Data

Model: Logistic Regression

Reculte

Conclusions

Future

Tulips - Nonlinear Logistic Regression

Arthur Lui

Department of Statistics Brigham Young University

November 13, 2014

Model: Logistic Regressio

.

Conclusion

Future

Introduction



Result

Conclusion

Future

Tulip Germination Experiment

 Goal: Understand the effect of chilling time on germination of tulip bulbs.

Data:

- 12 populations each with 210 tulips (2005-2009)
- Each population randomly and evenly split into 7 groups and assigned to one of 7 chilling times (0, 2, 4, ..., 12 weeks).
- Response Variable: Indicator (bulb germinated or not).
- Population 12 did not germinate at all, so it was removed from the analysis.

Model: Logistic Regression

Data

Results

Conclusion

Entire

Research Questions

- Is the effect of chilling time the same across all Populations?
 Which populations are the same / different?
- Is there an "ideal" chilling time?
 Does this ideal chilling time vary by population?
- What effect will a decrease from 10 to 8 weeks of chilling time have for tulips?

Future

Germination Rates

	0	2	4	6	8	10	12
1	0.40	0.97	0.83	0.87	0.87	0.97	0.90
2	0.13	0.53	0.73	0.73	0.83	0.90	0.83
3	0.00	0.53	0.80	0.83	0.97	0.90	0.87
4	0.00	0.17	0.53	0.60	0.73	0.90	0.73
5	0.33	0.87	0.67	0.73	0.70	0.57	0.50
6	0.00	0.03	0.07	0.40	0.43	0.80	0.67
7	0.00	0.00	0.10	0.33	0.47	0.83	0.67
8	0.00	0.03	0.27	0.33	0.33	0.30	0.30
9	0.00	0.00	0.00	0.00	0.07	0.60	0.60
10	0.00	0.17	0.10	0.53	0.87	0.87	0.83
11	0.00	0.00	0.20	0.23	0.67	0.83	0.47

Tulips -Nonlinear Logistic Regression

Arthur Lui

Introduction

IIItroductio

Model: Logistic Regression

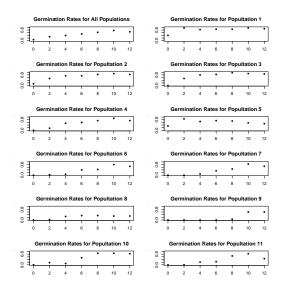
Data

Danilla

Conclusions

Future

Germination Rates



and the second

Data

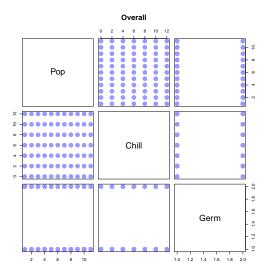
Model: Logistic Regressio

_ .

Conclusion

Euturo

Germination Rates



Model: Logistic Regression Model

Results

Conclusion

Logistic Regression Model (Linear)

$$Y_i \stackrel{ind}{\sim} \mathsf{Bernoulli}(p_i)$$
 $log\left(rac{p_i}{1-p_i}
ight) = \mathbf{x}_i'eta$
 $\Rightarrow p_i = rac{e^{\mathbf{x}_i'eta}}{1+e^{\mathbf{x}_i'eta}}$

where
$$p_i = P(Y_i = 1)$$

Model: Logistic Regression Model

Danilla

Conclusion

F.

Logistic Regression Model (Nonlinear)

$$Y_i \stackrel{ind}{\sim} \mathsf{Bernoulli}(p_i)$$
 $log\left(\frac{p_i}{1-p_i}\right) = (ns(\mathbf{x}_i))'\beta$

$$\Rightarrow p_i = \frac{e^{\mathsf{ns}(\mathbf{x}_i)'\beta}}{1+e^{\mathsf{ns}(\mathbf{x}_i)'\beta}}$$

where
$$p_i = P(Y_i = 1)$$

Introduction

Model: Logistic Regression Model

Docul+

Conclusion

e .

- + Model is flexible
 - Number of knots needs to be predetermined

Tulips -Nonlinear Logistic Regression

Arthur Lui

Introduction

.....

