

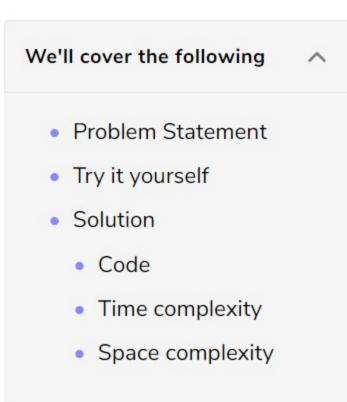
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Grokking the Coding Interview: Patterns for Coding Questions

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Find the Median of a Number Stream (medium)



Problem Statement

Design a class to calculate the median of a number stream. The class should have the following two methods:

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- 1. insertNum(int num): stores the number in the class
- 2. findMedian(): returns the median of all numbers inserted in the class

If the count of numbers inserted in the class is even, the median will be the average of the middle two numbers.

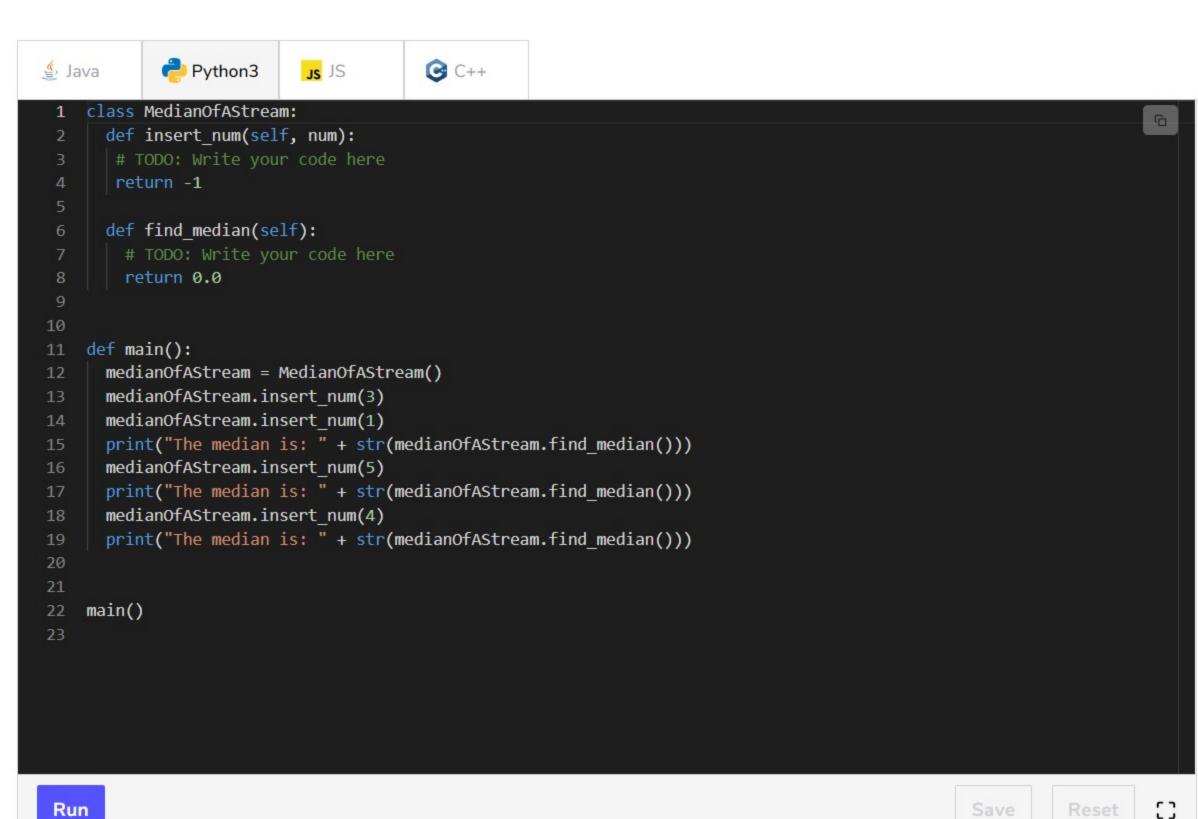
Example 1:

```
    insertNum(3)

2. insertNum(1)
3. findMedian() -> output: 2
4. insertNum(5)
5. findMedian() -> output: 3
6. insertNum(4)
7. findMedian() -> output: 3.5
```

Try it yourself

Try solving this question here:



Solution

As we know, the median is the middle value in an ordered integer list. So a brute force solution could be to maintain a sorted list of all numbers inserted in the class so that we can efficiently return the median whenever required. Inserting a number in a sorted list will take O(N) time if there are 'N' numbers in the list. This insertion will be similar to the Insertion sort. Can we do better than this? Can we utilize the fact that we don't need the fully sorted list - we are only interested in finding the middle element?

