
SYSC 4101 / 5105

Graph Criteria (Part II)

Graph Testing—Two Families of Criteria

- **Control Flow Criteria**
 - Only consider the flow of nodes and edges
 - Seven criteria
- **Data Flow Criteria**
 - Considers the definitions and usages of data along paths
 - Three criteria

Graph Testing—Data Flow Criteria

- Assumption: to test a program adequately, we should focus on the flows of data values.
 - To ensure that the values created at one point in the program are created and used correctly later on in the program.
 - Focus on definitions and uses of data values.
 - Definition
 - A definition (def) is a location where a value for a variable is stored in memory (assignment, input, ...)
 - Use
 - A use (use) is a location where a variable value is accessed.
 - Complementary definitions (not used in this course)
 - P-use: a use in a predicate
 - C-use: a use in a computation
 - DU-pair
 - A DU-pair is a pair (def, use) for a variable.
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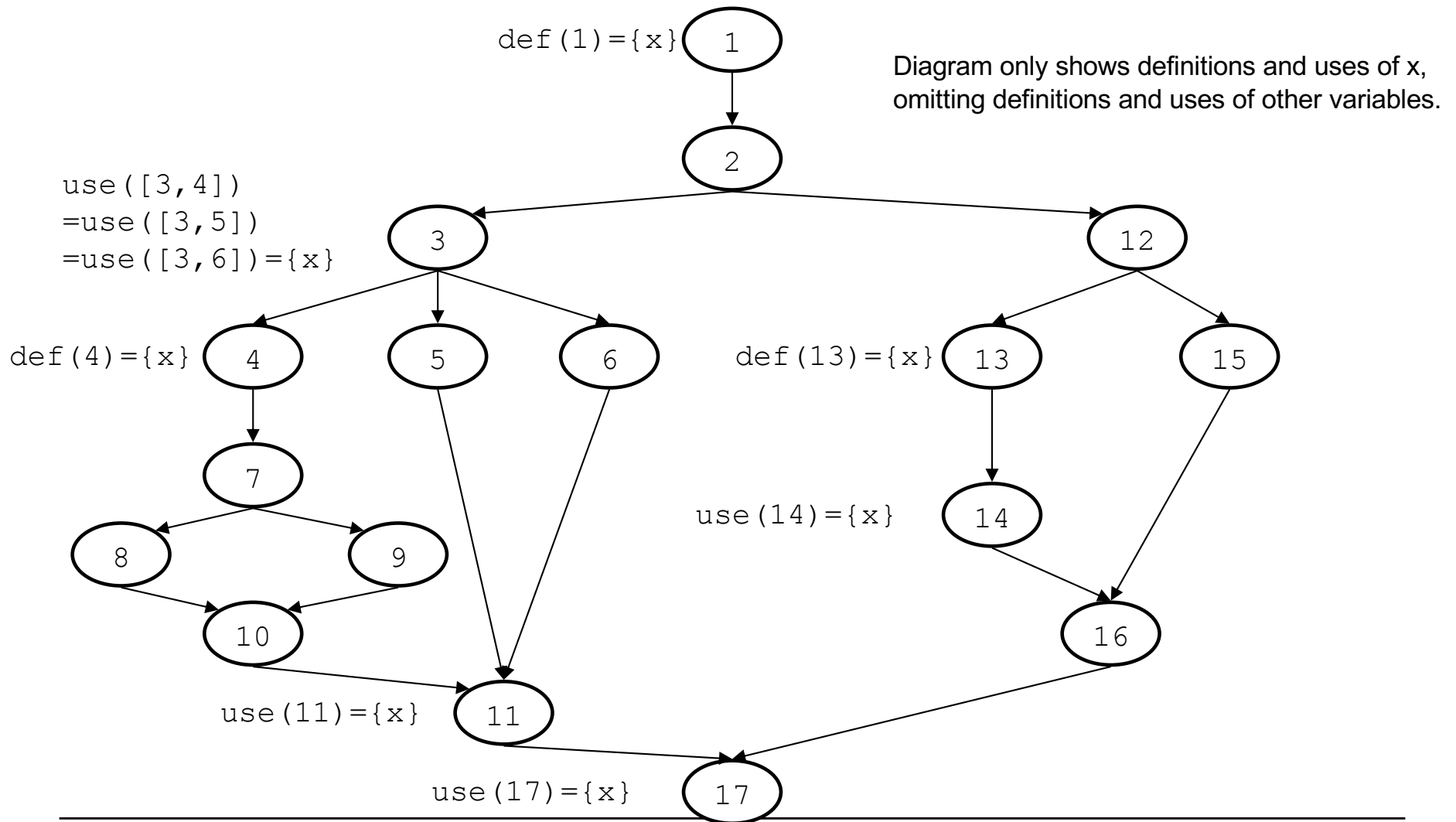
Data Flow Principles

