## **PhyloFormer:**

## Fast, accurate and versatile phylogenetic reconstruction with deep neural networks



Luca Nesterenko\*, **Luc Blassel**\*, Philippe Veber, Bastien Boussau<sup>†</sup>, Laurent Jacob<sup>†</sup> LISN Bioinfo Seminar - November 21<sup>st</sup>, 2024









#### Preamble - Who am I?

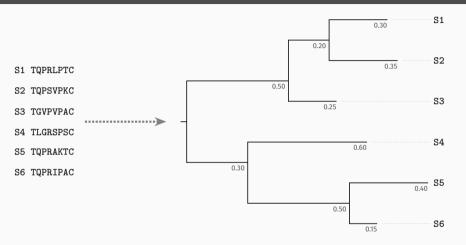
- Studied biology at AgroParisTech and machine-learning at Dauphine
- Did my **PhD.** at Institut Pasteur 2020-2022, working on:
  - 1. Drug resistance detection in HIV with O. Gascuel
  - 2. Improving long **read-mapping** with R. Chikhi
- Since March 2023, post-doc with Laurent Jacob at LCQB:
   Deep-learning for phylogenetic inference

Blassel, Zhukova, et al. 2021; Blassel, Tostevin, et al. 2021; Blassel, Medvedev, et al. 2022

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# What is Phylogenetic Inference ?

## Context - Phylogenetic inference



Goal: describe evolutionary-history of MSA

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#### Context - Why do phylgenetic inference?

Phylogenetic inference is a **base-task** essential in many **downstream** analyses:

**Epidemiology:** Track viral spread and evolution

**Virology:** Identify recombination events

**Biochemistry:** Identify functional constraints on proteins

**Ecology:** Characterize biodiversity

•••

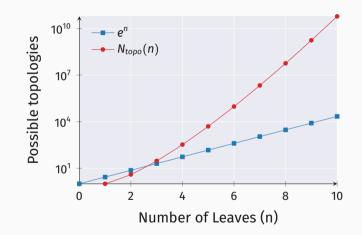
Hadfield et al. 2018; Nelson et al. 2008; Harms and Thornton 2013; Perez-Lamarque et al. 2022

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## Context - The problem with phylogenetic inference

- 1. Phylogenies are hard!
- 2. **Super-exponential** tree space

$$N_{topo}(n) = \frac{(2n)!}{(n+1)!}$$



Felsenstein 2004

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## **Context - Likelihood-based tree reconstruction (1)**

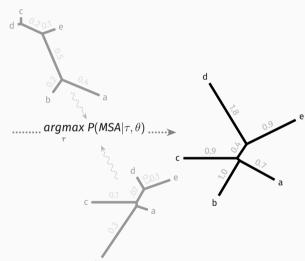


b TQPSVPKC

c TGVPVPAC

d TLGRSPSC

e TQPRAKTC



 $au = ext{Phylogeny}$   $au = ext{Model}$ 

 $\theta = \mathsf{Model}$ 

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#### **Context - Likelihood-based tree reconstruction (2)**

#### **Pros:**

- These methods are accurate
- The **whole MSA** is considered in  $P(MSA|\tau,\theta)$
- With Bayesian methods you quantify uncertainty

#### Cons:

- · These methods are slow
  - 1. **Computing** the likelihood is **costly**
  - 2. We have to **explore** the tree-space with **topological** moves
- We are **limited** to models where  $P(MSA|\tau,\theta)$  is **computeable**

## **Context - Distance-based tree reconstruction (1)**

 $au = f(\mathsf{DM})$ 

 $DM = \{d(i,j), (i,j) \in MSA\}$ 

we **choose** d

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#### Context - Distance-based tree reconstruction (2)

#### Pros:

- These methods are **fast**:  $\mathcal{O}(n^2)$  to  $\mathcal{O}(n^3)$
- These methods are statistically consistent
- Guaranteed to infer the true tree if  $\mathit{Err}(\mathit{DM}) \leq \varepsilon$
- Many **variants**: NJ, BioNJ, FastME, ...

