# **Identifying Drivers of Outcomes: Linear Models**

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**FAEDIS** 

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- Please Read Me
- **Purpose**
- Amusement park survey
- **Acknowledgments**



• This presentation is based on (Chapman and Feit 2019, chap. 7)



• Apply linear modeling to understand a response variable and make predictions of forecasts



- weekend: whether the visit was on a weekend
- num.child: number of children in the visit
- **distance**: how far the customer traveled to the park in miles
- rides: satisfaction with rides using a scale [0, 100]
- games: satisfaction with games using a scale [0, 100]
- wait: satisfaction with waiting times using a scale [0, 100]
- clean: satisfaction with cleanliness using a scale [0, 100]
- overall: overall satisfaction rating using a scale [0, 100]



## Import data

5 no

```
amusement_park <- read_csv("http://goo.gl/HKnl74")
amusement_park > head(n = 5)
```

68

```
# A tibble: 5 x 8
 weekend num.child distance rides games wait clean overall
                    <chr>>
            <db1>
                                                 <db1>
                    115.
                                  73
                                       60
                                                    47
1 yes
                     27.0
2 yes
                            87
                                  78
                                       76
                                             87
                                                    65
3 no
                     63.3
                            85
                                  80
                                       70
                                            88
                                                    61
                     25.9
                                 72
                                                    37
4 yes
                            88
                                       66
                                             89
```

84 87 74 87

54.7



#### Transform data

```
amusement_park <- amusement_park |>
 mutate(weekend = factor(x = weekend,
                          labels = c('no', 'yes'),
                          ordered = FALSE).
        num.child = as.integer(num.child).
         # logarithmic transform
        logdist = log(distance, base = exp(x = 1)))
amusement_park > head(n = 5)
```

#### # A tibble: 5 x 9

```
weekend num.child distance rides games wait clean overall logdist
                       <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
 <fct>
              <int>
                                                        <dbl>
                                                               <dbl>
1 ves
                       115.
                                      73
                                            60
                                                          47
                                                                4.74
                       27.0
2 yes
                                     78
                                            76
                                                          65
                                                                3.30
                        63.3
                                85
                                     80
                                           70
                                                          61
                                                                4.15
3 no
                                     72
4 ves
                        25.9
                                                 89
                                                                3.25
5 no
                        54.7
                                            74
                                                  87
                                                                4.00
```



- Summarize data
  - Ups the table is really big!!! Try it in your console to see the complete table

amusement\_park |> skim()



#### Correlation matrices

correlation\_matrix <- amusement\_park |>
 select(num.child, rides:logdist) |>

-0.00459 -0.0110 0.00187

• Pearson correlation coefficients for samples in a tibble

```
corrr::correlate()
correlation_matrix
# A tibble: 7 x 8
            num child
                                 games
                                           wait
                                                  clean overall
                                                                 logdist
  term
                        rides
                <db1>
                        <db1>
                                  <db1>
                                          <db1>
                                                  <db1>
                                                                   <db1>
  <chr>>
                                                          <dbl>
1 num.child
             NA
                      -0.0403
                               0.00466 -0.0210 -0.0135 0.319
                                                                -0.00459
2 rides
             -0.0403
                      NA
                               0.455
                                         0.314
                                                 0.790
                                                         0.586
                                                               -0.0110
3 games
            0.00466
                      0.455
                                         0.299
                                                 0.517
                                                         0.437
                                                                 0.00187
                       0.314
                               0.299
                                                 0.368
                                                         0.573
                                                                 0.0175
4 wait
             -0.0210
                                        NA
5 clean
             -0.0135
                       0.790
                               0.517
                                        0.368
                                                         0.639
                                                                 0.0221
                                                NA
            0.319
                       0.586
                               0.437
                                        0.573
                                                 0.639
                                                                 0.0763
6 overall
```

