# DHOscillator FFNN baseline model

March 10, 2024

```
[15]: # import numpy, scipy, and matplotlib
import numpy as np
import scipy as sp
import matplotlib.pyplot as plt

from sklearn.model_selection import train_test_split

import torch
%matplotlib widget

import os
import tempfile
```

### 1 Dumped Harmonic Oscillator FFNN baseline model

In this notebook, we will train a FFNN with the standard loss function given by the MSE on the train points. The architecture, number of data point, epochs and hyperparamenters, all shared with the ../models/PINN\_baseline\_model.pt, will be the baseline for further improvements.

```
[16]: # Number of epochs
n_epochs = 50000

# Batch size
batch_size = 595

# Learning rate and scheduler
lr = 0.01
factor = 0.9
patience = 200

# Model architecture
n_layers = 3
n_neurons = 20
```

```
[17]: # Model class
class FFNN(torch.nn.Module):
    def __init__(self, n_layers, n_neurons):
```

```
super(FFNN, self).__init__()
layers = []
for i in range(n_layers):
    if i == 0:
        layers.append(torch.nn.Linear(1, n_neurons))
    else:
        layers.append(torch.nn.Linear(n_neurons, n_neurons))
        layers.append(torch.nn.Tanh())
    layers.append(torch.nn.Linear(n_neurons, 2))
    self.model = torch.nn.Sequential(*layers)

def forward(self, x):
    return self.model(x)
```

### 1.1 Load data

```
[18]: # import data
# data are generated by "src/DHOscillator_data_gen.py"
data = np.load('../data/DHOscillator_data.npy')
X = data[:,0]
Y = data[:,1:]
```

```
[19]: def data_loader(X, Y, batch_size):
          Function to load data and divide it in batches
          input: X, Y, batch_size
          output: train_X_batches, train_Y_batches, val_X, val_Y, test_X, test_Y
          # divide in train, validation and test
          train_frac = 0.7
          val frac = 0.15
          test_frac = 0.15
          train_val_X = X[:int((train_frac+val_frac)*len(X))]
          train val Y = Y[:int((train frac+val frac)*len(X)), :]
          train_X, val_X, train_Y, val_Y = train_test_split(
             train_val_X,
              train_val_Y,
              test_size=val_frac/(train_frac+val_frac),
              random_state=42
          test_X = X[int((train_frac+val_frac)*len(X)):]
          test_Y = Y[int((train_frac+val_frac)*len(X)):, :]
          # convert to torch tensor
          train_X = torch.tensor(train_X, dtype=torch.float32).view(-1, 1)
```

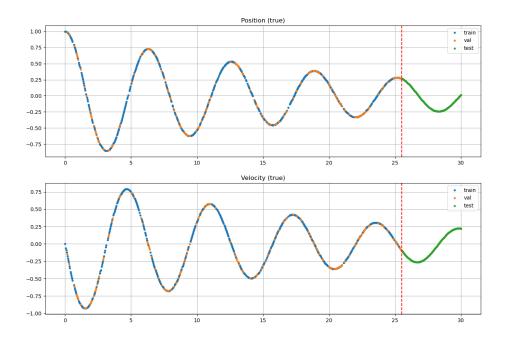
```
train_Y = torch.tensor(train_Y, dtype=torch.float32)
val_X = torch.tensor(val_X, dtype=torch.float32).view(-1, 1)
val_Y = torch.tensor(val_Y, dtype=torch.float32)
test_X = torch.tensor(test_X, dtype=torch.float32).view(-1, 1)
test_Y = torch.tensor(test_Y, dtype=torch.float32)

# divide in batches train
train_X_batches = torch.split(train_X, batch_size)
train_Y_batches = torch.split(train_Y, batch_size)
return train_X_batches, train_Y_batches, val_X, val_Y, test_X, test_Y
```

