

# Number Systems and the Foundations of Analysis

**Mathematical Adventures**

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# Preface

The aim of this book is to study the basic number system of mathematics using as a principal guide Mendelson (2008) and other supplementary materials.

The idea is to develop all the topics and solve the exercises proposed in Mendelson (2008) as it has done in [Mathematical Adventures](#)

# **1 Basic Facts and Notions of Logic and Set Theory**

This chapter introduces the concepts and terminology of logic and set theory

## **1.1**

## 2 The Natural Numbers

## 3 The Integers

## 4 Rational Numbers and Ordered Fields

## 5 The Real Number System



## References

Mendelson, Elliott. 2008. *Number Systems and the Foundations of Analysis*. Mineola, N.Y.: Dover Publications.

## A Equality

## B Finite Sums and the $\sum$ notation

## C Polynomials

## **D Finite, Infinite and Denumerable Sets and Cardinal Numbers**

## **E Axiomatic Set Theory and the Existence of the Peano System**

## **F Construction of the Real Numbers via Dedekind Cuts**

## **G Complex Numbers**