Identifying Drivers of Outcomes: Linear Models

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Please Read Me

Purpose

Amusement park survey

Acknowledgments



• This presentation is based on (Chapman and Feit 2019, chap. 7)



• Apply linear modeling to understand a response variable and make predictions of forecasts



- weekend: whether the visit was on a weekend.
- num.child: number of children in the visit.
- distance: how far the customer traveled to the park in miles
- rides: satisfaction with rides using a scale [0, 100]
- games: satisfaction with games using a scale [0, 100]
- wait: satisfaction with waiting times using a scale [0, 100]
- clean: satisfaction with cleanliness using a scale [0, 100]
- overall: overall satisfaction rating using a scale [0, 100]



Import data

```
amusement_park <- read_csv("http://goo.gl/HKnl74")
amusement_park > head(n = 5)
```

```
# A tibble: 5 x 8
 weekend num.child distance rides games wait clean overall
 <chr>>
             <db1>
                      <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
                                                       <dbl>
1 yes
                     115.
                                87
                                      73
                                            60
                                                  89
                                                          47
                       27.0
2 yes
                                     78
                                                          65
3 no
                     63.3
                                85
                                    80
                                          70
                                                88
                                                          61
                       25.9
                                                          37
4 yes
                        54.7
                                            74
5 no
                                                          68
```



Transform data

```
amusement_park <- amusement_park |>
 mutate(weekend = factor(x = weekend,
                          labels = c('no', 'yes'),
                          ordered = FALSE),
        num.child = as.integer(num.child),
         # logarithmic transform
        logdist = log(distance, base = exp(x = 1)))
amusement_park > head(n = 5)
```

```
# A tibble: 5 x 9
 weekend num.child distance rides games wait clean overall logdist
                       <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                                                         <dbl>
 <fct>
              <int>
                                                                 <dh1>
                       115.
                                       73
                                                                  4.74
1 yes
2 yes
                        27.0
                                 87
                                       78
                                             76
                                                                  3.30
                        63.3
                                 85
                                      80
                                            70
                                                   88
                                                            61
                                                                  4.15
3 no
                        25.9
                                     72
4 yes
                                 88
                                             66
                                                   89
                                                            37
                                                                  3.25
5 no
                        54.7
                                 84
                                       87
                                             74
                                                            68
                                                                  4.00
```



- Summarize data
 - Ups the table is really big!!! Try it in your console to see the complete table

```
amusement_park |> skim()
```



Correlation matrices

Pearson correlation coefficients for samples in a tibble

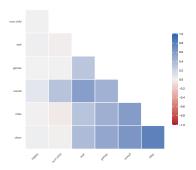
```
correlation_matrix <- amusement_park |>
 select(num.child, rides:logdist) |>
 corrr::correlate()
correlation matrix
```

```
# A tibble: 7 x 8
            num.child
                        rides
                                          wait
                                                 clean overall
                                                                 logdist
  term
                                 games
  <chr>>
                <dh1>
                        <dh1>
                                 <dbl>
                                         <dh1>
                                                  <dh1>
                                                          <dbl>
                                                                   <dh1>
                      -0.0403
                               0.00466 -0.0210 -0.0135
                                                         0.319
                                                                -0.00459
1 num.child
2 rides
             -0.0403
                               0.455
                                        0.314
                                                 0.790
                                                         0.586
                                                                -0.0110
3 games
            0.00466
                       0.455
                                        0.299
                                                 0.517
                                                         0.437
                                                                 0.00187
4 wait
             -0.0210
                       0.314
                               0.299
                                                 0.368
                                                         0.573
                                                                 0.0175
                                       NA
           -0.0135
                       0.790
                               0.517
                                        0.368
                                                         0.639
                                                                 0.0221
5 clean
            0.319
                       0.586
                               0.437
                                        0.573
                                                 0.639
                                                                 0.0763
6 overall
7 logdist
             -0.00459 -0.0110 0.00187
                                       0.0175
                                                0.0221
                                                       0.0763 NA
```