#### Cons:

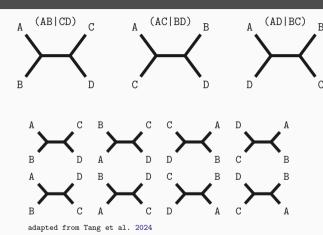
- These methods are innacurate compared to ML
- We **ignore** information when computing  $d(i,j), (i,j) \in MSA$

Gascuel and Steel 2016; Guindon and Gascuel 2003; Saitou and Nei 1987; Gascuel 1997; Lefort et al. 2015

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## Machine Learning for Phylogenetic Inference

#### **Background - Quartet methods**



Bandelt and Dress 1986; Strimmer and Von Haeseler 1996

- Unrooted quartet has 3 unique topologies
- An n tree topology is uniquely represented by its set of nC4 quartets
- Likelihood-based methods exist to infer trees from quartets

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#### Background - Quartet classifier networks

#### Classifier that predicts the quartet topology given a set of 4 sequences

#### **Pros:**

- Adaptable to different tree sizes
- Simple training and loss
- Deal with equivalent quartets:
  - Data augmentation
  - · Network architecture

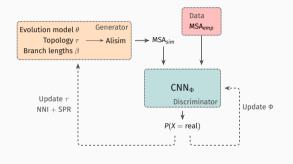
#### Cons:

- **Scaling**: Quartets(n) =  $\binom{n}{4}$
- Poor performance in settings with long branches and short sequences

Suvorov et al. 2019; Zou et al. 2020; Tang et al. 2024; Zaharias et al. 2022

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#### **Background - GANs**



- Given a real MSA M
- Generator builds a tree T and simulates an MSA M'
- Discriminator learns to differentiate M and M' with CNN
- Train D with backprop and G with topological moves on tree
- Need to train model for each inferred tree

Smith and Hahn 2023

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## Background - Learning to explore tree-space

#### **Topology search**

- Exploring the whole topology space is too expensive
- Heuristic topological moves:

**SPR** Subtree Prune Regraft **NNI** Nearest Neighbour
Interchange

- At each step select moves by best  $\mathcal L$ 

Azouri, Granit, et al. 2024; Azouri, Abadi, et al. 2021

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## Background - Learning to explore tree-space

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#### ML-guided topology search

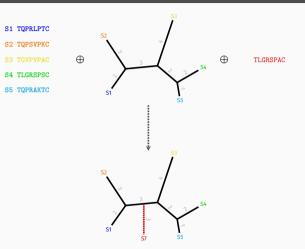
- Train models to predict the next best move
- Rank SPRs by predicted likelihood with RF regressor
- This was also done with NNs in an RL setting
- Once trained speeds up likelihood methods

Azouri, Granit, et al. 2024; Azouri, Abadi, et al. 2021

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## **Background - Phylogenetic placement**

- Given a tree, an MSA and a sequence, what is the best spot to add a new branch?
- ML and distance based methods for placement
- Better scaling than full tree search



Price et al. 2010; Nguyen et al. 2015; Lefort et al. 2015

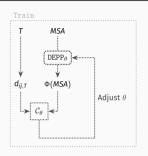
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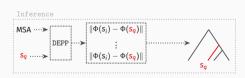
#### **Background - DEPP**

- With a Backbone tree T and MSA
- Minimize C w.r.t  $\Phi$  :

$$\mathcal{C} = \sum_{(i,j)} rac{1}{d_{ij,T}} \left( \| \Phi(\mathbf{s}_i) - \Phi(\mathbf{s}_j) \|_2 - \sqrt{d_{ij,T}} 
ight)^2$$

- **Embed** new **sequence**  $\Phi(s_{new})$
- Get **distances** from  $\Phi(s_{new})$  to others and place it
- Use distance-based placement method APPLES





Balaban et al. 2020; Jiang et al. 2022

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## Background - DEPP the good and the bad

#### The good:

- Small simple architecture:
   Conv × 3 + FCN
- Easy to train
- Scales to backbones of  $\approx 10^4$  tips
- Successful application on microbial tree-of-life

