Equilibrium effects of price updating: evidence from a centralized marketplace for annuities

Lucas Condeza <sup>1</sup> October 13, 2025 <sup>5</sup>Vale University

<sup>&</sup>lt;sup>1</sup>Yale University

## Motivation

- In several markets consumers receive initial offers, then they can request revised offers. Examples:
  - Loans: consumers get a loan estimate (LE) and showing a LE to another lender could lead to a revised offer. [1]
  - Auto dealerships: buyers can shop around and dealers are willing to revise their initial offers
     [2]
- What are the impacts of allowing consumers to request revised offers?
- vinat are the impacts
- Economic forces at play:
  - Learning: firms learn competitors' prices and can best respond.

• Discrimination: if search cost are correlated with preferences. [not today]

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marketplace for annuities

marketplace for annuities

Motivation

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I am going to

 I am going to study the effects of being able to request revised offers in a centralized marketplace for annuities in Chile.

- ► Studies a centralized marketplace for annuities in Chile (SCOMP)
- ► A recent law eliminated the possibility of requesting revised offers.
  - Before: consumers receive initial offers, then can request revised offers from one firm.
  - Before. Consumers receive initial offers, their can req
  - After: consumers can only accept/reject initial offers.Rationale for elimination: "firms will not make their best efforts in the initial phase"
- Also provides evidence on assymmetries in infomration precision in selection markets.

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This research

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2

- ► Aftermarkets: allen\_search\_2019
- ► Competition in selection markets: mahoney\_imperfect\_2017; cuesta\_price\_2018;
- cosconati\_competing\_2025 ▶ Selection in multiple dimensions: finkelstein\_adverse\_2004 and Finkelstein and McGarry (2006).

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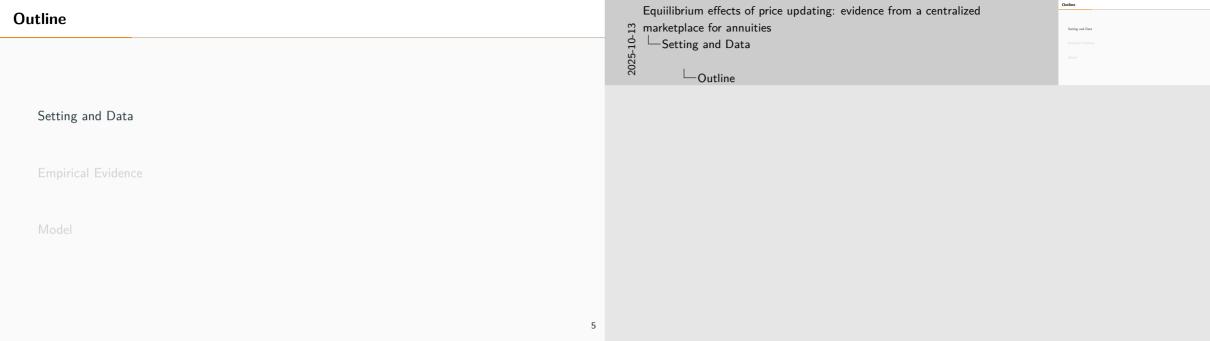
Literature

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Competition in selection markets: mahoney\_imperfect\_2017; cuesta\_price\_2018; cosconati\_competing\_2025

Aftermarkets: allen search 2019

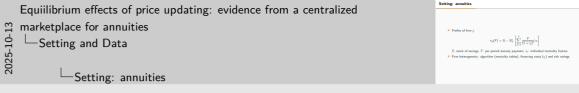
Selection in multiple dimensions: finkelstein\_adverse\_2004 and Finkelstein and



$$\pi_{ji}(F) = S_i - \mathbb{E}_{\mathcal{T}}^j \left[ \sum_{t=1}^T rac{F}{(1+r_j)^t} | x_i 
ight]$$

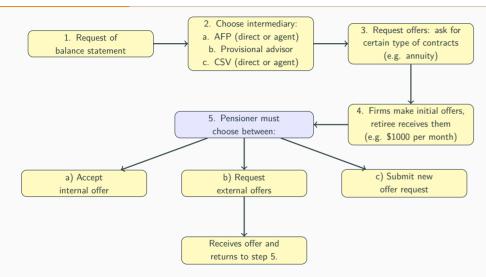
 $\triangleright$  Firm heterogeneity: algorithm (mortality tables), financing costs  $(r_i)$  and risk ratings.

