## **Quantitative Exploration of Fiscal Rules for WAEMU Countries**

Lucien CHAFFA

Université de Montréal

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**CIREQ** 

#### **Motivation**

- I document that WAEMU countries are heteregeneous in mean and volatility of government spendings, revenues, debts, budget balance
- Despite their heterogeneity they are subjected to the same fiscal rule (below 3% of deficit limit)

#### Questions

- Evaluation of current fiscal rule: Is the current homogeneous fiscal rule of 3% of deficit limit is Pareto improving over no rule?
- Potential reform: Is there an optimal fiscal rule that is Pareto improving over current rule?
  - The interest rate is exogenous ≡ Individually design the fiscal rule



#### Contributions

- I quantitatively evaluate the optimal rule using a model of fiscal policy with two ingredients:
  - Present-biased government: need for discipline
  - 2 Shocks to fiscal revenues: need for flexibility
- I perform the welfare analysis of the fiscal rules

#### Findings:

- Evaluation of current fiscal rule: All the countries benefit from 3% deficit limit over no rule
- Potential reform I: When each country individually designs their rule, the tighter deficit limit is 0.6% and the looser deficit limit is 3.9%
- Potential reform II: When the countries jointly design the rule, the tighter maximum deficit is 2% and the slacker deficit limit is 12%



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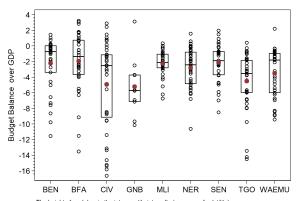
#### Fiscal rule in WAEMU countries: Uniform fiscal rule

- In 2000, WAEMU countries adopt a supranational rules refer as fiscal convergence criteria including:
  - Balanced budget rule (excluding budget grants and foreign-financed capital expenditures)
- Since 2015, a maximum of 3% deficit rule has been adopted

#### Data

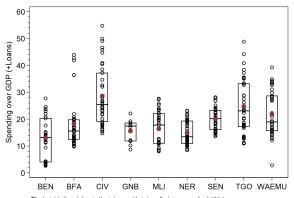
- Data source: "La Base des Données Economiques et Financières" de la BCEAO
- I extract data on government expenditures, revenues, debts for the eight WAEMU countries
- Annual time series data from 1960 to 2018





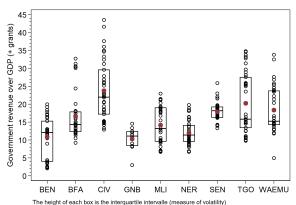
The height of each box is the interquartile intervalle (measure of volatility) The red dot represents the average point

#### Government Budget Balance over GDP



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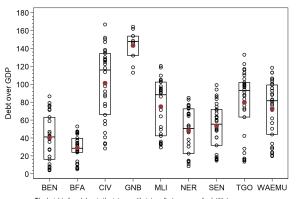
- Government Budget Balance over GDP
- Government Spending over GDP
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- a Go



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- Government Budget Balance over GDP
- Government Spending over GDP
- Government Revenue over GDP
- Government Debt over GDP



#### **Economic environment**

- ullet Model of fiscal policy of N governments where each makes decisions on spending and borrowing i=1,2,...,N
- Two periods model: each government chooses first-period public spending and second-period asset
- Governments are heterogeneous in two ways:
  - ▶ They experience each a preference shocks  $\theta_i \in \theta_i \equiv [\underline{\theta}_i, \overline{\theta}_i]; \theta_i > 0$  with cdf  $F_i(\theta_i);$
  - ▶ They are each present-biased :  $\delta_i$

$$\{t, t+1, t+2, t+3, ...\}$$
  $\{1, \delta_i \beta, \delta_i \beta^2, \delta_i \beta^3, ...\}$ 

- For each government i = 1, 2, ...N we have
  - Social welfare:

$$\mathbb{E}\left[\theta_i U(g_i, \theta_i) + \beta W(x_i)\right], \quad \beta \in (0, 1)$$
(1)