- Correlation matrices
 - Pearson correlation coefficients for samples in a tibble

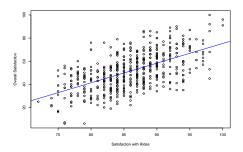
correlation_matrix |> autoplot(triangular = "lower")





Bivariate Association: the base R way

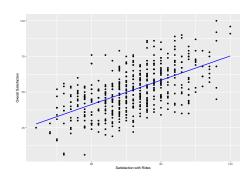
```
plot(overall~rides, data=amusement_park,
     xlab="Satisfaction with Rides", ylab="Overall Satisfaction")
abline(reg = lm(formula = overall~rides, data = amusement_park),
      col = 'blue')
```



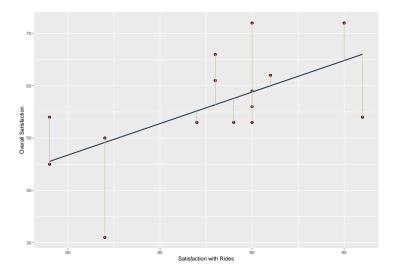


• Bivariate Association: the tidyverse way

```
amusement_park |> ggplot(aes(x = rides, y = overall)) +
 geom_point() +
 geom_smooth(method = 'lm',
             color = 'blue',
              se = FALSE) +
 labs(x = "Satisfaction with Rides".
      v = "Overall Satisfaction")
```









$$\begin{aligned} overall_i &= \beta_0 + \beta_1 rides_i + \epsilon_i \text{ where } \epsilon_i \sim \mathcal{N}(0, \sigma^2) \text{ and } i = 1, \dots, 500 \\ \widehat{overall_i} &= \hat{\beta}_0 + \hat{\beta}_1 rides_i \text{ and } \hat{\sigma}^2 \text{ where } i = 1, \dots, 500 \\ overall_i &- \widehat{overall_i} = \hat{\epsilon}_i \text{ where } i = 1, \dots, 500 \end{aligned}$$

```
model1 <- lm(formula = overall ~ rides, data = amusement park)
model1
```

```
Call:
lm(formula = overall ~ rides, data = amusement_park)
Coefficients:
(Intercept)
                   rides
    -94.962
                   1.703
```



ls.str(model1)

```
assign : int [1:2] 0 1
call: language lm(formula = overall ~ rides, data = amusement park)
coefficients: Named num [1:2] -95 1.7
df.residual: int 498
effects: Named num [1:500] -1146.2 -207.9 11.5 -17.9 20.3 ...
fitted.values: Named num [1:500] 53.2 53.2 49.8 54.9 48.1 ...
model: 'data.frame': 500 obs. of 2 variables:
$ overall: num 47 65 61 37 68 27 40 30 58 36 ...
$ rides : num 87 87 85 88 84 81 77 82 90 88 ...
ar : List of 5
$ qr : num [1:500, 1:2] -22.3607 0.0447 0.0447 0.0447 0.0447 ...
$ graux: num [1:2] 1.04 1.01
$ pivot: int [1:2] 1 2
$ tol : num 1e-07
$ rank : int 2
rank · int 2
residuals: Named num [1:500] -6.22 11.78 11.18 -17.93 19.89 ...
terms : Classes 'terms', 'formula' language overall ~ rides
xlevels : Named list()
```



summary (model1)

```
Call:
lm(formula = overall ~ rides, data = amusement_park)
Residuals:
   Min
            10 Median
                           30
                                 Max
-33 597 -10 048 0 425 8 694 34 699
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) -94.9622 9.0790 -10.46 <2e-16 ***
          1.7033
                   0.1055 16.14 <2e-16 ***
rides
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 12.88 on 498 degrees of freedom
Multiple R-squared: 0.3434, Adjusted R-squared: 0.3421
F-statistic: 260.4 on 1 and 498 DF, p-value: < 2.2e-16
```



```
(Intercept)
                  rides
-94.962246
               1.703285
# Make some predictions
# We want to forecast the overall satisfaction rating
# if the satisfaction with rides is 95
-94.962246 + 1.703285*95
```

```
[1] 66.84983
```

