# Sequential Circuits

#### 1 Circuits

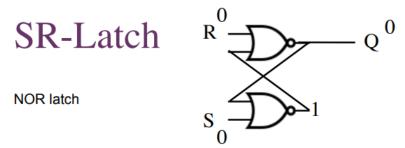
So far we have looked at **combinational circuits**: output depends only on current input (after propagation delay).

Now we consider sequential circuits.

- Output depends on history as well as current input
- I.e. the circuit has memory.
- Can be modelled as finite-state machines.
- In general hard to analyse.
- Fundamental components: latches and flip-flops, each store 1-bit.

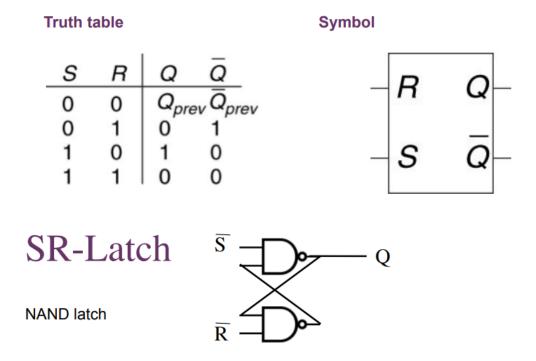
We will consider **synchronous** sequential circuits made from combinational components interleaved with banks of flip-flops containing the state of the circuit.

#### 2 SR Latch



- Both inputs 'usually' set to 0.
- If input S (set) has a pulse of 1, the output becomes 1.
- The output remains 1 even when the pulse is over.
- If input R (reset) has a pulse of 1, the output becomes 0.
- The output remains 0 even when the pulse is over.
- If the output is already 1, a pulse on S will not change it. If it is already 0, a
  pulse on R will not change it.
- Latches can be used to store a single bit of memory.

This circuit has two stable states for a given input – it is called bistable.

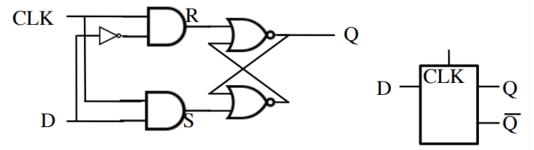


- Latches can also be built from NAND gates.
- In this case the 'usual' state for the inputs is 1, so the inputs are denoted with bars.
- Exercise: work out how the NAND latch behaves.

### 3 D Latch

In a latch a pulse on set or reset indicates what the new state should be, and when it should change (now!).

Designing circuits becomes easier if we can separate what and when.



D – data input. Defines what the new value should be.

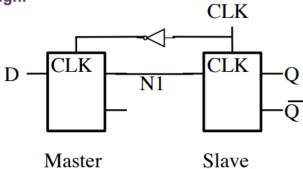
CLK – clock input. Define when the new value should arise.

• The output will be updated to whatever the data is whenever the clock gives a pulse

## 4 D Flip Flop

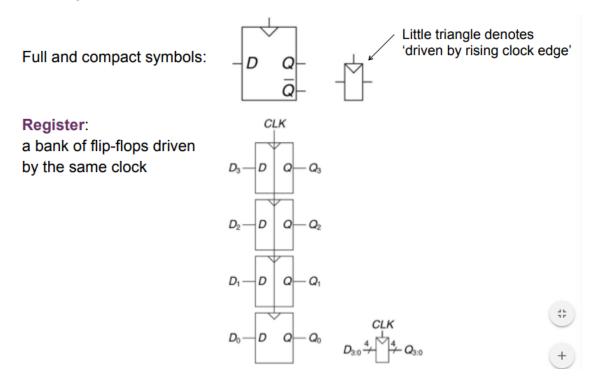
In the D-latch the output can change whenever the clock is high.

Even better is if we can make it change only at the moment the clock goes high.



