

# The Effects of Vertical Arrangements in a Vertical Supply Chain\*

Gloria Sheu<sup>†</sup>  
Federal Reserve Board      Charles Taragin<sup>‡</sup>  
Federal Trade Commission

April 15, 2021

## **Abstract**

Keywords: bargaining models; merger simulation; vertical markets

JEL classification: L13; L40; L41; L42

---

\*The analysis and conclusions set forth are those of the authors and do not indicate concurrence by other members of the Board research staff, by the Federal Reserve Board of Governors, by the Federal Trade Commission, or by its Commissioners.

<sup>†</sup>Board of Governors of the Federal Reserve System, gloria.sheu@frb.gov.

<sup>‡</sup>Federal Trade Commission, ctaragin@ftc.gov

# 1 Introduction

## Data Generating Process

This section provides an overview of our methodology, with additional details appearing in the Appendix. We simulate markets by randomly sampling shares from a Dirichlet distribution for 2, 3, 4, or 5 retailers or wholesalers, respectively.<sup>1</sup> We also assume that in the pre-merger state, anywhere from 0 to 4 retailers are vertically integrated with a single wholesaler. We assume that vertically integrated wholesalers supply inputs to non-integrated retailers and that vertically integrated retailers purchase inputs from non-integrated wholesalers. The price coefficient  $\alpha$  is calibrated by assuming that in the pre-merger world, there is a vertically integrated outside option available to all customers. The other goods are differenced relative to this option, which maintains the outside good normalization. The market size is set to 1.

We specify values for the bargaining parameter ranging from 0.1 (wholesalers have the advantage) to 0.9 (retailers have the advantage). To better understand the relative bargaining strength of these parameter values, we report our results in terms of  $(1 - \lambda)/\lambda$ , which range from 9 (wholesaler power is nine times greater than retailer power) to 1/9 (retailer power is nine times greater than wholesaler power). The bargaining parameter is identical for all of the retailers in each simulation, unless noted otherwise.

For each combination of number of retailers, number of wholesalers, and bargaining parameter, we draw 1,000 different sets of market primitives. This results in 3.85 million merger simulations. We then eliminate mergers where the merger is unprofitable to the merging firms, as well as markets that do not pass the Hypothetical Monopolist Test, yielding 2.69 million markets.**discrepancy between res.nests dimension and ALL Counts in Table 1**<sup>2</sup> All 2.69 million markets treat as primitives the number of retailers, the number of

---

<sup>1</sup>We parametrize the Dirichlet distribution so it is equivalent to a uniform distribution.

<sup>2</sup>The Hypothetical Monopolist Test requires that were a monopolist to jointly own all products in a

wholesalers, the bargaining parameter, and the wholesaler and retailer marginal costs, which we allow to be either constant or linear.

When simulating a horizontal merger, we assign the products produced by the two largest firms in the market to a single entity post-merger. Similarly, when simulating a vertical merger, we assign the products produced by the largest wholesaler and the largest retailer to a single entity post-merger. This assignment is purposefully skewed towards mergers that are more likely to have competitive effects and to come under agency review.

Table ?? provides summary statistics across our various simulations.<sup>3</sup> The median average wholesale pre-merger price is \$4.5, and the median average retail pre-merger price is \$13. Because the market size is set to 1, these average prices are equal to total pre-merger expenditures. Pre-merger HHIs range between 2,820 at the 25<sup>th</sup> percentile to 5,013 at the 75<sup>th</sup>, with a median of 3,689. HHIs for horizontal downstream mergers increase by 2,015 points at the median, resulting in a median post-merger HHI equal to 4,914. HHIs for upstream mergers increase by 2,063 points at the median, resulting in a median post-merger HHI equal to 5,238. HHIs for vertical mergers increase by 1,055 points at the median, resulting in a median post-merger HHI equal to 5,995.<sup>4</sup> HHIs for integrated mergers increase by 2,770 points at the median, resulting in a median post-merger HHI equal to 7,280. Many of these markets fall into the span designated by the DOJ/FTC Horizontal Merger Guidelines as “Highly Concentrated Markets,” with post-merger HHIs over 2,500 points and HHI Changes greater than 200 points.<sup>5</sup>

---

candidate market, that firm would raise the price of at least one of the merging producers’ products by at least a “small but significant non-transitory increase in price” (SSNIP), which we take to be 5%.

<sup>3</sup>The `antitrust` R package contains the computer code needed to calibrate and simulate the effects of mergers in a range of competitive scenarios, including the ones described here.

<sup>4</sup>We compute the post-merger HHI for vertical mergers by calculating the merged firms’ market share as the sum of all the shares of downstream products that either incorporate the upstream partner’s input or are sold by the downstream partner.

<sup>5</sup>HHI thresholds are discussed in the 2010 Horizontal Merger Guidelines, Section 5.3.