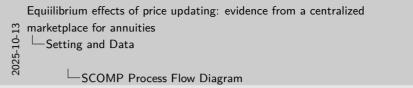
S: stock of savings, F: per period annuity payment,  $x_i$ : individual mortality factors



- Explicitly not link the annuities market with pensions because generates confusion
- Explain what annuities are.

# **SCOMP Process Flow Diagram**







## Data

- ► SCOMP data at the individual level
  - Posted and revised prices, and consumer decisions
  - Total savings
  - Demographics: age and gender Certificate with initial prices
- ► Retirement insurance companies: risk ratings

Particularities of the data/setting:

- ► One observes all the offers received by the buyers
- One observes the same information as the firms (gender, age, savings)

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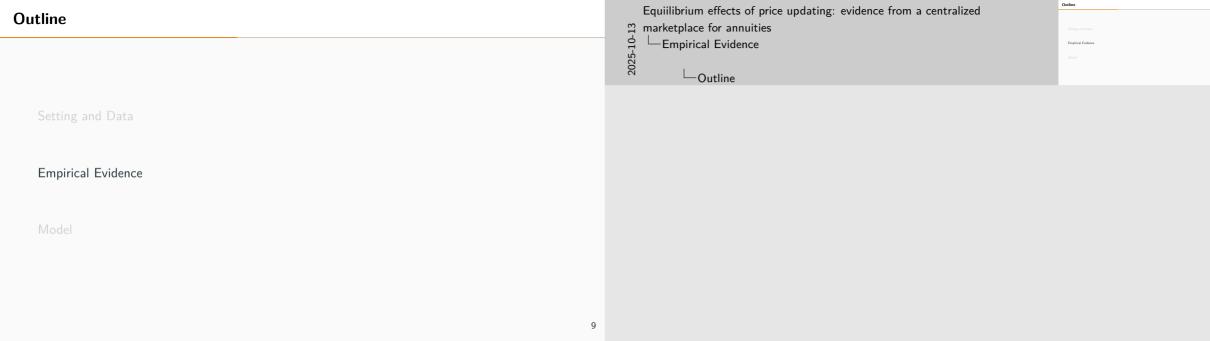
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Setting and Data

Data

Data

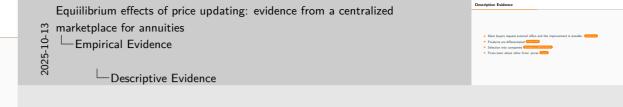
Formula of the price of



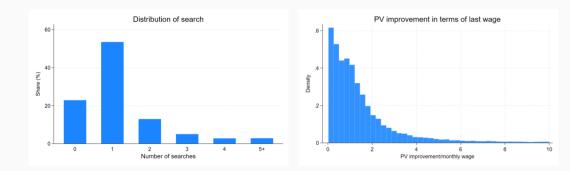
## **Descriptive Evidence**

- ► Most buyers request external offers and the improvement is sizeable. 

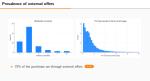
  [External offers]
- ► Products are differentiated Foregone value
- ► Selection into companies (Heterogeneity in algorithm precision)
- Firms learn about other firms' prices Learning



## Prevalence of external offers



► 75% of the purchases are through external offers. Go back



Prevalence of external offers

That only some people use the aftermarket suggest:

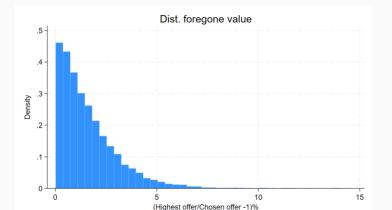
- There are search costs
- Firms could be discriminating based on the search likelihood.

Any assessment of the welfare effects of the aftermarket has to consider that by banning it buyers will save in search costs, but will not be able to improve on the initial posted prices.

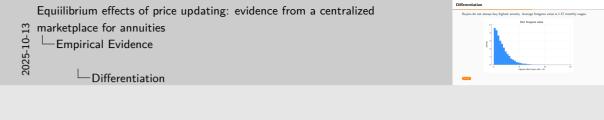
In a model where search costs are not correlated with valuations, the aftermarket prices by the sellers are the same as the initial prices.

