

# Reducing Data Complexity

Luis Francisco Gomez Lopez

FAEDIS

2024-02-25

# Contents

- Please Read Me
- Purpose
- Consumer brand perception survey
- Understanding the reduction of data complexity
- Consumer brand perception survey
- References

# Please Read Me

- This presentation is based on ([Chapman and Feit 2019, chap. 8](#))

# Purpose

- Apply data complexity reduction by using the principal component analysis technique

# Consumer brand perception survey

- On a scale from 1 to 10, where 1 is least and 10 is most, how <perceptual adjective> is <brand>?
- 100 respondents rate 10 brands on 9 perceptual adjectives
  - **perform**: has strong performance (1, 2, ..., 10)
  - **leader**: is a leader in the field (1, 2, ..., 10)
  - **latest**: has the latest products (1, 2, ..., 10)
  - **fun**: is fun (1, 2, ..., 10)
  - **serious**: is serious (1, 2, ..., 10)
  - **bargain**: products are a bargain (1, 2, ..., 10)
  - **value**: products are a good value (1, 2, ..., 10)
  - **trendy**: is trendy (1, 2, ..., 10)
  - **rebuy**: I would buy from <brand> again (1, 2, ..., 10)
  - **brand**: coffee brand rated by a consumer ( $a, b, \dots, j$ )

# Consumer brand perception survey

## • Import data

```
consumer_brand <- read_csv("http://goo.gl/IQ18nc")  
consumer_brand |> head(n = 5)
```

```
# A tibble: 5 x 10  
  perform leader latest fun serious bargain value trendy rebuy brand  
    <dbl>   <dbl>   <dbl> <dbl>   <dbl>   <dbl> <dbl>   <dbl> <dbl> <chr>  
1      2     4     8     8     2     9     7     4     6 a  
2      1     1     4     7     1     1     1     2     2 a  
3      2     3     5     9     2     9     5     1     6 a  
4      1     6    10     8     3     4     5     2     1 a  
5      1     1     5     8     1     9     9     1     1 a
```

# Consumer brand perception survey

## • Transform data

```
consumer_brand_scale <- consumer_brand |>
  mutate(across(perform:rebuy,
    .fns = ~ scale(x = .x,
                    center = TRUE,
                    scale = TRUE)[,1]))
consumer_brand_scale |> head()
```

# A tibble: 6 x 10

	perform	leader	latest	fun	serious	bargain	value	trendy	rebuy	brand
	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<chr>
1	-0.777	-0.160	0.586	0.704	-0.836	1.78	1.11	-0.445	0.893	a
2	-1.09	-1.31	-0.713	0.340	-1.20	-1.22	-1.39	-1.17	-0.679	a
3	-0.777	-0.543	-0.388	1.07	-0.836	1.78	0.276	-1.54	0.893	a
4	-1.09	0.607	1.24	0.704	-0.476	-0.0971	0.276	-1.17	-1.07	a
5	-1.09	-1.31	-0.388	0.704	-1.20	1.78	1.94	-1.54	-1.07	a
6	-0.777	1.37	0.911	-0.389	-0.476	1.40	1.11	-1.54	-0.679	a

# Consumer brand perception survey

- Summarize data
  - Ups the table is really big!!! Try it in your console to see the complete table

```
consumer_brand_scale |> skim()
```

**Table 1:** Data summary

Name	consumer_brand_scale
Number of rows	1000
Number of columns	10
Column type frequency:	
character	1
numeric	9
Group variables	None

**Variable type: character**

skim_variable	n_missing	complete_rate	min	max	empty	n_unique	whitespace
brand	0	1	1	1	0	10	0



# Consumer brand perception survey

- Correlation matrices
  - Pearson correlation coefficients for samples in a tibble

```
correlation_matrix <- consumer_brand_scale |>
  select(perform:rebuy) |>
  corrr::correlate(use = "pairwise.complete.obs", # There are NA values
    method = "pearson",
    diagonal = NA)
correlation_matrix # Ups!!! The tibble is wide. Check out the tibble in your console
```

