

Type





```
def getCurrency(country: Country): Option[String] =
  country.value match {
    case "United Kingdom" => Some("GBP")
    case "France" | "Germany" => Some("EUR")
    case _ => None
}
```



```
def getCurrency(country): Option [String] =
  country.value match {
    case "United Kingdom" => Some("GBP")
    case "France" | "Germany" => Some("EUR")
    case _ => None
}
```

```
scala> getCurrency(Country("UK"))
res0: Option[String] = None

scala> getCurrency(Country("GBR"))
res1: Option[String] = None

scala> getCurrency(Country("Royaume-Uni"))
res2: Option[String] = None
```



```
import Country._

def getCurrency(country: Country): String =
   country match {
    case UnitedKingdom => "GBP"
     case France | Germany => "EUR"
   }
```

```
def parseCountry(country: String): Option[Country] = ???
```



```
sealed trait Country
object Country {
    case object UnitedKingdom extends Country
    case object France extends Country
    case object Germany extends Country
}

sealed trait Currency
object Currency {
    case object BritishPound extends Currency
    case object Euro extends Currency
}
```

```
import Country._, Currency._

def getCurrency(country: Country): Currency =
   country match {
    case UnitedKingdom => BritishPound
    case France | Germany => Euro
   }
```



#### Plan

- What is the cost of misusing types
- How to use ADTs to encode data
- Learn how to measure impact of types and tests
- Explore relationship between types, algebra and logic



# Exercise 1: Misused types

exercises.types.TypeExercises.scala



# Type should exactly fit business requirements



# Imprecise data lead to errors and misleading documentation



# How should we encode data?



# Algebraic Data Type (ADT)

- OR, a ConfigValue is
  - a String OR
  - o an Int OR
  - Empty
- AND, a User is
  - o an userId AND
  - ∘ a name AND
  - o an address



#### OR

- a Boolean is true OR false
- an Int is a -10 OR 0 OR 1 OR ...
- a DayOfTheWeek is Monday OR Tuesday OR Wednesday OR ...
- an Option is a Some OR a None
- $\bullet$  a Json is a JsonNumber OR a JsonString OR a JsonArray OR a JsonObject OR ...



#### How should we encode OR?

A ConfigValue is a String OR an Int OR Empty



# OR Encoding

```
object ConfigValue {
  case class ConfigString(value: String) extends ConfigValue
  case class ConfigNumber(value: Double) extends ConfigValue
  case object ConfigEmpty extends ConfigValue
}
```



# OR Encoding

```
object ConfigValue {
  case class ConfigString(value: String) extends ConfigValue
  case class ConfigNumber(value: Double) extends ConfigValue
  case object ConfigEmpty extends ConfigValue
}
```

#### In Scala 3

```
enum ConfigValue {
  case ConfigString(value: String)
  case ConfigNumber(value: Double)
  case ConfigEmpty
}
```



#### **AND**

- a User is a userId AND a name AND an address
- a ZonedDateTime is a dateTime AND a timeZone
- a NonEmptyList is a head AND a tail
- a Tuple2 is a \_1 AND a \_2



#### How should we encode AND?

A User is a user Id AND a name AND an address



# **AND Encoding**

```
import java.util.UUID

case class User(userId: UUID, name: String, address: Address)

case class Address(streetNumber: Int, streetName: String, postCode: String)
```

```
scala> User(UUID.randomUUID(), "John Doe", Address(108, "Cannon Street", "EC4N 6EU"))
res3: User = User(6514dfd9-9b99-422d-818a-c23c07468fef, John Doe, Address(108, Cannon Street, EC4N 6EU))
```



# Algebraic data types mix AND and OR

```
object Role {
  case class Reader(accountId: Long, premiumUser: Boolean) extends Role
  case class Editor(accountId: Long, favoriteFont: Option[String]) extends Role
  case object Admin extends Role
}
case class User(userId: Long, role: Role, address: Option[Address])
```



# Exercise 2: Data Encoding

exercises.types.TypeExercises.scala



# Case class and sealed trait map exactly to business language AND and OR

Nested AND and OR form what is called Algebraic Data Types (ADTs)