0.0175



7 logdist

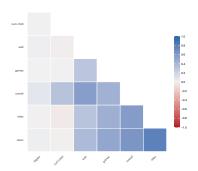
0.0221

0.0763 NA

#### Correlation matrices

Pearson correlation coefficients for samples in a tibble

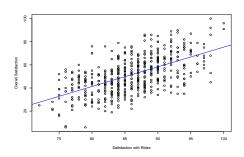
correlation\_matrix |> autoplot(triangular = "lower")





## Bivariate Association: the base R way

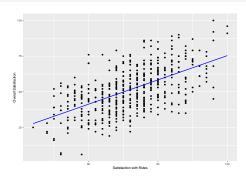
```
plot(overall~rides, data=amusement_park,
     xlab="Satisfaction with Rides", ylab="Overall Satisfaction")
abline(reg = lm(formula = overall~rides, data = amusement_park),
      col = 'blue')
```





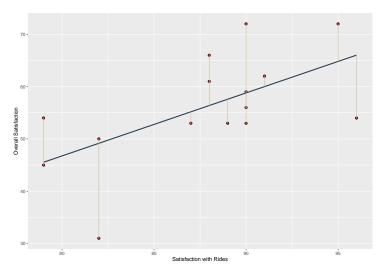
### Bivariate Association: the tidyverse way

```
amusement_park |> ggplot(aes(x = rides, y = overall)) +
 geom_point() +
 geom smooth(method = 'lm',
              color = 'blue'.
              se = FALSE) +
 labs(x = "Satisfaction with Rides",
      v = "Overall Satisfaction")
```





# • Linear Model with a Single Predictor





Linear Model with a Single Predictor

model1 <- lm(formula = overall ~ rides, data = amusement park)

$$\begin{split} overall_i &= \beta_0 + \beta_1 rides_i + \epsilon_i \text{ where } \epsilon_i \sim \mathcal{N}(0, \sigma^2) \text{ and } i = 1, \dots, 500 \\ \\ \widehat{overall_i} &= \widehat{\beta}_0 + \widehat{\beta}_1 rides_i \text{ and } \widehat{\sigma}^2 \text{ where } i = 1, \dots, 500 \\ \\ overall_i &= \widehat{\epsilon}_i \text{ where } i = 1, \dots, 500 \end{split}$$

```
model1
Call:
lm(formula = overall ~ rides, data = amusement_park)
```



rides

1.703

Coefficients: (Intercept)

-94.962

#### Linear Model with a Single Predictor

ls.str(model1)

```
assign : int [1:2] 0 1
call : language lm(formula = overall ~ rides, data = amusement park)
coefficients: Named num [1:2] -95 1.7
df residual : int 498
effects: Named num [1:500] -1146.2 -207.9 11.5 -17.9 20.3 ...
fitted.values: Named num [1:500] 53.2 53.2 49.8 54.9 48.1 ...
model : 'data frame': 500 obs. of 2 variables:
$ overall: num 47 65 61 37 68 27 40 30 58 36 ...
$ rides : num 87 87 85 88 84 81 77 82 90 88 ...
ar : List of 5
$ ar : num [1:500, 1:2] -22.3607 0.0447 0.0447 0.0447 0.0447 ...
$ graux: num [1:2] 1.04 1.01
$ pivot: int [1:2] 1 2
$ tol : num 1e-07
$ rank : int 2
rank: int 2
residuals: Named num [1:500] -6.22 11.78 11.18 -17.93 19.89 ...
terms : Classes 'terms', 'formula' language overall ~ rides
xlevels : Named list()
```



#### Linear Model with a Single Predictor

summary (model1)

Call:

```
lm(formula = overall ~ rides, data = amusement_park)
Residuals:
   Min
            1Q Median
                          30
                                 Max
-33.597 -10.048 0.425 8.694 34.699
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
(Intercept) -94.9622 9.0790 -10.46 <2e-16 ***
rides
           1.7033 0.1055 16.14 <2e-16 ***
---
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 12.88 on 498 degrees of freedom
Multiple R-squared: 0.3434. Adjusted R-squared: 0.3421
F-statistic: 260.4 on 1 and 498 DF. p-value: < 2.2e-16
```



