$\forall w \in \mathbb{Z}^{\times}, w \in L(M) (=> w \in L(M^{"}))$ $\forall w \in \mathbb{Z}^{\times}, (g, w) \vdash_{M'}^{\times} (p, e) (=> (E(g), w) \vdash_{M''}^{\times} (P, e), p \in P$ $\forall g, p \in \mu', (A', w) \vdash_{M'}^{\times} (f', e) (=> (E(A'), w) \vdash_{M''}^{\times} (Q, e), f' \in Q$ $f' \in F'$ $w \in L(M^{"})$

Deux -> fain inductie dupa |w|

Par de faxa

IWI=0, W=e

1p. inductiva

pp. adw. pf w, |w| ≤ K

Pas de inductie

$$\forall w, |w| = k+1$$
.

 $v = n \cdot a, \quad a \in \mathbb{Z}, \quad n \in \mathbb{Z}^*$
 $\Rightarrow p \quad (g, w) \quad t \times (p, e) \quad \Rightarrow \forall \pi_1, \pi_2 \in k' \text{ ai}$
 $(g, n \cdot a) \quad t \times (p, e) \quad \Rightarrow \forall \pi_1, \pi_2 \in k' \text{ ai}$
 $(g, n \cdot a) \quad t \times (p, e) \quad t \times (p, e)$

Cum $(g, n \cdot a) \quad t \times (p, e) \quad t \times (p, e)$

Don $1 \cdot k \quad t \times (p \cdot a) \quad t \times (p, e) \quad t \times (p, e)$

Cum $(\pi_1, a) \quad t \times (p \cdot a)$

Cum $(\pi_1, a) \quad t \times (p \cdot a)$
 $(\pi_1, a) \quad t \times (p \cdot a) \quad$

= Rp. (E(g), Na) + (Ri, a) + (Pie) + m amint Par pel i un armit R1 ai S'(R1, a) = P. Din def. S", S"(R1, a) este reminue a texturer mullimiler E(Mz) unde pl o amuità store MERI, (M, a, Mz) este o transitie a lui M'. Com pel=8"(Ry, a), Inz an peE(Hz), pt me amond heR, (M, a, Mz) este a traitie a lui M'. =) (Mz, e) (p, e) din E(Mz) Bin ip-ind. => (9, 0) 1 (H1, e) => (9, 0a) (H1, a) (H2, e) (P, e)

g.e.d

$$E(20) = 320, 21, 22, 234 = Q_0 = A^{\dagger}$$

$$E(24) = 323,244$$
.

$$S''(Q_0, a) = E(Q_0) \cup E(Q_1) = 3Q_0, Q_1, Q_2, Q_3, Q_4 = Q_1.$$

$$s^{h}(Q_{1}, L) = Q_{2}$$

$$S''(Q, \nabla) = U3E(p)|pex',$$

 $(Q, \nabla, p) \in A), Q \in QY$

$$S^{n}(Q_{2}, a) = E(g_{1}) = 3g_{3}, g_{4} = Q_{3}$$
 $S^{n}(Q_{2}, k) = E(g_{4}) = Q_{3}$
 $S^{n}(Q_{3}, a) = Q_{3}$
 $S^{n}(Q_{3}, k) = \emptyset$
 $S^{n}(Q_{3}, k) = \emptyset$
 $S^{n}(Q_{3}, k) = S^{n}(\emptyset, k) = \emptyset$
 $S^{n}(\emptyset, a) = S^{n}(\emptyset, k) =$

Proprietati al limfajelor acceptate de A-Finite

Teonera

clasa limbajelor acceptate de A. Finite este inchisa in raport ou oplise:

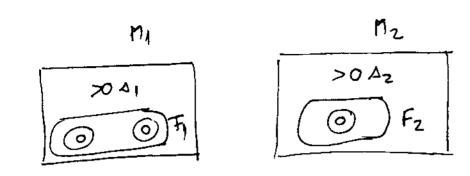
- a) remaine
- 1) concatenare
- c) pleene Star
- d) complementare
- e) intersectie

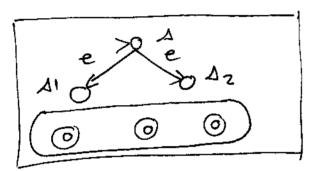
dem.

a)
$$L_1 = L(M_1)$$
 , $L_2 = L(M_2)$

$$M_1 = (K_1, Z_2, \Delta_1, \Delta_1, F_1)$$

$$M_2 = (K_2, \Sigma, \Delta_z, \Delta_z, F_2)$$





M=(K, Z, Δ, Δ, F), seale a mouà stares € KIA A € K2

K= K10 K2 1345

F= F1 UF2

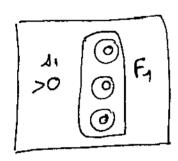
 $\Delta = \Delta_1 \cup \Delta_2 \cup \beta(\Delta, e, \Delta_1), (\Delta, e, \Delta_2)$

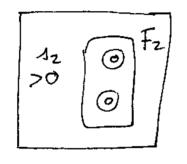
w=z*, (A,w) + (g,e), g=F (=)

