









- Optics capture something that is (close to) the final image.
- Computation mostly “enhances” the captured image (e.g., deblur).

- Generalized optics encode world into intermediate representation.
- Generalized computation decodes representation into one or multiple images.



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Sources: [CMU 15-463](#)



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Shadow pattern

Credit: B.J. Mattson, L3/NASA/GSFC

source may be inferred



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Shadow pattern

Credit: B.J. Mattson, L3/NASA/GSFC

R. H. Dicke (1968). "Scatter-hole cameras for x-rays and gamma rays". *The Astrophysical Journal*. **153**:L101.



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**Point Spread Function (PSF):** Response of a focused imaging system to a point source. Impulse response of an imaging system.















$$| * k = B$$









*scene by the PSF of the imaging system.*



















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mputer bereits simulieren. Für Praktisches Mikroskop. Foto: Brinkmann

schichten auf dem bewährten C-Silizium entwickelt. An beim herkömmlichen



0.4 0.6

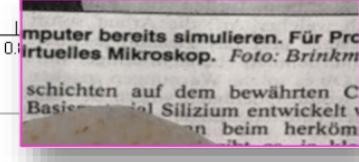
## Details





0.4 0.6

## Details

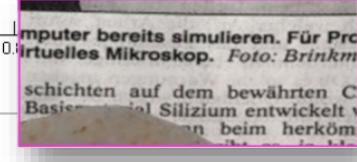


mputer bereits simulieren. Für Pro  
irtuelles Mikroskop. Foto: Brinkm  
schichten auf dem bewährten C  
Basierend auf Silizium entwickelt  
en beim herköm



0.4 0.6

## Details

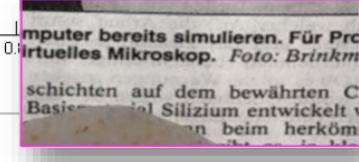


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en beim herköm



0.4 0.6

## Details

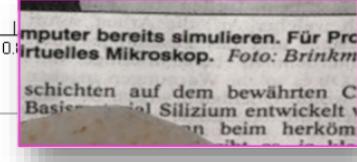


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0.4 0.6

## Details

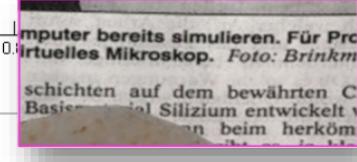


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en beim herköm



0.4 0.6

## Details









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# Calibrated kernels at a variety of depths from the focus plane



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**Captured Image**



**Captured Image**



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# Bad code



Computational Imaging for Astrophysics, Biology, and Computer Vision

# New code!



Computational Imaging

# New code!



Computational Imaging



Levin, A., Fergus, R., Durand, F., & Freeman, W. T. (2007).  
Image and depth from a conventional camera with a coded  
aperture. *ACM transactions on graphics (TOG)*, 26(3), 70-es.

Usually posed as an optimization problem,  
defining the appropriate objective function  
(& constraints).









object distance  $D$

focus distance  $D'$



object distance  $D$

focus distance  $D'$



object distance  $D$

focus distance  $D'$



object distance  $D$

focus distance  $D'$



object distance  $D$

focus distance  $D'$



object distance  $D$

focus distance  $D'$



object distance  $D$

focus distance  $D'$



input defocused image



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input defocused image

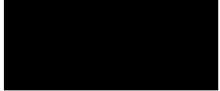


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measured PSFs at  
different depths





measured PSFs at  
different depths

$$\begin{matrix} A & B \\ C & D \end{matrix} *^{-1} \begin{matrix} \bullet & \bullet \\ \bullet & \bullet \end{matrix} = \begin{matrix} A & B \\ C & D \end{matrix} \begin{matrix} \downarrow \\ \downarrow \end{matrix}$$

$$\text{AB} \quad *^{-1} \quad \cdot \quad = \quad \text{ABC}$$

correct scale

?

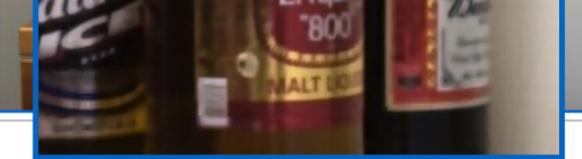


wrong scale





wrong scale 





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Course \_\_\_\_\_







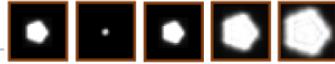




PSFs for object at depth 1



PSFs for object at depth 1



PSFs for object at depth 2

Sources: [CMU 15-463](#)



PSFs for object at depth 1



PSFs for object at depth 2



As we sweep through focus settings, each point is blurred by all possible PSFs.

Sources: [CMU 15-463](#)



PSFs for object at depth 1



PSFs for object at depth 2



As we sweep through focus settings, each point is blurred by all possible PSFs.

Sources: [CMU 15-463](#)

$$\int \text{[ ] } dt = \text{[ ] } \text{ effective PSF for object at depth 1}$$

$$\int \text{[ ] } dt = \text{[ ] } \text{ effective PSF for object at depth 2}$$

$$\int \begin{bmatrix} \text{hexagon} \\ \text{square} \\ \text{circle} \\ \text{star} \\ \text{diamond} \end{bmatrix} dt = \begin{bmatrix} \text{hexagon} \end{bmatrix} \text{ effective PSF for object at depth 1}$$

$$\int \begin{bmatrix} \text{circle} \\ \text{star} \\ \text{square} \\ \text{hexagon} \\ \text{cube} \end{bmatrix} dt = \begin{bmatrix} \text{hexagon} \end{bmatrix} \text{ effective PSF for object at depth 2}$$

Let's have a look at  
these PSFs...