# • Linear Model with a Single Predictor

```
model1$coefficients
```

```
(Intercept)
                  rides
-94.962246
               1.703285
# Make some predictions
# We want to forecast the overall satisfaction rating
# if the satisfaction with rides is 95
-94.962246 + 1.703285*95
```

```
[1] 66.84983
```



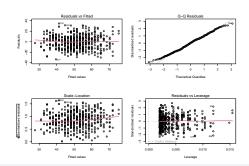
- Linear Model with a Single Predictor
  - Std. Frror column
    - Indicates uncertainty in the coefficient estimate
    - We can build a confidence interval

```
summary(model1)$coefficients[, 2]
(Intercept)
                  rides
 9.0790049
              0.1055462
confint(model1, level = 0.95)
                  2.5 %
                            97.5 %
(Intercept) -112.800120 -77.124371
rides
               1.495915
                          1.910656
```



### • Linear Model with a Single Predictor

```
par(mfrow=c(2,2))
plot(model1)
```



par(mfrow=c(1,1))



- Linear Model with a Single Predictor
  - **Linearity**: plot (1,1)
    - Reference line should be flat and horizontal
  - Normality of residuals: plot (1, 2)
    - Dots should fall along the line
  - Homogeneity of variance: plot (2,1)
    - Reference line should be flat and horizontal
  - Influential observations: plot (2, 2)
    - Points should be inside the contour lines



## Linear Model with Multiple Predictors

$$\begin{split} overall_i &= \beta_0 + \beta_1 rides_i + \beta_2 games_i \\ &+ \beta_3 wait_i + \beta_4 clean_i + \epsilon_i \\ &\text{where } \epsilon_i \sim \mathcal{N}(0, \sigma^2) \text{ and } i = 1, \dots, 500 \end{split}$$

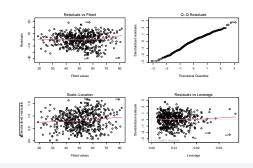
```
model2 <- lm(formula = overall ~ rides + games + wait + clean,
             data = amusement_park)
model2
Call:
```

```
lm(formula = overall ~ rides + games + wait + clean, data = amusement_park)
Coefficients:
(Intercept)
                   rides
                                               wait
                                                           clean
                                 games
 -131.4092
                  0.5291
                                0.1533
                                             0.5533
                                                          0.9842
```



# • Linear Model with Multiple Predictors

par(mfrow=c(2,2)) plot(model2)



par(mfrow=c(1,1))



#### Linear Model with Multiple Predictors

summary (model2)

```
Call:
lm(formula = overall ~ rides + games + wait + clean, data = amusement_park)
Residuals:
   Min
           1Q Median 3Q
                                Max
-29.944 -6.841 1.072 7.167 28.618
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -131.40919 8.33377 -15.768 < 2e-16 ***
rides
             0.15334 0.06908 2.220 0.026903 *
games
             0.55333    0.04781    11.573    < 2e-16 ***
wait
             0.98421 0.15987 6.156 1.54e-09 ***
clean
---
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' ' 1
Residual standard error: 10.59 on 495 degrees of freedom
Multiple R-squared: 0.5586, Adjusted R-squared: 0.5551
F-statistic: 156.6 on 4 and 495 DF. p-value: < 2.2e-16
```



#### Linear Model with Multiple Predictors

$$\begin{split} H_0: \beta_1 &= 0 \\ H_1: \beta_1 \neq 0 \\ t_{rides} &= \frac{\hat{\beta}_1 - \beta_1}{\sqrt{Var(\hat{\beta}_1)}} = \frac{0.529078 - 0}{0.14207176} = 3.724019 \end{split}$$

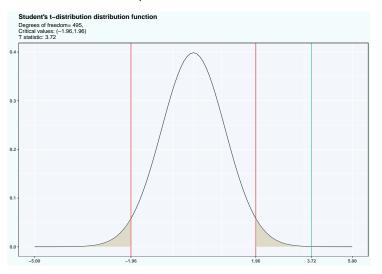
#### model2\$coefficients

```
rides
 (Intercept)
                                 games
                                                wait
                                                            clean
-131.4091939
               0.5290780
                             0.1533361
                                                       0.9842126
                                          0.5533264
# Calculate the variance-covariance matrix, extract
# the diagonal and calculate the standard deviaton of
# the parameters
model2 |> vcov() |> diag() |> sqrt()
```

```
(Intercept)
                rides
                            games
                                        wait
                                                   clean
8.33376643 0.14207176 0.06908486 0.04781282 0.15986712
```



