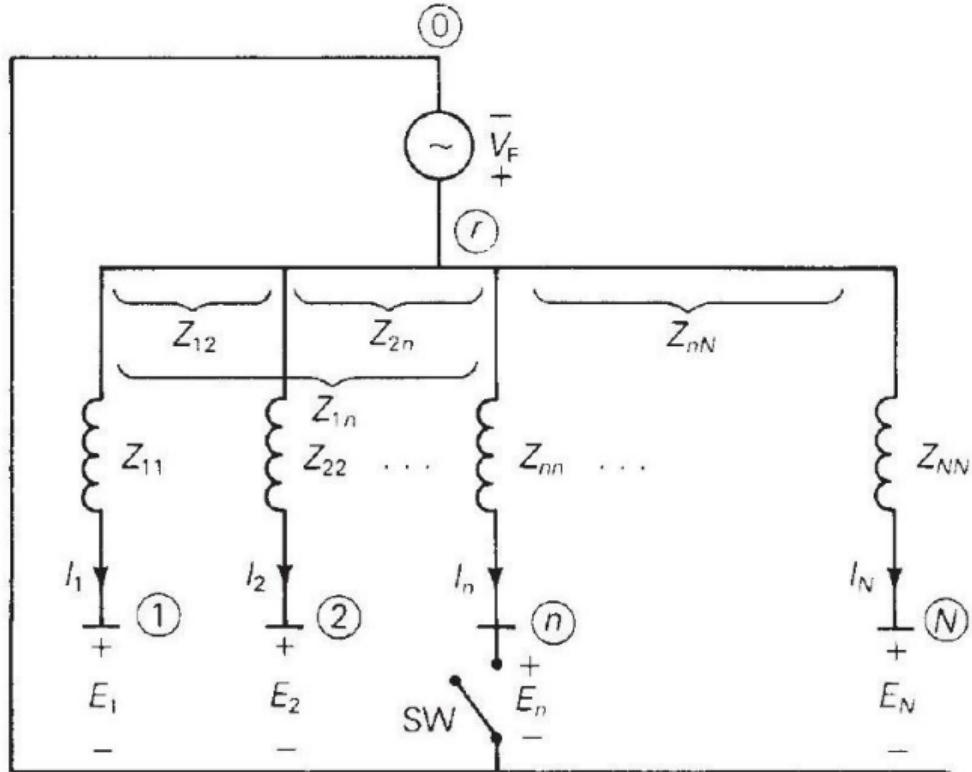
The second circuit represents the prefault conditions.

Neglecting prefault load current, all voltages throughout the second circuit are equal to the prefault voltage; that is, $E^{(2)} = V_F$ for each bus k .

Applying superposition, we have:

$$\begin{aligned} E_k &= E_k^{(1)} + E_k^{(2)} = \frac{-Z_{kn}}{Z_{nn}} V_F + V_F \\ &= \left(1 - \frac{Z_{kn}}{Z_{nn}}\right) V_F \quad k = 1, 2, \dots, N \end{aligned}$$

Short Circuit Analisys



Short Circuit Analisys

The Figure above shows a bus impedance equivalent circuit that illustrates the short-circuit currents in an N -bus system.

This circuit is given the name rake equivalent in Neuenswander [5] due to its shape, which is similar to a garden rake.

The diagonal elements $Z_{11}, Z_{22}, \dots, Z_{NN}$ of the bus impedance matrix, which are the self-impedances, are shown in Figure too.

The off-diagonal elements, or the mutual impedances, are indicated by the brackets in the figure.