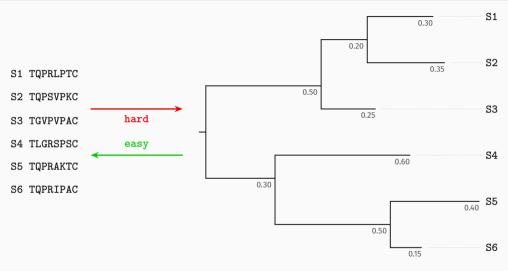
#### The less good:

- This is a simpler problem that what we want to solve
- Need to train for every backbone tree and MSA

Jiang et al. 2022

Likelihood-free phylogenetic inference with PhyloFormer

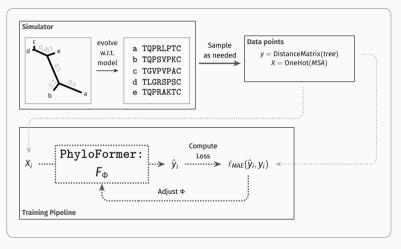
## Method - Likelihood-free inference, motivation



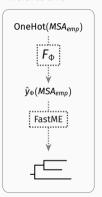
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#### Method - Amortized likelihood-free inference

#### Training time

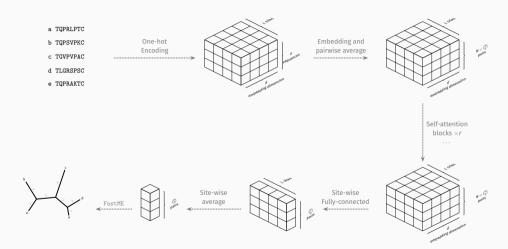


#### Inference time



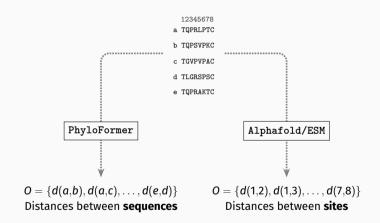
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#### **Method - PhyloFormer overview**



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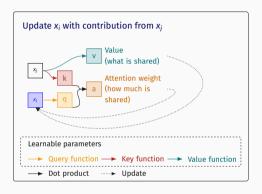
#### **Method - Similarity with structure prediction**



Jumper et al. 2021; Rao et al. 2021

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#### **Method - Why self-attention**

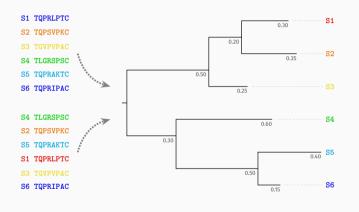


- Represents elements in a set as a weighted sum of all elements (including itself)
- Parametrized by learnable weights
- Yields a context-aware and learnable representation
- Applies to sets regardless of cardinality

Vaswani et al. 2017

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## Method - Ensuring invariance & equivariance

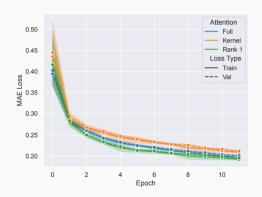


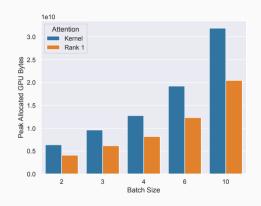
**Self-Attention** is already permutation **equivariant!** 

**Site-wise average** ensures **invariance** w.r.t. sites.

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#### **Method - Custom Rank 1 attention is better**





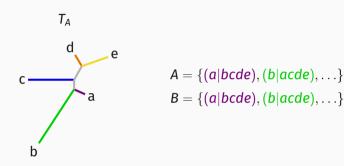
Vaswani et al. 2017; Katharopoulos et al. 2020

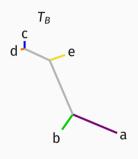
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## **How does PhyloFormer perform?**

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## Results - How do we measure performance?





$$RF_{\text{norm}}(T_A, T_B) = (|A| + |B|)^{-1}(|A \cup B| - |A \cap B|)$$

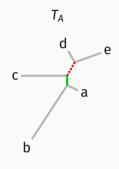
$$KF(T_A, T_B)^2 = \sum_{e \in A \cap B} (w_{(e,A)} - w_{(e,B)})^2 + \sum_{e \in A \setminus B} w_{(e,A)}^2 + \sum_{e \in B \setminus A} w_{(e,B)}^2$$

$$\ell_{MAE}(T_A, T_B) = {}_{n}C_{2}^{-1} \sum_{\{j,i\} \in T_A} |d(i,j,T_a) - d(i,j,T_B)|$$

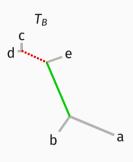
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## Results - How do we measure performance?