- V is the set of all program variables involved in graph model M .
 - $\text{def}(n)$ (or $\text{def}(e)$) is the subset of V defined at node n (or edge e)
 - $\text{use}(n)$ (or $\text{use}(e)$) is the subset of V used at node n (or edge e)
- **Def-clear path**
 - Given a variable $v \in V$, and two locations l_i and l_j such that $v \in \text{def}(l_i)$ and $v \in \text{use}(l_j)$:
 - v is defined in l_i and used in l_j .
 - A path p from l_i to l_j is def-clear with respect to v if and only if for every location l_k on the path ($k \neq i, k \neq j$), $v \notin \text{def}(l_k)$:
 - there is no re-definition of v between (the definition in) l_i and (the use in) l_j .
- **DU-path**
 - A du-path with respect to variable v is a def-clear (with respect to v), simple path.
(May not be def-clear for another variable.)

Data Flow Principles

- **Def-path: $du(n_i, v)$**
 - $du(n_i, v)$ is the set of du-paths with respect to variable v that start at node n_i .
- **Def-pair: $du(n_i, l_j, v)$**
 - $du(n_i, l_j, v)$ is the set of du-paths with respect to variable v that start at node n_i and end at location l_j .
 - All the simple ways to get from a definition of v at n_i to a use of v at l_j without further (re)definitions of v .
- **Notes:**
 - A definition clear path with respect to variable v is not necessarily definition clear with respect to other variables
 - A definition clear path with respect to variable v is not necessarily use clear with respect to variable v !
 - There might be other uses of v between the definition and the use.
 - $du(n_i, v) = \bigcup_{l_j} du(n_i, l_j, v)$
 - It is also possible (but difficult, and not used a lot) to generalize those definitions and define $du(l_i, v)$ and $du(l_i, l_j, v)$, i.e., def-paths and def-pairs that start at any location (nodes and edges).

Data Flow Criteria – An Example



Data Flow Criteria – An Example (cont.)

- $du(1, [3, 4], x) = \{[1, 2, 3, 4]\}$
- $du(1, [3, 5], x) = \{[1, 2, 3, 5]\}$
- $du(1, [3, 6], x) = \{[1, 2, 3, 6]\}$
- $du(1, 11, x) = \{[1, 2, 3, 5, 11], [1, 2, 3, 6, 11]\}$
- $du(1, 14, x) = \emptyset$
- $du(1, 17, x) = \{[1, 2, 3, 5, 11, 17], [1, 2, 3, 6, 11, 17], [1, 2, 12, 15, 16, 17]\}$
- $du(1, x) = \{[1, 2, 3, 4], [1, 2, 3, 5], [1, 2, 3, 6], [1, 2, 3, 5, 11], [1, 2, 3, 6, 11], [1, 2, 3, 5, 11, 17], [1, 2, 3, 6, 11, 17], [1, 2, 12, 15, 16, 17]\}$
- $du(4, 11, x) = \{[4.7.8.10.11], [4.7.9.10.11]\}$
- $du(4, 17, x) = \{[4.7.8.10.11, 17], [4.7.9.10.11, 17]\}$
- $du(4, x) = \{[4.7.8.10.11], [4.7.9.10.11], [4.7.8.10.11, 17], [4.7.9.10.11, 17]\}$
- $du(13, 14, x) = \{[13, 14]\}$
- $du(13, 17, x) = \{[13, 14, 16, 17]\}$
- $du(13, x) = \{[13, 14], [13, 14, 16, 17]\}$

Data Flow Criteria

- **All-Defs Criterion (ADC)**
 - For each def-path set $S = \text{du}(n, v)$, TR contains at least one path d in S .
- **All-Uses Criterion (AUC)**
 - For each def-pair set $S = \text{du}(n_i, n_j, v)$, TR contains at least one path d in S .
- **All-DU-Paths Criterion (ADUPC)**
 - For each def-pair set $S = \text{du}(n_i, n_j, v)$, TR contains every path d in S .

