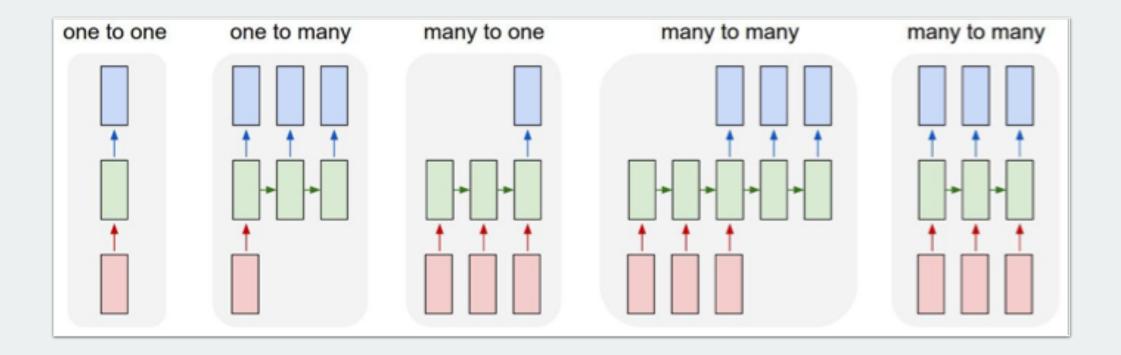
# Artificial Neural Networks and Deep Learning

Week 5

Recurrent neural networks

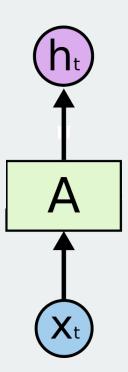
Recurrent Neural Networks
THE neural network architecture to use for sequential data

> Ways to process sequential data



# The problem with all feed forward neural networks

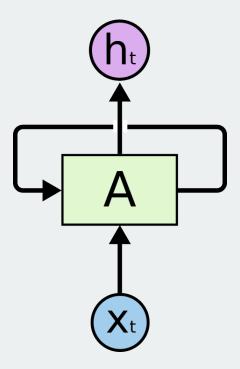
- Input and output must be of hardassigned dimensions
- The network makes a fixed number of computations
- If input is sequence-like (video, sound, etc.) the network is ignorant to the order of samples



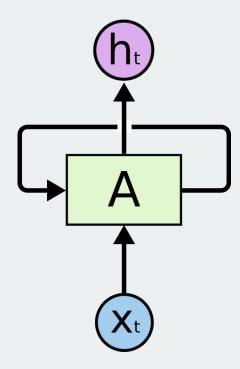
# The problem with all feed forward neural networks

> **Solution:** Recurrence!

- Input and output must be of hardassigned dimensions
- The network makes a fixed number of computations
- If input is sequence-like (video, sound, etc.) the network is ignorant to the order of samples