# ADT allow to encode data precisely



# How can we compare two encodings?

```
def getCurrency(country: String): Option[String]
```

#### Is it better to reduce input or reduce output?

```
def getCurrency(country: Country): String

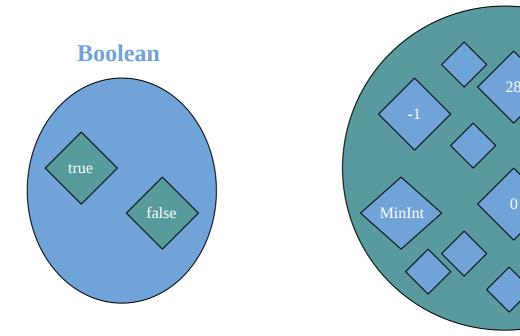
def getCurrency(country: String): Option[Currency]
```

#### How much better it is to reduce both?

```
def getCurrency(country: Country): Currency
```



# Type is a set

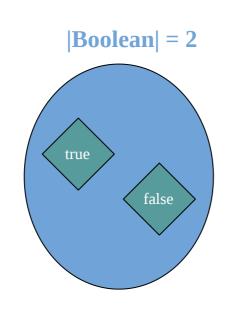


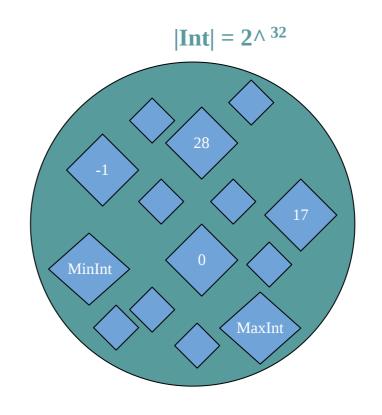
Int

MaxInt



# Cardinality







# Exercise 3: Cardinality

exercises.types.TypeExercises.scala



#### Sealed trait

```
case class AnInt(value: Int) extends IntOrBoolean
case class ABoolean(value: Boolean) extends IntOrBoolean
```

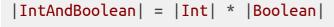
```
AnInt(Int.MinValue) // ~ -2 billion
...
AnInt(0)
AnInt(1)
...
AnInt(Int.MaxValue) // ~ +2 billion
ABoolean(false)
ABoolean(true)
```

```
|IntOrBoolean| = |AnInt| + |ABoolean|
= |Int| + |Boolean|
```



#### Case class

```
case class IntAndBoolean(i: Int, b: Boolean)
IntAndBoolean(Int.MinValue, false) // ~ -2 billion
IntAndBoolean(0, false)
IntAndBoolean(1, false)
IntAndBoolean(Int.MaxValue, false) // ~ +2 billion
IntAndBoolean(Int.MinValue, true) // ~ -2 billion
IntAndBoolean(0, true)
IntAndBoolean(1, true)
IntAndBoolean(Int.MaxValue, true) // ~ +2 billion
```