Government objective:

$$\theta_i U(g_i, \theta_i) + \delta_i \beta W(x_i), \quad \delta_i \in (0, 1]$$
 (2)

## Model implications for government i

- Unless  $\delta_i = 1$ , there is a trade-off between **commitment** and **flexibility** 
  - Rules provide commitment (limit distorted incentives)
  - Some discretion may be optimal (flexibility to react to shocks)
- Fiscal rule: Spending cap  $\equiv$  Threshold on  $\theta_i^* \in [\underline{\theta}_i, \overline{\theta}_i]$  Plot1

$$(g_i^{fr}(\theta_i, R), x_i^{fr}(\theta_i, R)) \equiv \begin{cases} (g_i^f(\theta_i, R), x_i^f(\theta_i, R)), & \text{if } \theta_i \le \theta_i^* \\ (g_i^f(\theta_i^*, R), x_i^f(\theta_i^*, R)), & \text{if } \theta_i > \theta_i^* \end{cases}$$
(3)

Where

where 
$$(g_i^f(\theta_i, R), x_i^f(\theta_i, R)) = \operatorname*{argmax}_{g_i, x_i} \left(\theta_i U(g_i, \theta_i) + \delta_i \beta W(x_i, \theta_i) \quad st \quad g_i + \frac{x_i}{R} = \tau_i\right)$$
 is

the government choice of allocations in absence of fiscal rule

 Assuming a constant revenue, the fiscal rule can be implemented by a maximum deficit limit rule



#### Calibration

• Functional forms:  $U(g)=1-e^{(-\alpha g)}$  ;  $W(x)=1-e^{-\alpha(\tau+x)}$ ;  $\theta\equiv$  Shock on government revenue

#### Parameters picked from literature and identical for all countries

- Discount factor  $\beta = 0.9524$
- Net interest rate r = 5%

## Parameters calibrated to match mean and variance of budget balance from 1960-1999

Table 1: Calibration

	BEN	BFA	CIV	GNB	MLI	NER	SEN	TGO
$\alpha$	0.365	0.121	0.621	0.654	0.178	0.482	0.533	0.569
δ	0.954	0.966	0.896	0.901	0.981	0.951	0.958	0.918

## Spending Equivalent variation of welfare

#### Spending Equivalent variation of welfare for Benin with $\delta = 0.954$

- Let  $g^f(\theta,R)$  be the government spending rule before the year 2000
- $\bullet$  Let  $g^{fr}(\theta,R)$  be the government spending rule under the maximum deficit rule of 3% of GDP
- Λ, the spending equivalent of welfare variation, satisfies:

$$\mathbb{E}[\theta U(g^f(\theta, R)(1 + \Lambda)) + \beta W(x^f(\theta, R))] = \mathbb{E}[\theta U(g^{fr}(\theta, R)) + \beta W(x^{fr}(\theta, R))]$$
 (4)

•  $\Lambda = 0.51\%$ 



## Spending Equivalent variation of welfare

## Spending Equivalent of welfare variation for WAEMU countries

Table 2

	From no rule to 3% deficit limit in %									
BEN BFA CIV GNB MLI NER SEN TGO										
δ	0.954	0.966	0.896	0.901	0.981	0.951	0.958	0.918		
$\Lambda$ (in%)	0.51	0.71	0.69	1.77	0.11	0.38	0.16	0.61		

#### **Proposition**

There exist  $\delta_i^*$  for each country such that if  $\delta_i < \delta_i^*$  the 3% rule improves government iwelfare over no rule

#### Present-bias parameters for indifference between no rule and current rule

Table 3:  $\delta$  and  $\delta^*$ 

	BEN	BFA	CIV	GNB	MLI	NER	SEN	TGO
δ	0.954	0.966	0.896	0.901	0.981	0.951	0.958	0.918
$\delta^*$	0.976	0.987	0.929	0.943	0.988	0.970	0.975	0.945

