HW 4.5

December 13, 2018

```
In [23]: import QuantLib as ql
         import quandl
         import numpy as np
         import pandas as pd
         import datetime
In [24]: token = "VmD_oxdaJACCTkt2Pry-"
         n = range(1,22)
         nms = ["CHRIS/CME ED"+str(i) for i in n]
         dfs = [quandl.get(nm, authtoken=token) for nm in nms]
In [25]: euro_dollar = pd.DataFrame()
         for i in range(21):
             euro_dollar['ED'+str(i+1)]= 100-dfs[i]['Settle']
         euro_dollar = euro_dollar.dropna()
In [26]: def getday(date,n=0):
             result_date = date + datetime.timedelta(days=n)
             d = result_date.strftime('%Y-%m-%d')
             d = pd.to_datetime(d)
             return d
In [27]: def ql_to_datetime(d):
             return datetime.datetime(d.year(), d.month(), d.dayOfMonth())
In [28]: # calculate maturity date
         maturity_date = []
         imm = ql.IMM()
         last_date = getday(pd.to_datetime('2018-12-10'), 30*2)
         d = ql.Date(13, 9, 1993)
         while ql_to_datetime(d) <= last_date:</pre>
             d = imm.nextDate(d)
             maturity_date.append(d)
         maturity = [ql_to_datetime(i) for i in maturity_date]
In [29]: # add the row with maturity date not in euro_dollar's index
         index_add = []
         for i in range(len(maturity)):
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if maturity[i] not in euro_dollar.index:
                 index_add.append(maturity[i])
         for i in range(len(index_add)):
             euro_dollar.loc[index_add[i],:] = np.nan
In [30]: euro_dollar = euro_dollar.sort_index()
In [31]: # find the rows with maturity date and calculate maturity date for every contract for
         maturity_date_table = pd.DataFrame(index = euro_dollar.index,columns=euro_dollar.columns)
         k = 0
         j = 0
         while j < len(maturity_date_table):</pre>
                 if maturity_date_table.index[j]<ql_to_datetime(maturity_date[k]):</pre>
                 elif maturity_date_table.index[j] == ql_to_datetime(maturity_date[k]):
                     imm = ql.IMM()
                     d = maturity_date[k]
                     for i in range (0,21):
                         maturity_date_table.iloc[j, i] = ql_to_datetime(imm.nextDate(d))
                         d = imm.nextDate(d)
                     j+=1
                 else:
                     k+=1
In [32]: #calculate the first row of contract maturity date
         maturity_date_table.iloc[0,:] = maturity[:21]
In [33]: # For the remaining row, use forward fill method to fill all the cells.
         maturity_date_table = maturity_date_table.fillna(method='ffill')
In [34]: maturity_date_table.head()
Out [34]:
                           ED1
                                       ED2
                                                  ED3
                                                              ED4
                                                                         ED5
                                                                                    ED6 \
         Date
         1993-09-14 1993-09-15 1993-12-15 1994-03-16 1994-06-15 1994-09-21 1994-12-21
         1993-09-15 1993-12-15 1994-03-16 1994-06-15 1994-09-21 1994-12-21 1995-03-15
         1993-09-16 1993-12-15 1994-03-16 1994-06-15 1994-09-21 1994-12-21 1995-03-15
         1993-09-17 1993-12-15 1994-03-16 1994-06-15 1994-09-21 1994-12-21 1995-03-15
         1993-09-20 1993-12-15 1994-03-16 1994-06-15 1994-09-21 1994-12-21 1995-03-15
                           ED7
                                       ED8
                                                  ED9
                                                             ED10
                                                                                   ED12 \
         Date
         1993-09-14 1995-03-15 1995-06-21 1995-09-20 1995-12-20
                                                                             1996-06-19
         1993-09-15 1995-06-21 1995-09-20 1995-12-20 1996-03-20
                                                                             1996-09-18
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         1993-09-16 1995-06-21 1995-09-20 1995-12-20 1996-03-20
                                                                             1996-09-18
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         1993-09-17 1995-06-21 1995-09-20 1995-12-20 1996-03-20
                                                                             1996-09-18
                                                                     . . .
