LAB PROJECT REPORT

for

ECE 2244: VLSI Design Lab

IEEE-754 32-BIT FLOATING POINT MULTIPLIER

Submitted by

Lakshit Verma Reg. 230959210 Roll No. 75

and

Pranav Saini Reg. 230959212 Roll No. 76

Batch: A3

DEPT. OF ELECTRONICS AND COMMUNICATION (ECE)
MANIPAL INSTITUTE OF TECHNOLOGY, MANIPAL - 576104

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OBJECTIVE

To design and implement an IEEE 754 compliant 32-bit floating point multiplier using Verilog and synthesize it, focusing on accuracy, power consumption, area, and timings.

CHAPTER 1: INTRODUCTION

Floating point arithmetic is widely used in various computing applications, including scientific computations, digital signal processing, and graphics processing. This project focuses on the design and implementation of an IEEE 754 compliant 32-bit floating point multiplier using VLSI design methodologies. The IEEE 754 standard defines a precise format for representing floating point numbers and ensures accuracy in floating point operations.

The proposed design consists of three main stages: exponent addition with bias adjustment, mantissa multiplication with normalization, and rounding to maintain precision. Special cases such as underflow, overflow, and handling of special numbers (NaN, INFINITY) are also considered. The implementation is carried out using Verilog HDL and synthesized using FPGA-based tools to evaluate the area, power, and timing performance.

The results demonstrate efficient multiplication with optimized resource utilization, making it suitable for high-performance computing applications. This mini-project provides insights into floating point arithmetic and its practical realization in VLSI circuits.

CHAPTER 2: PROJECT THEORY AND EXPLANATION

IEEE 754 Format

A 32-bit floating-point number consists of three parts:

where:

- 1. S (1 bit): Sign bit (1 = positive, 0 = negative)
- **2. E** (**8 bits**): Exponent (biased by 127)
- **3. M (23 bits):** Mantisssa (fractional part, normalized)

Let's take a sample 32-bit binary representation:

- 1. Sign bit (0) indicates that it is a positive number
- 2. Exponent (10000010 binary = 130 decimal) so actual exponent = 130 127 = 3
- 3. Mantissa (1.110 in binary = 1.75 in decimal, since implicit leading 1)

Thus, the value is:

$$1.75 \times 2^3 = 14.0$$

Structure of the module

The code is layed out as follows:

Internal Registers:

- counter: Controls execution stages (3-bit).
- a_m, b_m, z_m: Mantissas (24-bit).

- a_e, b_e, z_e: Exponents (10-bit).
- a_s, b_s, z_s: Signs (1-bit).
- product: Stores intermediate mantissa multiplication (50-bit).
- guard_bit, round_bit, sticky: Used for rounding.

The working of the code are as follows:

- 1. Counter Update: Increments on every clock cycle or resets if rst is high.
- 2. Extract Components: Extracts sign, exponent, and mantissa from inputs a and b.
- 3. Handle Special Cases:
 - Checks for NaN (Not a Number), Infinity, or Zero conditions.
 - Denormalizes subnormal numbers.
- 4. **Normalize Inputs**: Ensures mantissas are normalized.
- 5. Compute Product:
 - Computes sign (z_s), adds exponents (z_e), and multiplies mantissas (product).

6. Extract Mantissa and Guard Bits:

• Extracts top 24 bits from product and sets guard, round, and sticky bits.

7. Normalize & Round:

- Adjusts exponent and mantissa to maintain IEEE 754 compliance.
- Rounds the result if necessary.

8. Generate Output:

- Reconstructs final floating-point result in IEEE 754 format.
- Handles overflow/underflow cases.

