

SLICE SAMPLING

PDF recognizable
(sampleable)
↓
not

likelihood

$$p(x) \propto \underbrace{f(x)}_{\text{latent}} g(x)$$

e.g. $\{f(x) = \text{prior}; g(x) = \prod_{i=1}^N \ell_i(x)\}$

Introduce ~~latent~~ variable u
s.t. $u|x \sim \text{Unif}(0, g(x))$

invertible

$$p(u|x) = \frac{1}{g(x)} \mathbb{1}(u < g(x))$$

$$\begin{aligned} \Rightarrow p(u, x) &= p(x)p(u|x) \\ &= f(x)g(x)/g(x) \\ &= f(x) \mathbb{1}(u < g(x)) \end{aligned}$$

→ Full conditionals

② $p(x|u) \propto f(x) \cdot \mathbb{1}(u < g(x)) \sim \text{Truncated } f(x)$

① $p(u|x) = \frac{1}{g(x)} \mathbb{1}(u < g(x)) \sim \text{Unif}(0, g(x))$

Gibbs sample and discard
draws of u

$$\mathbb{1}(x)$$

$$\text{unif}(a, b) \quad a < \beta < \max(b, \max(a))$$

$$a < \beta < b$$

$$\text{unif}(a, b)$$

$$a < \beta < \max(b, \max(a))$$

$$x \quad g^{-1}(u)$$