Zhou, C., Miau, D., & Nayar, S. K. (2012). Focal sweep camera for space-time refocusing.



Zhou, C., Miau, D., & Nayar, S. K. (2012). Focal sweep camera for space-time refocusing.



Zhou, C., Miau, D., & Nayar, S. K. (2012). Focal sweep camera for space-time refocusing.





Images: Meyer Inst.



Images: Meyer Inst.

=> Focal sweep enables EDOF while maintaining high SNR.





OSC translation stage to move sensor relative  
to fixed lens during exposure



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Use translation stage to move sensor relative  
to fixed lens during exposure

Rotate focusing ring to move lens relative  
to fixed sensor during exposure



conver  
(sm



Sources: [CMU 15-463](#)

conv  
(large



conv  
(sm



conv  
(large



conv  
(sm







Original Image

$$f(x, y)$$

Coded Image

$$g(x, y)$$

Decoded Image

$$\hat{f}(x, y)$$



C. Wang, A. Serrano, X. Pan, K. Wolski, B. Chen, K. Myszkowski, & T. Leimkühler (2023). **An Implicit Neural Representation for the Image Stack: Depth, All in Focus, and High Dynamic Range**. *ACM Transactions on Graphics (TOG)*, 42(6), 1-11.



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Sources: [CMU 15-463](#)



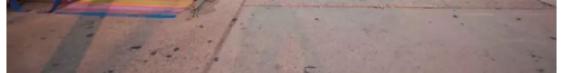




Can is moving linearly from left to right



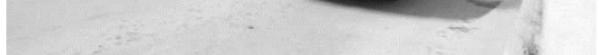
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Source: ExpertPhotography.



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Source: OpenCV.



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Source: ExpertPhotography.



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Spatially-varying kernel (velocity-dependent).





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blurry image of  
moving object

motion blur kernel

sharp image of  
static object

blurry image of  
moving object

motion blur kernel

sharp image of  
static object



# Why is flutter-shutter better?



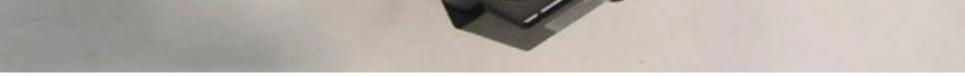
# Why is flutter-shutter better?



Input





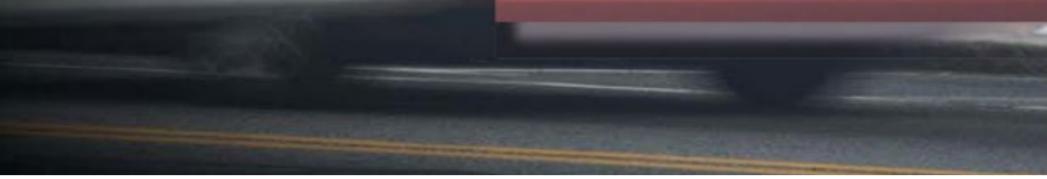


shutter



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Sources: [CMU 15-463](#)



License Plate Retrieval



License Plate Retrieval



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$$X * C = b$$

How do we  
detect this  
one?





continuous contours, and are always positive

## How do we use this information?





of gradients



Sparse





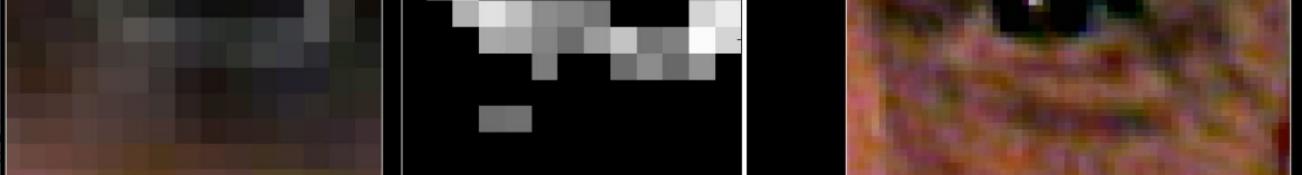
Note: Solving such optimization problems is complicated.



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*motion-invariant kernel at the cost of capturing everything blurry*

*(introducing additional motion)*

→ Out of the scope of the course.



Levin, A., Sand, P., Cho, T. S., Durand, F., & Freeman, W. T. (2008). Motion-invariant photography. *ACM Transactions on Graphics (TOG)*, 27(3), 1-9.





taken of a particular space-time chunk of the world  
(neglecting polarization and other wave-based effects)."

The Plenoptic Function and the Elements of  
Early Vision [Adelson and Bergen 1991]

- An observer takes samples from this function.

The Plenoptic Function and the Elements of Early Vision [Adelson and Bergen 1991]



May involve one or more cameras, and one or more captured images.

Different techniques for each – often there is *feedback* between dimensions.

Fergus et al., "Removing camera shake from a single image", SIGGRAPH 2006

Example of motion deblurring covered in this talk

Zhou et al., "Coded aperture pairs for depth from defocus", ICCV 2009.

Both papers show how to build on the basic approach to extract depth (also: see next topic in the course)