Assume 'x' is the median of a list. This means that half of the numbers in the list will be smaller than (or equal to) 'x' and half will be greater than (or equal to) 'x'. This leads us to an approach where we can divide the list into two halves: one half to store all the smaller numbers (let's call it smallNumList) and one half to store the larger numbers (let's call it largNumList). The median of all the numbers will either be the largest number in the smallNumList or the smallest number in the largNumList. If the total number of elements is even, the median will be the average of these two numbers.

The best data structure that comes to mind to find the smallest or largest number among a list of numbers is a Heap. Let's see how we can use a heap to find a better algorithm.

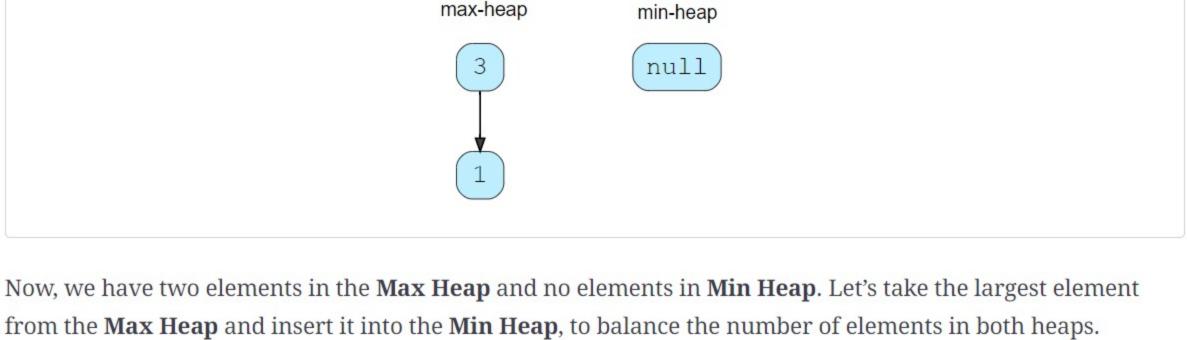
- 1. We can store the first half of numbers (i.e., smallNumList) in a Max Heap. We should use a Max Heap as we are interested in knowing the largest number in the first half.
- 2. We can store the second half of numbers (i.e., largeNumList) in a Min Heap, as we are interested in knowing the smallest number in the second half.
- 3. Inserting a number in a heap will take O(log N), which is better than the brute force approach.
- 4. At any time, the median of the current list of numbers can be calculated from the top element of the two heaps.

1. insertNum(3): We can insert a number in the Max Heap (i.e. first half) if the number is smaller than the

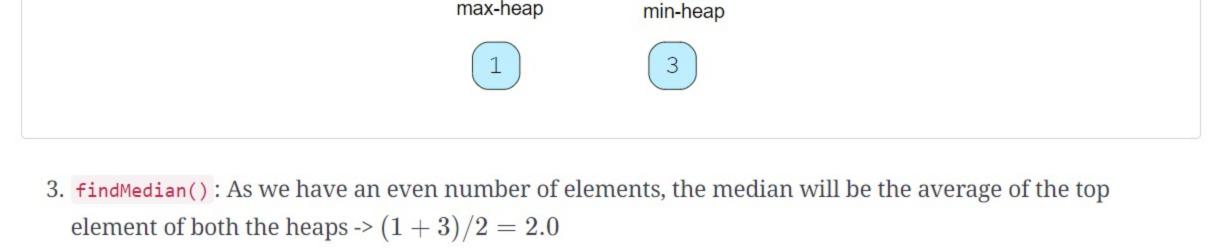
Let's take the Example-1 mentioned above to go through each step of our algorithm:

top (largest) number of the heap. After every insertion, we will balance the number of elements in both heaps, so that they have an equal number of elements. If the count of numbers is odd, let's decide to have more numbers in max-heap than the Min Heap.