A sealed trait is called a sum type

A case class is called a product type



$$|A OR B OR C| = |A| + |B| + |C|$$

$$|A AND B AND C| = |A| * |B| * |C|$$

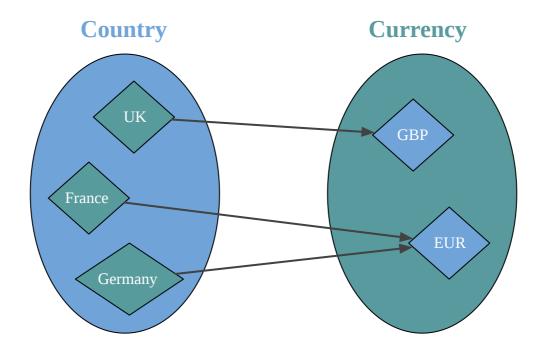


# Finish Exercise 3

exercises.types.TypeExercises.scala

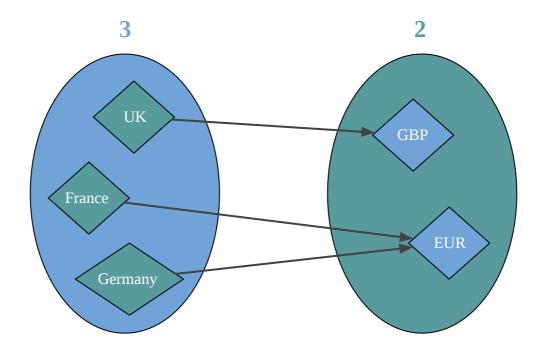


# |Country => Currency |



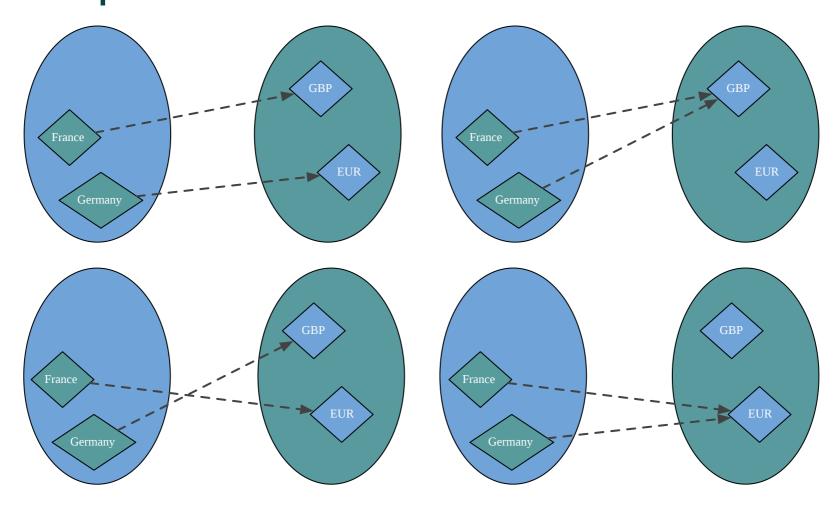


# 3 => 2



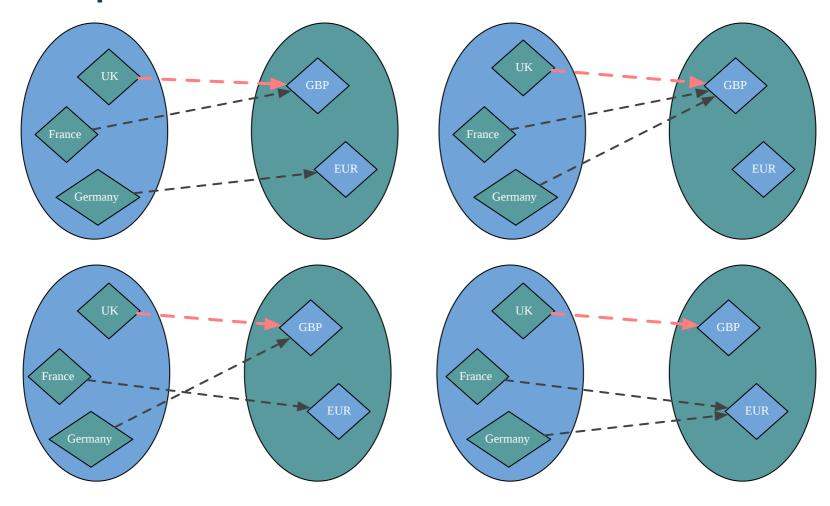


# |2 => 2| = 4





#### 3 => 2



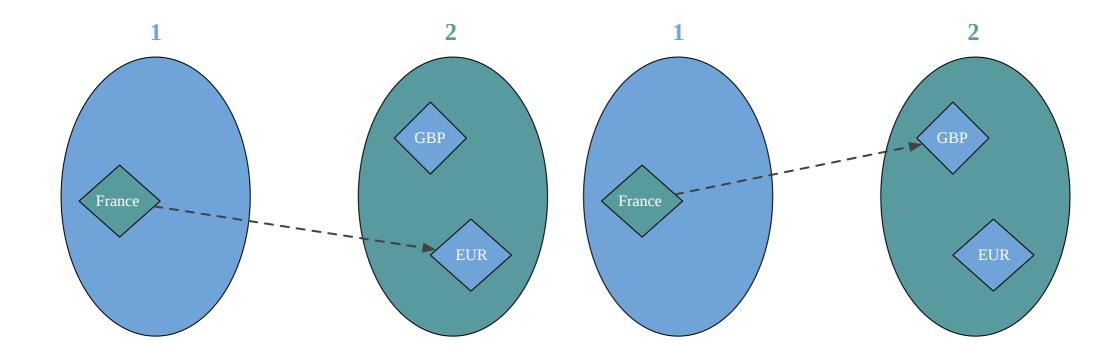








# 1 => 2 = 2









$$|A => B| = |B| ^ |A|$$

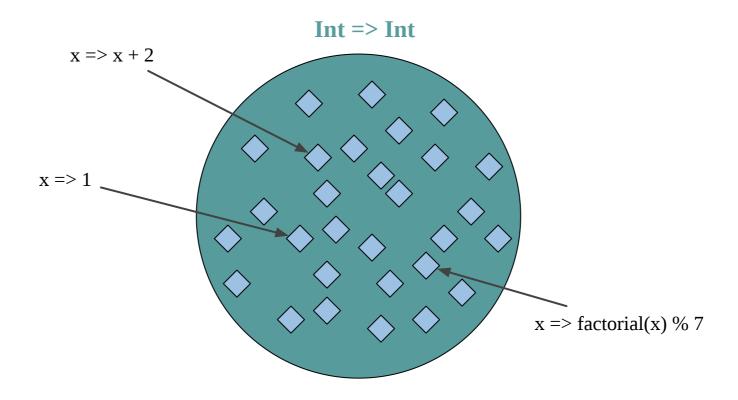


## Exercise 4: Parametricity

exercises.types.TypeExercises.scala

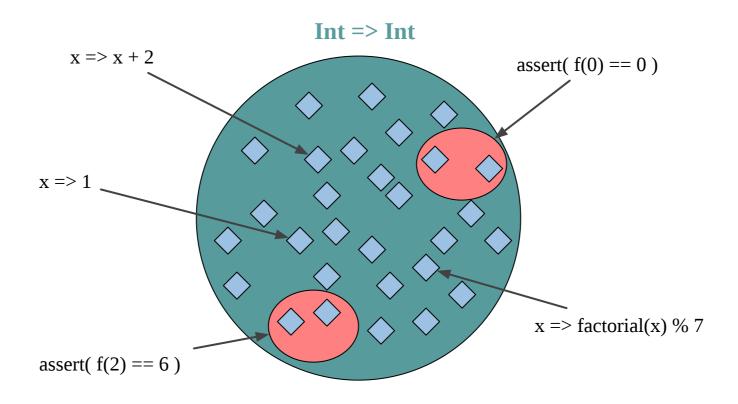


#### Functions are sets!





### Unit tests

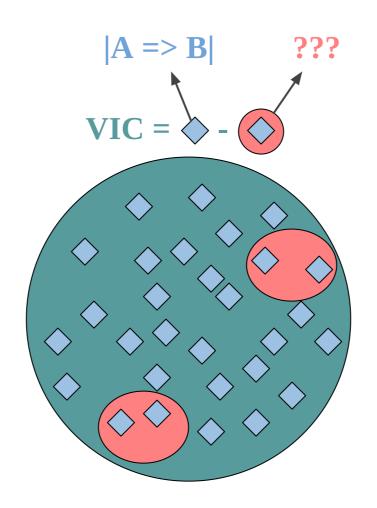




## Valid Implementation Count (VIC)

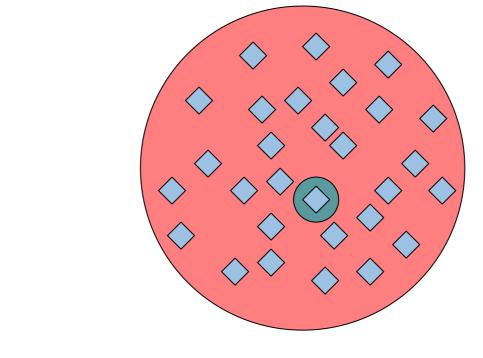








# VIC(f) = 1







## Exercise 5: Tests

exercises.types.TypeExercises.scala



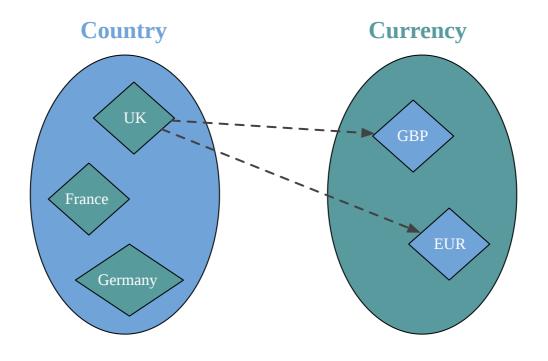
#### **Unit Test**

such as

```
assert(getCurrency(France) == EUR)
```

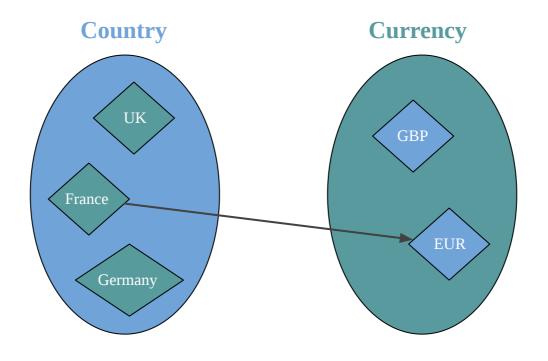


## VIC(getCurrency) = 2 \* ...



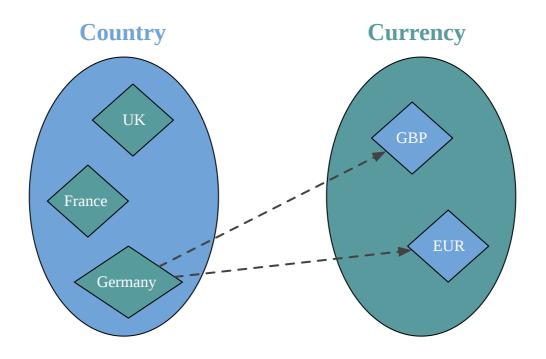


## VIC(getCurrency) = 2 \* 1 \* ...





# VIC(getCurrency) = 2 \* 1 \* 2





$$VIC(f: A => B) = |B| ^ (|A| - n)$$