## Uncoordinated Fiscal Rule Design

- Government i chooses its fiscal rule independently
- Program solve by this government: Plot 2

$$\max_{\theta_i^* \in [\underline{\theta_i}, \bar{\theta_i}]} \int_{\underline{\theta_i}}^{\theta_i^*} (\theta_i U(g_i(\theta_i, R)) + \beta W(x_i(\theta_i, R)) f(\theta_i) d\theta_i + \int_{\theta_i^*}^{\bar{\theta_i}} (\theta_i U(g_i(\theta_i^*, R)) + \beta W(x_i(\theta_i^*, R)) f(\theta_i) d\theta_i$$
(5)

s.t.

$$(g_i(\theta_i, R), x_i(\theta_i, R)) \in \underset{g_i, x_i}{\operatorname{argmax}} \left( \theta_i U(g_i, \theta_i) + \delta_i \beta W(x_i, \theta_i) \quad s.t. \quad g_i + \frac{x_i}{R} = \tau_i \right)$$

ullet Given R, the optimal uncoordinated fiscal rule is a cutoff  $heta_{iu}^*$  satisfying:

$$\frac{\mathbb{E}\left[\theta_{i}|\theta_{i} \geq \theta_{iu}^{*}\right]}{\theta_{iu}^{*}} = \frac{1}{\delta_{i}} \tag{6}$$



- Shock threshold as fiscal rule:  $\theta^* = 0.959$

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- Government spending cap as fiscal rule: gcap = 11.49% of GDP
- Optimal deficit limit as fiscal rule: deficit = 0.64% of GDF
- Spending welfare variation equivalent from 3% deficit limit to 0.64% deficit limit:  $\Lambda = 0.13\%$

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## Evaluation of optimal uncoordinated fiscal rule for WAEMU countries

### Optimal deficit limit rule and welfare variation for WAEMU countries

Table 4

Optimal deficit limit (DL) and $\Lambda$ from 3% to optimal rule in %								
	BEN	BFA	CIV	GNB	MLI	NER	SEN	TGO
δ	0.954	0.966	0.896	0.901	0.981	0.951	0.958	0.918
DL (in%)	0.64	3.91	1.79	3.50	2.06	1.80	1.06	2.17
$\Lambda$ (in%)	0.125	0.000	0.019	0.013	0.006	0.025	0.038	0.013

## Constraint Uniform fiscal rule Design

- The assumptions for this case are: common preference shocks  $\theta$ , common governments' present bias  $\delta$  for all countries
- Program solve by the Central Bank:

$$\max_{\theta^* \in [\underline{\theta}, \bar{\theta}]} \int_{\underline{\theta}}^{\theta^*} (\theta U(g(\theta, R)) + \beta W(x_i(\theta_i, R)) f(\theta) d\theta + \int_{\theta^*}^{\bar{\theta}} (\theta U(g(\theta^*, R)) + \beta W(x(\theta^*, R)) f(\theta) d\theta$$
(7)

 $\begin{array}{l} \text{s.t.} \\ (g(\theta,R),x(\theta,R)) \in \underset{g,x}{\operatorname{argmax}} \ \Big(\theta U(g,\theta) + \delta \beta W(x,\theta) \quad s.t. \quad g + \frac{x}{R} = \tau \Big) \\ \end{array}$ 

ullet Given R, the optimal constraint uniform fiscal rule is a cutoff  $heta^*_{uc}$  satisfying:

$$\frac{\mathbb{E}\left[\theta|\theta \ge \theta_{uc}^*\right]}{\theta_{uc}^*} = \frac{1}{\delta} \tag{8}$$



#### Evaluation of constraint uniform fiscal rule for WAEMU

- Model parameters:  $\alpha = 0.65$  and  $\delta = 0.93$

#### Evaluation of constraint uniform fiscal rule for WAEMU

- Model parameters:  $\alpha = 0.65$  and  $\delta = 0.93$
- Shock threshold as fiscal rule:  $\theta^* = 0.939$
- Government spending cap as fiscal rule: gcap = 19.09% of GDP
- Optimal deficit limit as fiscal rule: deficit = 0.73% of GDP
- Spending welfare variation equivalent from 3% deficit limit to 0.73% deficit limit:  $\Lambda = 0.088\%$