 $A = \{(ab|cde), (de|abc)\}$  $B = \{(ab|cde), (dc|abe)\}$ 



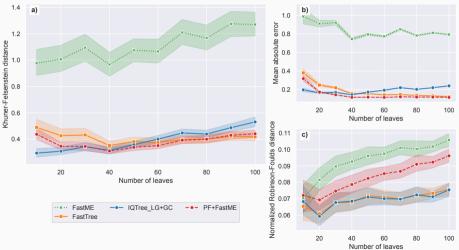
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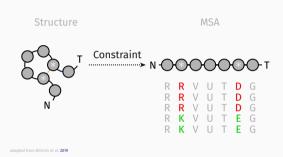
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## Results - Under LG+GC model, PF performs on par with ML



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#### Results - What about more complex models? - CherryML



- We simulate 250 pairs of adjacent co-evolving sites
- We use a 400 × 400 substitution matrix to describe residue co-evolution, from CherryML
- Most ML methods would consider sites independent

Prillo et al. 2023

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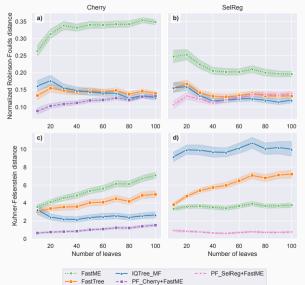
## Results - What about more complex models? - SelReg

- Sites are: positively, negatively or neutrally selected
- **Codon** model with a  $61 \times 61$  matrix
- 263 empirical amino-acid profiles
- ML-Inferrable with mixture-models but expensive

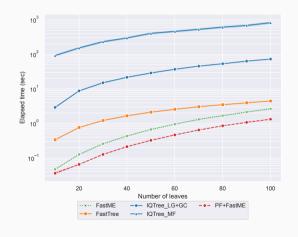
Duchemin et al. 2023; Halpern and Bruno 1998; Tamuri and Reis 2021

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#### Results - Under complex models, PF performs well



#### **Results - Inference speed**

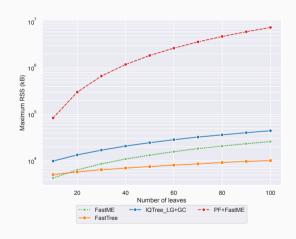


- PhyloFormer is the fastest method<sup>a</sup>
- PhyloFormer is even faster than FastME on its own
- Inference speed is independent from model complexity

<sup>a</sup>using a GPU & more memory

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#### **Results - Memory consumption**



- PhyloFormer has the highest memory footprint (by far)
- Even more-so at training-time
- However, PhyloFormer can be run on CPU

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### PhyloFormer - Take Home messages

#### **Take-Home**

- 1. On the standard **LG model**, PhyloFormer performs on **par with ML** methods
  - Especially w.r.t. pairwise distances
  - Less w.r.t pure topology
- 2. It is **easily adaptable** to **complex models**, where computing the **likelihood** is **impossible**
- 3. Once trained, it is the **fastest method**<sup>1</sup>

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<sup>&</sup>lt;sup>1</sup>Provided you have a GPU and a lot of trees to infer...

# **Improving PhyloFormer**

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### We heard the good, what about the bad?