[20]: # use the data loader to get the data, in this example we use only one batch train\_X\_batches, train\_Y\_batches, val\_X, val\_Y, test\_X, test\_Y = data\_loader(X,\_U \( \to Y \), batch\_size)

```
[21]: # plot the position
      plt.figure(figsize=(15, 10))
      plt.subplot(2, 1, 1)
      plt.plot(train X batches[0].detach().numpy(), train Y batches[0][:, 0].detach().
       →numpy(), '.', label='train')
      plt.plot(val_X.detach().numpy(), val_Y[:, 0].detach().numpy(), '.', label='val')
      plt.plot(test_X.detach().numpy(), test_Y[:, 0].detach().numpy(), '.', __
       ⇔label='test')
      plt.grid()
      plt.title('Position (true)')
      plt.axvline(x=30*0.85, color='r', linestyle='--')
      plt.legend()
      # plot the velocity
      plt.subplot(2, 1, 2)
      plt.plot(train_X_batches[0].detach().numpy(), train_Y_batches[0][:, 1].detach().
       →numpy(), '.', label='train')
      plt.plot(val_X.detach().numpy(), val_Y[:, 1].detach().numpy(), '.', label='val')
      plt.plot(test_X.detach().numpy(), test_Y[:, 1].detach().numpy(), '.',__
       ⇔label='test')
      plt.grid()
      plt.title('Velocity (true)')
      plt.axvline(x=30*0.85, color='r', linestyle='--')
      plt.legend()
```

[21]: <matplotlib.legend.Legend at 0x7fcd6f82bbc0>



#### 1.2 FFNN

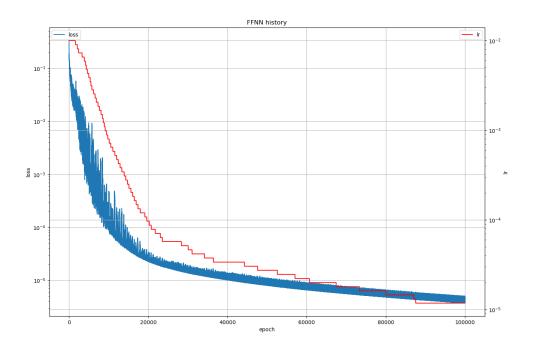
The FFNN will be trained on data point with time < 25, discarding validation data this means 595 point of the ODE.

```
[22]: # define the model
model_FFNN = FFNN(n_layers, n_neurons)

# define the loss function, mean squared error
loss_fn = torch.nn.MSELoss()

# define the optimizer and lr scheduler
optimizer = torch.optim.Adam(model_FFNN.parameters(), lr=lr)
scheduler = torch.optim.lr_scheduler.ReduceLROnPlateau(optimizer, 'min', u
factor=factor, patience=patience)
```

