

- Using open addressing with linear probing

$N = 13$

Array:	
0	13
1	27
2	15
3	54
4	24
5	135
6	174
7	
8	
9	
10	10
11	114
12	49

$$1 + 1^2$$

$$1 + 2^2$$

$$1 + 3^2$$

- Using open addressing with quadratic probing

$N = 13$

Array:

0	13
1	49
2	15
3	54
4	27
5	135
6	174
7	
8	
9	
10	10
11	114
12	24

$$54 + 1^2 \bmod 13 = 3$$

$$114 + 1^2 \bmod 13 = 11$$

$$49 + 1^2 \bmod 13 = 11$$

$$49 + 2^2 \bmod 13 = 1$$

$$174 + 1^2 \bmod 13 =$$

$$27 + 1^2 \bmod 13 = 2$$

$$27 + 2^2 \bmod 13 = 5$$

$$27 + 3^2 \bmod 13 = 10$$

$$27 + 4^2 \bmod 13 = 4$$

$$24 + 1^2 \bmod 13 =$$

- Using open addressing (division hashing) and the linear-quotient collision path algorithm

$N = 13$, $4k+3$ prime = 19

LQHashing:

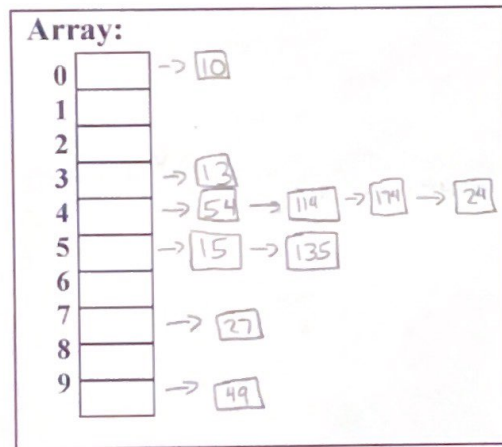
- $ip = pk \% N$
- $q = pk / N$
if ($q \% N \neq 0$)
offset = q
else
offset = $4k+3$ prime
- While collisions:
 $ip' = (ip + offset) \% N$
- Set $Array[ip] = key$

$54/13 = 4$
 $2+4 \% 13 = 6$
 $49/13 = 3$
 $10+3 \% 13 = 0$
 $0+3 \% 13 = 3$
 $174/13 = 13$
 $5+13 \% 13 = 11$
 $24/13 = 1$
 $11+1 \% 13 = 12$

Array:

0	13
1	27
2	15
3	49
4	112
5	135
6	54
7	
8	114
9	
10	10
11	174
12	24

- Bucket hashing where $(N=10)$ and $ip = (p_k) \% N$



$$\begin{aligned}
 15 \% 10 &= 5 \\
 54 \% 10 &= 4 \\
 13 \% 10 &= 3 \\
 10 \% 10 &= 0 \\
 135 \% 10 &= 5 \\
 114 \% 10 &= 4 \\
 49 \% 10 &= 9 \\
 174 \% 10 &= 4 \\
 27 \% 10 &= 7 \\
 24 \% 10 &= 4
 \end{aligned}$$

- Come up with your own 15 elements with an array size of 21 using an open addressing algorithm of your choice
- Challenge yourself! Use an algorithm that you are most unfamiliar with to maximize your learning experience

Elements: 15 $\rightarrow [3, 5, 13, 62, 17, 1, 0, 99, 113, 23, 73, 48, 56, 81, 66]$
 $\text{mod } 21$ 3 5 13 10 17 1 0 9 9 10 8 9 4 3 1
 N = 21

LQ Hashing From Previous Problem

Array:

0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
0	1		3	56	5	81	66	99	113	62	23		13	73	48		17			

$$23/21 = 1$$

$$10 + 1 \text{ mod } 21 = 11$$

$$73/21 = 3$$

$$8 + 3 \text{ mod } 21 = 11$$

$$11 + 3 \text{ mod } 21 = 14$$

$$48/21 = 2$$

$$9 + 2 \text{ mod } 21 = 11$$

$$11 + 2 \text{ mod } 21 = 13$$

$$13 + 2 \text{ mod } 21 = 15$$

$$81/21 = 3$$

$$3 + 3 \text{ mod } 21 = 6$$

$$66/21 = 3$$

$$1 + 3 \text{ mod } 21 = 4$$

$$4 + 3 \text{ mod } 21 = 7$$