

CS-174A Discussion 1A, Week 5

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@ <https://github.com/luckiday/cs174a-1a-2021w> (<https://github.com/luckiday/cs174a-1a-2021w>)

Logistics

- Online midterm instructions
- Midterm scope: slides02 to slides06.

Last time

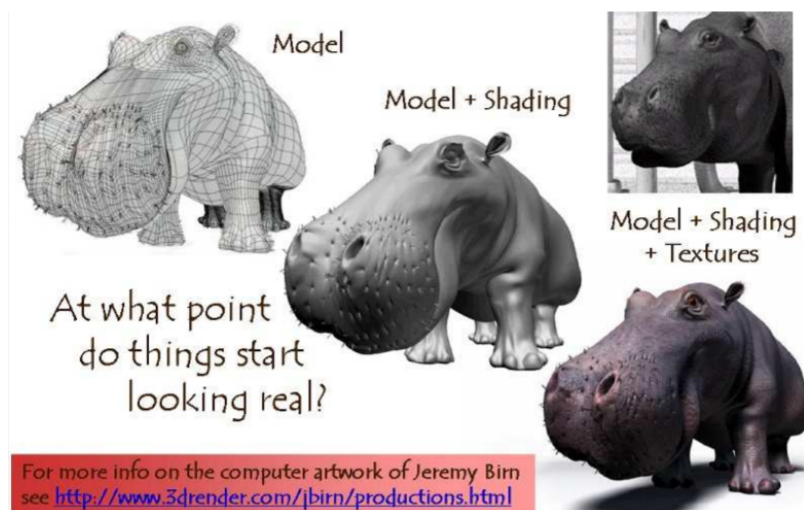
- Transformations: Pumpkin problem
- Change of basis
- Tiny graphics demos

Next up

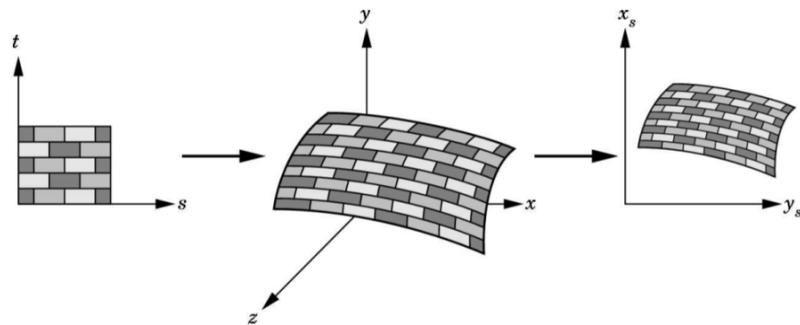
- Assignment 2
- Midterm review

Texture Mapping

- There are small surface details on real objects that need to be taken into account for better realism.



- To take these into account apply texture to our images to make the surfaces realistic
 - We can scan textures from real world or paint them
 - Store the texture as a 2D image
 - We map the texture to **object space** and then **screen space**



- From screen to texture:
 - Inverse the transform (s_x, s_y) to get the world (x, y, z)
 - With (x, y, z) :

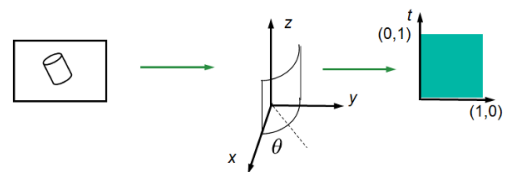
$$u = \tan^{-1}(y/x), \quad v = z$$

$$s = 2u/\pi, \quad t = v$$

Reminder: $u = s\pi/2, \quad v = t$

$$x = r \cos \theta, \quad y = r \sin \theta, \quad z$$

Surface parameters: $u = \theta, \quad v = z$



Assignment 2

- Demo

Midterm Review

Q: What is the diff between affine combinations and convex combination of points?

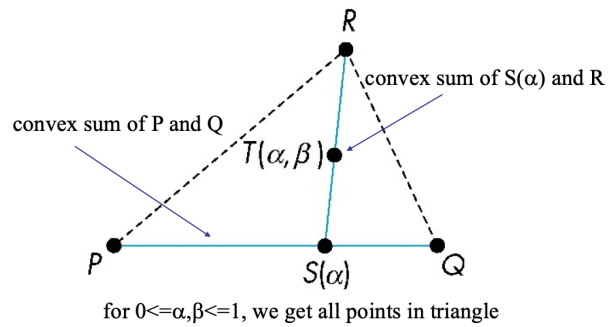
Points and Vectors

Q: Parametric equations of line and triangle (barycentric coordinamtes)

A:

