

We have

$$\frac{1}{n} \xrightarrow{n \rightarrow \infty} 0.$$

We also know, that

$$\begin{aligned} M &= \sum_{k=0}^{\infty} q^k = 1 + q + q^2 + q^3 + q^4 + \dots \\ &= 1 + q(1 + q + q^2 + q^3 + \dots) \\ &\stackrel{\text{Def.}}{=}_{\text{of } M} 1 + q \cdot M \end{aligned}$$

In contrary to

$$\begin{aligned} M &= \sum_{k=0}^{\infty} q^k = 1 + q + q^2 + q^3 + q^4 + \dots \\ &= 1 + q(1 + q + q^2 + q^3 + \dots) \\ &\stackrel{\text{Def.}}{=}_{\text{of } M} 1 + q \cdot M \end{aligned}$$

Note, that the `limit` function is used and that as such it become quite unreadable if used inside subscripts, etc.:

$$\underbrace{\frac{n-1}{n^2}}_{\xrightarrow{n \rightarrow \infty} 0} \cdot n = \frac{n-1}{n} = 1 - \frac{1}{n} \xrightarrow{n \rightarrow \infty} 1$$

However, we can also write small fractions quite nicely,  $\frac{1}{2}$ , or have something like this:  $2, \lim_n^n$  and  $\frac{1}{2}$ .