model1\$coefficients



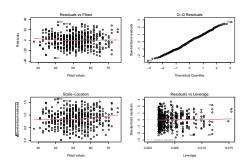
- Linear Model with a Single Predictor
 - Std. Frror column
 - Indicates uncertainty in the coefficient estimate
 - We can build a confidence interval

```
summary(model1)$coefficients[, 2]
(Intercept)
                  rides
  9.0790049
              0.1055462
confint(model1, level = 0.95)
```

```
2.5 %
                           97.5 %
(Intercept) -112.800120 -77.124371
rides
              1.495915
                        1.910656
```



```
par(mfrow=c(2,2))
plot(model1)
```



par(mfrow=c(1,1))



- Linear Model with a Single Predictor
 - Linearity: plot (1,1)
 - Reference line should be flat and horizontal
 - Normality of residuals: plot (1, 2)
 - Dots should fall along the line
 - Homogeneity of variance: plot (2,1)
 - Reference line should be flat and horizontal
 - Influential observations: plot (2, 2)
 - Points should be inside the contour lines



Linear Model with Multiple Predictors

$$\begin{split} overall_i &= \beta_0 + \beta_1 rides_i + \beta_2 games_i \\ &+ \beta_3 wait_i + \beta_4 clean_i + \epsilon_i \\ &\text{where } \epsilon_i \sim \mathcal{N}(0, \sigma^2) \text{ and } i = 1, \dots, 500 \end{split}$$

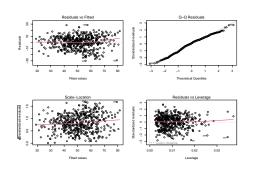
```
model2 <- lm(formula = overall ~ rides + games + wait + clean.
             data = amusement_park)
model2
```

```
Call:
lm(formula = overall ~ rides + games + wait + clean, data = amusement_park)
Coefficients:
(Intercept)
                   rides
                                games
                                                           clean
                                               wait
 -131.4092
                  0.5291
                               0.1533
                                             0.5533
                                                          0.9842
```



• Linear Model with Multiple Predictors

```
par(mfrow=c(2,2))
plot(model2)
```



par(mfrow=c(1,1))



Linear Model with Multiple Predictors

summary(model2)

```
Call:
lm(formula = overall ~ rides + games + wait + clean, data = amusement park)
Residuals:
          10 Median 30 Max
   Min
-29.944 -6.841 1.072 7.167 28.618
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) -131.40919 8.33377 -15.768 < 2e-16 ***
rides
            games
wait
          0.55333 0.04781 11.573 < 2e-16 ***
            0.98421 0.15987 6.156 1.54e-09 ***
clean
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 10.59 on 495 degrees of freedom
Multiple R-squared: 0.5586. Adjusted R-squared: 0.5551
F-statistic: 156.6 on 4 and 495 DF. p-value: < 2.2e-16
```



Linear Model with Multiple Predictors

$$H_0:\beta_1=0$$

$$H_1: \beta_1 \neq 0$$

$$t_{rides} = \frac{\hat{\beta}_1 - \beta_1}{\sqrt{Var(\hat{\beta}_1)}} = \frac{0.529078 - 0}{0.14207176} = 3.724019$$

model2\$coefficients

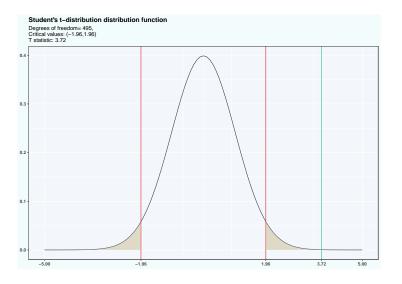
```
(Intercept)
                  rides
                              games
                                            wait
                                                       clean
-131.4091939
              0.5290780
                           0.1533361
                                       0.5533264
                                                   0.9842126
```

```
# Calculate the variance-covariance matrix, extract
# the diagonal and calculate the standard deviaton of
# the parameters
model2 |> vcov() |> diag() |> sqrt()
```

```
(Intercept)
                rides
                                                 clean
                           games
8 33376643 0 14207176 0 06908486 0 04781282 0 15986712
```



