

# Design of Framework Agreements

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Marek Bojko<sup>1</sup>   Lucas Condeza <sup>1</sup>

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<sup>1</sup>Yale University

# Introduction

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- ▶ Governments make repeated purchases of certain products (e.g. medical devices, gasoline, laptops)
- ▶ Framework Agreements (FAs) streamline procurement through a two-stage process.
  - **Stage 1 (Auction):** Pre-selection of suppliers/products via auction.
  - **Stage 2 (Marketplace):** Creation of a "marketplace" where pre-selected suppliers offer goods/services to government agencies.
- ▶ **Research Question:** How to design FAs?
- ▶ Focus on FAs for vehicles between 2017 and 2024 in Chile

- ▶ FAs are a common procurement tool. They are used in:
  - EU (2010): 17% of procured value
  - Chile: 25%
  - Brasil: 10%
  - Costa Rica, China, Trinidad & Tobago, etc.
- ▶ **Benefits of FA compared with public tenders:**
  - Centralize procurement expertise (Decarolis et al. 2020)
  - Increase competition by reducing firm participation costs
  - Decrease purchasing times
  - Decrease cost of running auctions

# Stages of FAs

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## 1. First Stage: selection through auction

- The procurement agency calls for a public tender.
- Firms submit bids (price, characteristics).
- Subset of firms/products are selected.

## 2. Second Stage: marketplace

- Selected firms offer products on a government-run online platform.
- Government agencies purchase directly.
- First-stage bid acts as a price-ceiling

- ▶ Framework Agreements
  - Choi et al. (2023), Gur et al. (2017), and Saban and Weintraub (2021)  
⇒ Theoretical literature, we aim to estimate a structural model
- ▶ Effects of centralizing procurement
  - Castellani et al. 2021; Dubois et al. 2021; Ferraresi et al. 2021; Lotti et al. 2024  
⇒ We study FAs, a specific way of centralizing procurement
- ▶ Market design
  - Agarwal and Budish (2021) and Kapor et al. (2024)  
⇒ Optimal design of FAs

## **Institutional Context and Data**

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## Institutional Context: Chile Compra

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- ▶ Chilean public procurement system managed by *Chile Compra* through the *Mercado Público* platform.
- ▶ Most gov. agencies (hospitals, ministries, universities) are required to use this platform.  
[▶ Details](#)
- ▶ FAs account for 25% of procurement value
- ▶ Currently 18 active FA. Examples: medical devices, hardware products, food, stationery, etc.
- ▶ FA for vehicles are active for  $\approx 3$  years and the public tender takes  $\approx 5$  months

## VEHÍCULOS LIVIANOS, MEDIANOS Y PESADOS

SUBCATEGORÍAS

- VEHÍCULOS PESADOS Y MAQUINARIAS
- VEHÍCULOS LIVIANOS Y MEDIANOS

Precio

REGIÓN

Combustible

Marca

Rendimiento Ciudad

Rendimiento Mixto

Transmisión

Año

Norma

Velocidades

Frenos ABS

N° PASAJEROS

TIPO DE CARROCERÍA

COMPARAR

No tiene ningún artículo para comparar.