         1993-09-20 1995-06-21 1995-09-20 1995-12-20 1996-03-20
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ED13
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         Date
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         1993-09-15 1996-12-18 1997-03-19 1997-06-18 1997-09-17 1997-12-17 1998-03-18
         1993-09-16 1996-12-18 1997-03-19 1997-06-18 1997-09-17 1997-12-17 1998-03-18
         1993-09-17 1996-12-18 1997-03-19 1997-06-18 1997-09-17 1997-12-17 1998-03-18
         1993-09-20 1996-12-18 1997-03-19 1997-06-18 1997-09-17 1997-12-17 1998-03-18
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                           ED19
         Date
         1993-09-14 1998-03-18 1998-06-17 1998-09-16
         1993-09-15 1998-06-17 1998-09-16 1998-12-16
         1993-09-16 1998-06-17 1998-09-16 1998-12-16
         1993-09-17 1998-06-17 1998-09-16 1998-12-16
         1993-09-20 1998-06-17 1998-09-16 1998-12-16
         [5 rows x 21 columns]
In [35]: # calculate each contract's time to maturity
         day_diff_actual = pd.DataFrame(index = euro_dollar.index,columns=euro_dollar.columns)
         for i in range(21):
             day_diff = (maturity_date_table.iloc[:,i].astype('datetime64[D]') - maturity_date
             day_diff = [day_diff[j].days for j in range(len(day_diff))]
             day_diff_actual.iloc[:,i] = day_diff
In [36]: day_diff_actual.head()
Out [36]:
                      ED1
                           ED2
                                ED3
                                     ED4
                                          ED5
                                                ED6
                                                     ED7
                                                          ED8
                                                               ED9
                                                                     ED10
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         Date
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         1993-09-14
                                183
                                     274
                                           372
                                                463
                                                     547
                                                                736
                                                                                  1009
                        1
                            92
                                                           645
                                                                      827
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         1993-09-15
                           182
                                273
                                     371
                                           462
                                                546
                                                     644
                                                          735
                                                                826
                                                                                  1099
                       91
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         1993-09-16
                                272
                                     370
                                           461
                                                545
                                                     643
                                                          734
                                                                825
                                                                                  1098
                       90
                           181
                                                                      916
                                           460
         1993-09-17
                       89
                           180
                                271
                                     369
                                                544
                                                     642
                                                          733
                                                                824
                                                                      915
                                                                                  1097
         1993-09-20
                       86
                           177
                                268
                                     366
                                           457
                                                541
                                                     639
                                                          730
                                                               821
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         Date
         1993-09-14
                     1100
                            1191
                                  1282
                                        1373
                                               1464
                                                     1555
                                                           1646
                                                                  1737
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         1993-09-15
                     1190
                            1281
                                  1372
                                        1463
                                               1554
                                                     1645
                                                           1736
                                                                  1827
                                                                        1918
         1993-09-16
                     1189
                            1280
                                  1371
                                         1462
                                               1553
                                                     1644
                                                           1735
                                                                  1826
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         1993-09-17
                      1188
                            1279
                                  1370
                                         1461
                                               1552
                                                     1643
                                                           1734
                                                                  1825
                                                                        1916
         1993-09-20
                     1185
                            1276
                                  1367
                                         1458
                                               1549
                                                     1640
                                                           1731
                                                                  1822
                                                                        1913
         [5 rows x 21 columns]
In [37]: #c = [91,90,92,92]
         \#a = 0
         \#constant = []
         #for i in range(21):
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\#a+=c[(i)\%4]
              #constant.append(a)
          constant = [90*(i+1) \text{ for } i \text{ in } range(21)]
          constant = np.array(constant)
         day_constant = pd.DataFrame(index = euro_dollar.index, columns=euro_dollar.columns)
         for i in range(len(day_constant)):
              day constant.iloc[i,:] = constant
         day constant.head()
Out [37]:
                       ED1
                            ED2
                                 ED3
                                       ED4
                                            ED5
                                                  ED6
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                                                             ED8
                                                                  ED9
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         Date
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         1993-09-15
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                                                                                     1080
          1993-09-16
                        90
                            180
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                                       360
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                                                                  810
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         1993-09-17
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          1993-09-20
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                                                       630
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                                                                  810
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                       ED13
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         Date
         1993-09-14
                      1170
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         1993-09-15
                      1170
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         1993-09-16
                      1170
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         1993-09-17
                       1170
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         1993-09-20
                      1170
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                                    1350
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                                                              1710
                                                                    1800
                                                                           1890
          [5 rows x 21 columns]
In [38]: yield_curve = pd.DataFrame(index= euro_dollar.index, columns = euro_dollar.columns)
         for i in range(len(euro_dollar)):
              yield_curve.iloc[i,:] = np.interp(day_constant.iloc[i,:].values, day_diff_actual.
In [39]: yield_curve = yield_curve.dropna()
In [40]: yield_curve.head()
Out [40]:
                           ED1
                                     ED2
                                              ED3
                                                        ED4
                                                                  ED5
                                                                            ED6
                                                                                      ED7
         Date
         1993-09-14
                      3.58868
                                3.79308
                                          4.04857
                                                    4.38469
                                                                 4.49
                                                                        4.68333
                                                                                 4.84398
         1993-09-15
                          3.48
                                 3.5289
                                          3.73308
                                                    3.97082
                                                              4.32121
                                                                          4.435
                                                                                     4.62
         1993-09-16
                          3.49
                                3.53945
                                          3.75516
                                                    3.98449
                                                              4.32648
                                                                        4.43583
                                                                                  4.62214
                                                    4.00704
                                                              4.35044
                                                                        4.45667
                                                                                  4.64429
          1993-09-17
                      3.49066
                                    3.55
                                          3.77747
          1993-09-20
                      3.49308
                                3.56791
                                          3.80531
                                                    4.04408
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                                                                                  4.68163
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         Date
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                                                                       5.67231
                                5.18253
                                          5.31033
                                                                                 5.76099
          1993-09-14 5.10077
                                                              5.62945
                                                     . . .
         1993-09-15
                      4.80033
                                5.06901
                                          5.15253
                                                              5.39703
                                                                        5.60725
                                                                                     5.66
                                                     . . .
         1993-09-16
                                 5.0722
                                          5.15297
                                                              5.40824
                      4.80231
                                                                        5.61989
                                                                                     5.67
                                                     . . .
         1993-09-17 4.81571
                                5.08538
                                          5.16341
                                                              5.41945
                                                                      5.63253
                                                                                     5.68
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1993-09-20	4.84242	5.11495	5.18473	• • •	5.44308	5.66044	5.7
	ED15	ED16	ED17	ED18	ED19	ED20	ED21
Date							
1993-09-14	5.84231	5.99989	6.02824	6.07	6.1111	6.23077	6.28
1993-09-15	5.75099	5.83231	5.98989	6.01824	6.06	6.1011	6.22077
1993-09-16	5.76231	5.84308	6.00945	6.03791	6.08077	6.12143	6.24956
1993-09-17	5.77363	5.85385	6.02165	6.04758	6.09154	6.13176	6.26143
1993-09-20	5.79758	5.87615	6.04824	6.06659	6.11385	6.16033	6.29703

[5 rows x 21 columns]

In []: