



Universidad Nacional de Asunción

FACULTAD POLITÉCNICA

## TABLE OF DATA AND RESULTS

Key information to understand the problems process and results included in  
*“Ubicación de casilleros para comercio electrónico. Un enfoque multiobjetivo”*  
research.

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# 1 Datos

## 1.1 Para el caso $n=20$

Tabla VI: Información de los barrios utilizados para el caso  $n = 20$ .

<b>N°</b>	<b>Acrónimo</b>	<b>Localidad</b>
1	BÑ	Bañado
2	OB	Obrero
3	PS	Pettirossi
4	RO	Republicano
5	SV	San Vicente
6	GD	Gral. Díaz
7	SR	San Roque
8	CT	Catedral
9	EN	Encarnación
10	DF	Dr. Francia
11	RB	Ricardo Brugada
12	TB	Tacumbú
13	MC	Mburicaó
14	SJ	Sajonia
15	LM	Las Mercedes
16	CN	Ciudad Nueva
17	PZ	Pinozá
18	RP	Roberto L. Petit
19	BC	Bernardino Caballero
20	ML	Mcal. López

Tabla VIII: Datos estimados de los clientes potenciales para el caso  $n = 20$

Localidad	EP	F	$K=EP \cdot F$
1	8.374	0.29	2.428
2	19.823	0.76	15.065
3	11.380	0.15	1.707
4	8.429	0.54	4.552
5	15.412	0.78	12.021
6	6.068	0.81	4.915
7	6.355	0.49	3.114
8	3.673	0.43	1.579
9	4.928	0.87	4.287
10	10.925	0.62	6.774
11	10.455	0.84	8.782
12	13.366	0.29	3.876
13	7.691	0.2	1.538
14	14.873	0.66	9.816
15	4.827	0.92	4.441
16	8.584	0.23	1.974
17	6.621	0.84	5.562
18	20.201	0.62	12.525
19	8.128	0.47	3.820
20	5.025	0.95	4.774
$\Sigma$	195.138		113.550