12 de 681 resultados

Precio de menor a mayor









<p>1 proveedor ID 2057541</p>  <p>CARGO JAC URBAN 1042 MT PLATAFORMA 2024</p> <p>Desde \$18.621.000</p> <p>Ver Producto</p> <p>Comparar</p>	<p>1 proveedor ID 2057558</p>  <p>CARGO JAC URBAN 1042 DC MT PLATAFORMA 2024</p> <p>Desde \$20.871.000</p> <p>Ver Producto</p> <p>Comparar</p>	<p>4 proveedores ID 2042562</p>  <p>CAMIONETA MAXUS T90 E6 4X4 AT 2024</p> <p>Desde \$26.721.000</p> <p>Ver Producto</p> <p>Comparar</p>	<p>3 proveedores ID 2041627</p>  <p>CAMIONETA JMC GRAND AVENUE 4X4 MT 2024</p> <p>Desde \$17.541.000</p> <p>Ver Producto</p> <p>Comparar</p>
<p>1 proveedor ID 2030705</p>  <p>SEDÁN CHANGAN ALSVIN COMFORT MT 2024</p> <p>Desde \$8.109.916</p> <p>Ver Producto</p> <p>Comparar</p>	<p>1 proveedor ID 2030722</p>  <p>SEDÁN CHANGAN ALSVIN LUXURY MT 2024</p> <p>Desde \$8.419.160</p> <p>Ver Producto</p> <p>Comparar</p>	<p>2 proveedores ID 2044823</p>  <p>SEDÁN KIA SOLUTO LX 1.4L G LL MT 2024</p> <p>Desde \$8.538.654</p> <p>Ver Producto</p> <p>Comparar</p>	<p>1 proveedor ID 2062009</p>  <p>FURGÓN KYC V3 CARGO VAN MT 2024</p> <p>Desde \$8.635.900</p> <p>Ver Producto</p> <p>Comparar</p>

Figure 1: Marketplace for vehicles



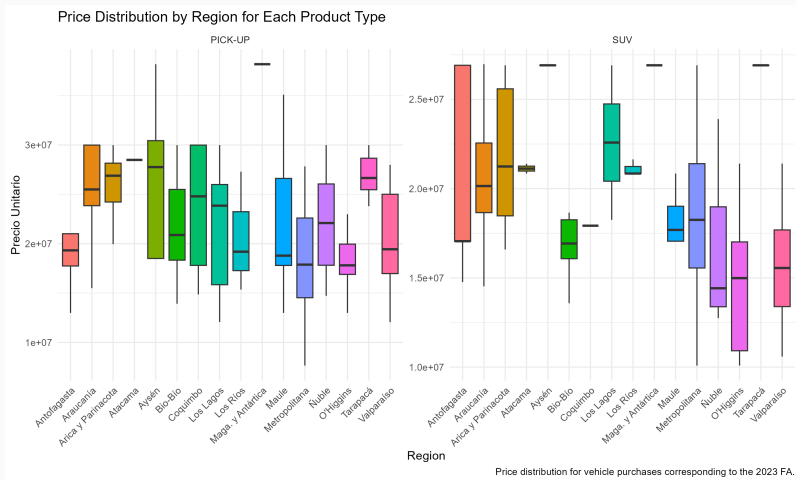
## Some details

	2017	2021	2023
<b>Categories</b>	Pick-up, SUV, sedan, minibuses, vans	SUV and pick-up	Pick-up, SUV, sedan, minibuses, vans
<b>Bids</b>	Discount over list price (e.g. 8%)	Price and delivery fee	Discount over list price and delivery fee
<b>Market</b>	National	5 macro-regions and 4 tiers	Region
<b>Selection criteria</b>	Score threshold	2-3 lowest price depending on region	60% highest scores, minimum of 5
<b>Auction level and number</b>	1	Product-tier-region: 40	Product-region $\approx$ 70

The tender for a fourth FA will be implemented this year

- ▶ **Purchase Data:** All vehicle transactions through FAs (2017-2024).
  - Buyer (agency type, location), Seller
  - Product (type, model)
  - Price
- ▶ **Auction Data:** Bids from 3 vehicle FAs (2017, 2021, 2023).
  - Bidder identity
  - Bids
  - Date of bid
  - Product (model, category, region)
  - List prices (work in progress)
- ▶ **Web-scraped data:** product characteristics (work in progress)

# Motivation



## What is the optimal design of a FA?

- ▶ Optimal number of firms to choose in auction
- ▶ Selection criteria (e.g. discount price or prices with tiers)
- ▶ Segmentation (e.g. national or regional auctions)
- ▶ other...?