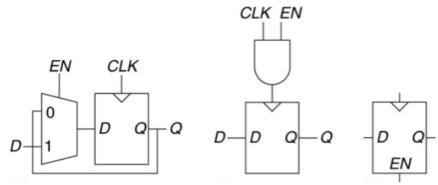
D flip-flop copies D to Q on the rising edge of the clock, and remembers its state at all other times.

• Whenever the clock is low, the data will transmit through the master, when the clock is high, the data will not transmit through the master



## 5 Enabled Flip Flop

Incorporates an additional input (enable) to control whether the data is loaded into the register or not.



EN can control the input with a multiplexor, or can control the clock. This is called a **gated clock**.

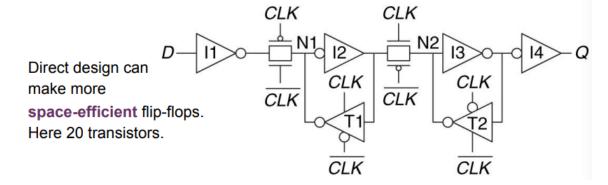
Gated clocks can cause timing errors and glitches on the clock.

• Therefore the 1st diagram is the best one to use as by using the end gate, timing errors can be included

## 6 Flip Flop Design

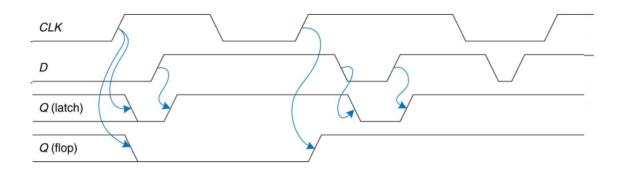
How many transistors are needed to build the D flip-flop?

- A NAND or NOR gate uses four transistors.
- A NOT gate uses two transistors.
- An AND gate is built from a NAND and a NOT, so it uses six transistors.
- The SR latch uses two NOR gates, or eight transistors.
- The D latch uses an SR latch, two AND gates, and a NOT gate, or 22 transistors.
- The D flip-flop uses two D latches and a NOT gate, or 46 transistors.

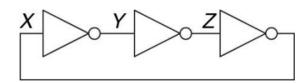


## 7 Example

How would a latch and flip-flop behave in the following setting?



### **8 Problem Circuits**



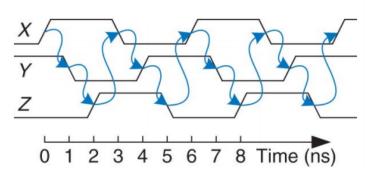
The gates have a delay of 1ns.

How does this circuit behave?

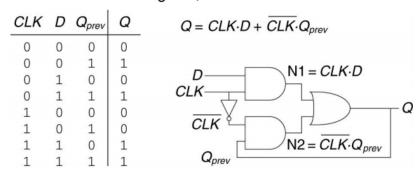
Suppose X=0, then Y=1 and Z=0, and so X=1!

X rises to 1, at 1ns Y falls, at 2ns Z rises and at 3ns X falls...

An unstable or astable circuit.



An improved D latch? Fewer gates, so fewer transistors!



Leads to **race conditions** – behaviour depends on which of two routes through the circuits carries signal the fastest.

Logically identical circuits may exhibit different behaviour depending on technicalities of the gate construction, or may exhibit odd behaviour at certain temperatures...

The problems are caused by outputs being fed back into inputs: the circuits contain **loops** or **cyclic paths**.

To avoid this we insert **registers** into cyclic paths:

- · the registers contain the 'state' of the circuit
- · they break the paths
- · they only update on a clock edge
- · say they are synchronised to the clock

If the clock is **sufficiently slow**, so that all inputs to all the registers have settled before the next clock edge, then race conditions cannot arise.