Data Flow Criteria – An Example (cont.)

Objectives (sub-paths)

- All-Defs:
 - [1,2,3,4]
 - [4,7,8,10,11]
 - [13,14]
- All-Uses:
 - [1,2,3,4]
 - [1,2,3,5]
 - [1,2,3,6]
 - [1,2,3,5,11]
 - [1,2,3,5,11,17]
 - [4,7,8,10,11]
 - [4,7,8,10,11,17]
 - [13,14]
 - [13,14,16,17]

Test cases (test paths)

- All-Defs:
 - [1,2,3,4,7,8,10,11,17]
 - [1,2,12,13,14,16,17]
- All-Uses:
 - [1,2,3,5,11,17]
 - [1,2,3,6,11,17]
 - [1,2,3,4,7,8,10,11,17]
 - [1,2,12,13,14,16,17]

Data Flow Criteria – An Example (cont.)

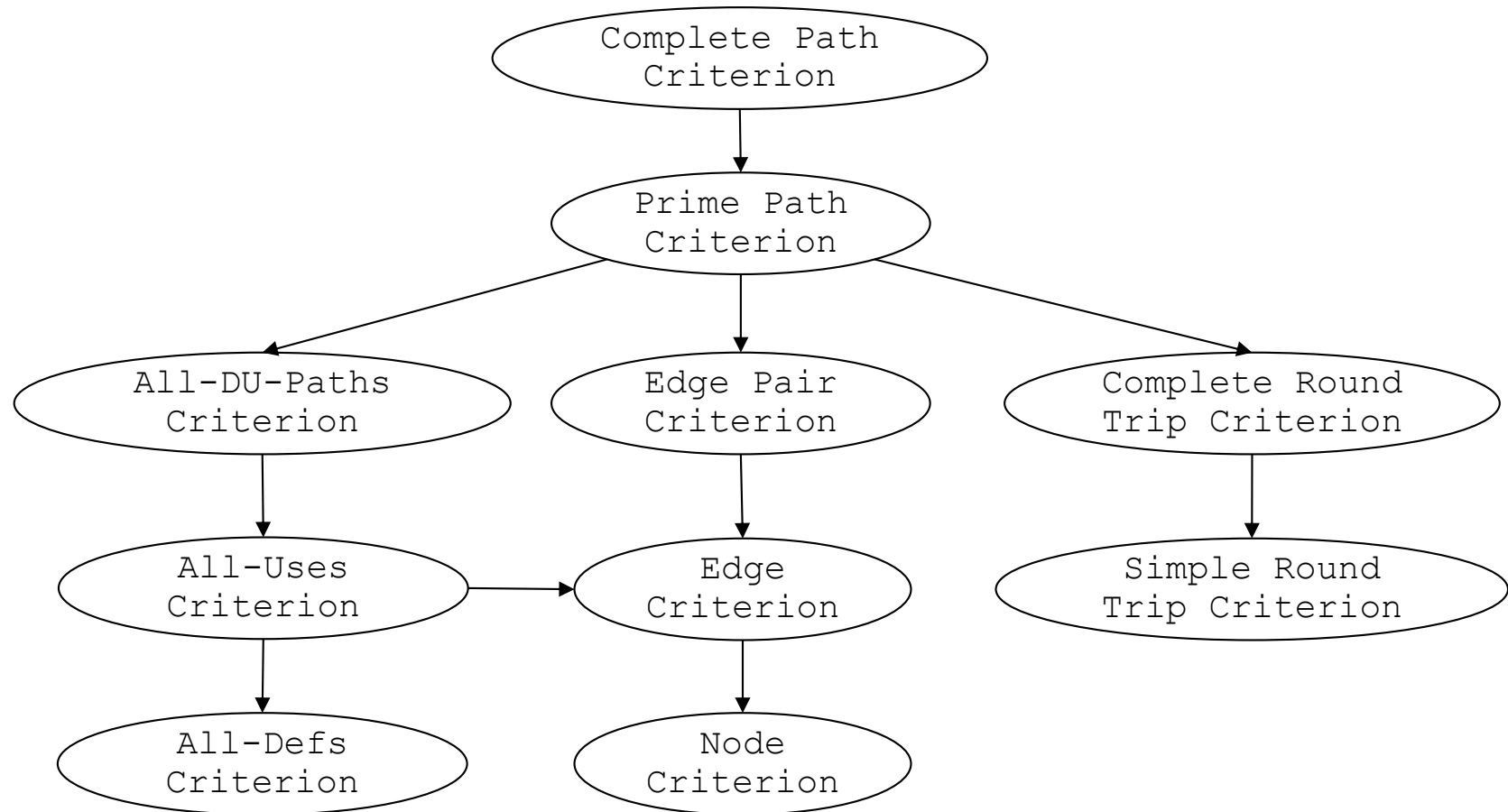
Objectives (sub-paths)