## Coordinated Fiscal Rule Design

• The Central Bank designs jointly the rules for each country in the Union such that:

$$\max_{\substack{\theta_{i=1}^{n}\theta_{i}^{*} \in \otimes_{i=1}^{n} [\underline{\theta_{i}}, \overline{\theta_{i}}]}} \sum_{i=1}^{n} v_{i} \left[ \int_{\underline{\theta_{i}}}^{\theta_{i}^{*}} \left( \theta_{i} U(g_{i}^{f}(\theta_{i}, R(\theta^{*}))) + \beta W(x_{i}^{f}(\theta_{i}, R(\theta^{*}))) \right) f_{i}(\theta_{i}) d\theta_{i} \right]$$

$$+ \int_{\theta^{*}}^{\overline{\theta_{i}}} \left( \theta_{i} U(g_{i}^{f}(\theta_{i}^{*}, R(\theta^{*}))) + \beta W(x_{i}^{f}(\theta_{i}^{*}, R(\theta^{*}))) \right) f_{i}(\theta_{i}) d\theta_{i}$$

$$(9)$$

subject to

$$\sum_{i}^{n} v_{i} \int_{\underline{\theta_{i}}}^{\bar{\theta_{i}}} \left( \left( g_{i}^{f}(\theta_{i}, R) \right) f_{i}(\theta_{i}) d\theta_{i} = \sum_{i}^{n} v_{i} \int_{\underline{\theta_{i}}}^{\bar{\theta_{i}}} \tau_{i} f_{i}(\theta_{i}) d\theta_{i} \right)$$

$$(10)$$

Where  $\theta^* = (\otimes_{i=1}^n \theta_i^*)$ 

• The solution of this program involves a system of equations;



## Solution of the program

• The optimal coordinated fiscal rule is a cutoff  $\theta^*$  and its associated interest rate  $R = R(\theta^*)$  satisfying,  $\forall \theta^* < \bar{\theta}$  and  $\forall i \in 1, 2, ..., N$ :

$$\begin{cases}
\frac{\mathbb{E}\left[\theta_{i} \middle| \theta_{i} \geq \theta_{i}^{*}\right]}{\theta_{i}^{*}} = \frac{1}{\delta_{i}} + \frac{R'(\theta_{i}^{*})}{(1 - F(\theta_{i}^{*}))\theta_{i}^{*}U'(g_{i}^{f}(\theta_{i}^{*}, R))\frac{\partial g_{i}^{f}(\theta_{i}^{*}, R)}{\partial \theta_{i}^{*}}}(\rho_{i} + \lambda_{i})} \\
\sum_{i}^{n} \upsilon_{i} \int_{\underline{\theta_{i}}}^{\bar{\theta_{i}}} \left(g_{i}^{f}(\theta_{i}, R) f_{i}(\theta_{i})d\theta_{i} = \sum_{i}^{n} \upsilon_{i} \int_{\underline{\theta_{i}}}^{\bar{\theta_{i}}} \tau_{i} f_{i}(\theta_{i})d\theta_{i}}\right) 
\end{cases} (11)$$

Where  $\rho_i \equiv$  redistributive effect and  $\lambda_i \equiv$  Discipline effect;

$$\begin{split} \rho_i &= -\frac{1}{R} \left[ \int_{\underline{\theta_i}}^{\theta_i^*} W'(x_i^f(\theta_i, R)) x_i^f(\theta_i, R) f_i(\theta_i) d\theta_i + \int_{\theta_i^*}^{\bar{\theta_i}} W'(x_i^f(\theta_i^*, R)) x_i^f(\theta_i^*, R) f_i(\theta_i) d\theta_i \right] \\ \lambda_i &= -(\int_{\underline{\theta_i}}^{\theta_i^*} \left( \theta_i U'(g_i^f(\theta_i, R)) - R W'(x_i^f(\theta_i, R)) \right) \frac{dg_i^f(\theta_i, R)}{dR} f_i(\theta_i) d\theta_i + \\ &\int_{\theta_i^*}^{\bar{\theta_i}} \left( \theta_i U'(g_i^f(\theta_i^*, R)) - R W'(x_i^f(\theta_i^*, R)) \right) \frac{dg_i^f(\theta_i^*, R)}{dR} f_i(\theta_i) d\theta_i ) \end{split}$$