- 1. **Embedding** sequence pairs scales in  $\mathcal{O}(n^2)$  in time and memory
  - ⇒ **Hard** to scale to **large MSAs** and/or **long sequences**
- 2. We have **no guarantees** that the predicted **distances** are **tree-like** 
  - ⇒ Is predicting distances and trees really equivalent here?
- 3. Not model-agnostic, we perform implicit model selection at simulation-time
- PhyloFormer is dependant on the MSA input, by aligning we are already introducing bias

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### Extensions - Linear scaling in n

- Basic idea: wait until last-minute to lift up into pair-space
- Use Axial Attention to learn MSA-aware sequence embeddings
- Compute parametrized pairwise embedding-distances:
  - Either euclidean distances between embeddings
  - Or with symmetric bilinear form
- Related work in NeuroSeed, e.g. edit-distance approximation with hyperbolic sequence embeddings

Corso et al. 2021; Vienne et al. 2012; Layer and Rhodes 2017

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# Extension - Learning embedding distances

Given **sequence-embeddings**  $\Phi(S)$  of shape  $(n \times d)$ 

$$E = \Phi(S)W_{euc}^{\top} + b_{euc}$$
  
 $O = PairwiseEuclidean(E)$ 

• Tree distance  $d_{ij,T}$  is not euclidean,  $\sqrt{d_{ii,T}}$  is though

 $O = SoftPlus(\Phi(S)^{\top}W_{bit}\Phi(S) + b_{bit})$ 

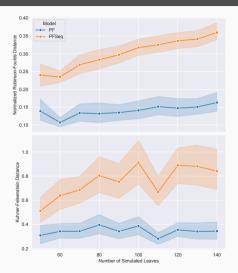
- bias  $b_{bil}$
- $W_{\theta}$  ensures that the distance **matrix** is **symmetric**

 $W_{bil} = W_{bil}^{\top}$ 

• SoftPlus ensures that **distances** are positive 35/48

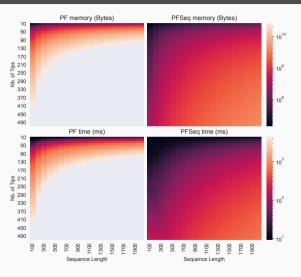
### **Extensions - How does PFSeq perform?**

- Training PFSeq well is harder than with PhyloFormer
- Maybe the pairwise information is harder to extract from sequence-embeddings?
- Similar train loss values but differing test performance
- Train longer and with more data?



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### Extensions - PFseq scales Much better than PhyloFormer



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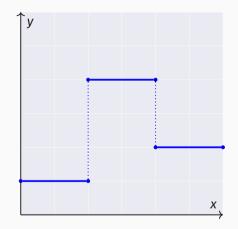
#### Extensions - End-to-end phylogenetic inference

- Theoretically, estimating distances or a tree are equivalent tasks
- **Practically**, not so much ...
- Can we constrain the output to tree-like distances?
- By adding a NJ step after PhyloFormer we can output trees directly
- Problem: NJ is iterative and discrete, i.e. not great for learning

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## Extensions - Estimating gradients through discrete operations

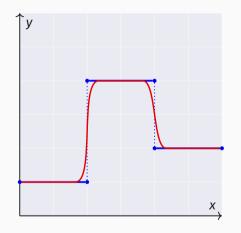
- Discrete implies non-differentiable
- Non-differentiability of a finite number of points is not always a problem: e.g. ReLU
- The **problem** is **piecewise** constance:  $\nabla f(x) = 0$ ;  $\forall x$



Berthet et al. 2020; Jang et al. 2017

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- The **problem** is **piecewise** constance:  $\nabla f(x) = 0$ ;  $\forall x$
- **Smooth** out f and  $\nabla f$ :
  - A perturbation approach
  - Straight-through trick



Berthet et al. 2020; Jang et al. 2017

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### Extensions - The Gumbel softmax straight-through "trick"

- Useful when you **need** to have **discrete steps** in your algorithm e.g:
  - Pairwise sequence alignment: average softmax values at each DP cell
    - ⇒ **No need** for discrete decision
  - Neighbour-Joining: You have to merge nodes to advance in the algorithm
    - $\Rightarrow$  **Need** to take discrete decision
- Given O a **discrete** operation with corresponding "soft" version  $\mathcal{O}$ :

(e.g. 
$$O = argmax$$
 and  $O = softmax$ )

```
forward: X \mapsto O(X)
backward: \nabla_{\theta} O(X) \approx \nabla_{\theta} \mathcal{O}(X)
```

```
out = (
  hard(in) - soft(in)
).detach() + soft(in)
```