where n is the number of unit tests



# Exercise 6: Type Algebra

exercises.types.TypeExercises.scala



# Type Algebra

Туре	Algebra	
Nothing	0	
Unit	1	
Either[A, B]	A + B	
(A, B)	A * B	
A => B	B ^ A	
Isomorphism	A == B	



## Curry—Howard isomorphism

**Propositions as types** from Philip Wadler



# Type Algebra Logic

Туре	Algebra	Logic
Nothing	0	$\perp$
Unit	1	Т
Either[A, B]	A + B	АνВ
(A, B)	A * B	АлВ
A => B	B ^ A	A → B
Isomorphism	A == B	A ⇔ B



Either[A, Nothing] == A



Either[A, Nothing] == A

 $A V \perp \Leftrightarrow A$ 



(A, Nothing) == Nothing



(A, Nothing) == Nothing

 $A \land \bot \Leftrightarrow \bot$ 



## Find the representation that makes sense to you

```
Either[Int, String] => Boolean <==> (Int => Boolean, String => Boolean)
```



## Find the representation that makes sense to you

```
Either[A, B] => C <==> (A => C, B => C)
```



#### Find the representation that makes sense to you

```
Either[A, B] => C <==> (A => C, B => C)
```

#### Algebra

#### Logic

```
Either[A, B] => C = (A V B) \rightarrow C
= (A \rightarrow C) \wedge (B \rightarrow C)
= (A => C, B => C)
```



#### Summary

- Cardinality of types matters
- Unit tests offer almost no benefit in term of correctness
- VIC(f: A => B) = |B| ^ (|A| n)
- Two techniques to achieve correctness
  - Property based testing