## • Linear Model with Multiple Predictors





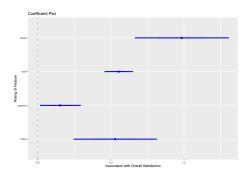
## • Linear Model with Multiple Predictors

```
confint(model2, level = 0.95)
                   2.5 %
                               97.5 %
(Intercept) -147.78311147 -115.0352764
rides
              0.24993998
                            0.8082161
games
              0.01760038
                          0.2890718
wait
                          0.6472675
              0.45938535
clean
              0.67011082
                            1.2983144
```



### Linear Model with Multiple Predictors

```
library(coefplot) # Remember to install the package if it is not installed
coefplot(model = model2,
         # The intercept is relatively large: -131.4092
        intercept = FALSE,
        ylab="Rating of Feature",
        xlab="Association with Overall Satisfaction".
        1 wdOuter = 1.5
```





summary(model1)\$r.squared

[1] 0.3433799 summary(model2)\$r.squared

Γ17 0.558621 summary(model1)\$adj.r.squared

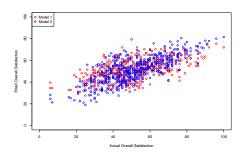
[1] 0.3420614 summary(model2)\$adj.r.squared

[1] 0.5550543



#### Base R way

```
plot(x = amusement_park$overall, y = fitted(model1),
     col = "red", xlim = c(0,100), ylim = c(0,100),
     xlab = "Actual Overall Satisfaction",
     vlab = "Fitted Overall Satisfaction")
points(x = amusement_park$overall, y = fitted(model2),
      col = "blue")
legend(x = "topleft", legend = c("Model 1", "Model 2"), col = c("red", "blue"), pch = 1)
```





#### • Tidymodels and tidyverse way: Prepare data

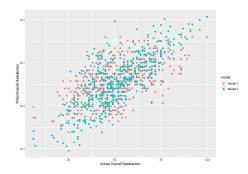
model1\_augment <- augment(x = model1) |> mutate(model = "Model 1")

```
model2_augment <- augment(x = model2) |> mutate(model = "Model 2")
models_performance <- model1_augment |> bind_rows(model2_augment)
models_performance |> glimpse()
Rows: 1,000
Columns: 12
                                   <dbl> 47, 65, 61, 37, 68, 27, 40, 30, 58, 36, 71, 48, 75, 46, 59,~
 $ overall
                                   <dbl> 87, 87, 85, 88, 84, 81, 77, 82, 90, 88, 93, 79, 94, 81, 86,~
$ rides
                                   <dbl> 53.22359, 53.22359, 49.81702, 54.92688, 48.11373, 43.00388,~
 $ .fitted
$ .resid
                                   <dbl> -6.2235914, 11.7764086, 11.1829795, -17.9268769, 19.8862650~
$ .hat
                                   <dbl> 0.002089430, 0.002089430, 0.002048063, 0.002311576, 0.00222~
$ .sigma
                                   <dbl> 12.88964, 12.88182, 12.88289, 12.86751, 12.86171, 12.87260,~
$ .cooksd
                                   <dbl> 2.449537e-04, 8.770564e-04, 7.751689e-04, 2.249493e-03, 2.6~
$ .std.resid <dbl> -0.48371422, 0.91529407, 0.86915315, -1.39348008, 1.5457218~
                                   <chr> "Model 1", 
$ model
                                   $ games
                                   $ wait
$ clean
```



#### • Tidymodels and tidyverse way: Visualize

```
models_performance |>
  ggplot() +
  geom_point(aes(x = overall, y = .fitted,
                 color = model)) +
  labs(x = "Actual Overall Satisfaction".
       y = "Fitted Overall Satisfaction")
```