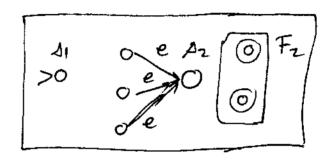
(11, w) + (2, e), 2 = F1 sau (12, w) + (2, e), 2 = F2 1(m)= L(M) UL(M2)

f) Concatenare

 $M_1, M_2 \rightarrow AFM$? $M \propto L(M) = L(M_1) \cdot L(M_2)$







$$M_1 = (K_1, Z, \Delta_1, \Delta_1, F_1)$$

 $M_2 = (K_2, Z, \Delta_2, \Delta_2, F_2)$
 $M_3 = (K_2, Z, \Delta_2, \Delta_2, F_2)$

$$M = (K, Z, \Delta, \Delta, F)$$

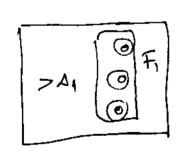
$$\Delta = \Delta_1 \cup \Delta_2 \cup (F_1 \times 3e^{\frac{1}{2}} \times 3A_2^{\frac{1}{2}})$$

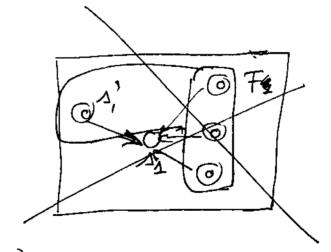
$$(\Delta, w) \stackrel{\times}{f_{m}} (g, e), g \in F (=) \stackrel{\times}{J} w_{1}, w_{2} \in Z^{*}, \stackrel{\times}{J} p \in F_{1} a$$

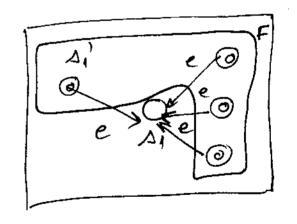
 $w = w_{1} w_{2} \stackrel{*}{f_{1}} (\Delta_{1}, w_{1}) \stackrel{\times}{f_{m_{1}}} (p, e) \stackrel{*}{f_{2}} (\Delta_{2}, w_{2}) \stackrel{*}{f_{m_{2}}} (g, e)$
 $L(M) = L(M) \cdot L(M_{2})$

c) Kleene Star

MI -> AFM







$$M_1 = (K_1, \overline{Z}, \Delta_1, \Delta_1, F_1)$$

$$M = (K, \Xi, \Delta, \Delta, F)$$

a

$$F = F_1 \cup 3A_1 \cup 1$$

 $A = \Delta_1 \cup (F \times 3e^{i} \times 3A_1 \cup 1) \cup 3(A_1, e, A_1) \cup 1$
 $W = L(M)$, for $W = e$, for $W = W_1 \cdot \dots \cdot w_K$, $K \ge 1$.
 $i = 1, \dots, K$, $Y = F = A_1 \cup A_1, W_1 \cup 1$
 $W = L(M_1)^*$, A_1 , for $W = e$ for $W = W_1 \cdot \dots \cdot W_K$, W_1, \dots , $W_K \in L(M_1)$
 $W = e = W = L(M)$ pf $Ca = A_1$ este S_1 , fuala
 $W = L(M)$ pf $Ca = A_1$ este S_1 , fuala
 $W = L(M)$ pf $Ca = A_1$ este S_1 , $Ca = A_1$ $Ca = A_1$ este S_1 .

d) Complementare

$$M = (K, Z, S, \Delta, F)$$
 AFD.
 $Z^* - L(M)$ accepted de AFD $\overline{M} = (K, Z, S, \Delta, K - F)$

10.

Insterse chie

$$4, L_2$$
 of $L_2 = L(M_1)$, $L_2 = L(M_2)$
 $L_1 \cap L_2 = \overline{z}^* - ((\overline{z}^* - L_1) \cup (\overline{z}^* - L_2))$

AFD

AFD

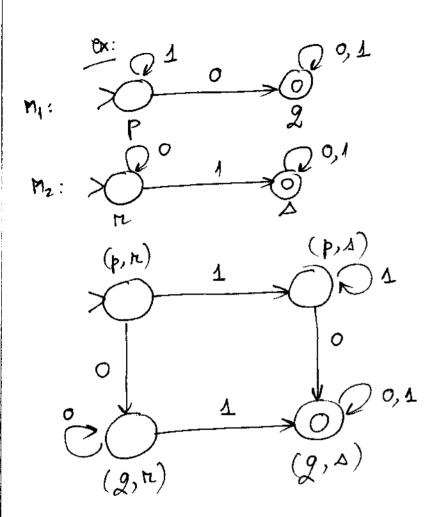
AFD

AFD

Constructie directa

$$M = (K_1 \times K_2, \Xi, 8, (A_1, A_2), F_1 \times F_2)$$

$$S((p,2),a) = (S_1(p,a), S_2(g,a))$$



Progrietali algoritmice

Tenema

Existà algoritmi care pot raspunde la vrue intrehavi reforitoure la L(A.F.):

- a) Det. find un A.F.M.; un sir w, este w & L(M)?
- +) A.F. M, L(M) = \$\phi\$?
- c) A.F. M, L(M) = 2 *?
- d) A.F. Mi, Mz, L(Mi) = L(M2)?
- e) A.F. Mi, Mz, L(Mi) = L(M2)?

dun. pp. M -> AF.D.

- a) thosex aplite his M pt smulw, Tu lw pain.
- 1) vouificand de 7 a seventé de sageli dui st unit untr-a et finale
 - construies M' of $L(M') = Z^{2} L(M)$ & vorific $L(M) = \emptyset$
- d) (= *- L(mg) n L(m) = \$