#### Quantitative coordinated fiscal rule

The optimal deficit limit for each country is:

Table 5: Joint Fiscal Rule

Optimal deficit limit (DL)									
	BEN	BFA	CIV	GNB	MLI	NER	SEN	TGO	
delta	0.954	0.966	0.896	0.901	0.981	0.951	0.958	0.918	
DL (in%)	12.40	2.11	3.21	2.98	9.79	4.19	5.22	3.33	

• The equilibrium net interest associated is: 6.8%

#### Quantitative coordinated fiscal rule

• The welfare equivalent variation from no rule to optimal joint rule is:

Table 6: Welfare variation

	$\Lambda$ from no rule to optimal rule in %									
BEN BFA CIV GNB MLI NER SEN TGO										
delta	0.954	0.966	0.896	0.901	0.981	0.951	0.958	0.918		
$\Lambda$ (in%)	0.019	0.581	0.656	1.875	0.000	0.263	0.050	0.575		

## Program solved

- In this setting while the countries are heterogeneous, central authority chooses the same spending limit for all the countries
- The program solved is the following:

$$\max_{\theta^* \in [\underline{\theta}, \overline{\theta}]} \sum_{i}^{N} \upsilon_i \left[ \int_{\underline{\theta}}^{\theta^*} \left( \theta U(g^f(\theta, R(\theta^*))) + \beta W(x^f(\theta, R(\theta^*))) \right) f_i(\theta) d\theta + \right.$$

$$\left. \int_{\theta^*}^{\overline{\theta}} \left( \theta U(g^f(\theta^*, R(\theta^*))) + \beta W(x^f(\theta^*, R(\theta^*))) \right) f_i(\theta) d\theta \right]$$

$$(12)$$

subject to

$$\sum_{i}^{N} v_{i} \int_{\underline{\theta}}^{\bar{\theta}} \left( g^{f}(\theta, R) \right) f_{i}(\theta) d\theta = \sum_{i}^{N} v_{i} \int_{\underline{\theta}}^{\bar{\theta}} \tau_{i} f_{i}(\theta) d\theta \tag{13}$$

Where  $\theta = h(\theta_i)$   $\forall i = 1, 2, ..., N$ 



## Specific case of $\delta_i = \delta$

• The optimal uniform coordinated fiscal rule is a cutoff  $\theta^*$  and its associate interest rate  $R=R(\theta^*)$  satisfying,  $\forall \theta_c^*<\bar{\theta} \colon f(\theta)=\sum v_i f_i(\theta)$ 

$$\begin{cases}
\frac{\mathbb{E}\left[\theta|\theta \ge \theta^*\right]}{\theta^*} = \frac{1}{\delta} + \frac{R'(\theta^*)}{(1 - F(\theta^*))\theta^* U'(g^f(\theta^*, R)) \frac{\partial g^f(\theta^*, R)}{\partial \theta^*}} (\rho + \lambda) \\
\int_{\underline{\theta}}^{\overline{\theta}} \left(g^f(\theta, R)\right) f(\theta) d\theta = \int_{\underline{\theta}}^{\overline{\theta}} (\sum_{i}^{N} \upsilon_i \tau_i f_i(\theta)) d\theta
\end{cases}$$
(14)