### **Extensions - Differentiable Neighbour-Joining**

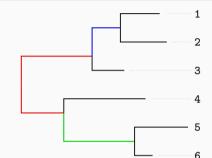
We have managed to build a PyTorch implementation of NJ that:

- Runs on the GPU
- Is **differentiable** w.r.t. model parameters because:
  - We use the straight-through trick to approximate gradients through merge-operations
  - We avoid any indexing and in-place operations that might break the computational graph

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### Extensions - Towards a topological loss function, splits

- Tree-topologies are uniquely represented by a set of leaf-splits
- With a leaf-ordering and a tie-breaking rule we have a unique matrix representation
- I.e we have a topological target



```
 \begin{array}{l} \{(1,2) \mid (3,4,5,6)\} \\ \{(1,2,3) \mid (4,5,6)\} \\ \{(1,2,3,4) \mid (5,6)\} \end{array} \Leftrightarrow \begin{bmatrix} 0 & 0 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}
```

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## Extensions - Topological Loss functions

Let S and  $\bar{S}$  be **row-normalized** split matrices,  $S_j$  the  $j^{th}$  row of S

#### RF as a loss

$$RF(S,\bar{S}) = \sum_{i,j} \mathbb{1}_{(S\bar{S}^\top)_{ij}=1}$$

$$RF(S,\bar{S}) \approx \sum_{i,j} (S\bar{S}^\top)_{ij}^p; p \gg 1$$

 $\mathbb{1}_{(S\overline{S}^{\top})=1}$  is discrete,  $x^{p}; p \gg 1$  not very stable

### **Relaxing RF**

$$RF_{ish}(S,\bar{S}) = \max_{\pi \in \Pi} \sum_{j=1}^{n-3} S_j^{\top} (\bar{S}_{\pi})_j$$
$$= \max_{A \in P} \operatorname{tr}(S\bar{S}^{\top}A)$$
$$= \max_{A \in conv(P)} \operatorname{tr}(S\bar{S}^{\top}A) + \varepsilon H(A)$$

**Optimal Transport** formulation of an **RF-like** topological **loss** 

### **Extensions - Topoformer preliminary results**

#### **Bad news:**

- Learning with a topological loss is hard
- The RF approximation with x<sup>p</sup> is too close to discrete version
- The OT RF-like loss is not behaving as we wish

#### **Good news:**

- We can recover a distance matrix easily from NJ's output
- We can use L<sub>1</sub> loss as with
   PhyloFormer, but guaranteed that
   d<sub>ij</sub> is tree-like
- This is more promising and training curves look better

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# **Wrapping things up**

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#### **Global Conclusion**

- Phyloformer enables phylogenetic inference from start to almost finish
- This is the first deep-learning method that does so
- Enables likelihood-free phylogenetic inference, paving the way for complex models

- Soon it will (hopefully)
  - Scale linearly with the number of sequences
  - Be truly **end-to-end** and produce trees
- Active work done to extend PhyloFormer functionality to other tasks

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#### Other related work (mostly not mine)

#### Exciting work being done in the team and with collaborators

- Estimating epidemiological parameters from MSAs directly
   V. Garot, L. Jacob, S. Alizon and A. Zhukova
- Quantifying selection at each MSA sites
   L. Nesterenko, C. West and B. Boussau
- Inferring phylogenies under Potts models
   P. Barrat-Charlaix, L. Jacob and J
- Estimating ecological parameters on trees using GNNs
   A. Leroy, H. Morlon and L. Jacob
- Detecting Ghost lineages an gene tree reconciliation with GNNs
   E. Marsot, B. Boussau, D. de Vienne and L. Jacob

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### Obligatory self-promotion slide

- The *updated* **PhyloFormer preprint** is out ⇒
- Help me build a phylogenetics crate in Rust: lucblassel/phylotree-rs
- You can find the slides here: lucblassel.com/files/slides\_lisn\_2024.pdf



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#### Thanks to:

- Luca Nesterenko
- Laurent Jacob
- Bastien Boussau
- Philippe Veber
- Martin Ruffel
- Dexiong Chen
- · Johanna Trost







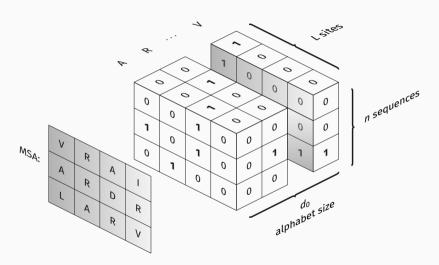




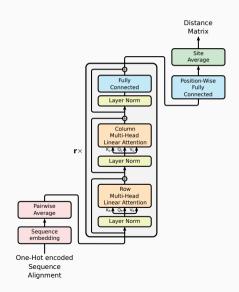


Special thanks to Jean-Zay for all the GPUs!