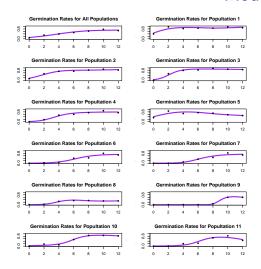
Model: Logistic Regression

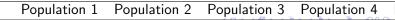
Results

Conclusions

Future

Model





Effect of Chilling Time

Models to compare for every pair of populations:

$$\log\left(\frac{p_i}{1-p_i}\right) = \beta_0 + pop_i\beta_1 + ns(chill_i)\beta_2 + pop_ins(chill_i)\beta_3$$

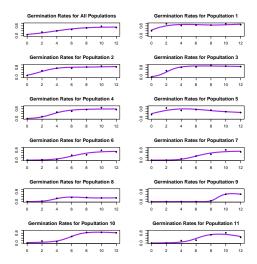
$$\log\left(\frac{p_i}{1-p_i}\right) = \beta_0 + ns(chill_i)\beta_2$$

Tulips -Nonlinear Logistic Regression

Arthur Lui

Results

Effect of Chilling Time



Populations that respond similarly to chilling time: (3,2), (4,2), (10,4), (7,6), (10,6), (11,6), (10,7), (11,7),

Introduction

Model: Logistic Regressio

Results

Conclusions

Futur

Ideal Chilling Time

	Estimate	95% Lower.CI	95% Upper.CI
Population 1	9.15	2.41	15.90
Population 2	10.21	5.96	14.45
Population 3	8.15	3.28	13.02
Population 4	10.60	7.27	13.94
Population 5	4.73	2.80	6.67
Population 6	11.27	9.02	13.51
Population 7	11.30	9.37	13.24
Population 8	7.41	2.34	12.48
Population 9	10.94	9.71	12.16
Population 10	10.11	8.17	12.06
Population 11	9.23	8.12	10.34
All Populations	11.44	9.71	13.16

1000

D . . .

Model: Logistic Regressio Model

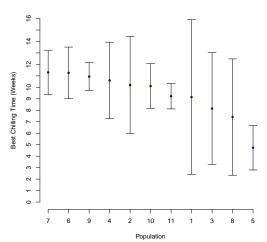
Results

Conclusions

Future

Ideal Chilling Time

Best Chilling Times



Introduction

Model: Logistic

Results

Conclusions

Future

Effect of Decrease in Chilling Time from 10 to 8 Weeks

Estimate	95% CI.Lo	95% CI.Hi
-0.02	-0.11	0.06
-0.02	-0.10	0.05
0.01	-0.05	0.06
-0.02	-0.09	0.05
0.08	0.00	0.16
-0.11	-0.20	-0.01
-0.10	-0.21	0.00
0.03	-0.05	0.10
-0.54	-0.72	-0.35
-0.05	-0.11	0.02
-0.02	-0.09	0.05
-0.04	-0.07	-0.02
	-0.02 -0.02 0.01 -0.02 0.08 -0.11 -0.10 0.03 -0.54 -0.05 -0.02	-0.02 -0.11 -0.02 -0.10 0.01 -0.05 -0.02 -0.09 0.08 0.00 -0.11 -0.20 -0.10 -0.21 0.03 -0.05 -0.54 -0.72 -0.05 -0.11 -0.02 -0.09

Model: Logistic Regressic

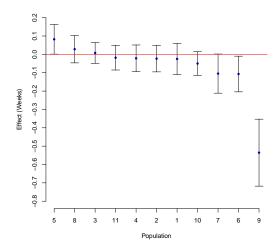
Results

Conclusions

Future

Effect of Decrease in Chilling Time from 10 to 8 Weeks

Effect of Decrease in Chilling Time from 10 to 8 Weeks



Results

Conclusions

Futur

Conclusions

- Populations: (3,2), (4,2), (10,4), (7,6), (10,6), (11,6), (10,7), (11,7), (11,10) are the same.
- Ideal Chilling Time: 11.5 (9.908898, 13.097589)
- Effect of Chilling Time Decrease on Germination Rates: -0.041 (-0.066 -0.017)

......

Dat

Model: Logistic Regression Model

December

Conclusion

Future

• Try Smoothing Splines

and the second

Data

Model: Logistic Regression Model

Danilla

Conclusion

Future

Thanks for the great semester!