## Differentiation

Buyers do not always buy highest annuity. Average foregone value is 1.57 monthly wages.

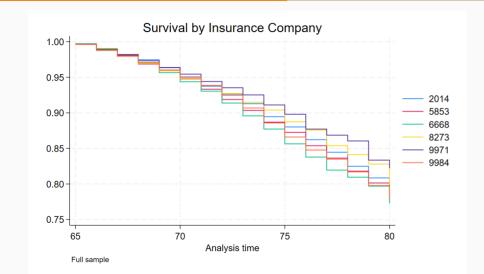


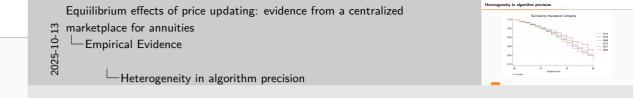






# Heterogeneity in algorithm precision







# Learning

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
	Increase	Increase	Increase	Increase	Increase	Increase	Has External Offer
main							
Avg. Gap	0.316***	0.155***	0.155***	0.139***	0.147***	0.071***	
	(0.006)	(0.010)	(0.010)	(0.016)	(0.019)	(0.020)	
Max. Gap		0.110***	0.110***		-0.021	-0.006	
		(0.009)	(0.009)		(0.029)	(0.028)	
gap_from_avg							-0.191***
							(0.032)
Constant	1.893***	1.375***	1.375***	1.381***	1.387***	1.511***	-2.012***
	(0.010)	(0.082)	(0.082)	(0.045)	(0.046)	(0.121)	(0.028)
Observations	14133	14133	14133	2046	2046	2046	16164

Observations 14133 14133 14133 2046 2046

Average: is the difference between the mean of other firms' initial offers and own initial offer

Max Gap: is the difference between the highest other firm's initial offer and own initial offer.

Cols (1)-(3) use the population of initial offers that are not the highest, (4)-(6) only use the highest offer

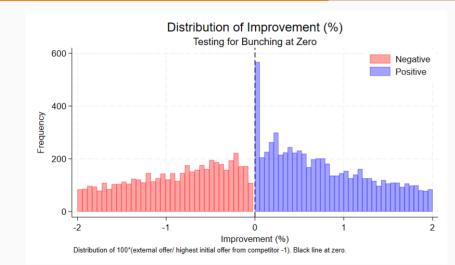
Cols (4) and (6) include firm fixed effects

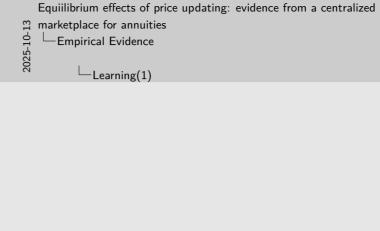
Go back

Equilibrium effects of price updating: evidence from a centralized marketplace for annuities -Empirical Evidence 2025-May Care in the difference between the highest other free's initial offer and our initial offer. Learning

14

# Learning(1)

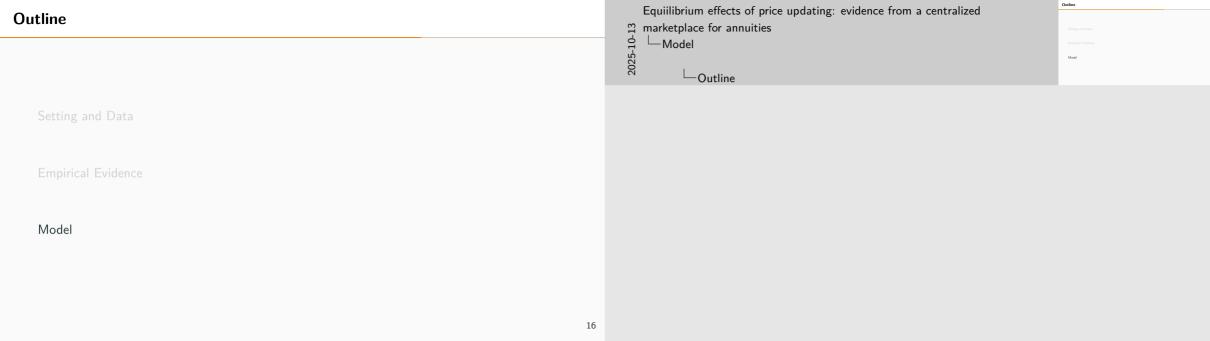




Learning(1)