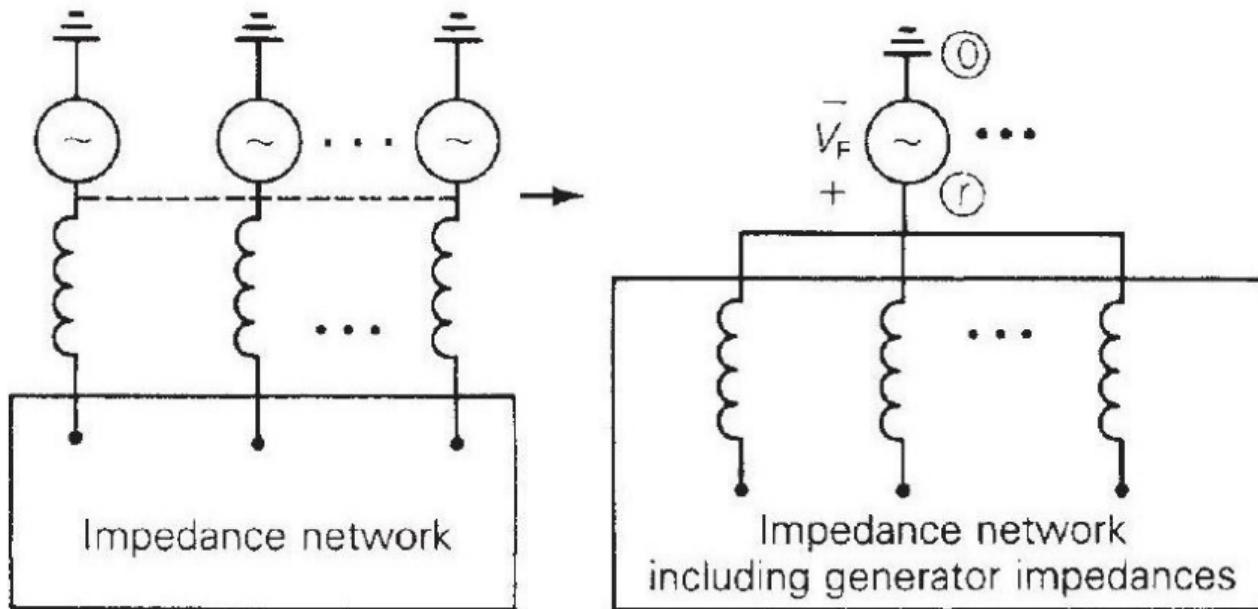
Short Circuit Analisys

Neglecting prefault load currents, the internal voltage sources of all synchronous machines are equal both in magnitude and phase.

As such, they can be connected, as shown in the same Figure, and replaced by one equivalent source V_F from neutral bus 0 to a references bus, denoted r .

This equivalent source is also shown in the rake equivalent of Figure.

Short Circuit Analisys



Short Circuit Analisys

Using Z_{bus} , the fault currents in Figure are given by:

$$\begin{bmatrix} Z_{11} & Z_{12} & \cdots & Z_{1n} & \cdots & Z_{1N} \\ Z_{21} & Z_{22} & \cdots & Z_{2n} & \cdots & Z_{2N} \\ \vdots & & & & & \\ Z_{n1} & Z_{n2} & \cdots & Z_{nn} & \cdots & Z_{nN} \\ \vdots & & & & & \\ Z_{N1} & Z_{N2} & \cdots & Z_{Nn} & \cdots & Z_{NN} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \\ \vdots \\ I_n \\ \vdots \\ I_N \end{bmatrix} = \begin{bmatrix} V_F - E_1 \\ V_F - E_2 \\ \vdots \\ V_F - E_n \\ \vdots \\ V_F - E_N \end{bmatrix}$$

Where I_1, I_2, \dots are the branch currents and $(V_F - E_1), (V_F - E_2), \dots$ are the voltages across the branches.

Short Circuit Analisys

If switch SW in Figure is open, all currents are zero and the voltage at each bus with respect to the neutral equals V_F . This corresponds to prefault conditions, neglecting prefault load currents.

If switch SW is closed, corresponding to a short circuit at bus n , $E_n = 0$ and all currents except I_n remain zero. The fault current is:

$$I''_{Fn} = I_n = V_F/Z_{nn}$$

Short Circuit Analisys

This fault current also induces a voltage drop $Z_{kn}I_n = (Z_{kn}/Z_{nn}) V_F$ across each branch k .

The voltage at bus k with respect to the neutral then equals V_F minus this voltage drop.

As shown by Figure, subtransient fault currents throughout an N -bus system can be determined from the bus impedance matrix and the prefault voltage.

Short Circuit Analisys

Concluding:

Z_{bus} can be computed by first constructing Y_{bus} , via nodal equations, and then inverting Y_{bus} .

Once Z_{bus} has been obtained, these fault currents are easily computed.