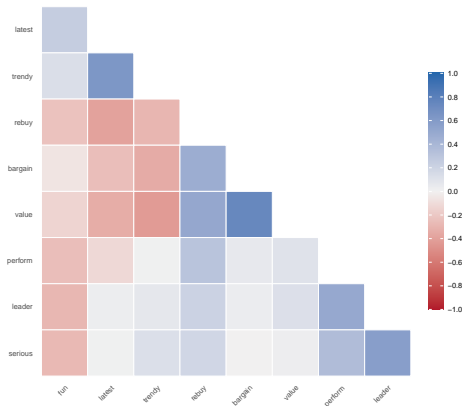
```
# A tibble: 9 x 10
  term      perform leader latest   fun serious bargain value trendy
<chr>      <dbl>   <dbl>   <dbl>   <dbl>   <dbl>   <dbl>   <dbl>   <dbl>
1 perform NA      0.500 -0.122 -0.256  0.359  0.0571  0.102  0.00873
2 leader  0.500    NA      0.0269 -0.290  0.571  0.0331  0.118  0.0665
3 latest -0.122  0.0269    NA      0.245  0.00995 -0.254 -0.343  0.628
4 fun    -0.256 -0.290  0.245    NA    -0.281 -0.0666 -0.145  0.128
5 serious 0.359  0.571  0.00995 -0.281    NA    -0.00266 0.0238  0.121
6 bargain 0.0571 0.0331 -0.254 -0.0666 -0.00266 NA      0.740 -0.351
7 value  0.102  0.118 -0.343 -0.145  0.0238  0.740    NA    -0.435
8 trendy 0.00873 0.0665  0.628  0.128  0.121 -0.351 -0.435    NA
9 rebuy  0.307  0.209 -0.397 -0.237  0.181  0.467  0.506 -0.298

# i 1 more variable: rebuy <dbl>
```

# Consumer brand perception survey

- Correlation matrices
  - Pearson correlation coefficients for samples in a tibble

```
correlation_matrix |>  
  autoplot(method = "HC", # Hierarchical clustering: More details in Chapter 11  
           triangular = "lower")
```



# Consumer brand perception survey

## • Mean ratings by brand

```
brand_mean <- consumer_brand_scale |>
  group_by(brand) |>
  summarise(across(everything(), .fns = mean))
brand_mean
```

# A tibble: 10 x 10

	brand	perform	leader	latest	fun	serious	bargain	value	trendy	rebuy
	<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	a	-0.886	-0.528	0.411	0.657	-0.919	0.214	0.185	-0.525	-0.596
2	b	0.931	1.07	0.726	-0.972	1.18	0.0416	0.151	0.740	0.237
3	c	0.650	1.16	-0.102	-0.845	1.22	-0.607	-0.441	0.0255	-0.132
4	d	-0.680	-0.593	0.352	0.187	-0.692	-0.881	-0.933	0.737	-0.494
5	e	-0.564	0.193	0.456	0.296	0.0421	0.552	0.418	0.139	0.0365
6	f	-0.0587	0.270	-1.26	-0.218	0.589	0.874	1.02	-0.813	1.36
7	g	0.918	-0.168	-1.28	-0.517	-0.534	0.897	1.26	-1.28	1.36
8	h	-0.0150	-0.298	0.502	0.715	-0.141	-0.738	-0.783	0.864	-0.604
9	i	0.335	-0.321	0.356	0.412	-0.149	-0.255	-0.803	0.591	-0.203
10	j	-0.630	-0.789	-0.154	0.285	-0.602	-0.0971	-0.0738	-0.481	-0.962

# Consumer brand perception survey

- Mean ratings by brand

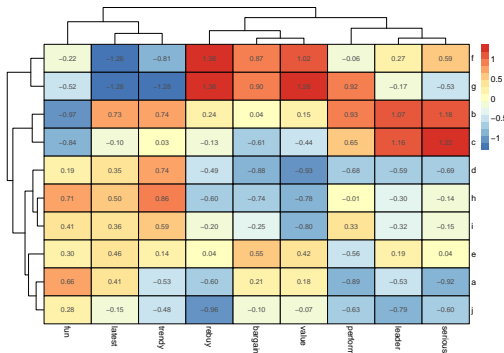
```
brand_mean_longer <- brand_mean |>
  pivot_longer(cols = perform:rebuy,
               names_to = "perceptual_adjectives",
               values_to = "value_mean") |>
  mutate(brand = fct_reorder(.f = brand, .x = value_mean),
         perceptual_adjectives = fct_reorder(.f = perceptual_adjectives, .x = value_mean))
brand_mean_longer
```

```
# A tibble: 90 x 3
  brand perceptual_adjectives value_mean
<fct> <fct>                <dbl>
1 a    perform              -0.886
2 a    leader                -0.528
3 a    latest                0.411
4 a    fun                  0.657
5 a    serious              -0.919
6 a    bargain              0.214
7 a    value                0.185
8 a    trendy               -0.525
9 a    rebuy                -0.596
10 b   perform              0.931
# i 80 more rows
```