Analysis of variance (anova) for nested models<sup>1</sup>

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

```
anova_lm <- anova(model1, model2, test = "F")
anova_lm
Analysis of Variance Table
Model 1: overall ~ rides
Model 2: overall ~ rides + games + wait + clean
        RSS Df Sum of Sq
  Res.Df
    498 82612
    495 55532 3
                     27080 80.463 < 2.2e-16 ***
```

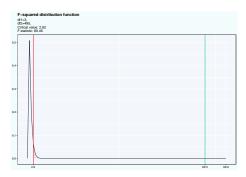
<sup>&</sup>lt;sup>1</sup>This statistical analysis only make sense for nested models that are fitted with the same data where the convention is to include the models from smallest to largest. See ?anova.lm



$$H_0:\beta_0=\beta_1=\beta_2=\beta_3=\beta_4=0$$

 $H_1:$  At least one  $eta_j 
eq 0$  for  $j=0\,,\,1\,,\,2\,,\,3\,,\,4$ 

$$F = \frac{\frac{RSS_1 - RSS_2}{p_2 - p_1}}{\frac{RSS_2}{n - p_2}} = \frac{\frac{82611.81 - 55531.53}{5 - 2}}{\frac{55531.53}{500 - 5}} = 80.46323$$





#### Predictions

$$\begin{split} \widehat{overall}_j &= \hat{\beta}_0 + \hat{\beta}_1 rides_j + \hat{\beta}_2 games_j \\ &+ \hat{\beta}_3 wait_j + \hat{\beta}_4 clean_j \end{split}$$

```
coef(model2) |> enframe(name = "coef")
# A tibble: 5 x 2
 coef
                value
 <chr>>
                <db1>
1 (Intercept) -131.
2 rides
        0.529
               0.153
3 games
```



0.553

0.984

4 wait

5 clean

#### Predictions

#### Manual

```
(coef(model2)["(Intercept)"]*1 + coef(model2)["rides"]*30 + coef(model2)["games"]*10 +
   coef(model2)["wait"]*57 + coef(model2)["clean"]*90) |>
 unname()
```

- [1] 6.11525
  - Predictions
    - Matrix multiplication

```
coef(model2) %*% c(1, 30, 10, 57, 90)
        [,1]
Γ1. ] 6.11525
```



#### Predictions

#### • predict

```
# New data
new_data <- tibble(rides = c(30, 70),
                   games = c(10, 80),
                   wait = c(57, 60).
                   clean = c(90, 93))
# Result
predict(object = model2, newdata = new_data) |>
 enframe(name = "observation", value = "overall pred") |>
 bind_cols(new_data)
```

```
# A tibble: 2 x 6
 observation overall_pred rides games wait clean
                     <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
 <chr>>
                               30
1 1
                      6.12
                                     10
                                           57
                                                  90
2 2
                     42.6
                               70
                                     80
                                           60
                                                  93
```



### Standardizing the predictors

- Compare the effect that different predictor variables have on a response variable
- It must be interpreted in terms of standard deviations
  - One standard deviation in x variable is associated with a standard deviation increase of decrease depending on the value of the estimated parameter

```
amusement_park_std <- amusement_park |>
 select(-distance) |>
 mutate(across(rides:logdist,
               .fns = ~ scale(x = .x.
                              center = TRUE.
                              scale = TRUE)[,1]))
amusement_park_std |> head()
# A tibble: 6 x 8
 weekend num.child rides
                          games
                                    wait clean overall logdist
```

```
<int> <dbl>
                         <db1>
                                        <db1>
                                               <dbl>
 <fct>
                                 <dbl>
                                                      <db1>
               0 0.211 -0.698 -0.919
                                       0.215 -0.268
                                                     1.79
1 yes
2 yes
               2 0.211 -0.0820 0.567
                                      -0.176 0.865
                                                    0.323
               1 -0.155 0.164 0.00966 0.0199 0.614 1.19
3 no
               0 0.394 -0.821 -0.362 0.215 -0.898
                                                      0.280
4 yes
5 no
               4 -0.338 1.03
                               0.381 -0.176 1.05
                                                      1.04
6 no
               5 -0 887 0 0411 -2 03
                                      -1.74
                                              -1.53
                                                      0.145
```