BÑ	BÑ	OB	PS	RO	SV	GD	SR	CT	EN	DF	RB	TB	MC	SJ	LM	CN	PZ	RP	BC	ML
1	0.38	0.79	0.12	0.46	1	0.16	0.49	0.34	0.45	0.59	0.03	0.03	0.14	0.19	0.16	0.27	0.49	0.75	0.3	0.75
0.88	1	0.53	0.87	0.76	0.72	1	0.42	0.03	0.52	0.19	0.8	0.59	0.36	0.51	0.77	0.69	0.43	0.37	0.62	0.62
0.89	0.46	1	0.09	0.09	0.65	0.38	0.22	0.86	0.12	0.28	0.31	0.86	0.36	0.18	0.61	0.64	0.7	0.07	0.73	0.74
0.1	0.2	0.1	1	1	0.11	0.7	0.6	0.64	0.14	0.17	0.14	0.56	0.14	0.65	0.15	0.32	0.21	0.36	0.46	0.63
0.18	0.79	1	0.16	0.46	1	0.16	0.49	0.34	0.45	0.59	0.03	0.03	0.14	0.19	0.16	0.27	0.49	0.75	0.3	0.75
0.42	0.53	0.87	0.76	0.76	0.72	1	0.42	0.03	0.52	0.19	0.8	0.59	0.36	0.51	0.77	0.69	0.43	0.37	0.62	0.62
0.07	0.64	0.34	0.43	0.43	0.03	0.71	1	0.18	0.68	0.48	0.5	0.1	0.59	0.61	0.27	0.89	0.73	0.27	0.07	0.74
0.86	0.28	0.02	0.8	0.8	0.35	0.84	0.75	1	0.49	0.05	0.64	0.09	0.11	0.37	0.85	0.24	0.47	0.36	0.38	0.26
0.87	0.01	0.54	0.42	0.42	0.45	0.29	0.14	0.45	1	0.62	0.11	0.2	0.71	0.73	0.15	0.13	0.11	0.37	0.28	0.26
0.85	0.29	0.22	0.47	0.47	0.54	0.43	0.44	0.86	0.58	1	0.23	0.13	0.53	0.48	0.44	0.89	0.79	0.34	0.25	0.55
0.68	0.76	0.04	0.09	0.09	0.84	0.9	0.03	0.45	0.2	0.31	1	0.77	0.11	0.64	0.44	0.16	0.4	0.35	0.23	0.82
0.37	0.22	0.64	0.32	0.32	0.7	0.65	0.36	0.62	0.41	0.12	0.13	1	0.44	0.34	0.89	0.73	0.51	0.42	0.65	0.17
0.52	0.47	0.46	0.46	0.46	0.23	0.4	0.73	0.14	0.69	0.33	0.31	0.24	1	0.29	0.76	0.64	0.56	0.82	0.36	0.35
0.57	0.26	0.65	0.02	0.02	0.89	0.64	0.75	0.5	0.22	0.09	0.48	0.48	0.06	1	0.49	0.36	0.25	0.57	0.78	0.5
0.16	0.39	0.22	0.73	0.73	0.04	0.88	0.71	0.82	0.14	0.5	0.11	0.39	0.42	0.05	1	0.57	0.07	0.72	0.8	0.6
0.04	0.34	0.56	0.47	0.47	0.84	0.62	0.04	0.82	0.41	0.11	0.88	0.21	0.84	0.84	0.75	1	0.76	0.42	0.39	0.1
0.42	0.79	0.42	0.68	0.68	0.07	0.38	0.28	0.18	0.15	0.17	0.57	0.52	0.22	0.7	0.15	0.4	1	0.11	0.46	0.13
0.63	0.49	0.62	0.65	0.65	0.44	0.4	0.43	0.66	0.23	0.27	0.13	0.33	0.54	0.29	0.78	0.07	0.08	1	0.0	0.16
0.88	0.61	0.34	0.1	0.1	0.35	0.64	0.5	0.01	0.02	0.84	0.06	0.2	0.64	0.11	0.64	0.31	0.25	0.33	1	0.51
0.7	0.79	0.18	0.66	0.66	0.66	0.28	0.44	0.39	0.54	0.41	0.68	0.69	0.82	0.42	0.14	0.51	0.03	0.8	0.04	1

Figura 3: Matriz  $MC$  para el caso  $n = 20$ .

## 2 Resultados

### 2.1 Numéricos

Tabla XI: Conjunto Pareto y frente Pareto correspondiente a la segunda instancia del problema  $n=20$ .

N°	$\Omega$	Colocar CP en	$f_1$	$f_2$	$f_3$	$f_4$
1	01001100010001100101	[OB, SV, GD, DF, SJ, LM, RP, ML]	7200	$5.36 \times 10^{-06}$	$1.42 \times 10^{-05}$	8354
2	01011110011100100100	[OB, RO, SV, GD, SR, DF, RB, TB, LM, RP]	8500	$5.22 \times 10^{-06}$	$1.31 \times 10^{-05}$	6748
3	01011110110100100101	[OB, RO, SV, GD, SR, EN, DF, TB, LM, RP, ML]	9200	$5.17 \times 10^{-06}$	$1.30 \times 10^{-05}$	5121
4	01011100110100100101	[OB, RO, SV, GD, EN, DF, TB, LM, RP, ML]	8500	$5.23 \times 10^{-06}$	$1.36 \times 10^{-05}$	5930
5	01011100011100100100	[OB, RO, SV, GD, DF, RB, TB, LM, RP]	7800	$5.29 \times 10^{-06}$	$1.37 \times 10^{-05}$	7651
6	01011110110000100101	[OB, RO, SV, GD, SR, EN, DF, LM, RP, ML]	8500	$5.24 \times 10^{-06}$	$1.37 \times 10^{-05}$	5615
7	01011110011000100101	[OB, RO, SV, GD, SR, DF, RB, LM, RP, ML]	8600	$5.20 \times 10^{-06}$	$1.29 \times 10^{-05}$	6287
8	01011110011000100100	[OB, RO, SV, GD, SR, DF, RB, LM, RP]	7800	$5.31 \times 10^{-06}$	$1.38 \times 10^{-05}$	7532
9	01011110110100100100	[OB, RO, SV, GD, SR, EN, DF, TB, LM, RP]	8400	$5.26 \times 10^{-06}$	$1.39 \times 10^{-05}$	6076
10	01001110011000100101	[OB, SV, GD, SR, DF, RB, LM, RP, ML]	7700	$5.34 \times 10^{-06}$	$1.38 \times 10^{-05}$	8187
11	01011110010000101101	[OB, RO, SV, GD, SR, DF, LM, PZ, RP, ML]	8500	$5.24 \times 10^{-06}$	$1.35 \times 10^{-05}$	6077
12	01011110010100101101	[OB, RO, SV, GD, SR, DF, TB, LM, PZ, RP, ML]	9200	$5.17 \times 10^{-06}$	$1.28 \times 10^{-05}$	5582
13	01011100010100101101	[OB, RO, SV, GD, DF, TB, LM, PZ, RP, ML]	8500	$5.23 \times 10^{-06}$	$1.34 \times 10^{-05}$	6392
14	01011100011101100100	[OB, RO, SV, GD, DF, RB, TB, SJ, LM, RP]	9800	$5.08 \times 10^{-06}$	$1.20 \times 10^{-05}$	6099
15	01011110011001100100	[OB, RO, SV, GD, SR, DF, RB, SJ, LM, RP]	9800	$5.10 \times 10^{-06}$	$1.21 \times 10^{-05}$	5981
16	01011100011001100101	[OB, RO, SV, GD, DF, RB, SJ, LM, RP, ML]	9900	$5.05 \times 10^{-06}$	$1.19 \times 10^{-05}$	5546
17	01011100011001100100	[OB, RO, SV, GD, DF, RB, SJ, LM, RP]	9100	$5.16 \times 10^{-06}$	$1.26 \times 10^{-05}$	6884
18	11011110010000100101	[BN, OB, RO, SV, GD, SR, DF, LM, RP, ML]	8600	$5.28 \times 10^{-06}$	$1.41 \times 10^{-05}$	5569
19	01011110010100100101	[OB, RO, SV, GD, SR, DF, TB, LM, RP, ML]	7500	$5.29 \times 10^{-06}$	$1.38 \times 10^{-05}$	6750
20	01011110010101100100	[OB, RO, SV, GD, SR, DF, TB, SJ, LM, RP]	8700	$5.18 \times 10^{-06}$	$1.29 \times 10^{-05}$	6153
21	01011110010001100100	[OB, RO, SV, GD, SR, DF, SJ, LM, RP]	8000	$5.27 \times 10^{-06}$	$1.36 \times 10^{-05}$	6938
22	01011100010001100101	[OB, RO, SV, GD, DF, SJ, LM, RP, ML]	8100	$5.22 \times 10^{-06}$	$1.33 \times 10^{-05}$	6503
23	01011110010101100101	[OB, RO, SV, GD, SR, DF, TB, SJ, LM, RP, ML]	9500	$5.08 \times 10^{-06}$	$1.22 \times 10^{-05}$	5199
24	01001100011001100101	[OB, SV, GD, DF, RB, SJ, LM, RP, ML]	9000	$5.18 \times 10^{-06}$	$1.26 \times 10^{-05}$	7397
25	01001100011101100101	[OB, SV, GD, DF, RB, TB, SJ, LM, RP, ML]	9700	$5.11 \times 10^{-06}$	$1.20 \times 10^{-05}$	6902
26	01011100010101100100	[OB, RO, SV, GD, DF, TB, SJ, LM, RP]	8000	$5.24 \times 10^{-06}$	$1.35 \times 10^{-05}$	7056
27	01011100010001100100	[OB, RO, SV, GD, DF, SJ, LM, RP]	7300	$5.34 \times 10^{-06}$	$1.42 \times 10^{-05}$	7841
28	01001110011001100101	[OB, SV, GD, SR, DF, RB, SJ, LM, RP, ML]	9700	$5.12 \times 10^{-06}$	$1.21 \times 10^{-05}$	6587
29	01011100010101100101	[OB, RO, SV, GD, DF, TB, SJ, LM, RP, ML]	8800	$5.14 \times 10^{-06}$	$1.26 \times 10^{-05}$	6008
30	01011110010001100101	[OB, RO, SV, GD, SR, DF, SJ, LM, RP, ML]	8800	$5.16 \times 10^{-06}$	$1.28 \times 10^{-05}$	5693
31	01001100010101100101	[OB, SV, GD, DF, TB, SJ, LM, RP, ML]	7900	$5.28 \times 10^{-06}$	$1.34 \times 10^{-05}$	7859
32	01011100011000100101	[OB, RO, SV, GD, DF, RB, LM, RP, ML]	7900	$5.26 \times 10^{-06}$	$1.35 \times 10^{-05}$	7097
33	01011110011100100101	[OB, RO, SV, GD, SR, DF, RB, TB, LM, RP, ML]	9300	$5.12 \times 10^{-06}$	$1.23 \times 10^{-05}$	5793
34	01011100011100100101	[OB, RO, SV, GD, DF, RB, TB, LM, RP, ML]	8600	$5.19 \times 10^{-06}$	$1.28 \times 10^{-05}$	6602
35	01001100011100100101	[OB, SV, GD, DF, RB, TB, LM, RP, ML]	7700	$5.32 \times 10^{-06}$	$1.36 \times 10^{-05}$	8502
36	01001110011100100101	[OB, SV, GD, SR, DF, RB, TB, LM, RP, ML]	8400	$5.26 \times 10^{-06}$	$1.31 \times 10^{-05}$	7692
37	01011110010110100101	[OB, RO, SV, GD, SR, DF, TB, MC, LM, RP, ML]	8400	$5.26 \times 10^{-06}$	$1.35 \times 10^{-05}$	6087