# Consumer brand perception survey

- Heat map mean ratings by brand

```
library(tidyheatmaps)
tidyheatmap(df = brand_mean_longer,
  rows = brand, columns = perceptual_adjectives, values = value_mean,
  cluster_rows = TRUE, cluster_cols = TRUE,
  clustering_method = "complete", # See ?hclust and chapter 11
  display_numbers = TRUE, border_color = "black", fontsize = 12)
```



# Consumer brand perception survey

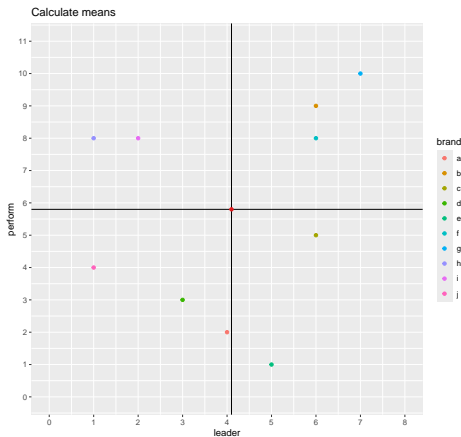
- Principal component analysis (PCA) and perceptual maps
  - PCA reduced example

```
set.seed(seed = 1234)
consumer_brand_sample <- consumer_brand |>
  slice_sample(n = 1, by = brand) |>
  select(brand, perform, leader)
consumer_brand_sample
```

```
# A tibble: 10 x 3
  brand perform leader
  <chr>    <dbl> <dbl>
1 a         2     4
2 b         9     6
3 c         5     6
4 d         3     3
5 e         1     5
6 f         8     6
7 g        10     7
8 h         8     1
9 i         8     2
10 j         4     1
```

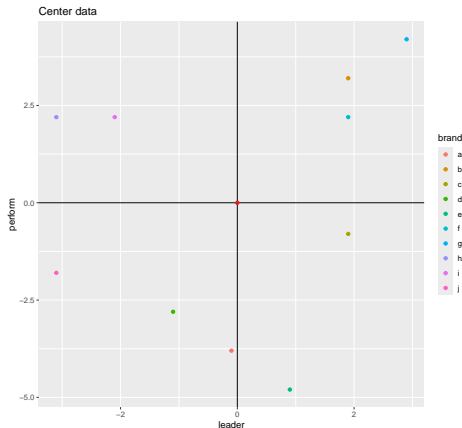
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Visualizing original data



# Consumer brand perception survey

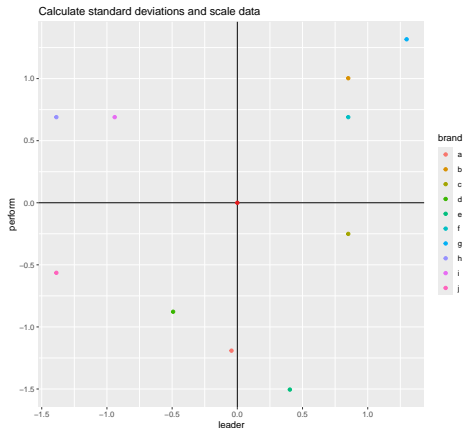
- Principal component analysis (PCA) and perceptual maps
  - Centering data using the mean





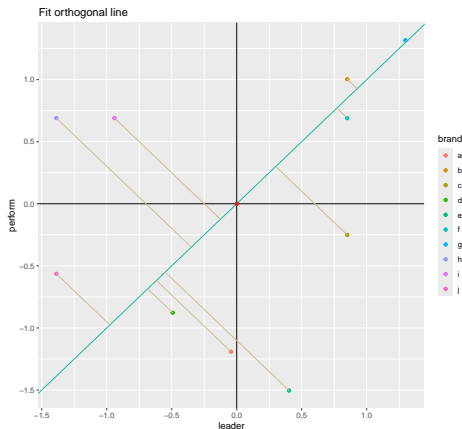
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Scaling data using the standard deviation