#### Standardizing the predictors

```
model2_std <- lm(formula = overall ~ rides + games + wait + clean,
            data = amusement park std)
summary(model2 std)
Call:
lm(formula = overall ~ rides + games + wait + clean, data = amusement park std)
Residuals:
              10 Median 30
    Min
                                       Max
-1.88578 -0.43082 0.06749 0.45136 1.80231
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) -2.607e-16 2.983e-02 0.000 1.000000
rides
         1.820e-01 4.888e-02 3.724 0.000219 ***
          7.844e-02 3.534e-02 2.220 0.026903 *
games
wait
          3.753e-01 3.243e-02 11.573 < 2e-16 ***
          3.170e-01 5.150e-02 6.156 1.54e-09 ***
clean
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.667 on 495 degrees of freedom
Multiple R-squared: 0.5586, Adjusted R-squared: 0.5551
F-statistic: 156.6 on 4 and 495 DF. p-value: < 2.2e-16
```



```
model3 <- lm(formula = overall ~ rides + games + wait + clean + weekend + logdist + num.child,
            data = amusement park std)
tidy(model3)
# A tibble: 8 x 5
            estimate std.error statistic p.value
 term
 <chr>>
               <db1>
                        <db1>
                                  <db1>
                                          <db1>
1 (Intercept) -0.373
                        0.0465
                                 -8.01 8.41e-15
2 rides
             0.213
                        0.0420
                               5.07 5.57e- 7
3 games
              0.0707
                       0.0303
                              2.34 1.99e- 2
                      0.0278
                                13.7
                                      1.45e-36
4 wait
              0.381
                     0.0441 6.72 4.89e-11
5 clean
             0.297
6 weekendves -0.0459 0.0514
                                -0.893 3.73e- 1
                      0.0257 2.52 1.22e- 2
7 logdist
             0.0647
8 num.child
              0.227
                       0.0171
                                      1.37e-34
                                 13.3
glance(model3)
```

```
# A tibble: 1 x 12
                  r.squared adj.r.squared sigma statistic p.value df logLik AIC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            BIC
                                                                 <db1>
                                                                                                                                                                                                                          <db1> <db1>
                                                                                                                                                                                                                                                                                                                                                                                                              <db1>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               <dbl> <dbl > <dbl > <dbl > <db > <db
                                                               0.679
                                                                                                                                                                                                                          0.674 0.571
                                                                                                                                                                                                                                                                                                                                                                                                                        148. 5.97e-117
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           7 -425, 868, 906,
```

# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>



Overall satisfaction is about the same regardless the number of children

```
amusement park std <- amusement park std |>
 mutate(num.child.factor = factor(num.child))
model4 <- lm(formula = overall ~ rides + games + wait + clean + weekend + logdist + num.child.factor,
             data = amusement_park_std)
tidy(model4) |> slice(1, 2, 8:12)
# A tibble: 7 x 5
                    estimate std.error statistic p.value
  term
  <chr>>
                       <dh1>
                                 <dh1>
                                           <dh1>
                                                    <dh1>
1 (Intercept)
                      -0.691
                                0.0449
                                          -15.4 7.00e-44
2 rides
                       0.223
                                0.0354
                                            6.30 6.61e-10
3 num child factor1
                      1.02
                                0.0713
                                         14 3 8 96e-39
                     1.04
4 num child factor?
                               0.0564
                                           18 4 8 77e-58
                                           14.0 1.75e-37
5 num.child.factor3
                       0.980
                               0.0702
6 num child factor4
                       0.932
                                0.0803
                                           11.6 1.22e-27
7 num child factor5
                      1.00
                                0.104
                                            9.66 2.50e-20
glance(model4)
```

```
# A tibble: 1 x 12
 r.squared adj.r.squared sigma statistic p.value
                                                      df logLik
                                                                  AIC
                                                                        BTC
      <dbl>
                   <dbl> <dbl>
                                   <db1>
                                             <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
     0.775
                   0.770 0.480
                                    153 2 68e-150
                                                      11 -336 698 753
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>
```