## Results Overview

Our overall results are depicted in Figure 1, which is divided into four panels, each showing how the distribution of surplus changes for a particular set of agents (consumers, retailers, or wholesalers), as well as the net effect on the market as a whole. Surplus is presented as a percentage change relative to total pre-merger expenditure in the downstream market.

Each panel contains four pairs of box and whisker plots, with each pair corresponding to a different type of merger. The blue box and whisker plots (on the left in each pair) depict outcomes assuming that marginal costs are constant, and the orange box and whisker plots (on the right in each pair) show outcomes assuming that marginal costs are linear. The whiskers display the 5<sup>th</sup> and 95<sup>th</sup> percentiles of the outcome distribution, the boxes denote the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and the solid horizontal line marks the median. Note that negative outcome values imply agent harm, and positive values imply agent benefits.

We focus first on the results for consumers in the left-most panel of Figure 1. The median change is negative, indicating harm, across all four types of mergers for both cost specifications. However, the distributions and magnitudes differ. In particular, there is only a partial rank-ordering of consumer harm across different types of mergers: consumer harm from integrated mergers first-order stochastically dominates consumer harm from all other merger types, while downstream and upstream mergers each first-order stochastically dominate consumer harm from vertical mergers, but do not stochastically dominate one other. Median consumer harm from integrated mergers is about 16% of pre-merger total expenditures, 1.37 times the magnitude of that from downstream mergers, 2.4 times the magnitude of that from upstream mergers, and more than 3.5 times the magnitude of vertical mergers.

Consumer harm is less prevalent for mergers where firms have constant marginal costs than when firms have linear costs. Vertical mergers when firms have constant marginal costs benefit consumers in about 30% of all simulations , but only in about 2.3% of simulations

when firms have linear costs. Upstream mergers with constant marginal cost firms benefit consumers in about 12% of simulations, but only 0.2% of simulations when firms have linear costs. Downstream mergers with constant marginal cost firms benefit consumers in about 11% of simulations, but only about 6% of simulations when firms have linear costs. Finally, integrated mergers benefit consumers in about 10% of all simulations when firms have constant costs, but less than 1% of simulations when firms have linear costs.

**Is it worth exploring which effect dominates: the lessening of EDM or the strengthening of RRC? Maybe do this by allowing assymetric cost structures between merging and non-merging parties?**

Turning to retailers in the second panel of Figure 1, we find that while downstream mergers, vertical mergers and integrated mergers always benefit retailers, upstream mergers harm retailers in about 70% of all simulations. Moreover, there is a partial rank-ordering across mergers: the retailer surplus distribution from integrated mergers first-order stochastically dominates the retailer surplus distribution from downstream mergers, which dominates the retailer surplus distribution from upstream mergers, but not the retailer surplus distribution from vertical mergers. We also find that for upstream, vertical, and integrated mergers, retailer surplus under constant marginal cost first-order stochastically dominates the retail surplus distribution under linear costs, again suggesting that the incentive to raise rivals' costs dominates the benefits from EDM. By contrast, for downstream mergers, there is no clear rank-ordering between markets with constant marginal costs and markets with linear costs.

As for wholesaler surplus, which appears in the third panel, the effects seen there are largely the reflection of those for retailers: wholesaler surplus increases in about 82% of all upstream simulated mergers, 28% of simulated vertical mergers, 20% of simulated downstream mergers, and 17% of simulated integrated mergers. However, only wholesaler surplus from upstream mergers first-order stochastically dominates the wholesaler surplus of the

other merger types.

In terms of total welfare, with the exception of the approximately 10% of vertical mergers and 8.5% of integrated mergers with constant costs that are beneficial, our simulated mergers are almost always net harmful. Moreover there is a complete rank ordering of mergers, with total harm from integrated mergers first-order stochastically dominating total harm from downstream mergers, which dominates total harm from upstream mergers, which dominates totals harm from vertical mergers. Finally, for each merger type, total harm under linear costs first-order stochastically dominates total harm under constant marginal costs, with the greatest differences occurring for vertical and integrated mergers.

## Vertically Integrated Incumbent Firms

Here, we investigate how the presence of one or more incumbent vertically integrated firms affects merger outcomes when firms either have constant or linear marginal costs. In particular, we examine merger outcomes when a vertically integrated merges with either an unintegrated upstream or unintegrated downstream firm, or another integrated firm. We also examine merger outcomes for these integrated mergers as the number of integrated non-merging firms increases.

Figure 2 depicts box and whisker plots summarizing consumer harm (top row) and total harm (bottom row) as the number of incumbent integrated firms increases from 0 to 6 firms. The box and whisker plots when the number of incumbent integrated firms equals 0 correspond to the results depicted in Figure 1 of Sheu and Taragin (2017). For downstream and upstream mergers, the plots when the number of incumbent integrated firms equals 1 depict the outcome of a merger between an integrated firm and an unintegrated rival, and all 3rd parties are unintegrated. By contrast, for vertical mergers, the plots when the number of incumbent integrated firms equals 1 depict the outcome from an unintegrated wholesaler merging with an unintegrated retailer when a single 3rd party is integrated. Likewise, for

integrated mergers, the plots when the number of incumbent integrated firms equals 2 depict a merger between two integrated firms, and all rivals are unintegrated. The blue box and whisker plots (left) assume that firms face constant marginal costs, while the orange box and whisker plots (right) assume that firms face linear marginal costs.

## **References**

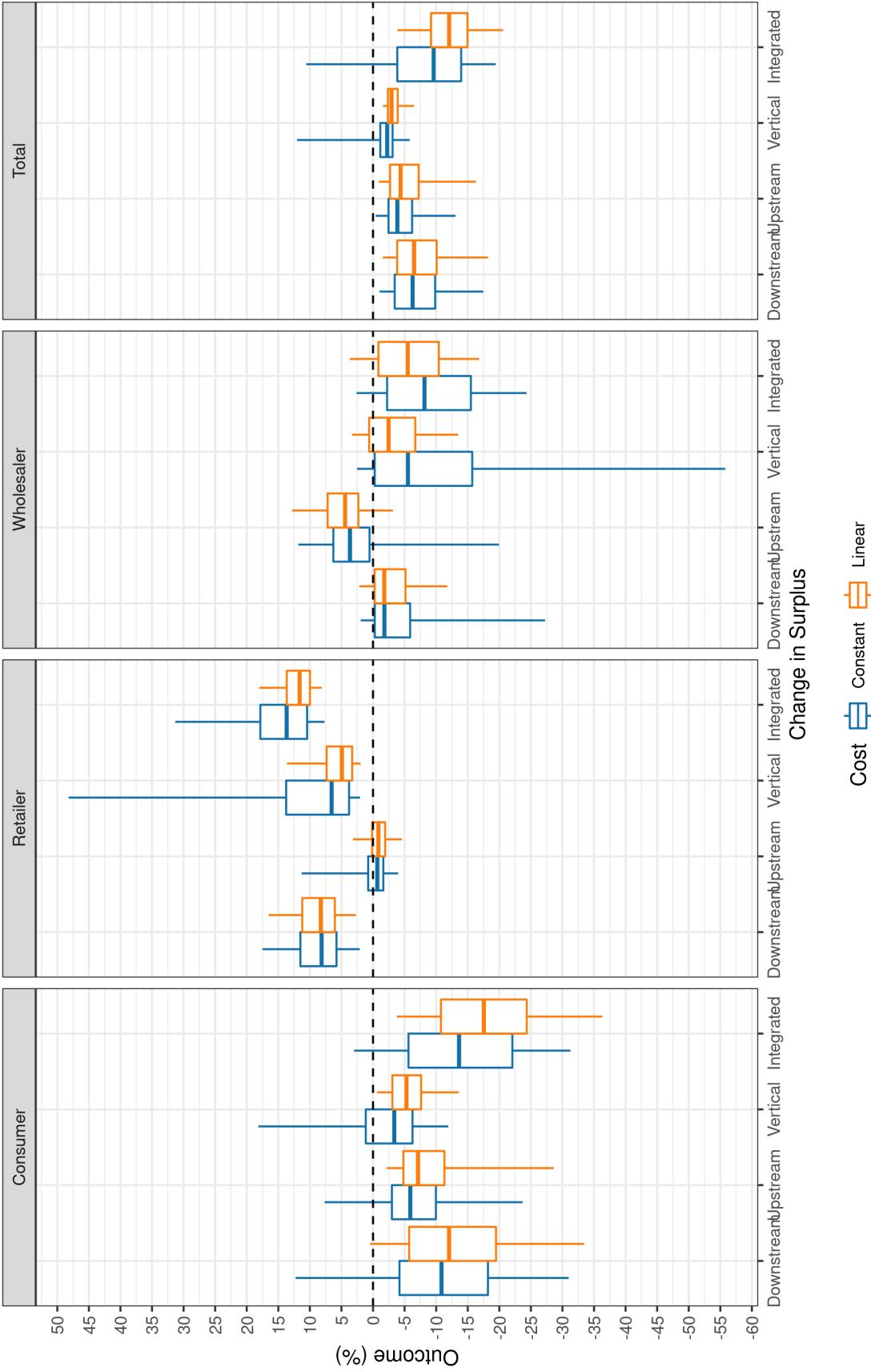
Sheu, G. and C. Taragin (2017). Simulating Mergers in a Vertical Supply Chain with Bargaining. EAG Discussion Papers 17-3, Economic Analysis Group.

Variable	Merger	Markets	Min	25th	50th	75th	Max
\# Retailers	All	2,687,297	2	3	4	5	5
\# Wholesalers			2	3	4	5	5
\# Integrated			0	0	1	3	6
Bargaining Power			0.1	0.4	0.6	0.8	0.9
Nesting Parameter			0	0	0	0	0
Avg. Upstream Price ()			0.19	2.3	4.5	9	253
Avg. Downstream Price ()			5.8	10	13	19	276
Market Elasticity			-61	-0.89	-0.52	-0.38	-0.23
Pre-Merger HHI	Integrated	679,620	2,178	3,620	4,298	5,515	9,996
	Upstream	756,570	2,010	2,574	3,171	4,236	10,000
	Downstream	745,941	2,010	2,374	2,852	3,733	10,000
	Vertical	505,166	2,118	3,620	4,386	5,554	9,970
Post-Merger HHI	Integrated	679,620	3,449	6,278	7,280	8,707	10,000
	Upstream	756,570	2,931	4,150	5,238	7,380	10,000
	Downstream	745,941	2,926	3,983	4,914	6,688	10,000
	Vertical	505,166	3,118	5,070	5,995	7,216	10,000
Delta HHI	Integrated	679,620	4	2,442	2,770	3,135	4,996
	Upstream	756,570	0	1,455	2,063	2,952	5,000
	Downstream	745,941	0	1,543	2,015	2,873	5,000
	Vertical	505,166	24	1,055	1,298	1,765	4,376

Table 1: Summary Statistics

## The Distributions of Merger Outcomes

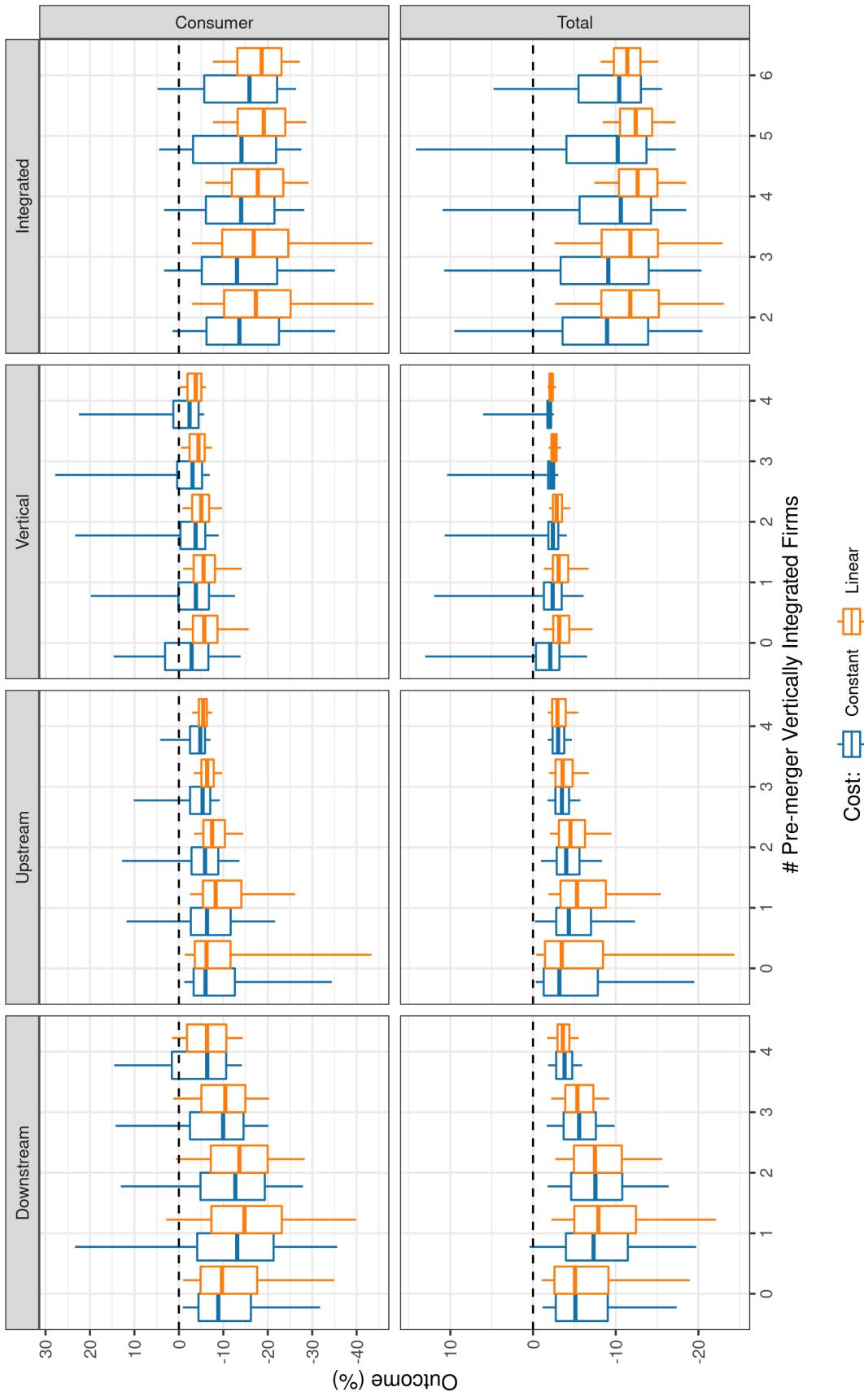
Outcomes are reported as a percentage of pre-merger total expenditures.



**Figure 1** The figure displays box and whisker plots summarizing the extent to which mergers affect consumer, retailer, wholesaler, and total surplus. Each blue box depicts the effects assuming that firms face constant marginal costs, while each orange box depicts the effects assuming that firms face linear marginal costs. Whiskers depict the 5<sup>th</sup> and 95<sup>th</sup> percentiles of a particular outcome, boxes depict the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and the solid horizontal line depicts the median.

## The Distributions of Merger Outcomes as the Number of Integrated Firms Increases

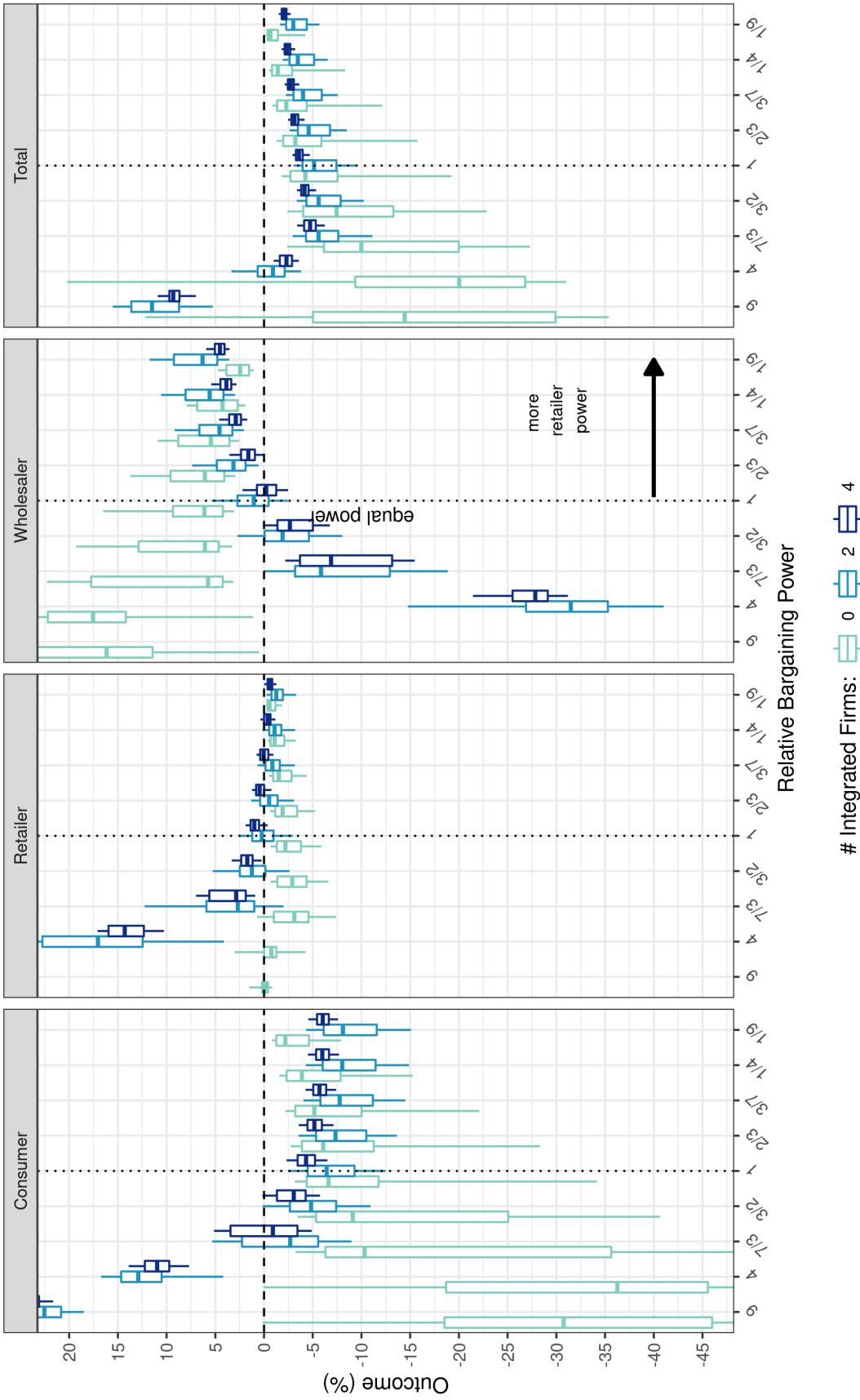
Outcomes are reported as a percentage of pre-merger total expenditures.  
 Horizontal mergers occur between a vertically integrated and un-integrated firm.



**Figure 2** The figure displays box and whisker plots summarizing the extent to which mergers affect consumer and total surplus as the number of vertically integrated firms present in a market change. Each blue box depicts the effects assuming that firms face constant marginal costs, while each orange box depicts the effects assuming that firms face linear marginal costs. Whiskers depict the 5<sup>th</sup> and 95<sup>th</sup> percentiles of a particular outcome, boxes depict the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and the solid horizontal line depicts the median.

## How Changing Bargaining Strength Affects Surplus in a Merger Among Wholesalers

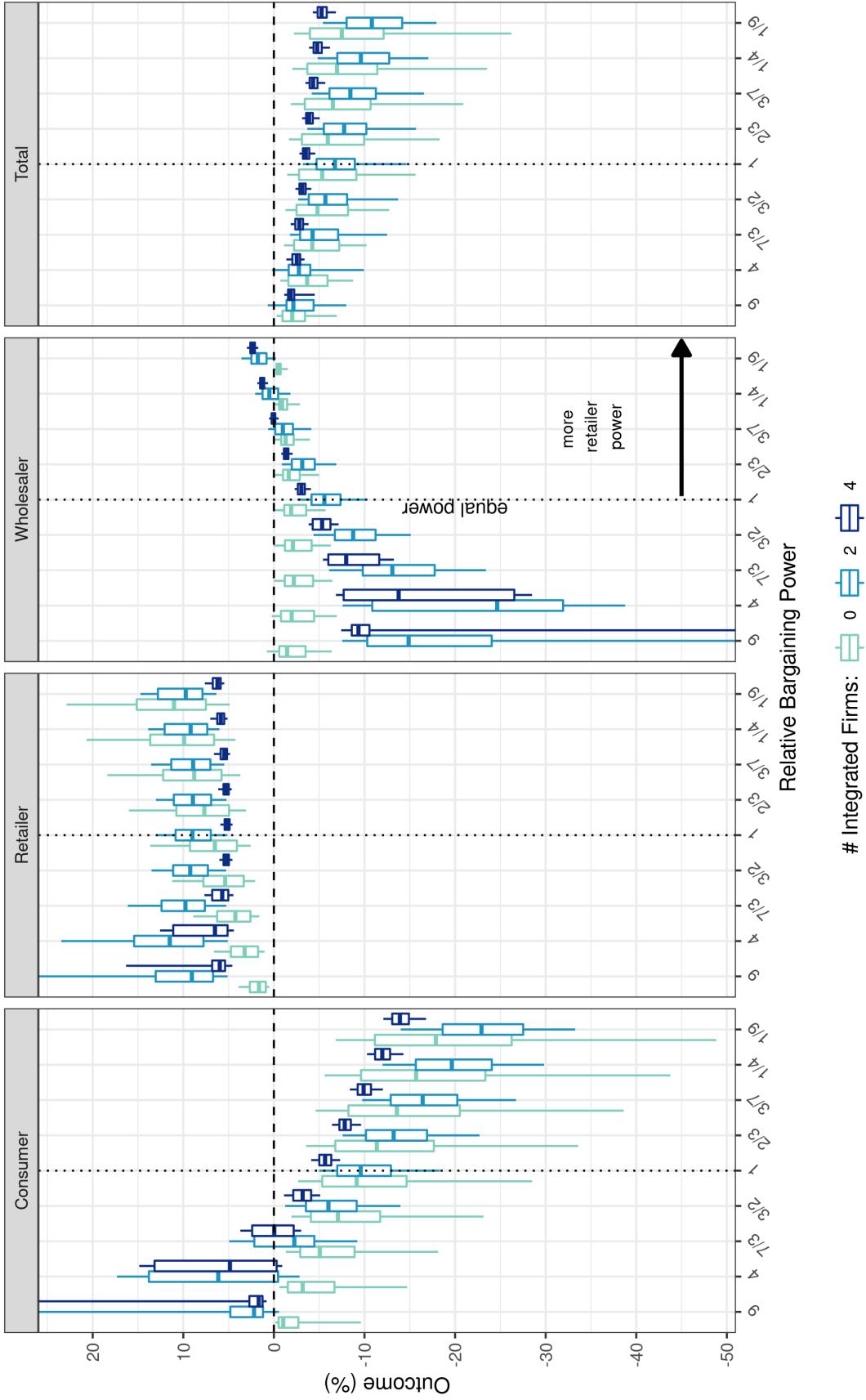
Outcomes are reported as a percentage of pre-merger total expenditures.



**Figure 3** The figure displays box and whisker plots summarizing the extent to which mergers among an integrated and un-integrated wholesaler affect consumer, retailer, wholesaler, and total surplus as the bargaining power of wholesalers relative to retailers changes. The different colored boxes display how outcomes change as the number of vertically integrated firms increases. Whiskers depict the 5<sup>th</sup> and 95<sup>th</sup> percentiles of a particular outcome, boxes depict the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and the solid horizontal line depicts the median.

## How Changing Bargaining Strength Affects Outcomes in a Merger Among Retailers

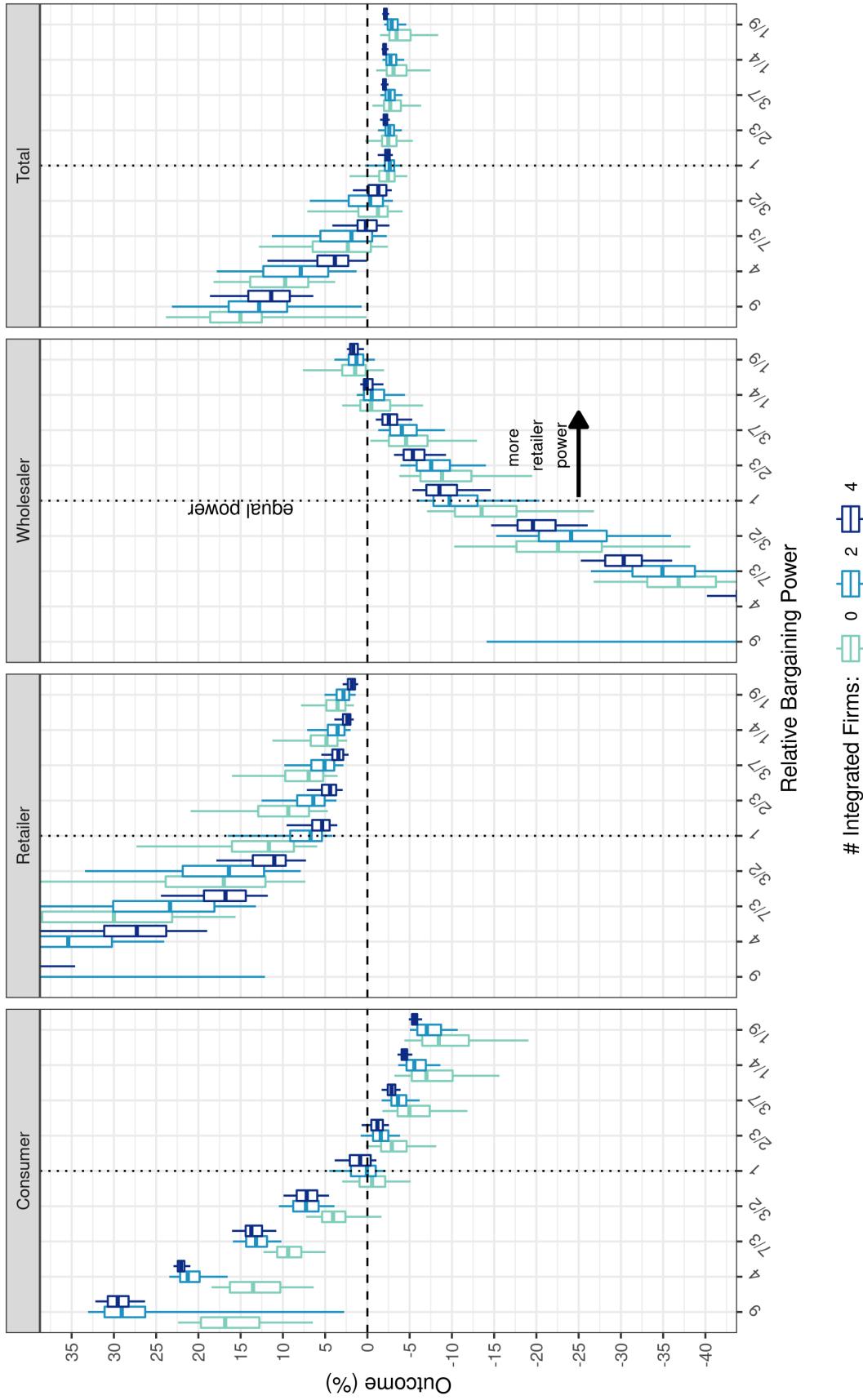
Outcomes are reported as a percentage of pre-merger total expenditures.



**Figure 4** The figure displays box and whisker plots summarizing the extent to which mergers among an integrated and un-integrated retailer affect consumer, retailer, wholesaler, and total surplus as the bargaining power of wholesalers relative to retailers changes. The different colored boxes display how outcomes change as the number of vertically integrated firms increases. Whiskers depict the 5<sup>th</sup> and 95<sup>th</sup> percentiles of a particular outcome, boxes depict the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and the solid horizontal line depicts the median.