- *Line*: $P = \alpha_1 P_1 + \alpha_2 P_2$, and $\alpha_1 + \alpha_2 = 1$.
- *Triangle*:

Triangles



A: Barycentric coordinates

Triangle is convex so any point inside can be represented as a convex sum

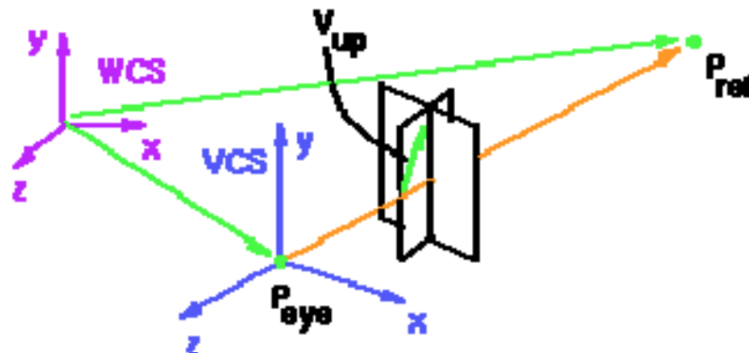
$$P(a_1, a_2, a_3) = a_1 P + a_2 Q + a_3 R$$

where

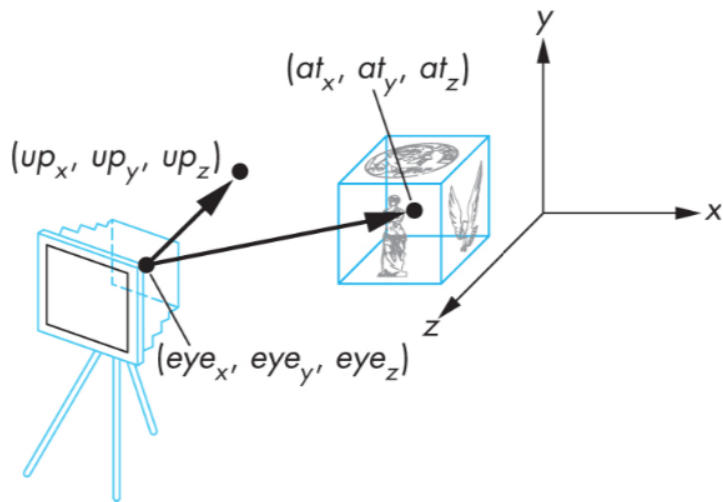
$$a_1 + a_2 + a_3 = 1, a_i \geq 0$$

The representation is called the barycentric coordinate representation of P.

Change of Basis and Model-view transformation



Viewing



Projection

- Orthographic projection matrix:

$$N = ST = \begin{pmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{l+r}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{b+t}{t-b} \\ 0 & 0 & -\frac{2}{f-n} & -\frac{f+n}{f-n} \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

- Perspective projection matrix:

$$P = NSH = \begin{pmatrix} \frac{n}{r} & 0 & 0 & 0 \\ 0 & \frac{n}{t} & 0 & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

- Derivation

$$N = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & a & b \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

After perspective division, the point $(x, y, z, 1)$ goes to

$$x'' = -x/z, \quad y'' = -y/z, \quad z'' = -(a + b/z)$$

When $z = f$, $z'' = -1$; when $z = n$, $z'' = 1$.

Sample Questions

1. Q: Briefly describe what changes you would expect to see in the image with respect to the following changes in viewing parameters, all other params remaining unchanged:
- A. Half-angle-of-view decreases
 - // 2. Aspect ratio increases
 - B. COI moves closer to eye point
 - C. Eye point moves away from COI
 - D. Top vector becomes upside down
 - E. Distance between hither and yon increases

1. Answers:

- A. Half-angle-of-view decreases: objects will project larger on window and viewport, because camera is now capturing lesser volume of the scene while image size remains same
- B. Aspect ratio increases: AR increases implies viewport became wider or the height decreased; if angle did not change then some objects may be clipped off; the final image will definitely look wider
- C. COI moves closer to eye point: no change in image
- D. Eye point moves away from COI: a different image will be grabbed because the location of eye changed
- E. Top vector becomes upside down: image will rotate 180
- F. Distance between hither and yon increases: depending on which direction H and Y moves, more or less objects will be included in the view volume

2. Prove that the perspective projection of a 3D point (x, y, z) onto the plane $z = d$ is given by $(\frac{x}{z}d, \frac{y}{z}d, d)$

3. Given this pumpkin at (1,1), do the following:

```
model *= trans(x+2,y+2);
model *= rot_z(90);
model *= scale_x(-1);
model *= trans(x-1,y-1);
```