## Empirical model

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- ▶ Model stages
  - Second stage: Demand estimation following Berry et al. (1995) and Petrin (2002)
  - First stage: Auction

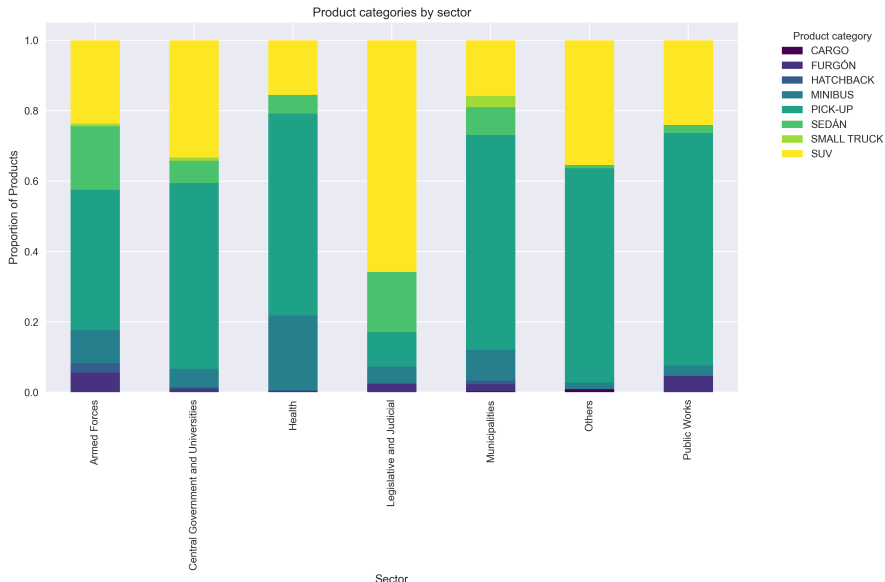
- ▶ We consider the demand of gov. agencies in markets defined as a region-semester. Given evidence of different consumption patterns we group gov. agencies in types according to their sector (e.g. hospital, university, etc.)
- ▶ Gov. agency  $i$ , in market  $t \in \mathcal{T}$  in sector  $s$  has a utility for product  $j \in \mathcal{J}_t$ .

[▶ Details](#)

$$u_{ijt} = \underbrace{x'_{jt}\beta_{s(i)}}_{\delta_{jts(i)}} + \underbrace{x'_{jt}\sum \nu_{it}}_{\mu_{ijt}} + \varepsilon_{ijt}, \quad u_{i0t} = \varepsilon_{i0t} \quad (1)$$

where  $\nu_{it}$  are random taste shocks.

# Demand heterogeneity





## Demand(2)

The probability that a buyer in sector  $s$  in market  $t$  chooses a product  $j \in \mathcal{J}_t$

$$s_{jts} = \int \frac{\exp(\delta_{jts} + \mu_{ijt})}{1 + \sum_{k \in \mathcal{J}_t} \exp(\delta_{kts} + \mu_{ikt})} dF_{\mu}(\mu_{it}) \quad (2)$$

Aggregate market shares are given

$$s_{jt} = \sum_s w_{st} \cdot s_{jts} \quad (3)$$

where  $w_{st}$  is the share of agencies of type  $s$  in market  $t$

The vector of parameters to estimate is  $\theta = (\beta, \Sigma)$

► Moments

# Supply

- ▶ Firm's ( $z$ ) profits, in market  $t$  are:

$$\pi_{zt} = \sum_{j \in P_z} N_t s_{jt} (p_{jt} - MC_{jt}) \quad (4)$$

Where  $N_t$  is the number of buyers in market  $t$  and  $MC_{jt}$  is the marginal cost.

