

02/10/2020.

- IIA - if a voter changes their ranking of  $z$  but leaves  $x$  and  $y$  the same relatively then the relative outcomes for  $x$  and  $y$  do not change.
- Condorcet - if a candidate wins all pairwise match up they are the single winner
- Pareto - if every voter prefers  $x$  to  $y$  then  $y$  does not beat  $x$
- \* IIA = independence of irrelevant alternatives.

Do they or do they not?

	IIA	condorcet	pareto	up mono	add mono	anon
instant run-off	X	(x)	✓	X	✓	✓
coombs	X	X	✓	X	X	✓
Borda count	(x)	X	✓	✓	✓	✓
plurality	X	X	✓	✓	✓	✓
sequential pair	(x)	✓	X	✓	✓	✓
dictatorship	✓	X	✓	✓	✓	X

Eric: Borda-Condorcet-Counter

A A B

B B C

C C D

D D A

Austin: Borda-Pareto.

In Borda every vote gives candidates points relative to their rankings the higher the ranking the more points a candidate receives. If a candidate  $x$  places higher than candidate  $y$  on every voters ballot they then consistently received more points and thus must have more points than candidate  $y$  and so  $y$  could not beat  $x$

Carlin: Plurality-Condorcet-Counter

$V_1$   $V_2$   $V_3$   $V_4$   $V_5$

A B B C D

B A A A A

C C C D B

D D D B C

A = condorcet

B wins.

Plurality-IIA-Counter

$V_1$   $V_2$   $V_3$

A B C

B C A

C A B

tie (A=B)

$V_1$   $V_2$   $V_3$

A B A

B C B

C A C

A wins (A > B)

	IIA	condorcet	pareto	up mono	add mono	anon
copeland	(x)	✓	✓	✓	✓	✓

Emily: Pareto - Plurality

Suppose every voter prefers  $x$  to  $y$ . Then  $y$  can never be in first place since at a minimum  $x$  beats  $y$ . So  $y$  has 0 first place votes and is in last place. It may tie with  $x$  if  $x$  receives first place votes but it cannot place over (1)  $x$ .

Emily: Pareto - Dictatorship

Supposing every voter prefers  $x$  to  $y$  then the dictator also prefers  $x$  to  $y$  so  $x$  beats  $y$ .

Coombs - Condorcet - Counter

A	A	A	B	B
B	D	C	C	C
C	B	D	D	D
D	C	B	A	A

Instant runoff - Condorcet - Counter

B	D	C	C	D
A	A	A	A	A
C	C	B	D	C
D	B	D	B	B

Kit Kat: Coombs - IIA - counter

A	C	A	C	A
B	B	C	A	C
C	A	B	B	B

→

A	C	A	C	A
B	B	C	B	C
C	A	B	A	B

3-B 2-C 1-A

C < A

2-A/B 1-C

A < C

B moves.

Eric: IIA - instant runoff - counter

(1)	x	y	y
	y	x	x
	z	z	z

y wins →

x	y	z
y	x	y
z	z	x

all tie

\* A lot of this criteria are contradictory

Arrow's theorem: the only system that is IIA and up mound, is dictatorship.

\* You cannot Condorcet and IIA at the same time (another theorem)