



















# Impulse response function $H(\mathbf{x}_l, \mathbf{x}_s, t)$

$\times$   $S$  SPAD positions  $\mathbf{x}_S$

## Transport at wall

Transport at wall

0 ns

time ( $T$  bins)

40 ns





# Transport at wall



## PROBLEM: Spatial ambiguities

## PROBLEM: Spatial ambiguities

$$J(\mathbf{x}_v) = \iint_{S \setminus L} \textcolor{red}{I}(\mathbf{x}_l, \mathbf{x}_s, \nu_{lv} + \nu_{sv}) d\mathbf{x}_l d\mathbf{x}_s$$

$$\xrightarrow{H' = H * K}$$

$$f(\mathbf{x}_v) = \iint_S L H'(\mathbf{x}_l, \mathbf{x}_s, t_{lv} + t_{sv}) d\mathbf{x}_l d\mathbf{x}_s$$

Hidden scene

Reconstructed image

Hidden scene

Reconstructed image



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Hidden scene

Reconstructed image

Hidden scene

Reconstructed image



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# All scene points contribute to all sensor pixels

# All scene points contribute to all sensor pixels

# All scene points contribute to all sensor pixels

Lenses map “bundles” of rays from points on the scene to the sensor.





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# Resemble lens propagation operators



# Propagate complex waves instead of scalar radiance

SPAD



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45

**Propagate complex  
waves instead of scalar radiance**

SPAD

Defined by classic optics models

- Leverage LOS imaging methods



$$H(\mathbf{x}_l, \mathbf{x}_s, t)$$



$$H(\mathbf{x}_l, \mathbf{x}_s, t)$$



$$H(\mathbf{x}_l, \mathbf{x}_s, t)$$



$$H(\mathbf{x}_l, \mathbf{x}_s, t)$$



$$H(\mathbf{x}_l, \mathbf{x}_s, t)$$

# VIRTUAL WAVE PROPAGATION



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# VIRTUAL WAVE PROPAGATION



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Re



Time

# VIRTUAL WAVE PROPAGATION



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Re



Time

# VIRTUAL WAVE PROPAGATION MODELS



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# VIRTUAL WAVE PROPAGATION



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# VIRTUAL WAVE PROPAGATION



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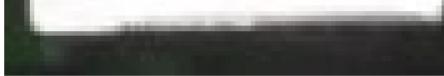
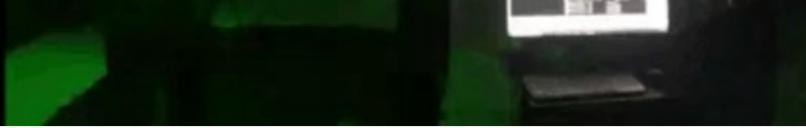


$$\int \int_S L$$

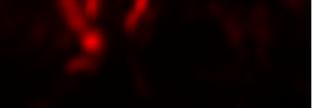
$$\int_S \quad \int_L$$

$$\int_S \quad \int_L$$

$$\int_S \quad \int_L$$





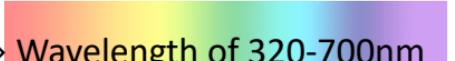






but...

visible light (real optics)  $\Rightarrow$  Wavelength of 320-700nm



but...

visible light (real optics)  $\Rightarrow$  Wavelength of 320-700nm



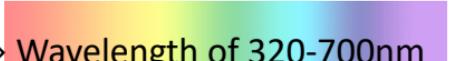
but...

visible light (real optics)  $\Rightarrow$  Wavelength of 320-700nm



but...

visible light (real optics)  $\Rightarrow$  Wavelength of 320-700nm



*lenses*

$$\Delta x = 1.22c \frac{1}{A}$$

Aperture = Relay wall

*lenses*

$$\lambda = \frac{1}{\Omega}$$

$$\Delta x = 1.22c \frac{\textcolor{red}{A}}{A}$$

Aperture = Relay wall

*lenses*

$$\Delta x = 1.22c \frac{A}{\lambda}$$

*Aperture = Relay wall*

*lenses*

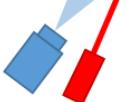
$$\Delta x = 1.22c \frac{A}{\lambda}$$

Aperture = Relay wall

*lenses*

$$\Delta x = 1.22c \frac{A}{\lambda}$$

Aperture = Relay wall



# REAL DEVICES



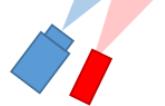
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# REAL DEVICES



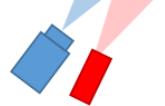
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**REAL DEVICES**



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# REAL DEVICES



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# of the hidden scene!

(N<sup>2</sup>x1)

Known

(N<sup>2</sup>xM)

Unknown

(Mx1)

Maybe  
(un)known

NxN image



# for Unseen Human Segmentation



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(e.g. relighting, direct-indirect separation)



[\[Young et al. 2020\]](#) Non-line-of-sight surface reconstruction using the directional light-cone transform

[\[Iseringhausen et al. 2020\]](#) Non-Line-of-Sight Reconstruction using Efficient Transient Rendering

