

PONTIFICIA UNIVERSIDAD CATÓLICA DEL PERÚ  
FACULTAD DE CIENCIAS E INGENIERÍA

Algoritmia  
Laboratorio 5  
2014-1

Aplicación de los TDA

1.- (14 puntos) Emplee una pila para eliminar la recursión de las siguientes rutinas:

a) (7 puntos)

```
function comb (n, m : integer): integer;  
  {calcula  $\binom{n}{m}$  suponiendo que  $0 \leq m \leq n$  y  $n \geq 1$ }  
  begin  
    if (n = 1) or (m = 0) or (m = n) then  
      return (1)  
    else  
      return (comb (n - 1, m) + comb(n - 1, m - 1))  
    end; {comb}
```

b) (7 puntos)

```
Algoritmo Torres de Hanoi  
Rutina Principal  
Inicio  
  Anillos ← Pide la cantidad de anillos a mover  
  Mueve(Anillos, origen, intermedio, destino)  
Fin  
  
Rutina Mueve (a, o, i, d)  
Inicio  
  Si a = 1  
    Entonces Muestra o "--->" d  
    En otro caso Mueve(a-1, o, d, i)  
    Muestra o "--->" d  
    Mueve(a-1, i, o, d)  
  Fin Si  
Fin
```

2.- (6 puntos)

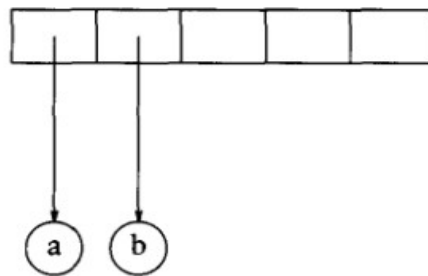
### Constructing an Expression Tree

We now give an algorithm to convert a postfix expression into an expression tree. Since we already have an algorithm to convert infix to postfix, we can generate expression trees from the two common types of input. The method we describe strongly resembles the postfix evaluation algorithm of Section 3.2.3. We read our expression one symbol at a time. If the symbol is an operand, we create a one-node tree and push a pointer to it onto a stack. If the symbol is an operator, we pop pointers to two trees  $T_1$  and  $T_2$  from the stack ( $T_1$  is popped first) and form a new tree whose root is the operator and whose left and right children point to  $T_2$  and  $T_1$  respectively. A pointer to this new tree is then pushed onto the stack.

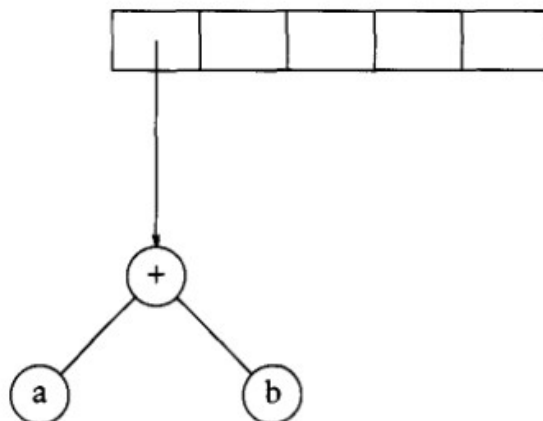
As an example, suppose the input is

$a\ b\ +\ c\ d\ e\ +\ * \ *$

The first two symbols are operands, so we create one-node trees and push pointers to them onto a stack.<sup>†</sup>



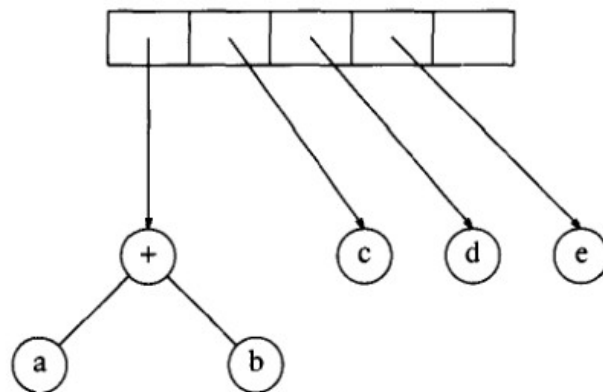
Next, a '+' is read, so two pointers to trees are popped, a new tree is formed, and a pointer to it is pushed onto the stack.