Tabla X: Progreso del algoritmo *NSGA-II* teniendo en cuenta las 10 ejecuciones sobre la segunda instancia del problema  $n=20$ .

Ejecución	Generación 1		Generación 10		Generación 100		Generación 500		Generación 1000		Generación 1500	
	Tiempo(s)	N° de soluciones	Tiempo(s)	N° de soluciones	Tiempo(s)	N° de soluciones	Tiempo(s)	N° de soluciones	Tiempo(s)	N° de soluciones	Tiempo(s)	N° de soluciones
1	0.90	1	18.04	11	215.48	23	1080.58	33	2179.77	35	2179.77	35
2	0.72	1	28.09	8	289.53	30	1315.25	35	2609.07	35	3818.21	35
3	0.75	2	19.42	13	216.12	24	1144.07	35	2181.65	37	3198.47	37
4	0.92	1	25.54	7	278.30	23	1279.88	32	2444.73	36	3566.76	36
5	0.67	2	17.68	10	241.08	24	1158.16	31	2217.62	34	3265.99	34
6	0.75	4	26.57	10	251.41	18	1246.56	26	2519.13	30	3704.72	33
7	0.67	1	16.27	9	195.76	18	1067.33	25	2263.28	35	3609.08	36
8	0.91	1	19.66	10	224.45	27	1222.12	33	2769.09	33	3899.61	35
9	0.66	2	16.29	6	196.61	30	1069.09	33	2151.72	35	3390.24	35
10	0.68	1	33.98	13	426.08	23	1604.76	29	2765.86	32	4290.11	35
<b>Promedio</b>	0.763	1.6	22.154	9.7	253.48	24	1218.78	31.2	2410.19	34.2	3492.29	35.1
<b>Desv est (<math>\sigma</math>)</b>	0.1	0.92	5.70	2.19	64.89	3.95	153.79	3.31	232.10	1.94	533.26	1.04