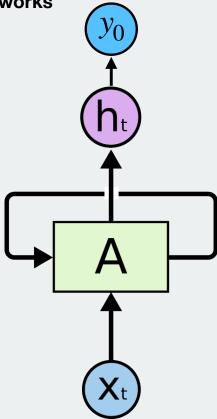
#### > Fundamental idea



$$h_t = f_W(h_{t-1}, x_t)$$

**Notice:** W is the same in each iteration

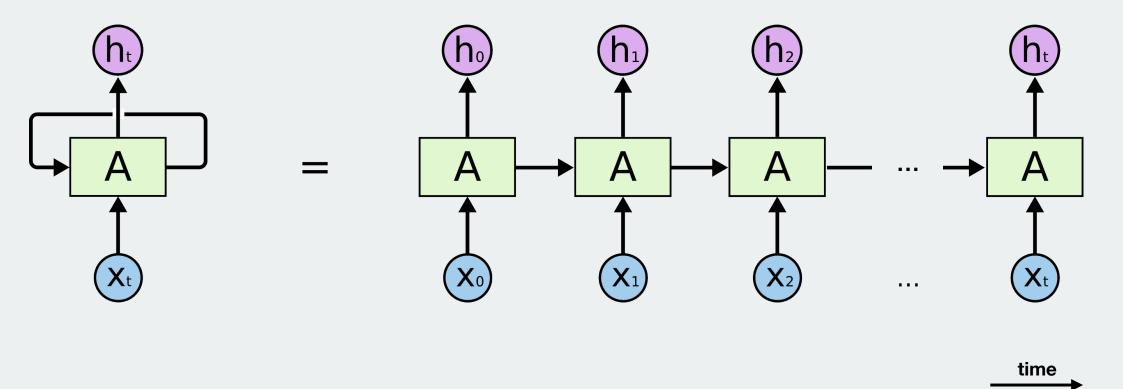
> Fundamental idea



$$h_t = f_W(h_{t-1}, x_t)$$

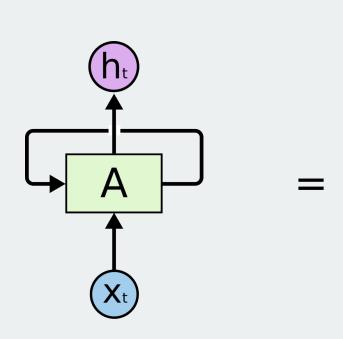
$$y_t = W_{hy}h_t$$

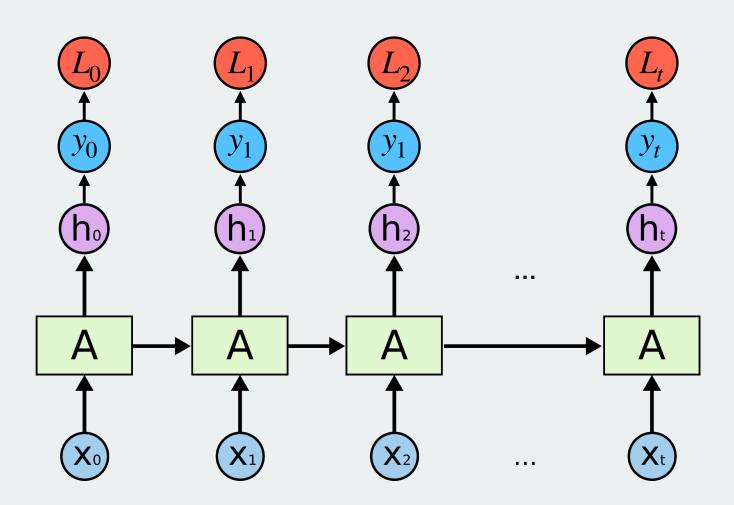
> Unrolled in time



http://colah.github.io/posts/2015-08-Understanding-LSTMs/

> Backpropagation

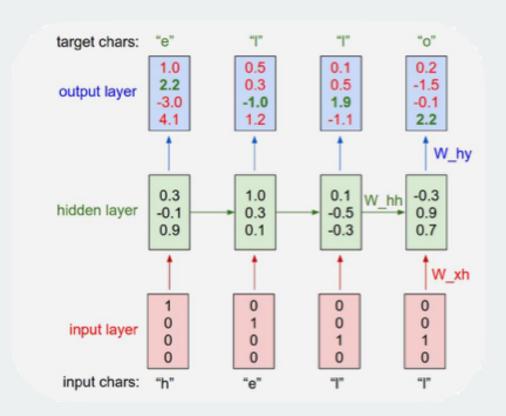




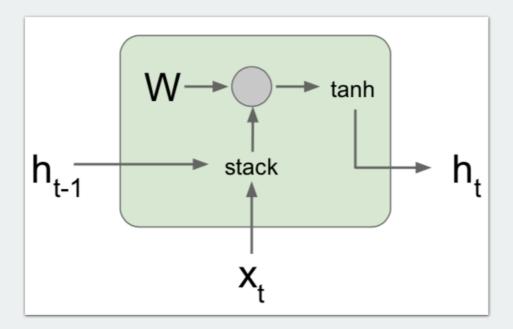
http://colah.github.io/posts/2015-08-Understanding-LSTMs/

> Example: predicting next character

training sequence: "hello"

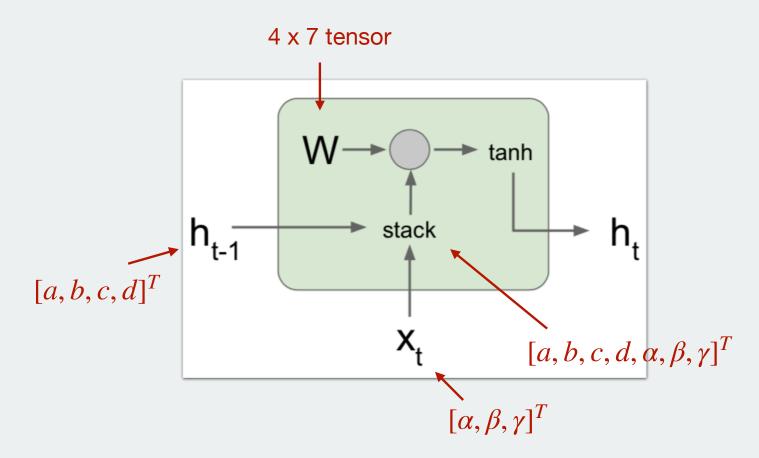


> Vanilla RNN, architecture



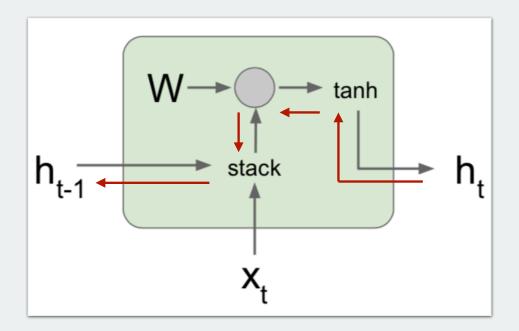
> Vanilla RNN, architecture

- 4: because dotting (h, t) onto it should result in a new vector with 4 elements
- 7: because the (h, t) vector we are dotting onto it has 7 elements in it