  - Parametric polymorphism



All dynamic languages are static languages with a single type



## Any



## Any => Any

```
def inc(value: Any): Any = value match {
  case x: Int => x + 1
  case x: Double => x + 1
  case x: Char => x.toString + "1"
  case x: String => x + "1"
}
```



## Any => Any

```
def inc(value: Any): Any = value match {
   case x: Int => x + 1
   case x: Double => x + 1
   case x: Char => x.toString + "1"
   case x: String => x + "1"
}
```

```
scala> inc(5)
res4: Any = 6

scala> inc(10.3)
res5: Any = 11.3

scala> inc('c')
res6: Any = c1
```

```
scala> inc(java.time.Instant.ofEpochMilli(0))
scala.MatchError: 1970-01-01T00:00:00Z (of class java.time.Instant)
  at .inc(<console>:2)
  ... 42 elided
```



$$VIC(Any => Any) = |Any| \sim (|Any| - n)$$

where n is the number of unit tests



## Resources and further study

- <u>Programming with Algebra</u>: property based testing with storage
- Much Ado About Testing: property based testing best practices and pitfalls
- Choosing properties for property-based testing
- Property-Based Testing in a Screencast Editor
- Property-Based Testing The Ugly Parts: Case Studies from Komposition
- <u>Types vs Tests</u>
- Counting type inhabitants
- Thinking with types: type, algebra, logic
- <u>Propositions as types</u>: Curry–Howard isomorphism



# **Conclusion**