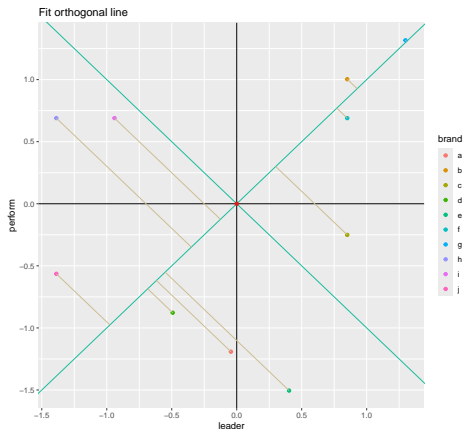
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Fitting a line by performing an orthogonal regression



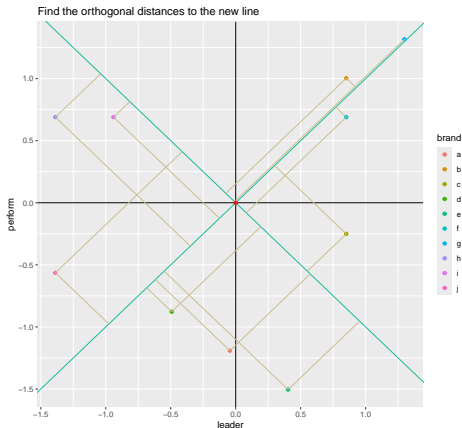
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Find a line orthogonal to the fitted line



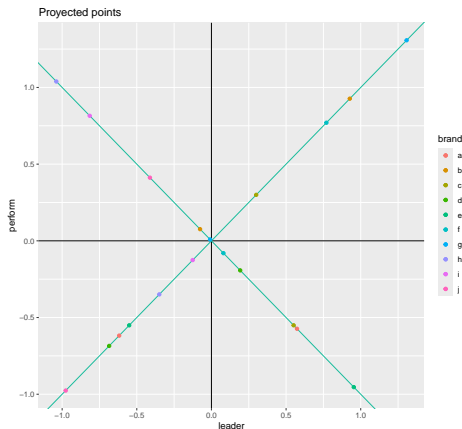
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Find the orthogonal distances between the points and the new line



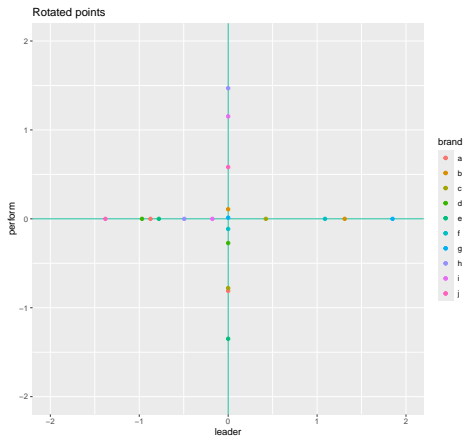
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Project the points onto each line



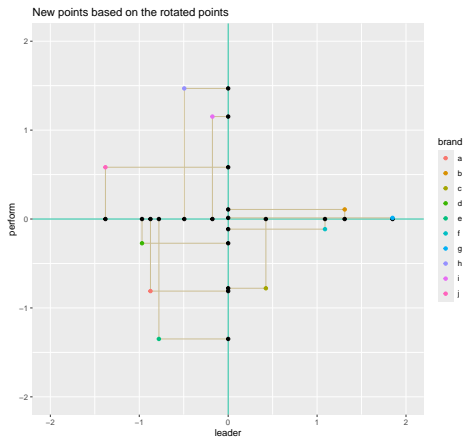
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Rotate the fitted line and the projected points around  $(0,0)$



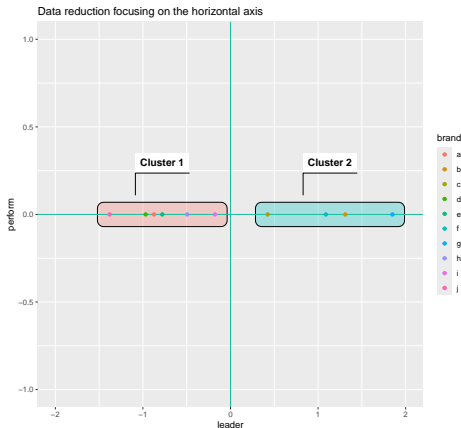
# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
- Fix the new points based on the projected points