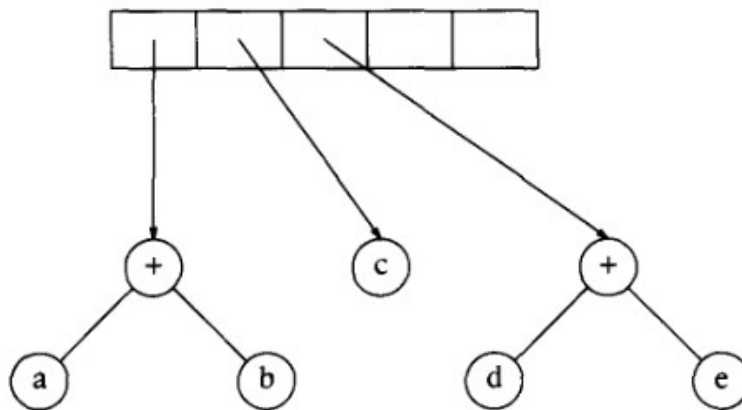
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<sup>†</sup>For convenience, we will have the stack grow from left to right in the diagrams.

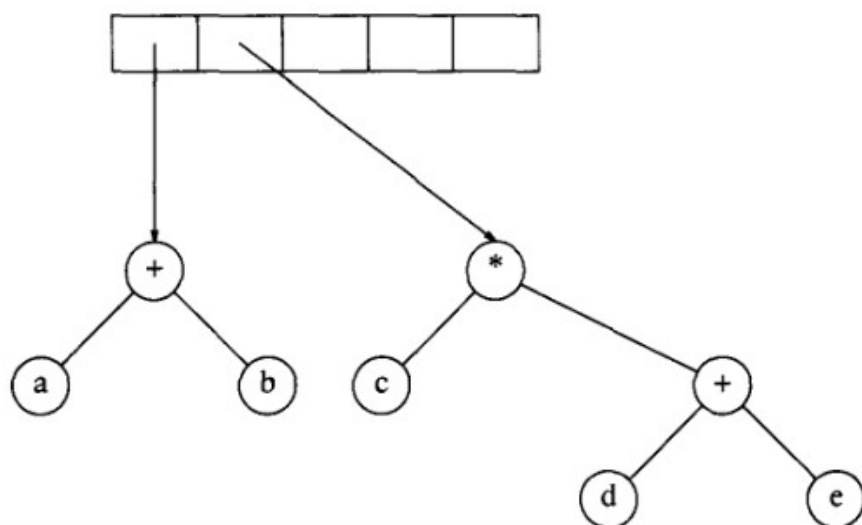
Next,  $c$ ,  $d$ , and  $e$  are read, and for each a one-node tree is created and a pointer to the corresponding tree is pushed onto the stack.



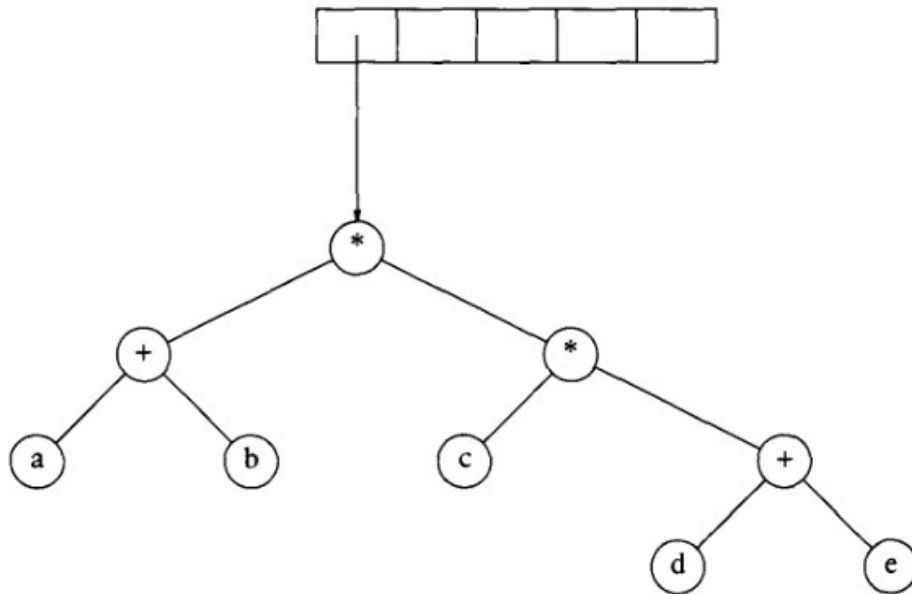
Now a '+' is read, so two trees are merged.



Continuing, a '\*' is read, so we pop two tree pointers and form a new tree with a '\*' as root.



Finally, the last symbol is read, two trees are merged, and a pointer to the final tree is left on the stack.



Implemente este algoritmo, siguiendo las indicaciones dadas por el autor.

Pando, 10 de junio del 2014

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