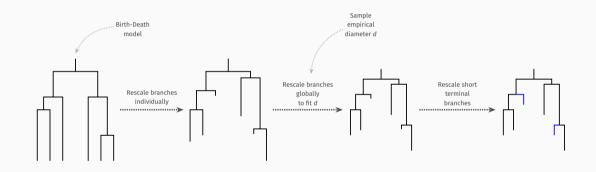
### **Additional Methods - Data Encoding**



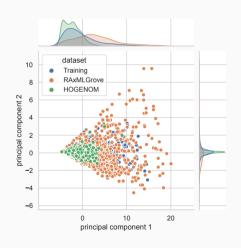
#### **Additional Methods - Network Architecture**



#### **Additional Methods - Tree simulation**

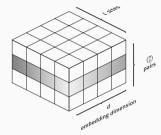


#### Additional Methods - Realistic tree distribution



#### **Additional Methods - Axial self-attention<sup>2</sup>**

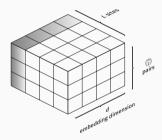
#### **Row attention**



Update sites in a pair by **looking** at all **other sites** in the same **pair** 

<sup>2</sup>Ho et al. 2019; Rao et al. 2021.

#### **Column attention**



Update sites in a pair by **looking** at the same site in all other pairs

#### **Additional Methods - Custom Rank1 Attention**

#### **Scaled dot-product**

$$Z = softmax \left(\frac{QK^{\top}}{\sqrt{d_k}}\right) V$$

#### **Linear Kernel Attention**

$$z_i = \frac{\tilde{\phi}(q_i)^{\top} \sum_{j=1}^{M} \tilde{\phi}(k_j) v_j}{\tilde{\phi}(q_i)^{\top} \sum_{h=1}^{M} \tilde{\phi}(k_h)}$$

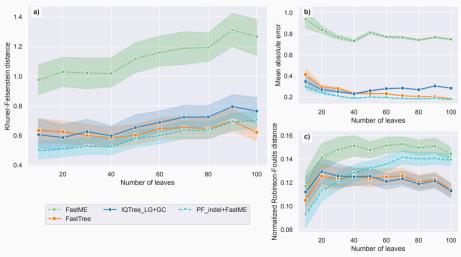
#### **Our Rank-1 Attention**

$$\tilde{\phi}(x) = \left\{ egin{array}{ll} x+1, & \mbox{if } x>0 \ \exp\{(x)\} & \mbox{if } x\leq 0, \end{array} 
ight.$$

$$z_i' = \frac{\tilde{\phi}(q_i)}{\mathsf{M}^{-1} \sum_{g=1}^{M} \tilde{\phi}(q_g)} \cdot \frac{\sum_{j=1}^{M} \tilde{\phi}(k_j) \mathsf{v}_j}{\sum_{h=1}^{M} \tilde{\phi}(k_h)}$$

Vaswani et al. 2017; Katharopoulos et al. 2020

#### **Additional Results - Indel Model**

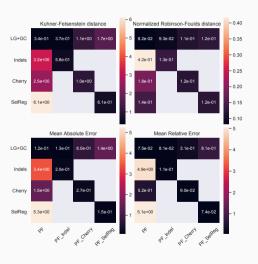


### Additional Results - PF captures co-evolution out of the box

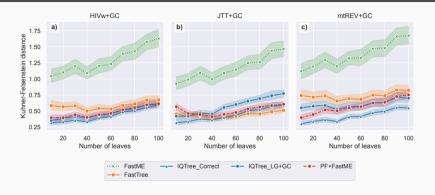
Network on test dataset:	PF <sub>Cherry</sub> on <b>Cherry</b>	PF on <b>Cherry</b>	PF <sub>Cherry</sub> on <b>LG</b>	PF on <b>LG</b>
a = co-evolution attentions	0.256	0.255	0.120	0.135
b = other attentions	0.098	0.115	0.121	0.136
Ratio a/b	4.424	3.408	0.999	0.995
auto-attentions	0.579	0.535	0.542	0.523