# Consumer brand perception survey

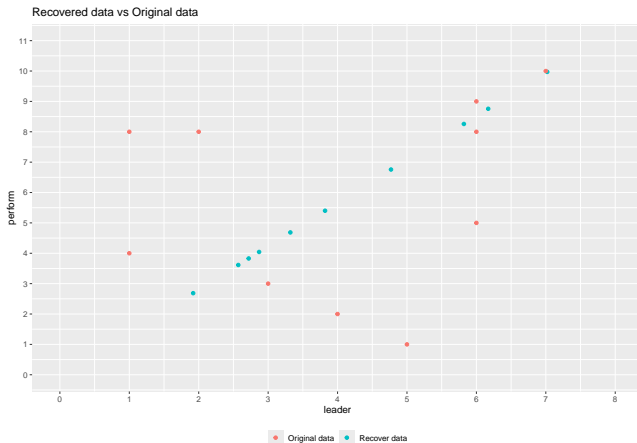
- Principal component analysis (PCA) and perceptual maps
  - Apply data complexity reduction by focusing on the horizontal axis





# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Recover the data that was reduced when focusing in the horizontal axis



# Understanding the reduction of data complexity

- Principal component analysis (PCA) and perceptual maps
  - Using an image to understand data complexity reduction



# Understanding the reduction of data complexity

- Principal component analysis (PCA) and perceptual maps
  - Represent and image as data
    - $x, y$ : position of a point in a cartesian plane  $(x, y)$
    - value: a gray scale where 0 is white, 1 is black and  $(0, 1)$  is an intermediate color between white and black

```
# A tibble: 262,144 x 3
      x     y value
  <int> <int> <dbl>
1     1     1  1 0.498
2     2     2  1 0.482
3     3     3  1 0.490
4     4     4  1 0.471
5     5     5  1 0.494
6     6     6  1 0.482
7     7     7  1 0.498
8     8     8  1 0.502
9     9     9  1 0.490
10    10    10  1 0.506
# i 262,134 more rows
```

# Understanding the reduction of data complexity

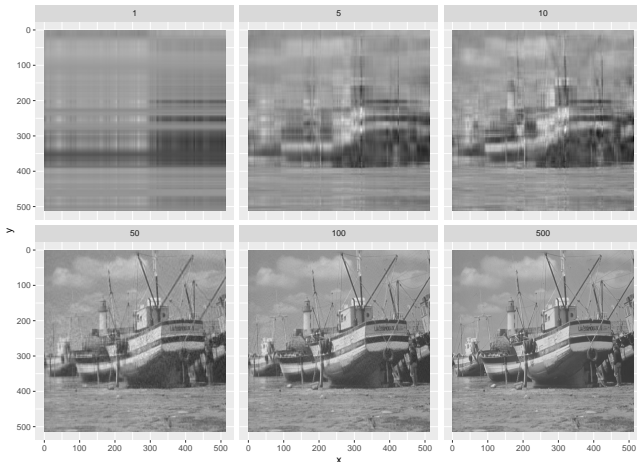
- Principal component analysis (PCA) and perceptual maps
  - Prepare data for PCA

```
# A tibble: 512 x 513
  x   `1`   `2`   `3`   `4`   `5`   `6`   `7`   `8`   `9`  `10`  `11`  `12`
<int> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl> <dbl>
1     1  0.498 0.502 0.502 0.486 0.494 0.490 0.498 0.482 0.494 0.486 0.478 0.494
2     2  0.482 0.494 0.486 0.498 0.490 0.498 0.498 0.529 0.502 0.502 0.494 0.498
3     3  0.490 0.502 0.502 0.502 0.502 0.494 0.494 0.471 0.486 0.498 0.502 0.490
4     4  0.471 0.478 0.494 0.506 0.494 0.494 0.486 0.502 0.502 0.486 0.494 0.478
5     5  0.494 0.490 0.498 0.475 0.494 0.502 0.471 0.475 0.490 0.498 0.482 0.490
6     6  0.482 0.490 0.471 0.502 0.490 0.502 0.498 0.482 0.482 0.475 0.498 0.475
7     7  0.498 0.478 0.502 0.506 0.498 0.502 0.502 0.494 0.502 0.502 0.486 0.498
8     8  0.502 0.506 0.506 0.502 0.502 0.494 0.494 0.494 0.510 0.510 0.506 0.502
9     9  0.490 0.498 0.502 0.506 0.514 0.510 0.502 0.502 0.502 0.518 0.514 0.514
10    10  0.506 0.502 0.514 0.522 0.498 0.506 0.514 0.522 0.518 0.522 0.525 0.514

# i 502 more rows
# i 500 more variables: `13` <dbl>, `14` <dbl>, `15` <dbl>, `16` <dbl>,
# `17` <dbl>, `18` <dbl>, `19` <dbl>, `20` <dbl>, `21` <dbl>, `22` <dbl>,
# `23` <dbl>, `24` <dbl>, `25` <dbl>, `26` <dbl>, `27` <dbl>, `28` <dbl>,
# `29` <dbl>, `30` <dbl>, `31` <dbl>, `32` <dbl>, `33` <dbl>, `34` <dbl>,
# `35` <dbl>, `36` <dbl>, `37` <dbl>, `38` <dbl>, `39` <dbl>, `40` <dbl>,
# `41` <dbl>, `42` <dbl>, `43` <dbl>, `44` <dbl>, `45` <dbl>, `46` <dbl>, ...
```