• Linear Model with Multiple Predictors





• Linear Model with Multiple Predictors

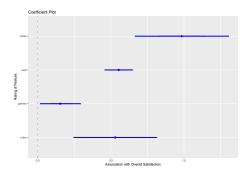
```
2.5 %
                               97.5 %
(Intercept) -147.78311147 -115.0352764
rides
              0.24993998
                            0.8082161
games
              0.01760038
                          0.2890718
wait
              0.45938535
                          0.6472675
clean
              0.67011082
                           1.2983144
```

confint(model2, level = 0.95)



Linear Model with Multiple Predictors

```
library(coefplot) # Remember to install the package if it is not installed
coefplot(model = model2,
         # The intercept is relatively large: -131.4092
        intercept = FALSE,
        ylab="Rating of Feature",
        xlab="Association with Overall Satisfaction",
        lwdOuter = 1.5)
```





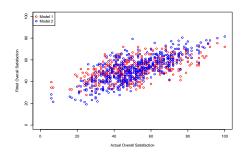
```
summary(model1)$r.squared
[1] 0.3433799
summary(model2)$r.squared
[1] 0.558621
summary(model1)$adj.r.squared
[1] 0.3420614
summary(model2)$adj.r.squared
```

[1] 0.5550543



Base R way

```
plot(x = amusement_park$overall, y = fitted(model1),
     col = "red", xlim = c(0,100), ylim = c(0,100),
     xlab = "Actual Overall Satisfaction".
     vlab = "Fitted Overall Satisfaction")
points(x = amusement_park$overall, y = fitted(model2),
      col = "blue")
legend(x = "topleft", legend = c("Model 1", "Model 2"), col = c("red", "blue"), pch = 1)
```





Tidymodels and tidyverse way: Prepare data

```
model1_augment <- augment(x = model1) |> mutate(model = "Model 1")
model2 augment <- augment(x = model2) |> mutate(model = "Model 2")
models_performance <- model1_augment |> bind_rows(model2_augment)
models performance |> glimpse()
```

```
Rows: 1,000
Columns: 12
                                      <dbl> 47, 65, 61, 37, 68, 27, 40, 30, 58, 36, 71, 48, 75, 46, 59,~
$ overall
$ rides
                                      <dbl> 87, 87, 85, 88, 84, 81, 77, 82, 90, 88, 93, 79, 94, 81, 86,~
                                      <dbl> 53.22359, 53.22359, 49.81702, 54.92688, 48.11373, 43.00388,~
$ fitted
                                      <dbl> -6.2235914, 11.7764086, 11.1829795, -17.9268769, 19.8862650~
$ .resid
                                      <dbl> 0.002089430, 0.002089430, 0.002048063, 0.002311576, 0.00222~
$ .hat
$ .sigma
                                      <dbl> 12.88964, 12.88182, 12.88289, 12.86751, 12.86171, 12.87260,~
$ .cooksd
                                      <dbl> 2.449537e-04. 8.770564e-04. 7.751689e-04. 2.249493e-03. 2.6~
$ .std.resid <dbl> -0.48371422, 0.91529407, 0.86915315, -1.39348008, 1.5457218~
$ model
                                      <chr> "Model 1", 
$ games
                                      $ wait
                                      $ clean
```



• Tidymodels and tidyverse way: Visualize

```
models_performance |>
  ggplot() +
  geom_point(aes(x = overall, y = .fitted,
                 color = model)) +
  labs(x = "Actual Overall Satisfaction",
       y = "Fitted Overall Satisfaction")
```