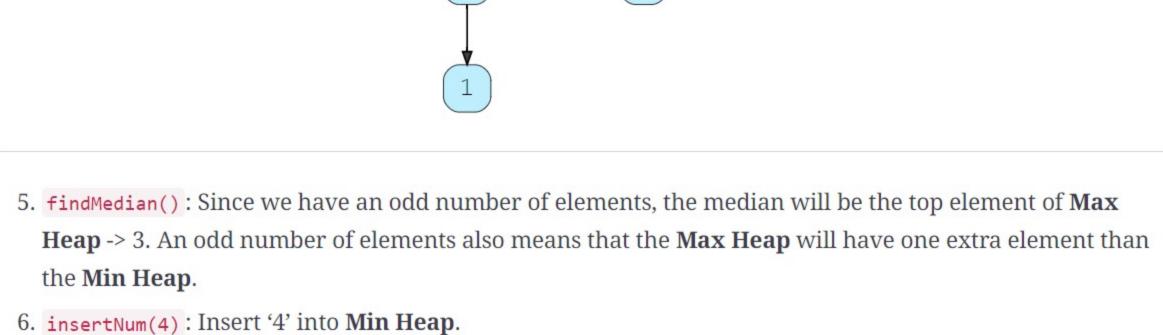


max-heap

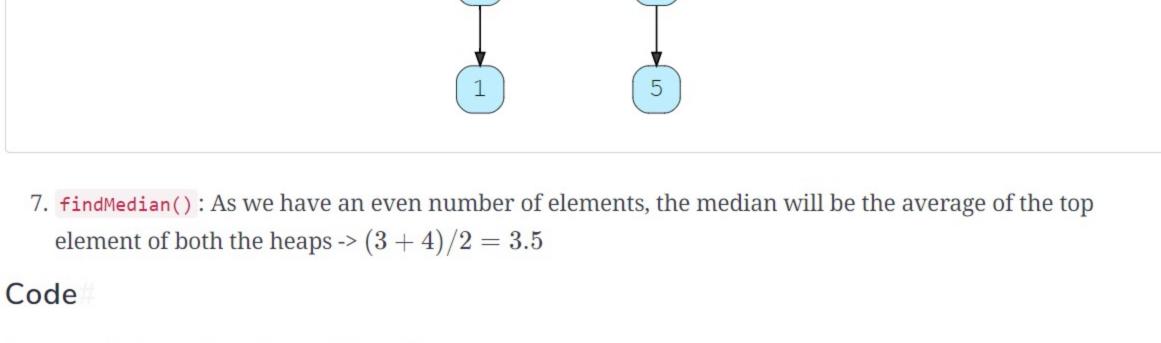


4. insertNum(5): As '5' is greater than the top element of the Max Heap, we can insert it into the Min Heap.

- After the insertion, the total count of elements will be odd. As we had decided to have more numbers in the Max Heap than the Min Heap, we can take the top (smallest) number from the Min Heap and insert
- it into the Max Heap. max-heap min-heap



max-heap min-heap



class MedianOfAStream: maxHeap = [] # containing first half of numbers minHeap = [] # containing second half of numbers def insert_num(self, num): if not self.maxHeap or -self.maxHeap[0] >= num: 10 heappush(self.maxHeap, -num) 11 12 else: heappush(self.minHeap, num) 13 14 15 # either both the heaps will have equal number of elements or max-heap will have one # more element than the min-heap if len(self.maxHeap) > len(self.minHeap) + 1: 17 heappush(self.minHeap, -heappop(self.maxHeap)) elif len(self.maxHeap) < len(self.minHeap):</pre> heappush(self.maxHeap, -heappop(self.minHeap)) 21 def find_median(self): 22 if len(self.maxHeap) == len(self.minHeap): # we have even number of elements, take the average of middle two elements 24 return -self.maxHeap[0] / 2.0 + self.minHeap[0] / 2.0 25 # because max-heap will have one more element than the min-heap 27 return -self.maxHeap[0] / 1.0 29 30 31 def main(): Run Save Reset

Time complexity The time complexity of the insertNum() will be O(logN) due to the insertion in the heap. The time

complexity of the findMedian() will be O(1) as we can find the median from the top elements of the heaps.

The space complexity will be O(N) because, as at any time, we will be storing all the numbers.

Space complexity

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Introduction

Here is what our algorithm will look like:

G C++

JS JS

Python3

from heapq import *

Java

```
Sliding Window Median (hard)
               ✓ Mark as Completed
Propert an Issue Ask a Question
```

Next ->