## How Changing Bargaining Strength Affects Surplus in a Vertical Merger

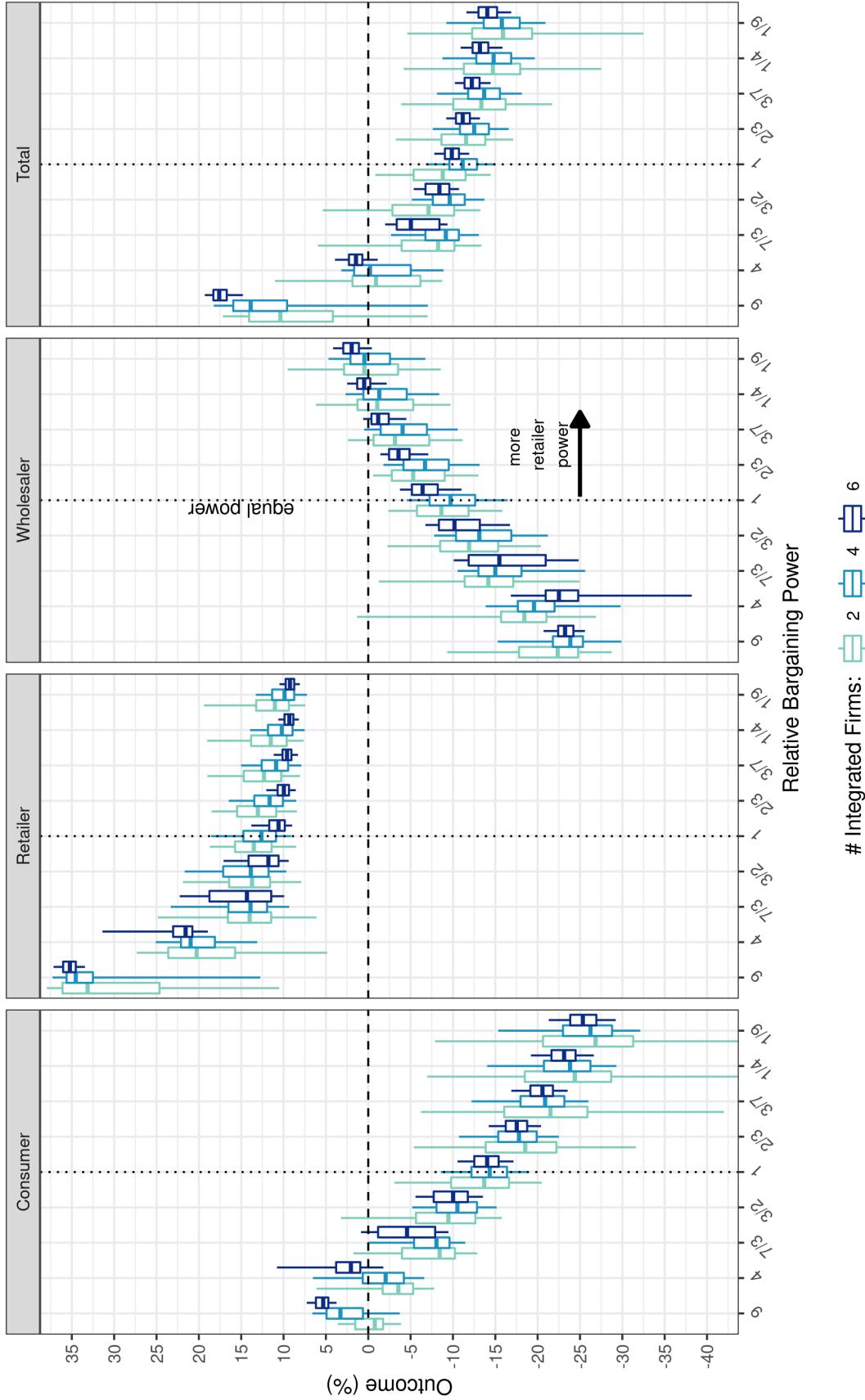
Outcomes are reported as a percentage of pre-merger total expenditures.



**Figure 5** The figure displays box and whisker plots summarizing the extent to which mergers among an un-integrated wholesaler and un-integrated retailer affect consumer, retailer, wholesaler, and total surplus as the bargaining power of wholesalers relative to retailers changes. The different colored boxes display how outcomes change as the number of vertically integrated firms increases. Whiskers depict the 5<sup>th</sup> and 95<sup>th</sup> percentiles of a particular outcome, boxes depict the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and the solid horizontal line depicts the median.

## How Changing Bargaining Strength Affects Surplus in an Integrated Merger

Outcomes are reported as a percentage of pre-merger total expenditures.



**Figure 6** The figure displays box and whisker plots summarizing the extent to which mergers among two integrated wholesalers and retailers affect consumer, retailer, wholesaler, and total surplus as the bargaining power of wholesalers relative to retailers changes. The different colored boxes display how outcomes change as the number of vertically integrated firms increases. Whiskers depict the 5<sup>th</sup> and 95<sup>th</sup> percentiles of a particular outcome, boxes depict the 25<sup>th</sup> and 75<sup>th</sup> percentiles, and the solid horizontal line depicts the median.