- All-DU-paths:
 - [1,2,3,4]
 - [1,2,3,5]
 - [1,2,3,6]
 - [1,2,3,5,11]
 - [1,2,3,6,11]
 - [1,2,3,5,11,17]
 - [1,2,3,6,11,17]
 - [1,2,12,15,16,17]
 - [4,7,8,10,11]
 - [4,7,9,10,11]
 - [4,7,8,10,11,17]
 - [4,7,9,10,11,17]
 - [13,14]
 - [13,14,16,17]

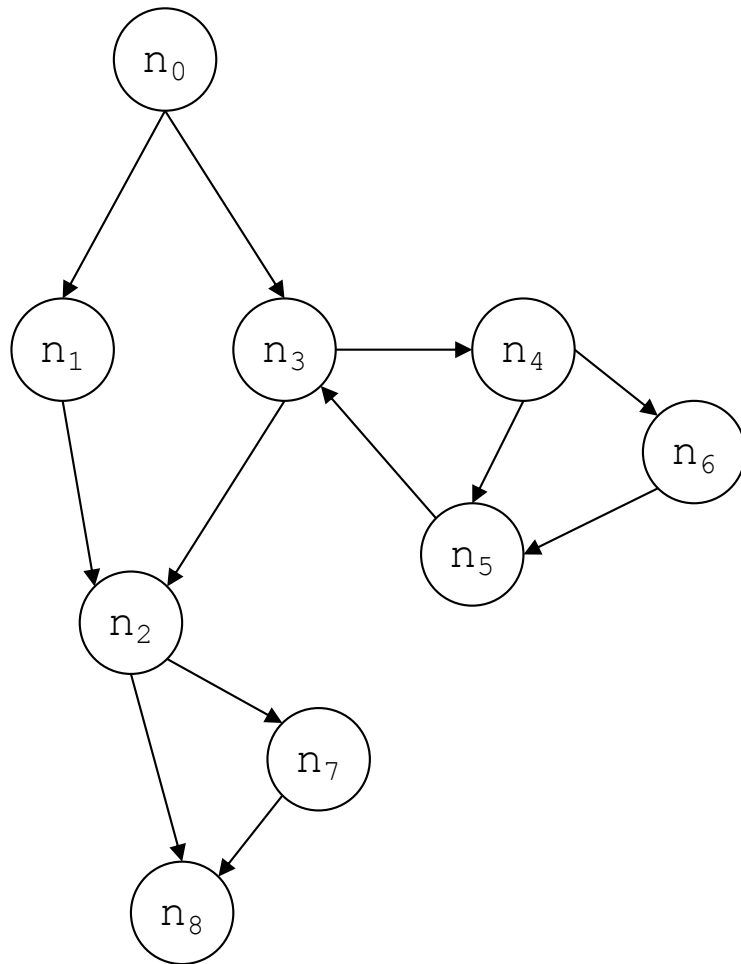
Test cases (test paths)

- All-DU-paths:
 - [1,2,3,5,11,17]
 - [1,2,3,6,11,17]
 - [1,2,3,4,7,8,10,11,17]
 - [1,2,3,4,7,9,10,11,17]
 - [1,2,12,15,16,17]
 - [1,2,12,13,14,16,17]

Subsumption



Comment on Feasibility



- We only used the syntax of the graph to determine test requirements and build test cases
 - (we did not consider actual inputs)
- What if (n_2, n_7) can only execute after n_3 ?
 - $\text{path}[t_1] = [n_0, n_1, n_2, n_7, n_8]$ was used for the All-Edges criterion (recall previous lecture)
 - t_1 is not feasible
- The test sets we built may not all be feasible.
 - Not necessarily because of unfeasible test requirements
 - But because we build test paths that are unfeasible
- Alternative test sets must be investigated.
 - To still satisfy all feasible test requirements for the selected criterion