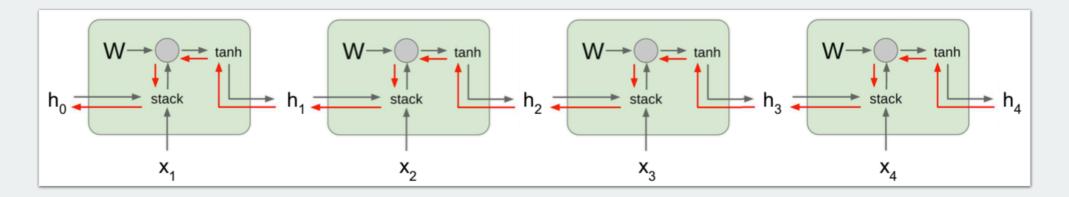


http://cs231n.stanford.edu/syllabus.html

> Vanilla RNN, backpropagation



> Vanilla RNN, backpropagation



**Problem:** Repeated multiplications by **W** during backpropagation

Leads to: Exploding/vanishing gradients

Solution: Gradient clipping (solves exploding gradients), or change architecture

> Vanilla RNN vs. LSTM

#### Vanilla RNN

$$h_t = \tanh\left(W\begin{bmatrix} h_{t-1} \\ x_t \end{bmatrix}\right)$$

## **Long Short Term Memory (LSTM)**

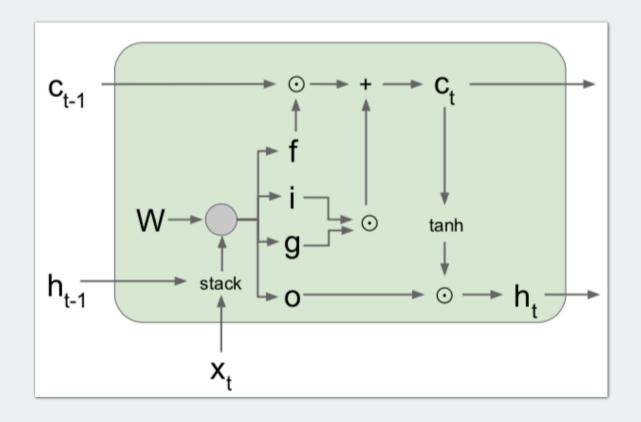
$$\begin{bmatrix} i \\ f \\ o \\ g \end{bmatrix} = \begin{bmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{bmatrix} W \begin{bmatrix} h_{t-1} \\ x_t \end{bmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

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$$h_t = o \odot \tanh(c_t)$$

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> Vanilla RNN vs. LSTM



# Long Short Term Memory (LSTM)

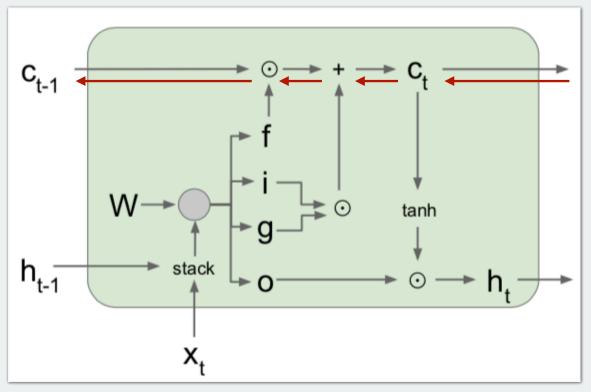
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> Vanilla RNN vs. LSTM

# "Gradient highway": solves vanishing/exploding gradient problems



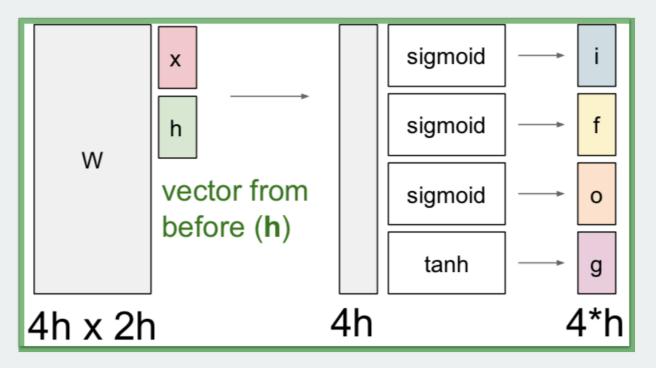
# Long Short Term Memory (LSTM)

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> Vanilla RNN vs. LSTM



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