Chapter 11 Checkpoint

Directions:

mistakes. Learning is my superpower.

- You will have 2 hours to complete as many of the following questions as you can. When you begin the checkpoint, please write down the current time at the top of your cover page, and leave a space to write the time you finish. When you finish please immediately write the time.
- You may use your notes, the book, and any materials posted on the course website. Also, feel free to ask me clarifying questions or about typos. You may not use any other resource. In particular, you may not use any other resource on the internet, you may not use a computer to assist you with graphing or computations (unless the problem explicitly states otherwise) and you may not discuss the problems with anyone else.
- Each problem corresponds to a standard and specifically asks about that standard. You many complete as many or as few of the problems as you wish.
- If you have a question about any of the problems, or think there is an error please email me immediately. Also, if something occurs during your allotted time or some other special circumstance arises, please email me immediately.
- Write your own personal growth mindset statement. This really does help you do better on the checkpoint. If you have trouble thinking of a growth mindset statement you can use this one:

 I am a problem solver and my mind grows everyday. I improve with lots of practice. I learn from my

□ I.1	I can define and interpret double integrals of functions of two variables over rectangles and numerically approximate them using double Riemann sums.
□ I.2	I can set up and evaluate double integrals over general regions. I can interchange the order of integration.
□ I.3	I can set up and evaluate double integrals in polar coordinates.
□ I.4	I can set up and evaluate triple integrals over general regions. I can interchange the order of integration.

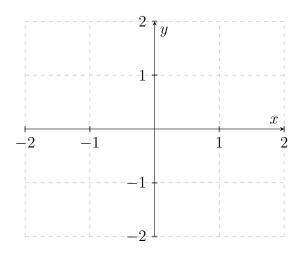
Chapter 11: I can calculate, use, and interpret multiple integrals.

- I.1 Consider the integral $\int_{-1}^{2} \int_{0}^{2} e^{x^{2}} dy dx$.
 - (a) Sketch the region of integration.
 - (b) Partition the region into six boxes and use this partition to estimate the value of the integral using a Riemann sum. For each box use the bottom right point to estimate the value of the function.
 - (c) In at least one full English sentence describe what the geometric meaning of $f(x_{ij}^*, y_{ij}^*) \Delta x \Delta y$ is in the Riemann sum $\sum_{i=1}^n \sum_{j=1}^m f(x_{ij}^*, y_{ij}^*) \Delta x \Delta y$.
- I.2 Exchange the order of the bounds of the integral.

$$\int_0^4 \int_{x/2}^{\sqrt{x}} f(x, y) \, dy \, dx = \int_?^? \int_?^? f(x, y) \, dx \, dy.$$

I.3 Draw a sketch of the region of integration. Convert the integral to polar coordinates. You do not need to evaluate the integral. (Hint: split the integral into two separate integrals)

$$\int_{-\frac{1}{\sqrt{2}}}^{1} \int_{-x}^{\sqrt{1-x^2}} x(x^2 + y^2) \, dy \, dx.$$



- I.4 Let E be the tetrahedron defined bounded by the planes x=0, z=0, z=2y, and 2x+2y+z=4. In this problem we set up the integral to find the volume of E with the given order of integration. You may need to write your answer as the sum of two or more integrals. **Do not evaluate** any of the integrals.
 - a) Sketch the region of integration.
 - b) Set up the integral to find the volume of E with order of integration dx dz dy.
 - c) Set up the integral to find the volume of E with order of integration dy dz dx.