### 9 Synchronous Circuits

A synchronous sequential circuit consists of interconnected elements such that:

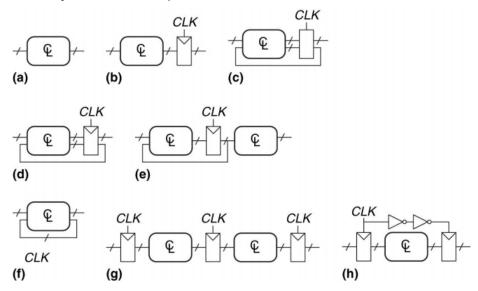
- Every circuit element is either a register or a combinational circuit
- At least one circuit element is a register
- All registers receive the same clock signal
- Every cyclic path contains at least one register.

#### A synchronous sequential circuit has:

- A discrete set of states {S<sub>0</sub>,...,S<sub>k-1</sub>}
- · A clock input, whose rising edge indicates when a state change occurs
- A functional specification which details the next state and all outputs for each possible current state and set of inputs.

## 10 Examples

Which are synchronous sequential circuits?



b,d,e,g,

## 11 Timing

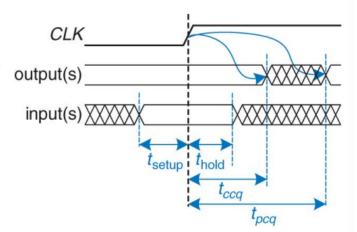
The **dynamic discipline** restricts us to using circuits satisfying timing constraints that allow us to combine components.

 t<sub>setup</sub> – time before rising edge during which inputs must be stable

t<sub>hold</sub> – time after rising edge during which inputs must be stable

t<sub>ccq</sub> – time until output starts to change

t<sub>pcq</sub> – time by which output has stabilized

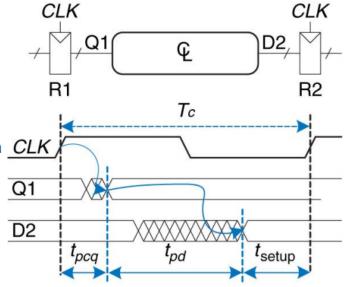


With these constraints we can think of signals as discrete in time as well as logic.

- ccq contamination clock to q
- pcq propagation clock to q

## 12 Setting Time

- The clock frequency determines how fast the computer operates.
- Register 2 will not get an answer until the clock ticks a second time.
- 30 years ago 1MHz was a <u>CLK</u> fast computer now several GHz is common.
- 'Overclocking' is setting the clock cycle fast than the manufacturers recommend.



Time between ticks ( $T_c$ ) must be at least  $t_{pcq}+t_{pd}+t_{setup}$ 

Rearranging we see that  $t_{pd} < T_c - (t_{pcq} + t_{setup})$ ( $t_{pcq} + t_{setup}$ ) is called the **sequencing overhead**.

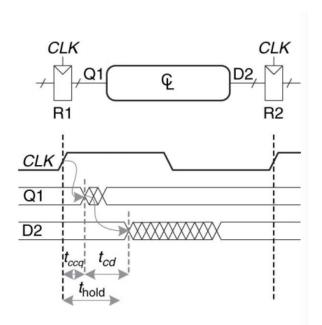
The clock speed and sequencing overhead are normally fixed and the designer must work with them.

Designers must get all elements of combinational logic to work within the bound on  $t_{\rm pd}$  in order for the circuit to be reliable.

There is also a minimum delay requirement:

- D2 must hold its value for at least t<sub>hold</sub> time after the rising edge.
- It could change as soon as t<sub>ccq</sub> + t<sub>cd</sub>.
- Designers have a min-delay constraint: t<sub>cd</sub> > t<sub>hold</sub>-t<sub>ccq</sub>.
- Often, in order to allow direct connection of flip-flops, t<sub>hold</sub> < t<sub>ccq</sub>.