Analysis of variance (anova) for nested models¹

```
anova lm <- anova(model1, model2, test = "F")
anova_lm
Analysis of Variance Table
Model 1: overall ~ rides
Model 2: overall ~ rides + games + wait + clean
 Res.Df RSS Df Sum of Sq F
                                    Pr(>F)
    498 82612
    495 55532 3 27080 80.463 < 2.2e-16 ***
---
               0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

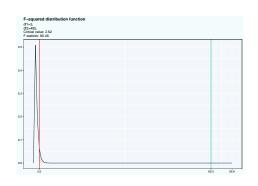
¹This statistical analysis only make sense for nested models that are fitted with the same data where the convention is to include the models from smallest to largest. See ?anova.lm



$$H_0:\beta_0=\beta_1=\beta_2=\beta_3=\beta_4=0$$

 H_1 : At least one $eta_j
eq 0$ for j=0,1,2,3,4

$$F = \frac{\frac{RSS_1 - RSS_2}{p_2 - p_1}}{\frac{RSS_2}{n - p_2}} = \frac{\frac{82611.81 - 55531.53}{5 - 2}}{\frac{55531.53}{500 - 5}} = 80.46323$$





Predictions

$$\begin{split} \widehat{overall}_j &= \hat{\beta}_0 + \hat{\beta}_1 rides_j + \hat{\beta}_2 games_j \\ &+ \hat{\beta}_3 wait_j + \hat{\beta}_4 clean_j \end{split}$$

```
# A tibble: 5 x 2
 coef
                 value
 <chr>>
                 <db1>
1 (Intercept) -131.
2 rides
               0.529
3 games
               0.153
4 wait
                0.553
```

5 clean

coef(model2) |> enframe(name = "coef")

0.984



- Predictions
 - Manual

```
(coef(model2)["(Intercept)"]*1 + coef(model2)["rides"]*30 + coef(model2)["games"]*10 +
   coef(model2)["wait"]*57 + coef(model2)["clean"]*90) |>
 unname()
```

[1] 6.11525

- Predictions
 - Matrix multiplication

```
coef(model2) %*% c(1, 30, 10, 57, 90)
        Γ.17
[1.] 6.11525
```



Predictions

predict

```
# New data
new_data <- tibble(rides = c(30, 70),
                   games = c(10, 80),
                   wait = c(57, 60),
                   clean = c(90, 93)
# Result
predict(object = model2, newdata = new_data) |>
 enframe(name = "observation", value = "overall pred") |>
 bind cols(new data)
```

```
# A tibble: 2 x 6
 observation overall_pred rides games wait clean
                      <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
 <chr>>
                       6.12
                               30
                                     10
                                           57
                                                  90
1 1
                               70
2 2
                     42.6
                                     80
                                           60
                                                  93
```



Standardizing the predictors

- Compare the effect that different predictor variables have on a response variable
- It must be interpreted in terms of standard deviations
 - One standard deviation in x variable is associated with a standard deviation increase of decrease depending on the value of the estimated parameter

```
amusement_park_std <- amusement_park |>
 select(-distance) |>
 mutate(across(rides:logdist,
                .fns = ~scale(x = .x.)
                               center = TRUE.
                               scale = TRUE)[,1]))
amusement park std |> head()
```

```
# A tibble: 6 x 8
 weekend num.child rides
                                         clean overall logdist
                           games
                                   wait
             <int> <dbl>
                           <db1>
                                    <dbl>
                                           <db1>
                                                   <db1>
                                                           <db1>
  <fct>
                 0 0.211 -0.698 -0.919
                                          0.215
                                                  -0.268
                                                           1.79
1 ves
2 yes
                 2 0.211 -0.0820 0.567
                                          -0.176
                                                 0.865
                                                          0.323
                 1 -0.155 0.164
                                  0.00966 0.0199 0.614
                                                         1.19
3 no
4 yes
                 0 0.394 -0.821 -0.362
                                        0.215
                                                  -0.898
                                                           0.280
5 no
                 4 -0.338 1.03
                                  0.381
                                         -0.176
                                                 1.05
                                                           1.04
                 5 -0.887 0.0411 -2.03
                                                  -1.53
6 no
                                         -1.74
                                                           0.145
```



Standardizing the predictors

data = amusement_park_std)

Residual standard error: 0.667 on 495 degrees of freedom Multiple R-squared: 0.5586. Adjusted R-squared: 0.5551 F-statistic: 156.6 on 4 and 495 DF, p-value: < 2.2e-16

model2 std <- lm(formula = overall ~ rides + games + wait + clean.

