$$\left[\frac{-\hbar^2}{2m}\nabla_{\mathbf{r}}^2 + v_{\text{ext}}(\mathbf{r}) + v_{\text{ee}}(\mathbf{r})\right]\phi_i(\mathbf{r}) = \epsilon_i\phi_i(\mathbf{r})$$