## 13 Example

Flip-flops:

$$t_{ccq} = 30 \text{ ps}$$

$$t_{pcq}$$
 = 80 ps

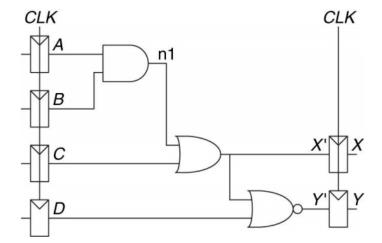
$$t_{\text{setup}} = 50 \text{ ps}$$

$$t_{hold} = 60 ps$$

Gates:

$$t_{cd} = 25 \text{ ps}$$

$$t_{pd} = 40 \text{ ps}$$



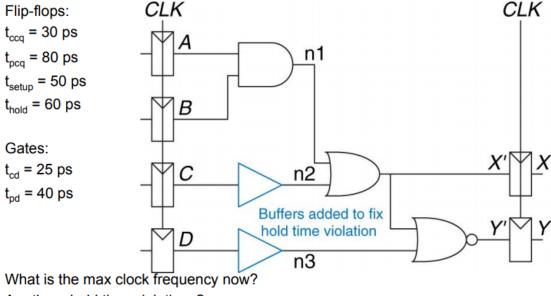
What is the max clock frequency? Are there hold time violations?

- Critical path goes through all 3 gates
  - $CL_{pd} = 120ps$

- $T_c \ge 80 + 120 + 50 = 250ps$
- 1/250ps = 4GHz

There would be a hold time violation

## 14 Fixing the hold time violation



Are there hold time violations?

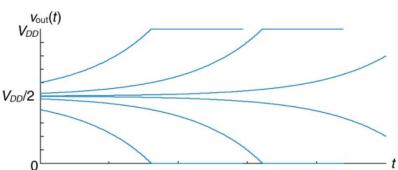
#### 15 Metastable States

Suppose the input D to a flip-flop is connected to a button

If D is unpressed or pressed when the clock rises, Q will be set to a stable state.

If D is in the process of being pressed just when the clock rises, Q may be set to a **metastable** state.

The state will be driven to 1 or 0 eventually, but it may take time.



metastable

stable

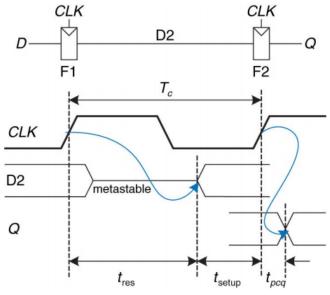
stable

## 16 Synchronisers

A pair of flip-flops can be used to synchronise the input with the clock.

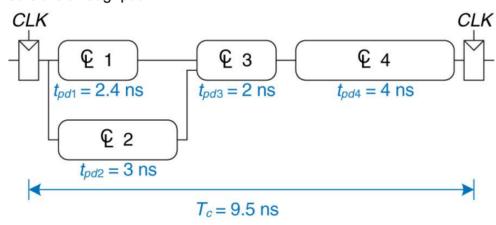
The value of D2 may be indeterminate if D is not synchronised.

If the resolution time of F1 is small enough compared to the clock rate, Q will be synchronised.

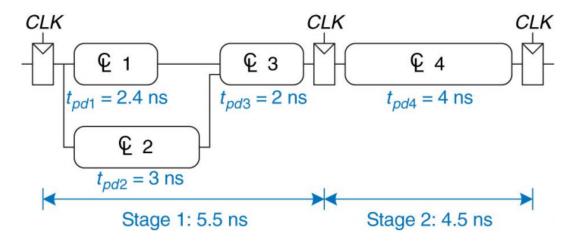


## 17 Pipelining

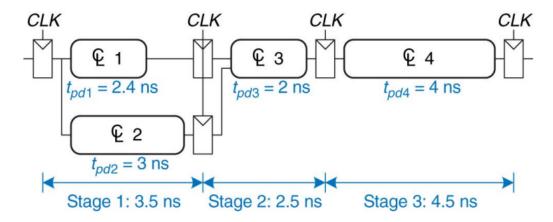
What is the maximum clock rate of this circuit? What is the throughput?



Insert an additional register in the circuit.



Insert another register in the circuit.



• Doing this gives higher latency, but greater throughput