```
summary(model2_std)
Call:
lm(formula = overall ~ rides + games + wait + clean, data = amusement park std)
Residuals:
    Min
              10 Median
                                      Max
-1 88578 -0 43082 0 06749 0 45136 1 80231
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -2.607e-16 2.983e-02 0.000 1.000000
rides
          1.820e-01 4.888e-02 3.724 0.000219 ***
games
          7.844e-02 3.534e-02 2.220 0.026903 *
wait
          3.753e-01 3.243e-02 11.573 < 2e-16 ***
           3.170e-01 5.150e-02 6.156 1.54e-09 ***
clean
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
```



```
model3 <- lm(formula = overall ~ rides + games + wait + clean + weekend + logdist + num.child,
             data = amusement park std)
tidy(model3)
```

```
# A tibble: 8 x 5
          estimate std.error statistic p.value
 term
 <chr>
             <dbl>
                    <db1>
                             <dbl>
                                    <db1>
                            -8.01 8.41e-15
1 (Intercept) -0.373
                    0.0465
2 rides
        0.213 0.0420 5.07 5.57e- 7
3 games
      0.0707 0.0303 2.34 1.99e- 2
          0.381 0.0278 13.7
                                 1.45e-36
4 wait
5 clean
           0.297 0.0441 6.72 4.89e-11
6 weekendyes -0.0459 0.0514 -0.893 3.73e- 1
        0.0647 0.0257 2.52 1.22e- 2
7 logdist
8 num child 0.227
                    0.0171
                            13.3 1.37e-34
```

glance(model3)

```
# A tibble: 1 x 12
 r.squared adj.r.squared sigma statistic p.value df logLik AIC
     <db1>
                  <db1> <db1>
                                 <db1>
                                           <db1> <db1> <db1> <db1> <db1> <db1>
     0.679
                  0.674 0.571
                                 148. 5.97e-117
                                                   7 -425, 868, 906,
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```



Overall satisfaction is about the same regardless the number of children

```
amusement_park_std <- amusement_park_std |>
 mutate(num.child.factor = factor(num.child))
model4 <- lm(formula = overall ~ rides + games + wait + clean + weekend + logdist + num.child.factor,
            data = amusement_park_std)
tidy(model4) |> slice(1, 2, 8:12)
# A tibble: 7 x 5
                  estimate std.error statistic p.value
 term
                     <db1>
                                        <dbl>
 <chr>>
                              <db1>
                                                <db1>
1 (Intercept)
                                       -15.4 7.00e-44
                   -0.691
                             0.0449
2 rides
                    0.223
                             0.0354
                                         6.30 6.61e-10
3 num.child.factor1
                   1.02 0.0713 14.3 8.96e-39
4 num.child.factor2 1.04 0.0564
                                       18.4 8.77e-58
5 num.child.factor3 0.980 0.0702 14.0 1.75e-37
6 num child factor4
                   0.932
                             0.0803
                                       11.6 1.22e-27
7 num.child.factor5
                   1.00
                                        9.66 2.50e-20
                             0.104
```

glance(model4)

```
# A tibble: 1 x 12
                r.squared adj.r.squared sigma statistic p.value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   df logLik
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            AIC
                                                    <dh1>
                                                                                                                                                                           <dh1> <dh1>
                                                                                                                                                                                                                                                                                                                   <dh1>
                                                                                                                                                                                                                                                                                                                                                                                                          <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl< <dbl> <dbl> <dbl> <dbl< <dbl > <db > </db > <db > <
                                                  0.775
                                                                                                                                                                       0.770 0.480
                                                                                                                                                                                                                                                                                                               153. 2.68e-150
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       11 -336 698 753
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```



r.squared adj.r.squared sigma statistic p.value df logLik AIC

0.771 0.478 282 1.03e-155

i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>

<db1>

<db1> <db1>

Using factors as predictors

Preparing data