- ▶ Assuming single product firms,  $p_{jt}^*$  is the price that satisfies the FOC:

$$p_{jt}^* = MC_{jt} - s_{jt} \left[ \frac{\partial s_{jt}}{\partial p_{jt}} \right]^{-1} \quad (5)$$

- ▶ Hence the observed price ( $p_{jt}$ ) will satisfy

$$p_{jt} = \min\{\bar{P}_{jt}, p_{jt}^*\} = \min\left(\bar{P}_{jt}, MC_{jt} - s_{jt} \left[ \frac{\partial s_{jt}}{\partial p_{jt}} \right]^{-1}\right)$$

- ▶ Cost is point identified if the price ceiling is not binding

Set-up:

- ▶  $i \in \{1, \dots, N\}$  have costs  $c_i$  and bid  $\bar{p}_i$ , assume  $c_1 < \dots < c_N$
- ▶ Assume that costs are common knowledge  $\rightarrow$  firms compete in the private market
- ▶ Selection of  $K$  firms using selection rule  $S_k(\bar{P}_k)$
- ▶  $\Psi_k = (S_k, \bar{P}_k)$  the equilibrium selected firms ( $S_k$ ) and their bids
- ▶  $\pi_i(\Psi_k)$ : second-stage profits

Differences from standard auction:

- ▶ Valuations depend on 1) bids and 2) selected firms
- ▶ Discount over list prices

# What lies ahead

- ▶ Obtain list prices (or assume there are no discounts)
- ▶ Model the first stage
- ▶ Estimate the model
- ▶ Counterfactuals, estimate the impact of:
  1. Choose the optimal number of sellers in the auction stage
  2. Allow the selection criteria to depend on product characteristics

descriptives

- number of selected firms
- important sources of variation in the data

what are the effects of changing the procurement rules for the selection

1. motivation-: minimize frictions, cost of the government

how the cost of procurement would change when we change the rules

weighted sum of the welfare and cost

# Appendix

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# Acquisition process

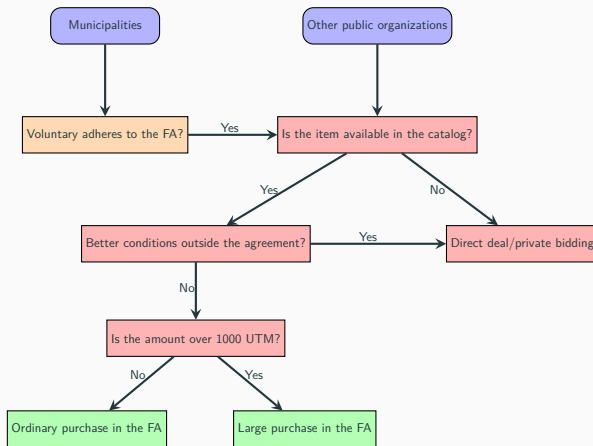


Figure 2: Procurement decision process (Castro et al. 2020)

# Moments

- ▶ Aggregate moments:  $\mathbb{E}[\xi_{jt} \cdot z_{jt}] = 0$  with sample moment:

$$\hat{g}_A(\theta) = \frac{1}{N_A} \sum_{t \in \mathcal{T}} \sum_{j \in \mathcal{J}_t} \left( \hat{\delta}_{jt}(\Pi, \Sigma) - x'_{jt} \beta \right) \cdot z_{jt}, \quad (6)$$

- ▶ Micro-moments: target 1) buying a certain type of vehicle  $\lambda$  given the type of the state agency and 2) the average price of the vehicles bought by each state agency type. Denote by  $n$  a state agency, by  $i(n)$  its type,  $N = \sum_{n \in \mathcal{N}} 1$  and  $p_{j_n}$  the price of the good bought by  $n$ . Then the in sample moments are:

$$\bar{v}_{ip} = \frac{\frac{1}{N} \sum_{n \in \mathcal{N}} 1\{(i(n) = i)\} 1\{j_n \in \mathcal{J}_\lambda\}}{\frac{1}{N} \sum_{n \in \mathcal{N}} 1\{(i(n) = i)\}}} \equiv f_1(\bar{v}) \quad (6)$$

$$\bar{v}_{i\lambda} = \frac{\frac{1}{N} \sum_{n \in \mathcal{N}} 1\{(i(n) = i)\} p_{j_n}}{\frac{1}{N} \sum_{n \in \mathcal{N}} 1\{(i(n) = i)\}}} \equiv f_2(\bar{v}) \quad (7)$$