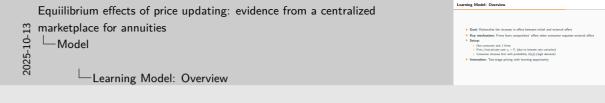
Distribution of Improvement (%) Testing for Bunching at Zoro





## **Learning Model: Overview**

- ► **Goal:** Rationalize the increase in offers between initial and external offers
- ► Key mechanism: Firms learn competitors' offers when consumer requests external offers
- ► Setup:
  - .
  - One consumer and *J* firms
  - Firm j has private cost  $c_j \sim F_j$  (due to interest rate variation)
- Consumer chooses firm with probability  $D_j(p)$  (logit demand)
- ► Innovation: Two-stage pricing with learning opportunity



## Two-Stage Game: Timeline

## 1. Stage 1 (Initial offers):

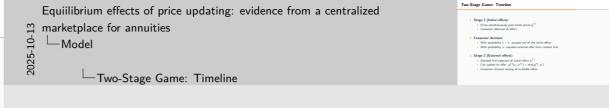
- Firms simultaneously post initial prices  $p_i^{T1}$
- Consumer observes all offers

# 2. Consumer decision:

- With probability  $1-\lambda$ : accepts one of the initial offers
- With probability  $\lambda$ : requests external offer from random firm

# 3. Stage 2 (External offers):

- Stage 2 (External offers).
- Selected firm observes all initial offers  $p^{T1}$
- Can update its offer: p<sub>j</sub><sup>T2</sup>(c<sub>j</sub>, p<sup>T1</sup>) = min(p<sub>j</sub><sup>T1</sup>, p\*)
   Consumer chooses among all available offers



# **Second Stage: Optimal Pricing with Learning**

# When selected for external offer, firm observes competitors' initial prices

# **Optimal updated offer:**

$$p_i^{T2}(c_i, p^{T1}) = \min(p_i^{T1}, p^*)$$

 $p^* = \arg \max_{p_j} (p_j - c_j) D_j(p_j, p_{-j}^{T1})$ 

**Key insight:** Firm can only lower its price (or keep it unchanged)

After observing competitors, firm best-responds to known prices rather than expected prices



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 $p^{T2}(c_1, p^{T1}) = min(p^{T1}, p^*)$  $p^* = \arg \max(p_i - c_i)D_i(p_i, p_{-i}^{T1})$ Key insight: Firm can only lower its price (or keep it unchanged)

Second Stage: Ontimal Pricing with Learning

# **Expected Profits in Second Stage**

When consumer searches, firm *j* faces two scenarios:

1. Selected for external offer 
$$(\frac{1}{J}$$
 probability):

$$\pi_j^{(j)}(p^{T1},c_j) = (p_j^{T2}(c_j,p^{T1}) - c_j)D_j(p_j^{T2}(c_j,p^{T1}),p_{-j}^{T1})$$

2. Competitor 
$$j'$$
 selected  $(\frac{1}{J}$  probability):

$$\pi_j^{(j')}(p^{T1},c_j,c_{j'}) = (p_j^{T1}-c_j)D_j(p_{-j'}^{T1},p_{j'}^{T2}(c_{j'},p^{T1}))$$

# **Expected second stage profits:**

ond stage profits: 
$$\pi_j^{T2}(p^{T1},c_j,c_{-j}) = \frac{1}{J} \left[ \pi_j^{(j)}(p^{T1},c_j) + \sum_{j' \neq j} \pi_j^{(j')}(p^{T1},c_j,c_{j'}) \right]$$



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### 2. Competitor / selected (4 probability) $\pi_i^{(j')}(p^{T1}, c_i, c_{i'}) = (p_i^{T1} - c_i)D_i(p_{-j'}^{T1}, p_{i'}^{T2}(c_{i'}, p^{T1}))$ Expected second stare profits: $\pi_j^{Y2}(\rho^{Y1}, c_j, c_{-j}) = \frac{1}{j} \left[ \pi_j^{(j)}(\rho^{Y1}, c_j) + \sum_{c,c} \pi_j^{(f)}(\rho^{Y1}, c_j, c_{j'}) \right]$