# Understanding the reduction of data complexity

- Principal component analysis (PCA) and perceptual maps
  - Data complexity reduction



# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Applying to the reduced example

```
consumer_brand_sample_matrix <- consumer_brand_sample |>  
  select(-brand) |>  
  as.matrix()  
consumer_brand_sample_matrix |> head()
```

	perform	leader
[1,]	2	4
[2,]	9	6
[3,]	5	6
[4,]	3	3
[5,]	1	5
[6,]	8	6

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - prcomp output from R

```
consumer_brand_sample_matrix_pca <- consumer_brand_sample_matrix |>
  prcomp(center = TRUE, scale. = TRUE)
consumer_brand_sample_matrix_pca
```

```
Standard deviations (1, .., p=2):
[1] 1.1051789 0.8823716
```

```
Rotation (n x k) = (2 x 2):
      PC1      PC2
perform 0.7071068 0.7071068
leader  0.7071068 -0.7071068
```

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Structure of prcompfrom R

```
List of 5
 $ sdev      : num [1:2] 1.105 0.882
 $ rotation: num [1:2, 1:2] 0.707 0.707 0.707 -0.707
 ..- attr(*, "dimnames")=List of 2
 .. ..$ : chr [1:2] "perform" "leader"
 .. ..$ : chr [1:2] "PC1" "PC2"
 $ center   : Named num [1:2] 5.8 4.1
 ..- attr(*, "names")= chr [1:2] "perform" "leader"
 $ scale    : Named num [1:2] 3.19 2.23
 ..- attr(*, "names")= chr [1:2] "perform" "leader"
 $ x        : num [1:10, 1:2] -0.874 1.311 0.424 -0.969 -0.779 ...
 ..- attr(*, "dimnames")=List of 2
 .. ..$ : NULL
 .. ..$ : chr [1:2] "PC1" "PC2"
 - attr(*, "class")= chr "prcomp"
```



# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Extracting scores: principle components space

```
scores <- consumer_brand_sample_matrix_pca$x  
scores
```

	PC1	PC2
[1,]	-0.8739101	-0.81059416
[2,]	1.3107664	0.10776349
[3,]	0.4241852	-0.77881770
[4,]	-0.9688445	-0.27236914
[5,]	-0.7789757	-1.34881917
[6,]	1.0891211	-0.11388181
[7,]	1.8489914	0.01282907
[8,]	-0.4937775	1.46901678
[9,]	-0.1771978	1.15243706
[10,]	-1.3803587	0.58243559

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Extracting loadings: map from principle components space back into the original space

```
loadings <- consumer_brand_sample_matrix_pca$rotation  
loadings
```

	PC1	PC2
perform	0.7071068	0.7071068
leader	0.7071068	-0.7071068

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Extracting loadings: map from principle components space back into the original space

```
consumer_brand_sample_matrix_center_scale <- consumer_brand_sample_matrix |>
  scale(center = TRUE, scale = TRUE)
consumer_brand_sample_matrix_center_scale
```

```
      perform      leader
[1,] -1.1911244 -0.04477113
[2,]  1.0030521  0.85065153
[3,] -0.2507630  0.85065153
[4,] -0.8776706 -0.49248246
[5,] -1.5045782  0.40294020
[6,]  0.6895983  0.85065153
[7,]  1.3165059  1.29836285
[8,]  0.6895983 -1.38790512
[9,]  0.6895983 -0.94019379
[10,] -0.5642168 -1.38790512
attr(,"scaled:center")
perform leader
      5.8      4.1
attr(,"scaled:scale")
perform leader
3.190263 2.233582
```