```
amusement_park_std <- amusement_park_std |>
 mutate(has.child = factor(x = num.child > 0, labels = c("No", "Yes")))
model5 <- lm(formula = overall ~ rides + games + wait + clean + logdist + has.child.
            data = amusement park std)
tidy(model5) |> slice(1, 2, 7)
# A tibble: 3 x 5
             estimate std.error statistic p.value
 term
 <chr>
                        <db1>
                                 <dh1>
                                            <dh1>
               <dh1>
1 (Intercept) -0.702
                         0.0391 -18.0 6.68e-56
2 rides
               0.223 0.0351 6.34 5.12e-10
3 has.childYes 1.01 0.0468 21.5 1.08e-72
glance(model5)
```



A tibble: 1 x 12

<dbl> 0.774 <dbl> <db> <db> <db> <db> <db > <db

6 -337 690 724

 Maybe having children and the visits on weekends are important for the scores so an interaction will be useful

```
model6 <- lm(formula = overall ~ rides + games + wait + clean + weekend + logdist +
                                has.child + rides:has.child + games:has.child + wait:has.child +
                                clean:has.child + rides:weekend + games:weekend + wait:weekend +
                                clean:weekend, data = amusement_park_std)
tidy(model6) |> slice(9:16)
# A tibble: 8 x 5
                    estimate std.error statistic p.value
  term
                                           <db1>
  <chr>>
                       <db1>
                                 <db1>
                                                   <db1>
1 rides:has.childYes
                     0.0578
                                0.0731
                                          0.792 4.29e- 1
2 games:has.childYes -0.0640
                                0.0528
                                         -1.21 2.26e- 1
3 wait:has.childYes
                     0.351
                                       7.42
                                              5.21e-13
                                0.0472
4 clean has childYes -0.00185
                                0.0797
                                        -0.0233 9.81e- 1
5 rides:weekendves
                     0.0618
                                0.0678 0.912 3.62e- 1
6 games:weekendyes 0.0185
                               0.0490 0.377 7.06e- 1
7 wait:weekendves
                    0.0352
                                0.0445 0.791 4.29e- 1
8 clean:weekendves
                    -0.0273
                                0.0710
                                         -0.385 7.01e- 1
glance(model6)
```

```
# A tibble: 1 x 12
                r.squared adj.r.squared sigma statistic
                                                                                                                                                                                                                                                                                                                                                                                               p.value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 df logLik
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          AIC
                                                     <dh1>
                                                                                                                                                                                <dh1> <dh1>
                                                                                                                                                                                                                                                                                                                           <dh1>
                                                                                                                                                                                                                                                                                                                                                                                                                    <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl< <dbl> <dbl> <dbl> <dbl< <dbl > <db > </db > <db > <
                                                   0.802
                                                                                                                                                                            0.796 0.452
                                                                                                                                                                                                                                                                                                                                 130. 3.69e-159
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 15 -304, 643, 714,
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```



Only an interaction was significant

```
model7 <- lm(formula = overall ~ rides + games + wait + clean + logdist + has.child +
                       wait:has.child, data = amusement_park_std)
tidv(model7)
```

```
# A tibble: 8 x 5
                 estimate std.error statistic p.value
 term
 <chr>>
                                             <db1>
                   <dbl>
                            <db1>
                                     <dbl>
1 (Intercept)
                  -0.693
                           0.0368
                                    -18.8 6.91e-60
                  0.213 0.0331 6.42 3.24e-10
2 rides
                  0.0487 0.0239 2.03 4.25e- 2
3 games
                  0.151 0.0369 4.09 4.98e- 5
4 wait
                  0.302 0.0349 8.68 5.94e-17
5 clean
                  0.0292 0.0203 1.44 1.50e- 1
6 logdist
7 has.childYes
                 0.998 0.0442
                                     22.6 4.02e-78
8 wait:has_childVes
                 0.347 0.0438
                                  7 92 1 59e-14
```