Where  $\rho \equiv$  redistributive effect and  $\lambda \equiv$  Discipline effect;

$$\begin{split} \rho &= -\frac{1}{R} \left[ \int_{\underline{\theta}}^{\theta^*} W'(x^f(\theta,R)x^f(\theta,R)f(\theta)d\theta + \int_{\theta^*}^{\bar{\theta}} W'(x^f(\theta^*,R)x^f(\theta^*,R)f(\theta)d\theta \right] \\ \lambda &= -(\int_{\underline{\theta}}^{\theta^*} \left( \theta U'(g^f(\theta,R)) - RW'(x^f(\theta,R) \right) \frac{dg^f(\theta,R)}{dR} f(\theta)d\theta + \int_{\theta^*}^{\bar{\theta}} \left( \theta U'(g^f(\theta^*,R)) - RW'(x^f(\theta^*,R) \right) \frac{dg^f(\theta^*,R)}{dR} f(\theta)d\theta ) \end{split}$$

- **Parameters**:  $\alpha = 0.44$ ;  $\delta = 0.94$

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• Corresponding net interest rate: 4.34%

26.96	21.16	11.86	27.48	23.64	25.78	17.58

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• Fiscal Rule as uniform deficit limit : 21.8%

Fiscal Rule as deficit limit for each country:

Table 7

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• Fiscal Rule as deficit limit for each country:

Table 7

Optimal deficit limit (DL)									
	BEN	BFA	CIV	GNB	MLI	NER	SEN	TGO	
DL (in%)	26.96	21.16	11.86	27.48	23.64	25.78	19.93	17.58	

## Summary

- I show that WAEMU countries are very heterogeneity in the volatility of their revenues, expenditure and debts and balanced budget;
- I design an optimal quantitative fiscal rule for each country of the union base on a model that uses each country preference shocks;
- Some countries benefit from 3% deficit limit rule in place in WAEMU while others don't.
- The joint optimal deficit limit design shows that we may strengthen the rule for BFA, while loosen it for BEN, MLI, NER, SEN and leave it unchangeable for CIV, GNB and TGO.



# Thank You!

#### Literature Review

#### Hyperbolic discount literature

Amador, Manuel, Iván Werning, and George Marios Angeletos. "Commitment vs. flexibility." Econometrica 74, no. 2 (2006): 365-396.

#### Uncoordinated and coordinated fiscal rule

Halac, Marina, and Pierre Yared. "Fiscal Rules and Discretion in a World Economy." The American Economic Review 108, no. 8 (2018): 2305-2334.

▶ Presentation 1

Figure 1: Fiscal Policy

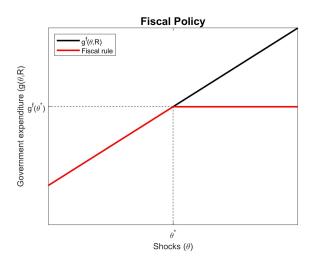


Figure 2: Fiscal Policy Designing

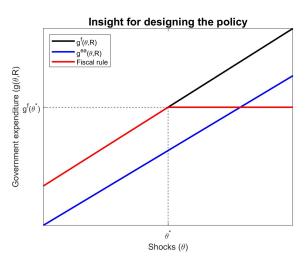




Table 8

Homogeneity to	Homogeneity tests between WAEMU countries 1960-1999									
		Fstat	p-values							
Revenue	H0: Mean equality	19.023	0.000							
	H0: Variance equality	12.256	0.000							
Spendings	H0: Mean equality	16.359	0.000							
	H0: Variance equality	9.942	0.000							
Budget Balance	H0: Mean equality	4.484	0.000							
	H0: Variance equality	9.111	0.000							
Debts	H0: Mean equality	30.454	0.000							
	H0: Variance equality	7.817	0.000							

Levene's test for equality of variances is used for test of variances homogeneity





## Another interpretation of preference shock

- With utility function  $U(g)=-e^{-\alpha g}$ , preference shock  $(\theta)$  can be interpreted as shock on government revenue  $(\epsilon)$ ;
  - Maximization problem (15) and (16 are equivalents.

$$\max_{g,x} \{ \frac{\theta}{\theta} U(g) + \delta \beta W(x) \}$$

$$x = \pi$$
(15)

$$st \quad g + \frac{x}{R} = \tau$$

$$\max_{g,x} \{ U(g) + \delta \beta W(x) \} \tag{16}$$

$$st \quad g + \frac{x}{R} = (\tau + \epsilon)$$