## 2.2 Gráficos

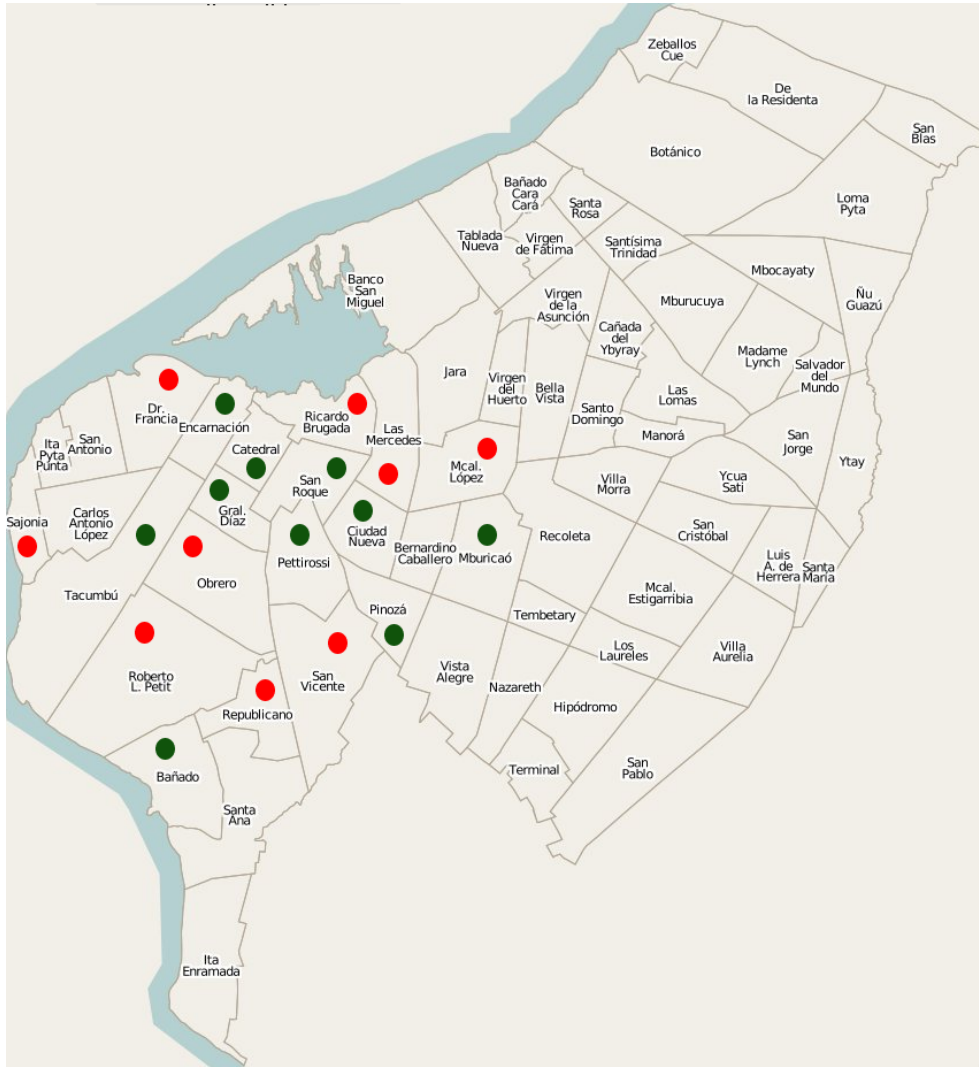


Figura 5: Solución 16 de la Tabla XI representada en el mapa de Asunción. Los puntos rojos representan la instalación de CP, mientras que los puntos verdes, ausencia de CP en las respectivas localidades.

## 3 Algoritmos

### 3.1 Exhaustivo

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**Algoritmo 1** Búsqueda exhaustiva

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```
1: procedure  
2:    $leer \rightarrow n$   
3:    $dominatedSet = \emptyset$   
4:    $paretoSet = \emptyset$   
5:   for  $i = 1$  to  $2^n - 2$  do  
6:     for  $j = i + 1$  to  $2^n - 1$  do  
7:       if  $i \succ j$  then  
8:          $dominatedSet \cup \{j\}$   
9:       else if  $j \succ i$  then  
10:         $dominatedSet \cup \{i\}$   
11:   for  $i = 1$  to  $2^n - 1$  do  
12:     if  $i \notin dominatedSet$  then  
13:        $paretoSet \cup \{i\}$   
   return  $paretoSet$ 
```

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