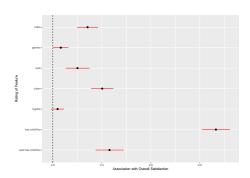
```
glance(model7)
```

```
# A tibble: 1 x 12
                r.squared adj.r.squared sigma statistic p.value
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      df logLik
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              AIC
                                                                                                                                                                           <db1> <db1>
                                                                                                                                                                                                                                                                                                                   <db1>
                                                                                                                                                                                                                                                                                                                                                                                                             <dbl> <db> <db> <db> <db> <db > <db 
                                                    <dbl>
                                                  0.800
                                                                                                                                                                    0.797 0.451
                                                                                                                                                                                                                                                                                                                           280. 2.96e-167
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        7 -307, 632, 670,
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```



Final model

```
library(dotwhisker) # Remember to install the package if it is not installed
tidy(model7) |>
 dwplot(ci = 0.95,
        dot args = list(size = 2, color = "black"), whisker args = list(color = "red"),
        vline = geom_vline(xintercept = 0, color = "black", linetype = 2)) +
 labs(x = "Association with Overall Satisfaction", y = "Rating of Feature")
```





Formula syntax

Formula in R	Statistical Model
y ~ x	$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$
y \sim -1 $+$ $ imes$	$y_i = \beta_1 x_i + \varepsilon_i$
$y \sim x + z$	$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \varepsilon_i$
$y \sim x + z + x:z$	$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \beta_3 x_i z_i + \varepsilon_i$
$y\simx^{f *}z$	$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \beta_3 x_i z_i + \varepsilon_i$
$y \sim (x + z + w)^2$	$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \beta_3 w_i + \beta_4 x_i z_i + \beta_5 x_i w_i + \beta_6 w_i z_i + \varepsilon_i$
$y \sim (x + z + w)^2 - x:z$	$\boldsymbol{y}_i = \boldsymbol{\beta}_0 + \boldsymbol{\beta}_1 \boldsymbol{x}_i + \boldsymbol{\beta}_2 \boldsymbol{z}_i + \boldsymbol{\beta}_3 \boldsymbol{w}_i + \boldsymbol{\beta}_4 \boldsymbol{x}_i \boldsymbol{w}_i + \boldsymbol{\beta}_5 \boldsymbol{w}_i \boldsymbol{z}_i + \boldsymbol{\varepsilon}_i$
$y \sim x + I(x^2)$	$y_i = \beta_0 + \beta_1 x_i + \beta_1 x_i^2 + \varepsilon_i$

Try the following models using tidy:

```
lm(formula = overall ~ rides, data = amusement_park_std) |> tidy()
lm(formula = overall ~ -1 + rides, data = amusement park std) |> tidv()
lm(formula = overall ~ rides + has.child, data = amusement park std) |> tidv()
lm(formula = overall ~ rides + has.child + has.child, data = amusement park std) |> tidy()
lm(formula = overall ~ (rides + has.child + weekend)^2.
   data = amusement_park_std) |> tidy()
lm(formula = overall ~ (rides + has.child + weekend)^2 - rides:has.child,
   data = amusement_park_std) |> tidy()
lm(formula = overall ~ rides + I(rides^2) - rides:has.child. data = amusement park std) |> tidy()
```

- To my family that supports me
- To the taxpayers of Colombia and the UMNG students who pay my salary
- To the Business Science and R4DS Online Learning communities where I learn R and π -thon
- To the R Core Team, the creators of RStudio IDE, Quarto and the authors and maintainers of the packages tidyverse, skimr, tidymodels, dotwhisker, kableExtra and tinytex for allowing me to access these tools without paying for a license
- To the Linux kernel community for allowing me the possibility to use some **Linux distributions** as my main **OS** without paying for a license



References I

Chapman, Chris, and Elea McDonnell Feit. 2019. R For Marketing Research and Analytics. 2nd ed. 2019. Use R! Cham: Springer International Publishing: Imprint: Springer. https://doi-org.ezproxy.umng.edu.co/10.1007/978-3-030-14316-9.