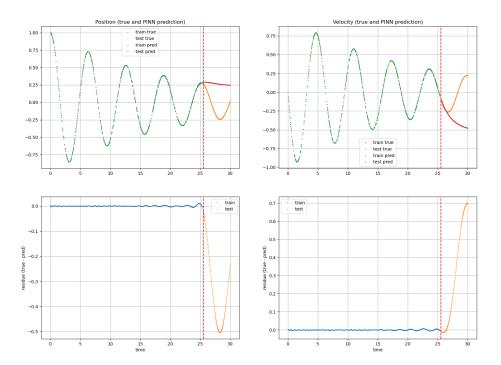
```
Y_pred = model_FFNN(X)
              loss = loss_fn(Y_pred, Y)
              loss.backward()
              optimizer.step()
              optimizer.step()
              scheduler.step(loss)
              history_FFNN.append([loss.item(), optimizer.param_groups[0]['lr']])
          if epoch % 10000 == 0:
              print(epoch, loss.item())
     0 0.26025626063346863
     10000 2.473035237926524e-05
     20000 1.0696694516809657e-05
     30000 6.7767400651064236e-06
     40000 4.859512955590617e-06
     CPU times: user 13min 16s, sys: 7.64 s, total: 13min 24s
     Wall time: 3min 21s
[36]: # plot history_FFNN loss and lr in two subplots
      history_FFNN = np.array(history_FFNN)
      fig, ax = plt.subplots(figsize=(15, 10))
      # plot the loss
      ax.plot(history_FFNN[:, 0], label='loss')
      ax.legend(loc='upper left')
      ax.set_yscale('log')
      ax.set_xlabel('epoch')
      ax.set_ylabel('loss')
      plt.grid()
      # plot the learning rate
      ax2 = ax.twinx()
      ax2.plot(history_FFNN[:, 1], label='lr', color='r')
      ax2.set_yscale('log')
      ax2.set_ylabel('lr')
      # legend to the right
      ax2.legend(loc='upper right')
      plt.grid()
      plt.title('FFNN history')
      # save the figure
      plt.savefig('../plot/DHOscillator_FFNN_baseline_history.png')
```



```
[35]: # get predictions
     Y_pred_train = model_FFNN(train_X_batches[0])
     Y_pred_val = model_FFNN(val_X)
     Y_pred_test = model_FFNN(test_X)
     # plot the position, and subplot the residue
     plt.figure(figsize=(18, 13))
     plt.subplot(2, 2, 1)
     marker='.'
     markersize=2
     plt.plot(train_X_batches[0].detach().numpy(), train_Y_batches[0][:, 0].detach().
      →numpy(), marker, label='train true', markersize=markersize)
     plt.plot(test_X.detach().numpy(), test_Y[:, 0].detach().numpy(), marker,__
      →label='test true', markersize=markersize)
     plt.plot(train_X_batches[0].detach().numpy(), Y_pred_train[:, 0].detach().
      plt.plot(test_X.detach().numpy(), Y_pred_test[:, 0].detach().numpy(), marker,__
      plt.grid()
     plt.title('Position (true and PINN prediction)')
```

```
plt.axvline(x=30*0.85, color='r', linestyle='--')
plt.legend()
plt.subplot(2, 2, 3)
plt.plot(train X batches[0].detach().numpy(), train Y batches[0][:, 0].detach().
 onumpy()-Y_pred_train[:, 0].detach().numpy(), marker, label='train',_
 →markersize=markersize)
plt.plot(test X.detach().numpy(), test Y[:, 0].detach().numpy()-Y pred test[:, ...
 40].detach().numpy(), marker, label='test', markersize=markersize)
plt.grid()
plt.ylabel('residue (true - pred)')
plt.xlabel('time')
plt.legend()
plt.axvline(x=30*0.85, color='r', linestyle='--')
# new figure for the velocity
plt.subplot(2, 2, 2)
plt.plot(train X batches[0].detach().numpy(), train Y batches[0][:, 1].detach().
 →numpy(), marker, label='train true', markersize=markersize)
plt.plot(test_X.detach().numpy(), test_Y[:, 1].detach().numpy(), marker,__
 ⇔label='test true', markersize=markersize)
plt.plot(train_X_batches[0].detach().numpy(), Y_pred_train[:, 1].detach().
 →numpy(), marker, label='train pred', markersize=markersize)
plt.plot(test_X.detach().numpy(), Y_pred_test[:, 1].detach().numpy(), marker,__
 →label='test pred', markersize=markersize)
plt.grid()
plt.title('Velocity (true and PINN prediction)')
plt.axvline(x=30*0.85, color='r', linestyle='--')
plt.legend()
plt.subplot(2, 2, 4)
plt.plot(train_X_batches[0].detach().numpy(), train_Y_batches[0][:, 1].detach().
 →numpy()-Y_pred_train[:, 1].detach().numpy(), marker, label='train', __
 →markersize=markersize)
plt.plot(test_X.detach().numpy(), test_Y[:, 1].detach().numpy()-Y_pred_test[:,_
 41].detach().numpy(), marker, label='test', markersize=markersize)
plt.grid()
plt.ylabel('residue (true - pred)')
plt.xlabel('time')
plt.legend()
plt.axvline(x=30*0.85, color='r', linestyle='--')
# save the figure
```

## plt.savefig('../plot/DHOscillator\_FFNN\_baseline\_results.png')



```
[26]: # test loss
loss_test_FFNN = loss_fn(Y_pred_test, test_Y)
print('test loss:', loss_test_FFNN.item())
```

test loss: 0.1473110467195511

```
[27]: # save the model
model_path = os.path.join('../models', 'DHO_FFNN_baseline.pt')
torch.save(model_FFNN, model_path)
```

Comment: The model do not reproduce qualitatively the beheviour of the ODE outside the train time span.