<db1> <db1>

0.771 0.478

<db1>

# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>

282. 1.03e-155

#### Preparing data

```
amusement_park_std <- amusement_park_std |>
 mutate(has.child = factor(x = num.child > 0, labels = c("No", "Yes")))
model5 <- lm(formula = overall ~ rides + games + wait + clean + logdist + has.child,
            data = amusement park std)
tidy(model5) |> slice(1, 2, 7)
# A tibble: 3 x 5
              estimate std.error statistic p.value
 term
  <chr>
                 <db1>
                         <db1>
                                   <dh1>
                                            <dh1>
1 (Intercept) -0.702 0.0391 -18.0 6.68e-56
2 rides
              0.223
                         0.0351 6.34 5.12e-10
3 has childYes
              1.01
                         0.0468 21.5 1.08e-72
glance(model5)
# A tibble: 1 x 12
 r.squared adi.r.squared sigma statistic p.value df logLik
                                                               AIC
```



<dbl> 0.774 <dbl> <dbl > <dbl > <dbl > <db > <db

6 -337, 690, 724,

 Maybe having children and the visits on weekends are important for the scores so an interaction will be useful

```
model6 <- lm(formula = overall ~ rides + games + wait + clean + weekend + logdist +
                               has.child + rides:has.child + games:has.child + wait:has.child +
                               clean:has.child + rides:weekend + games:weekend + wait:weekend +
                               clean:weekend, data = amusement_park_std)
tidy(model6) |> slice(9:16)
# A tibble: 8 x 5
                   estimate std.error statistic p.value
  term
                                <db1>
                                         <db1>
  <chr>>
                      <db1>
                                                  <dbl>
1 rides:has_childVes 0.0578
                               0.0731
                                        0.792 4.29e- 1
2 games:has.childYes -0.0640
                               0.0528 -1.21 2.26e- 1
3 wait:has.childYes
                               0.0472 7.42 5.21e-13
                    0.351
4 clean:has.childYes -0.00185
                              0.0797
                                       -0.0233 9.81e- 1
5 rides:weekendyes 0.0618 0.0678 0.912 3.62e- 1
6 games:weekendyes 0.0185 0.0490 0.377 7.06e- 1
7 wait:weekendyes
                   0.0352
                           0.0445 0.791 4.29e- 1
8 clean:weekendyes
                   -0.0273
                               0.0710
                                       -0.385 7.01e- 1
glance(model6)
# A tibble: 1 x 12
```

```
r.squared adj.r.squared sigma statistic p.value df logLik AIC
   <db1>
                 <db1> <db1>
                                <db1>
                                          <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
   0.802
                0.796 0.452
                                130. 3.69e-159
                                                  15 -304, 643, 714,
```





#### Only an interaction was significant

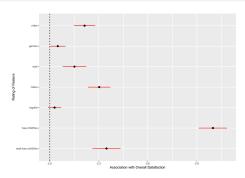
# i 3 more variables: deviance <dbl>, df.residual <int>, nobs <int>

```
model7 <- lm(formula = overall ~ rides + games + wait + clean + logdist + has.child +
                      wait:has.child. data = amusement park std)
tidy(model7)
# A tibble: 8 x 5
                   estimate std.error statistic p.value
  term
  <chr>>
                      <dh1>
                               <dh1>
                                         <dh1>
                                                  <dh1>
                    -0.693
                              0.0368
                                        -18.8 6.91e-60
1 (Intercept)
2 rides
                    0.213
                            0.0331
                                          6.42 3.24e-10
                              0.0239
3 games
                    0.0487
                                          2.03 4.25e- 2
                    0.151
                              0.0369
                                        4.09 4.98e- 5
4 wait
                    0.302
                              0.0349
                                        8.68 5.94e-17
5 clean
6 logdist
                     0.0292 0.0203
                                        1.44 1.50e- 1
                    0.998 0.0442
7 has childYes
                                         22.6 4.02e-78
8 wait:has.childYes
                    0.347
                             0.0438
                                         7.92 1.59e-14
glance(model7)
# A tibble: 1 x 12
 r.squared adj.r.squared sigma statistic p.value df logLik
                                                                AIC
     <dh1>
                   <dbl> <dbl>
                                  <dbl>
                                            <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <
                   0.797 0.451
                                   280. 2.96e-167
                                                     7 -307, 632, 670,
     0.800
```