 $\pi^{(j)}(\rho^{T1}, c_i) = (\rho^{T2}(c_i, \rho^{T1}) - c_i)D_i(\rho^{T2}(c_i, \rho^{T1}), \rho^{T2})$ 

- 20

# First Stage: Strategic Pricing

Firms anticipate the second stage when setting initial prices

**Expected profits in first stage:** 

$$\pi_j^{T1}(p^{T1}, c_j, c_{-j}) = (1 - \lambda) \underbrace{(p_j^{T1} - c_j)D_j(p^{T1})}_{\text{Immediate acceptance}} + \lambda \underbrace{\pi_j^{T2}(p^{T1}, c_j, c_{-j})}_{\text{Search occurs}}$$

**Equilibrium condition:** 

ondition: 
$$\int_{-\pi}^{\pi} T_1(x) = \int_{-\pi}^{\pi} T_1$$

 $p_j^{T1}(c_j) = \arg\max_{o_i} \int \pi_j^{T1}(p_j, p_{-j}^{T1}(c_{-j}), c_j) dF(c_{-j}|c_j)$ 

Trade-off: higher initial price (if accepted) vs. competitive position if search occurs

-Model Equilibrium condition:  $\rho_i^{T1}(c_i) = \arg \max \int \pi_i^{T1}(\rho_i, \rho_{-i}^{T1}(c_{-i}), c_i) dF(c_{-i}|c_i)$ First Stage: Strategic Pricing Trade-off: higher initial price (if accepted) vs. competitive position if warch occur

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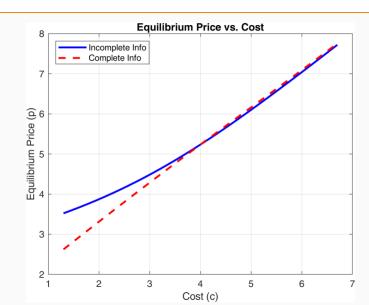
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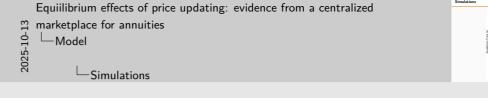
21

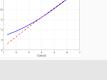
 $\pi_j^{T1}(\rho^{T1},c_j,c_{-j}) = (1-\lambda)\underbrace{(\rho_j^{T1}-c_j)D_j(\rho^{T1})}_{\text{tended on some points}} + \lambda\underbrace{\pi_j^{T2}(\rho^{T1},c_j,c_{-j})}_{\text{tended on some points}}$ 

First Stage: Strategic Pricing

# Simulations







# **Initial prices**

### MODALIDAD RENTA VITALICIA INMEDIATA

RENTA VITALICIA INMEDIATA SIMPLE

Annuitize full wealth, 0 guarantee, 0 deferral

N° Oferta	Compañía de Seguros de Vida	Pensión final Mensual sin Retiro de	Pensión final Mensual en UF Considerando un retiro de	Pensión con retiro de Excedente Máximo		Clasificación de riesgo de la
	Brand Name	Excedente UF	excedente de 0,00 UF	Pensión final Mensual UF	Excedente UF	Compañía de Seguros (2)
43872093	CRUZ DEL SUR	26,61	<- Monthly payment		Risk rating ->	AA-
43872099	RENTA NACIONAL	26,58				BBB-
43872083	METLIFE	26,52				AA
43872100	CORPSEGUROS	26,34				AA-
43872094	PRINCIPAL	26,28				AA
43872097	CORPVIDA	26,26				AA-
43872084	EUROAMERICA VIDA	26,25				AA-
43872090	PENTA VIDA	26,25				AA-
43872091	OHIO NATIONAL	26,24				AA
43872098	SURA	26,21				AA
43872095	CN LIFE	25,90				AA
43872092	BICE VIDA	25,86				AA+
43872085	CHILENA CONSOLIDADA	25,59				AA
43872086	CONSORCIO VIDA	25,36				AA+

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Model

Initial prices