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Using matrix multiplication,  $\%*\%$ , the original centered and scaled data,  $X_{c,s}$ , and the loadings,  $L$ , loadings to obtain the scores,  $S$

$$S = X_{c,s}L$$

```
consumer_brand_sample_matrix_center_scale %*% loadings
```

```
      PC1      PC2
[1,] -0.8739101 -0.81059416
[2,]  1.3107664  0.10776349
[3,]  0.4241852 -0.77881770
[4,] -0.9688445 -0.27236914
[5,] -0.7789757 -1.34881917
[6,]  1.0891211 -0.11388181
[7,]  1.8489914  0.01282907
[8,] -0.4937775  1.46901678
[9,] -0.1771978  1.15243706
[10,] -1.3803587  0.58243559
```

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Recovering original centered and scaled data,  $X$ , using loadings,  $L$ ,<sup>1</sup> and scores,  $S$

$$SL^t = X_{c,s}LL^t = X_{c,s}I = X_{c,s}$$

```
(scores %*% t(loadings)) |> set_colnames(c("perform", "leader"))
```

	perform	leader
[1,]	-1.1911244	-0.04477113
[2,]	1.0030521	0.85065153
[3,]	-0.2507630	0.85065153
[4,]	-0.8776706	-0.49248246
[5,]	-1.5045782	0.40294020
[6,]	0.6895983	0.85065153
[7,]	1.3165059	1.29836285
[8,]	0.6895983	-1.38790512
[9,]	0.6895983	-0.94019379
[10,]	-0.5642168	-1.38790512

<sup>1</sup> $L$  is an orthogonal matrix, which means that  $L$  is a real square matrix such that  $L^tL = LL^t = I$  where  $I$  is the identity matrix.

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Reconstructing original centered and scaled data using the first principal component,  $X_{c,s,p_1}$

$$S_{p_1} L_{p_1}^t = X_{c,s,p_1}$$

```
scores[, 1] %*% t(loadings[, 1])
```

	perform	leader
[1,]	-0.6179478	-0.6179478
[2,]	0.9268518	0.9268518
[3,]	0.2999442	0.2999442
[4,]	-0.6850765	-0.6850765
[5,]	-0.5508190	-0.5508190
[6,]	0.7701249	0.7701249
[7,]	1.3074344	1.3074344
[8,]	-0.3491534	-0.3491534
[9,]	-0.1252977	-0.1252977
[10,]	-0.9760610	-0.9760610

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Reconstructing original centered data using the first principal component,  $X_{c,p_1}$

```
scores[, 1] %*% t(loadings[, 1]) |>  
  scale(center = FALSE, scale = 1/consumer_brand_sample_matrix_pca$scale)
```

```
      perform    leader  
[1,] -1.9714158 -1.3802370  
[2,]  2.9569010  2.0701996  
[3,]  0.9569010  0.6699501  
[4,] -2.1855743 -1.5301747  
[5,] -1.7572574 -1.2302994  
[6,]  2.4569010  1.7201372  
[7,]  4.1710595  2.9202620  
[8,] -1.1138912 -0.7798628  
[9,] -0.3997327 -0.2798628  
[10,] -3.1138912 -2.1801123  
attr("scaled:scale")  
      perform    leader  
0.3134538 0.4477113
```

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Reconstructing original data using the first principal component,  $X_{p_1}$

```
scores[, 1] %*% t(loadings[, 1]) |>  
  scale(center = FALSE, scale = 1/consumer_brand_sample_matrix_pca$scale) |>  
  scale(center = -consumer_brand_sample_matrix_pca$center, scale = FALSE)
```

```
      perform leader  
[1,] 3.828584 2.719763  
[2,] 8.756901 6.170200  
[3,] 6.756901 4.769950  
[4,] 3.614426 2.569825  
[5,] 4.042743 2.869701  
[6,] 8.256901 5.820137  
[7,] 9.971059 7.020262  
[8,] 4.686109 3.320137  
[9,] 5.400267 3.820137  
[10,] 2.686109 1.919888  
attr("scaled:scale")  
      perform leader  
0.3134538 0.4477113  
attr("scaled:center")  
perform leader  
-5.8 -4.1
```



# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Eigenvalues, in this case variance, represent the variance explained by each principal component

```
eigenvalues <- consumer_brand_sample_matrix_pca |>
  tidy(matrix = "eigenvalues") |>
  mutate(variance = std.dev^2, .after = std.dev)
eigenvalues
```