#### Final model

```
library(dotwhisker) # Remember to install the package if it is not installed
tidy(model7) |>
 dwplot(ci = 0.95,
        dot args = list(size = 2, color = "black"), whisker args = list(color = "red"),
        vline = geom_vline(xintercept = 0, color = "black", linetype = 2)) +
 labs(x = "Association with Overall Satisfaction", y = "Rating of Feature")
```





#### Formula syntax

Formula in R	Statistical Model
y ∼ x	$y_i = \beta_0 + \beta_1 x_i + \varepsilon_i$
$y \sim -1 + x$	$y_i = \beta_1 x_i + \varepsilon_i$
$y \sim x + z$	$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \varepsilon_i$
$y \sim x + z + x:z$	$\boldsymbol{y}_i = \boldsymbol{\beta}_0 + \boldsymbol{\beta}_1 \boldsymbol{x}_i + \boldsymbol{\beta}_2 \boldsymbol{z}_i + \boldsymbol{\beta}_3 \boldsymbol{x}_i \boldsymbol{z}_i + \boldsymbol{\varepsilon}_i$
$y \sim x*z$	$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \beta_3 x_i z_i + \varepsilon_i$
$y \sim (x + z + w)^2$	$y_{i} = \beta_{0} + \beta_{1}x_{i} + \beta_{2}z_{i} + \beta_{3}w_{i} + \beta_{4}x_{i}z_{i} + \beta_{5}x_{i}w_{i} + \beta_{6}w_{i}z_{i} + \varepsilon_{i}$
$y \sim (x + z + w)^2 - x:z$	$y_i = \beta_0 + \beta_1 x_i + \beta_2 z_i + \beta_3 w_i + \beta_4 x_i w_i + \beta_5 w_i z_i + \varepsilon_i$
$y \sim x + I(x^2)$	$y_i = \beta_0 + \beta_1 x_i + \beta_1 x_i^2 + \varepsilon_i$

#### Try the following models using tidy:

```
lm(formula = overall ~ rides, data = amusement park std) |> tidy()
lm(formula = overall ~ -1 + rides, data = amusement park std) |> tidv()
lm(formula = overall ~ rides + has.child, data = amusement_park_std) |> tidy()
lm(formula = overall ~ rides + has.child + has.child, data = amusement park std) |> tidy()
lm(formula = overall ~ (rides + has.child + weekend)^2.
  data = amusement_park_std) |> tidy()
lm(formula = overall ~ (rides + has.child + weekend)^2 - rides:has.child,
  data = amusement_park_std) |> tidy()
lm(formula = overall ~ rides + I(rides^2) - rides:has.child, data = amusement_park std) |> tidy()
```



- To my family that supports me
- To the taxpayers of Colombia and the UMNG students who pay my salary
- To the Business Science and R4DS Online Learning communities where I learn R and  $\pi$ -thon
- To the R Core Team, the creators of RStudio IDE, Quarto and the authors and maintainers of the packages tidyverse, skimr, tidymodels, dotwhisker, kableExtra and tinytex for allowing me to access these tools without paying for a license
- To the **Linux kernel community** for allowing me the possibility to use some **Linux distributions** as my main **OS** without paying for a license



# References I

Chapman, Chris, and Elea McDonnell Feit. 2019. R For Marketing Research and Analytics. 2nd ed. 2019. Use R! Cham: Springer International Publishing: Imprint: Springer. https://doi-org.ezproxy.umng.edu.co/10.1007/978-3-030-14316-9.