CHAPTER 3: VERILOG CODE AND TESTBENCH

The Verilog code for the multiplier is given below:

```
module fmultiplier(clk, rst, a, b, z);
input clk, rst;
input [31:0] a, b;
output reg [31:0] z;
reg [2:0] counter;
reg [23:0] a_m, b_m, z_m;
reg [9:0] a_e, b_e, z_e;
reg a_s, b_s, z_s;
reg [49:0] product;
reg guard bit, round bit, sticky;
always @(posedge clk or posedge rst) begin
    if (rst)
        counter ≤ 0;
    else
        counter ≤ counter + 1;
end
always @(counter) begin
    if(counter = 3'b001) begin
        a m \leq a[22:0];
            b_m \leq b[22:0];
             a_e \leq a[30:23] - 127;
            b_e \le b[30:23] - 127;
            a_s \leq a[31];
             b_s \leq b[31];
        end
end
always @(counter) begin
    if(counter = 3'b010) begin
        if ((a_e = 128 \& 6 a_m \neq 0) || (b_e = 128 \& 6 b_m \neq 0)) begin // NAN
                   z[31] \leq 1;
                   z[30:23] \leq 255;
                   z[22] \leq 1;
                   z[21:0] \leq 0;
               end
               else if (a_e = 128) begin //INF A
                   z[31] \leq a_s \wedge b_s;
                   z[30:23] \leq 255;
```

```
if ((\$signed(b_e) = -127) & (b_m = 0)) begin // NAN if B=0
                          z[31] \leq 1;
                          z[30:23] \leq 255;
                          z[22] \leq 1;
                          z[21:0] \leq 0;
                   end
               end
               else if (b_e = 128) begin //INF B
                   z[31] \leq a_s \wedge b_s;
                   z[30:23] \leq 255;
                   z[22:0] \leq 0;
                   if ((\$signed(a_e) = -127) & (a_m = 0)) begin //NAN if A=0
                          z[31] \leq 1;
                          z[30:23] \leq 255;
                          z[22] \leq 1;
                          z[21:0] \leq 0;
                   end
               end
               else if ((\$signed(a_e) = -127) \delta\delta (a_m = 0)) begin // 0 if A = 0
                 z[31] \leq a_s \wedge b_s;
                 z[30:23] \leq 0;
                   z[22:0] \leq 0;
               end
               else if ((\$signed(b_e) = -127) & (b_m = 0)) begin // 0 if B = 0
                   z[31] \leq a_s \cdot b_s;
                    z[30:23] \leq 0;
                    z[22:0] \leq 0;
               end
               else begin
                   if (\$signed(a_e) = -127) // denormalizing A
                          a_e \leq -126;
                   else
                          a_m[23] \leq 1;
                     if (\$signed(b_e) = -127) // denormalizing B
                          b e \leq -126;
                   else
                          b_m[23] \leq 1;
               end
        end
end
always @(counter) begin
    if(counter = 3'b011) begin
        if (~a_m[23]) begin // normalize A
                 a_m \leq a_m \ll 1;
                a_e \leq a_e - 1;
             if (~b_m[23]) begin // normalize B
                 bm \leq bm \ll 1;
                b_e \leq b_e - 1;
             end
```

 $z[22:0] \leq 0;$

```
end
end
always @(counter) begin
    if(counter = 3'b100) begin // get the signs xored and exponents added and
        z_s \leq a_s \wedge b_s;
                                 // the intermediate mantissa multiplication
            z_e \le a_e + b_e + 1;
            product \leq a_m * b_m * 4;
    end
end
always @(counter) begin
    if(counter = 3'b101) begin
        z_m \leq product[49:26];
           guard_bit ≤ product[25];
              round bit ≤ product[24];
              sticky \leq (product[23:0] \neq 0);
    end
end
always @(counter) begin
    if(counter = 3'b110) begin
        if (signed(z_e) < -126) begin
                z_e \leq z_e + (-126 - signed(z_e));
                z_m \leq z_m \gg (-126 - signed(z_e));
                 guard_bit \leq z_m[0];
               round_bit ≤ guard_bit;
               sticky ≤ sticky | round_bit;
            end
        else if (z_m[23] = 0) begin
                z_e \leq z_e - 1;
                z_m \leq z_m \ll 1;
                z_m[0] \leq guard_bit;
                guard_bit ≤ round_bit;
                round bit \leq 0;
            end
            else if (guard_bit & (round_bit | sticky | z_m[0])) begin
                z_m \leq z_m + 1;
                  if (z m = 24'hffffff)
                         z_e \leq z_e + 1;
            end
        end
end
always @(counter) begin
    if(counter = 3'b111) begin
        z[22:0] \leq z_m[22:0];
            z[30:23] \leq z_e[7:0] + 127;
            z[31] \leq z_s;
            if (\$signed(z e) = -126 \& z m[23] = 0)
                   z[30:23] \leq 0;
            if ($signed(z_e) > 127) begin // if overflow return INF
```

```
z[22:0] \leq 0;
                   z[30:23] \leq 255;
                   z[31] \leq z_s;
            end
    end
end
endmodule
And the Verilog code for the testbench is given below:
module fmultiplier_tb;
reg [31:0] a, b;
wire [31:0] z;
reg clk, rst;
fmultiplier multiplier(clk, rst, a, b, z);
initial begin
      $dumpfile("wave.vcd"); // dumps the waveforms
      $dumpvars(0, fmultiplier_tb);
end
initial begin
      clk \leq 0;
      rst \leq 1;
      repeat (17000) // clocks 17,000 times with a period of 5ns
            #5 clk \leq ~clk;
end
initial #13 rst ≤ 0;
initial begin
      #3
      repeat (500) begin
            a = $random; // assigns random values to
            b = $random; // both a and b
      end
      #80 $finish;
end
endmodule
```

CHAPTER 4: RESULTS

CONCLUSION

Through this project, we gained a deeper understanding of floating-point arithmetic. We explored the IEEE 754 standard, learning how floating-point numbers are represented and manipulated in hardware. Implementing normalization, rounding, and handling special cases gave us insight into practical challenges in floating-point multiplication. Additionally, we developed skills in Verilog coding, simulation, and synthesis, understanding how different design choices impact performance in terms of area, power, and timing. Having to debug and verify the design using a testbench also strengthened our problem-solving abilities, showing the importance of careful design validation in VLSI development.

REFERENCES

- 1. IEEE Standard for Floating-Point Arithmetic, IEEE Std 754-2008.
- 2. Floating Point Numbers Computerphile (YouTube): https://www.youtube.com/watch?v=PZRI1IfStY0
- 3. Online resources and research papers on IEEE 754 floating point arithmetic and Verilog design methodologies.
- 4. https://numeral-systems.com/ieee-754-multiply/