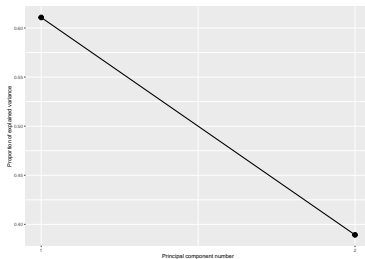
```
# A tibble: 2 x 5
```

	PC	std.dev	variance	percent	cumulative
	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1	1	1.11	1.22	0.611	0.611
2	2	0.882	0.779	0.389	1

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Eigenvalues, in this case variance, represent the variance explained by each principal component

```
library(ggbiplot)
consumer_brand_sample_matrix_pca |>
  ggscreeplot() +
  scale_x_continuous(breaks = 1:2)
```



# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - A **biplot** represents visually the scores of the first, x-axis, and second, y-axis, of the principal components and the corresponding loadings both **scaled by a factor**<sup>2</sup>
  - In the case of principal component analysis there are many different ways to produce a biplot
    - For the different ways to build a biplot check out [Positioning the arrows on a PCA biplot](#)

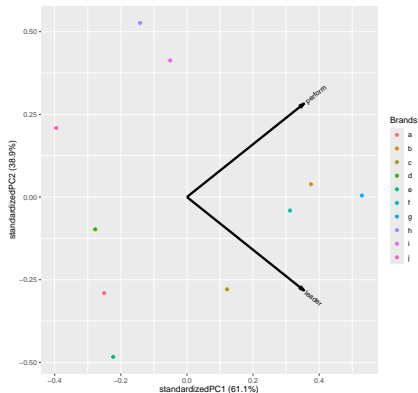
---

<sup>2</sup>For specific details check out `?stats::biplot.prcomp`, `?ggbiplot::ggbiplot` and `?ggbiplot::get_SVD`

# Consumer brand perception survey

- Principal component analysis (PCA) and perceptual maps
  - Building a biplot using the package ggbiplot

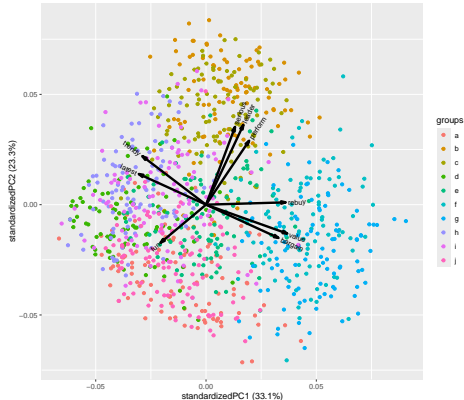
```
ggbiplot(pcoobj = consumer_brand_sample_matrix_pca,  
         groups = consumer_brand_sample$brand,  
         scale = 1, pc.biplot = FALSE) +  
labs(color = "Brands")
```



# Consumer brand perception survey

## • Bibplot for all the consumer brand perception survey

```
consumer_brand_pca <- consumer_brand |>
  select(-brand) |>
  prcomp(center = TRUE, scale. = TRUE)
consumer_brand_pca |>
  ggbiplot(groups = consumer_brand$brand, scale = 1, pc.biplot = FALSE)
```



# Consumer brand perception survey

- A biplot is a generalization of a scatterplot of 2 variables for the case of many variables ([Greenacre 2010, 9](#))
- Variables of the brands that are grouped together are positively correlated to each other
  - For example serious, leader and perform or trendy and latest
- Variables of the brands that are displayed to the opposite sides of the biplot origin are negatively correlated to each other
  - For example fun in relation to serious, leader and perform or trendy and latest in relation to value and bargain

# Consumer brand perception survey

- A biplot is an **approximated** representation of a data table ordered by rows which represents some observations and columns which represents some variables
  - By the term **approximated** it means that the representation is not exact
  - In our case the last biplot was used to represent the data table `consumer_brand_sample` by reducing its complexity
- In a biplot the distance between points represent some measure of similarity
  - In the case of the last biplot for example brand g, that is colored in blue, tend to be spatially grouped in the plot

# References

Chapman, Chris, and Elea McDonnell Feit. 2019. *R For Marketing Research and Analytics*. 2nd ed. 2019. Use R! Cham: Springer International Publishing : Imprint: Springer.  
<https://doi.org/10.1007/978-3-030-14316-9>.

Greenacre, Michael J. 2010. *Biplots in Practice*. Bilbao: Fundación BBVA.  
<https://www.fbbva.es/microsite/multivariate-statistics/biplots.html>.