- PF Already assigns high-attention values to co-evolving site pairs
- PF<sub>Cherry</sub> likely exploits this signal for better performance
- PF does this without needing positional encoding

#### Additional Results - PF performs model-based inference



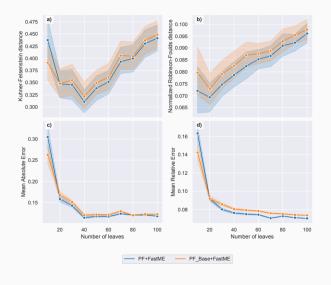
#### Additional Results - PhyloFormer is likelihood-free not model-free



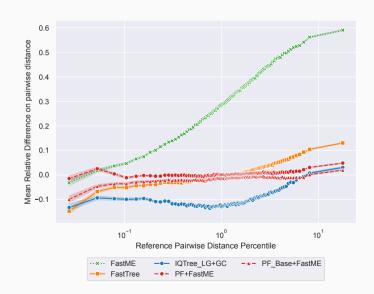
Substitution models chosen to be far from LG

Minh et al. 2021: Norn et al. 2021

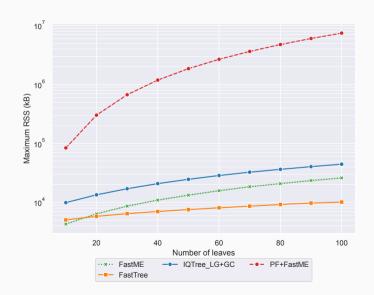
### Additional Results - Fine tuning with MRE loss



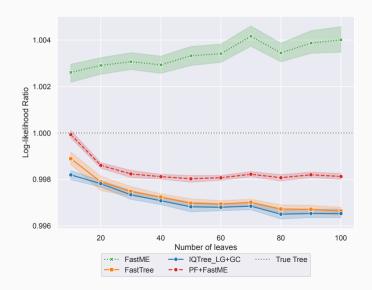
#### Additional Results - Mean relative error



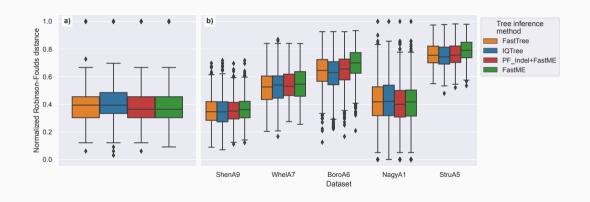
### **Additional Results - Memory requirements**



### Additional Results - PhyloFormer outputs likely trees



### Additional Results - PhyloFormer is similar to SoTA on empirical data



### **Additional Results - Training runs**

Network Name	Starting Network	Batch Size	Dataset Size	Model of evolution	Effective number of Steps/Epochs	GPUs used	Target learning rate	Target schedule steps	Selected checkpoint step	Loss Function
$PF_{Base}$	Initialized network	4	170k	LG+GC	145.18k/20.5	6×A100	$10^{-3}$	213.2k	144k	MAE
PF	$PF_{Base}$	4	224k	LG+GC	40.3k/4.32	6×A100	$10^{-4}$	66k	40,3k	MRE
PF <sub>Indel</sub>	$PF_{Base}$	1	55k	LG+GC+indels	240k/17.45	4×V100	$10^{-3}$	240k	136.5k	MAE
PF <sub>Cherry</sub>	$PF_{Base}$	4	1M	Cherry	30k/0.72	6×A100	$10^{-3}$	66k	18k	MAE
PF <sub>SelReg</sub>	$PF_{Base}$	4	1M	SelReg	66k/1.58	6×A100	10 <sup>-3</sup>	66k	66k	MAE

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